

Testing Cosmology with Extreme Galaxy Clusters

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Harrison & Coles (2011) MNRAS 418, L20, arXiv:1108.1358

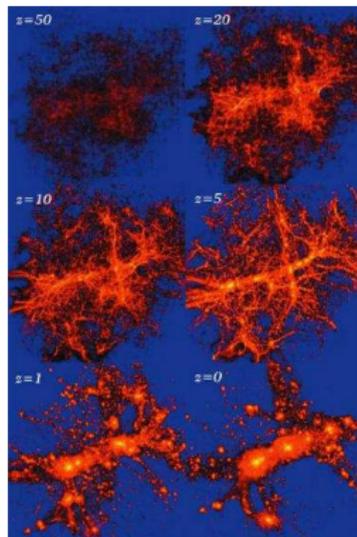
Harrison & Coles (2012) MNRAS 421, L19, arXiv:1111.1184

Table of Contents

- 1 The Problem of Big Clusters
 - Structure Formation in Λ CDM
 - High-Mass, High-Redshift Clusters
- 2 Extreme Value Statistics
 - Introduction to EVS
 - EVS and the HMF
- 3 Cosmological Null Tests
 - Λ CDM
 - Alternative Models
- 4 Future Prospects
 - Parameter Estimation
 - Example: f_{NL} using SPT Clusters

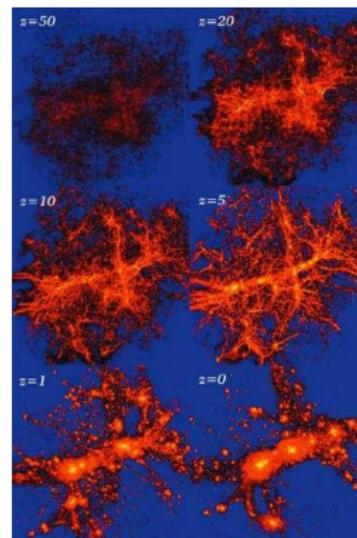
Structure Formation

- **Standard Model** Cosmology in 2012
- Makes **definite predictions** for structure formation
 - 'bottom up' or hierarchical
 - Haloes, filaments, voids
 - Quantitatively: HMF, linear growth function
- Many of the **plausible extensions** to Λ CDM are capable of enhancing (or depleting) structure formation



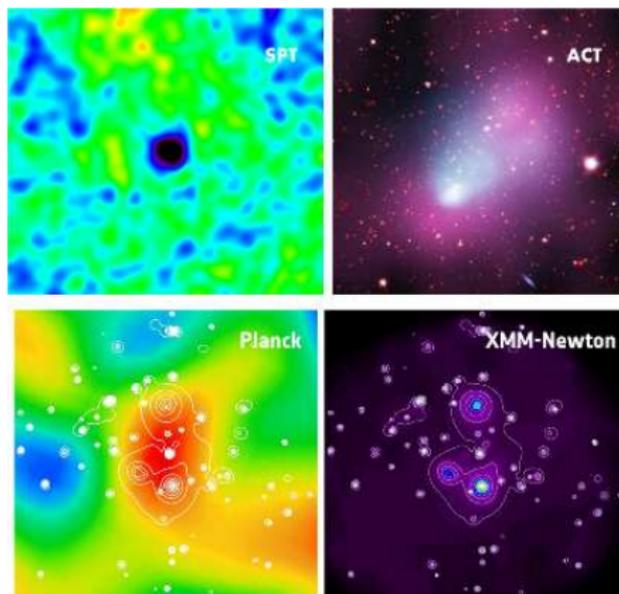
Structure Formation

- **Standard Model** Cosmology in 2012
- Makes **definite predictions** for structure formation
- Many of the **plausible extensions** to Λ CDM are capable of enhancing (or depleting) structure formation
 - Primordial non-Gaussianity
 - Scalar fields
 - Modified gravity, *etc*



High m, z Clusters – Concerns for Λ CDM?

- Have recently begun to probe the **largest structures** at higher and **higher redshifts** (XMM-Newton, SPT, ACT, Planck)





High m , z Clusters – Concerns for Λ CDM?

- Have been claims that some of the galaxy clusters observed are **too massive, too early** to have been produced by the Λ CDM model

(Jimenez & Verde, Hoyle et al, Cayon et al, Holz & Perlmutter, Jee et al, Enqvist et al)

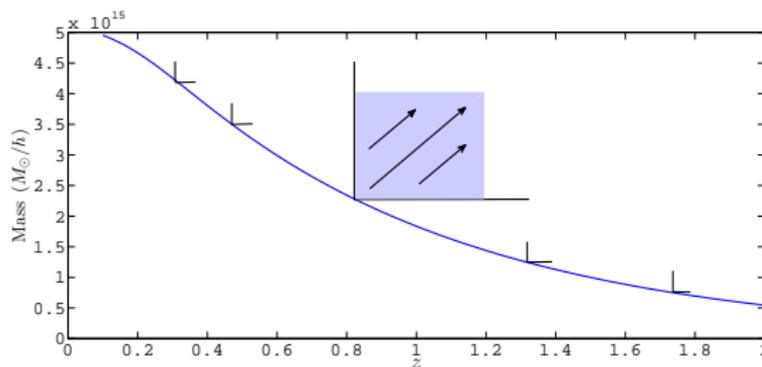
- Calculate abundance of clusters $\langle N(> m_{cl}, > z_{cl}) \rangle$ in a survey from the HMF
- Find fraction of realisations of Λ CDM with such a cluster to be **very low** \rightarrow tension with Λ CDM
- Point out tension can be eased with **large f_{NL}** ($\sim 300 - 500!$)

High m , z Clusters – Concerns for Λ CDM?

- Unfortunately, these analyses shown to be **biased** as count the wrong number of ‘equally rare’ events

Fergus Simpson on CosmoCoffee, Hotchkiss (2011)

- Overestimate** the tension with Λ CDM
- Take bias into account: tension **goes away**



Hotchkiss (2011)



High m , z Clusters – Concerns for Λ CDM?

- But high- m , high- z clusters are still interesting
 - Have only surveyed fraction of the sky with enough sensitivity for these objects
 - A Λ CDM-killer could still be out there

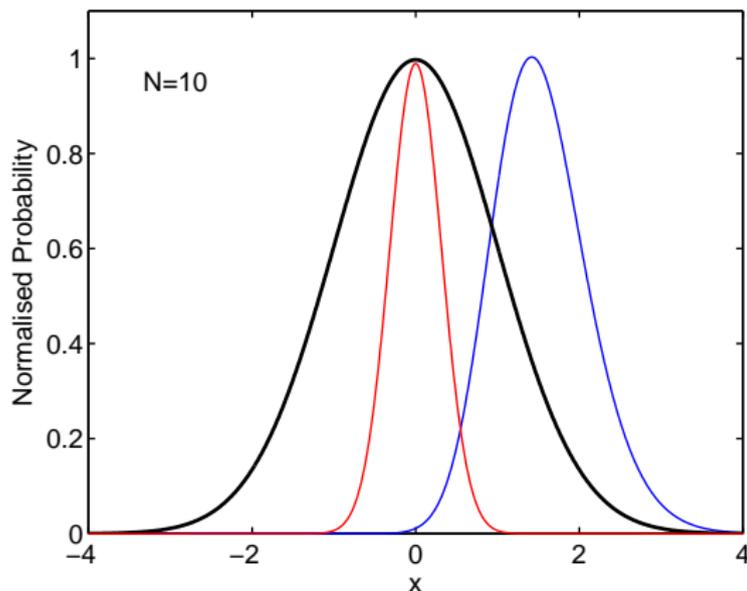
‘Rareness’ based estimates can clearly be slippery,
is there a cleaner option?

Can ask: what do we expect the most massive cluster in the
Universe to be?

Answer lies in Extreme Value Statistics

Predicting Extremes

- Usual question: “What is the distribution of **sample means**?”
- EVS question: “What is the distribution of **sample extrema**?”



Extreme Value Statistics

- Have a long history in **environmental sciences, finance** etc...
- **Exact distribution for maximum** M_{\max} of N i.i.d. random variates from underlying pdf $f(m)$, cdf $F(m)$

$$\Phi(M_{\max} \leq m; N) = F^N(m)$$

$$\phi(M_{\max} = m; N) = Nf(m) [F(m)]^{N-1}$$

- Just as CLT, is an **asymptotic distribution** as $N \rightarrow \infty$

$$P_{GEV}(m; \alpha_N, \beta_N, \gamma) = \exp \left\{ - \left[1 + \gamma \left(\frac{m - \alpha_N}{\beta_N} \right) \right]^{-1/\gamma} \right\}$$

- Where γ depends on the **underlying distribution**

EVS of HMFs - Exact Distribution

- For CDM haloes, we know $f(m)$: the **Halo Mass Function**
- Can construct PDF:

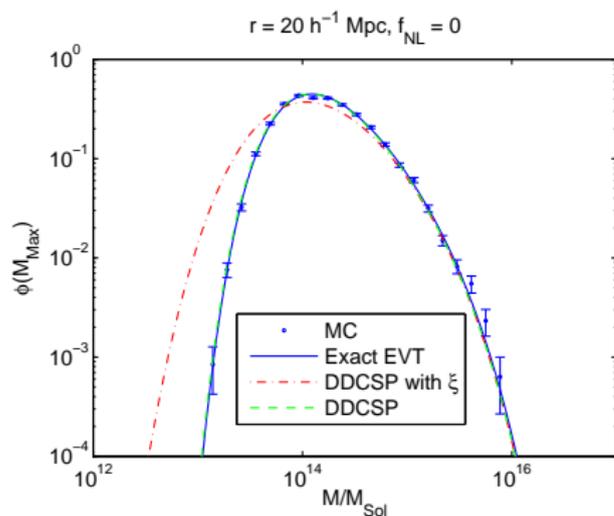
$$f(m) = \frac{1}{n_{\text{tot}}} \frac{dn(m)}{dm},$$

$$F(m) = \frac{1}{n_{\text{tot}}} \left[\int_{-\infty}^M dM \frac{dn(M)}{dM} \right].$$

- ...and feed this into $\phi(M_{\text{max}} = m; N)$ with $N = n_{\text{tot}} V$
- Can predict the **PDF of highest mass object** on a spatial hypersurface



EVS of HMFs - Results



IH & Coles (2011)

- Well matches other results (& N-body simulations)

Davis et al 2011 (DDCSP)

$$\Phi^{\text{void}}(M_{\text{max}} = m) = \frac{dP_0(m)}{dm}$$

$$P_0(m) = \exp(-n(> m)V)$$

Comparing with Observations

Can do EVS for simulations, what about observations?

- EVS **in a survey**, not just a spatial hypersurface
 - $n(m) \rightarrow n(m, z)$
 - $V \rightarrow dV/dz$

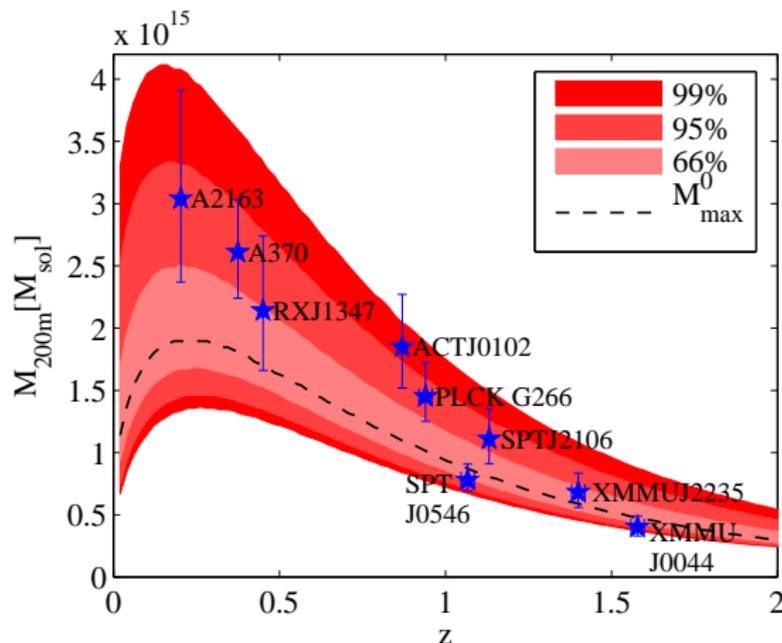
$$f(m) = \frac{1}{N_{tot}} \left[f_{sky} \int_{z_{min}}^{z_{max}} dz \frac{dV}{dz} \frac{dn(m, z)}{dM} \right],$$

$$N_{tot} = \left[f_{sky} \int_{z_{min}}^{z_{max}} \int_{-\infty}^{\infty} dz dM \frac{dV}{dz} \frac{dn(m, z)}{dM} \right].$$

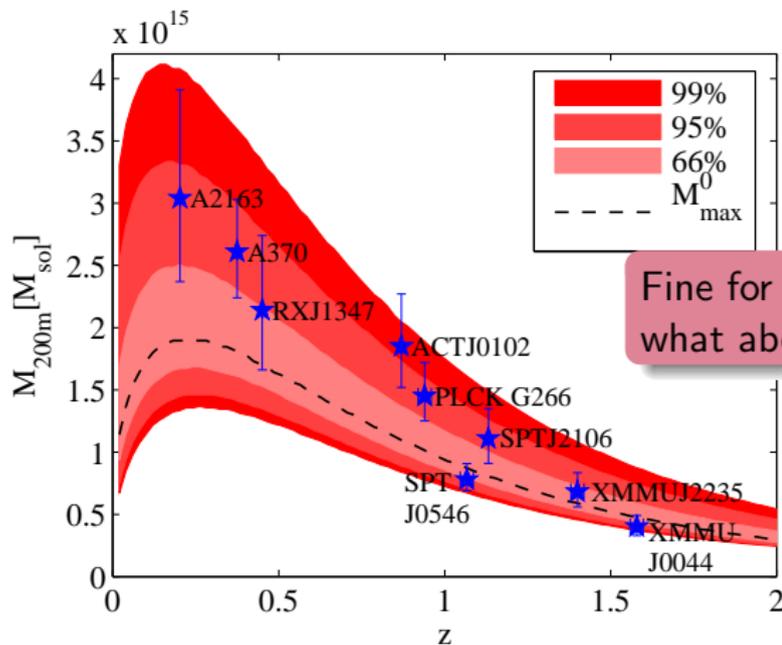
- Specify cosmology
 - WMAP7 parameters
 - Tinker HMF
 - Use cluster M_{200m}^{Edd} masses

Result – ΛCDM Survives

- Compute confidence regions in bins $\Delta z = 0.02$, with $f_{sky} = 1$ and plot clusters



Result – ΛCDM Survives



Fine for ruling out Λ CDM,
what about alternative models?

Two Toy Models

1. Primordial non-Gaussianity

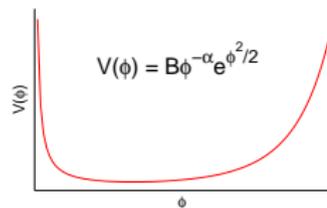
- Generated by **non-vanilla inflaton** Lagrangians
- $f_{NL} \sim 300 - 500$ **suggested** as explanation for high- m , high- z clusters
- Include via non-Gaussian **correction factor** $\mathcal{R}(f_{NL})$ to a Λ CDM mass function:

$$\mathcal{R}(f_{NL}) = n_{nG}^{th}(f_{NL})/n_G^{th},$$

$$n_{nG}^{sim}(f_{NL}) = \mathcal{R}(f_{NL})n_G^{sim}$$

2. Coupled scalar field Dark Energy 'SUGRA003'

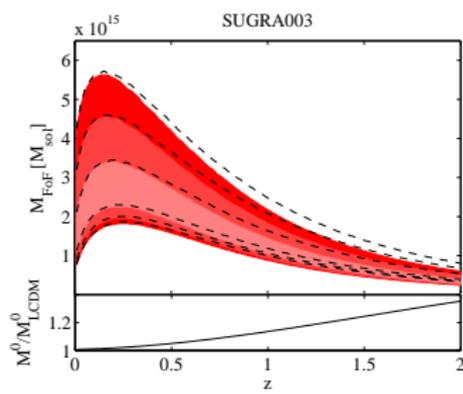
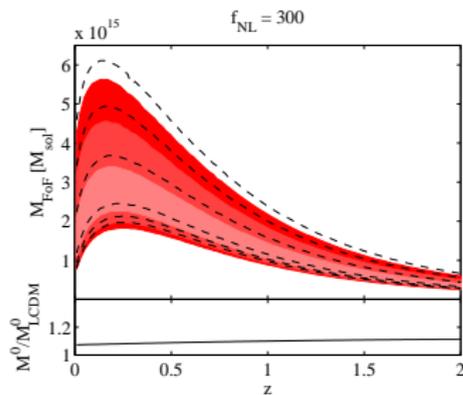
- SUGRA motivated quintessence model with **'bounce'** (Brax & Martin 1999)



- Structure formation enhanced (depleted) before (after) the bounce

Two Toy Results

- Make use of Λ CDM and SUGRA003 CoDECS simulations (Baldi 2011)
 - $h(z)$
 - $D(z)$
 - Halo mass function
- Large clusters at high and/or low redshifts can disfavour different models of enhanced structure formation





Beyond a Null Test

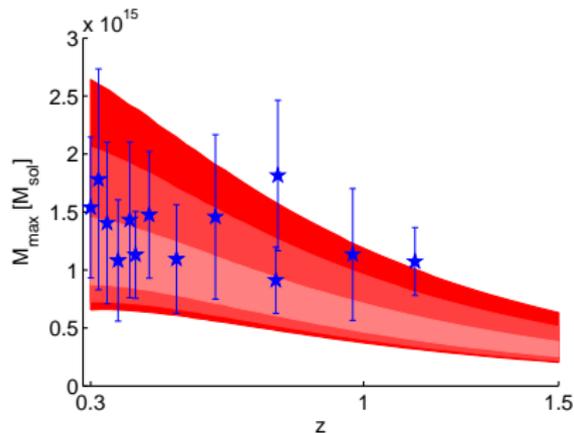
- Can test **one cluster** at a time, what about information from **multiple clusters** to do proper parameter estimation?
- To get constraints on a parameter, need to **guarantee** are not missing any **more extreme** clusters in our survey
- SZ surveys are 'nearly **mass-limited** to arbitrarily high redshift'

Consider an idealised survey:
complete above some mass threshold $m_{\text{thresh}} \sim 5 \times 10^{14} M_{\odot}$

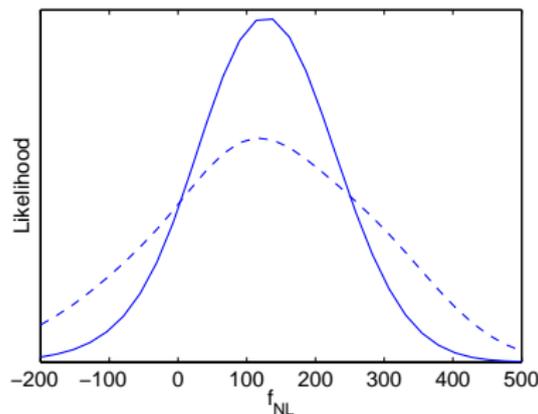
f_{NL} from 'idealised' SPT

- Take the 26 highest SZ S/N clusters from SPT [Williamson et al \(2011\)](#), treat as **complete above the mass of the lowest** of these 26 (i.e. $m_{thresh} = \min\{m_1 \dots m_{26}\}$)
- Define redshift bins
 - Occupied bins: Treat this as most massive cluster
 - Unoccupied bins: Most massive cluster is **not more massive** than m_{thresh}
- Take **sharp priors** on everything else (σ_8 , hmf parameters...)
- Calculate probabilities for both types of bins and **form likelihood** for f_{NL}

$$\mathcal{L}(f_{NL}) = \prod_{Occ.} \phi(m_{obs}; f_{NL}, \Delta z_i) \prod_{Unocc.} \left[\int_{-\infty}^{m_{thresh}} \phi(m; f_{NL}, \Delta z_j) dm \right]$$

Example: f_{NL} using SPT ClustersLikelihood for f_{NL} 

- Have 13 filled bins



- $f_{\text{NL}} = 128_{-119}^{+75}$, $\sigma_8 = 0.801$
- $f_{\text{NL}} = 101_{-197}^{+111}$, $\sigma_8 = 0.801 \pm 0.030$

Preliminary!



Summary and Prospects

- Extreme Value Statistics can **predict PDF for the most massive cluster** M_{max} in a given cosmology
- Observation of even a single cluster significantly larger than M_{max} is **good evidence against that cosmology**
 - Λ CDM survives current observations
 - Other models easily tested
- In order to do parameter estimation, require **survey with mass limit less** than expected region for M_{max}

Open Questions

- EVS for cluster *observables* (rather than masses)?
- Are we throwing too much information away?
- Extension to other objects (e.g. lenses, voids, quasars, superstructures...)
- How much can we trust the halo mass function?

End

Thanks