



### Introduction to polarisation (aka the hard stuff)

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#### Why is polarisation info interesting?

- Radio is key to measuring polarisation, better than any other wavelength >
- High-z seed fields (Widrow 2002; Subramanian 2007)
- Intergalactic Medium
- Intracluster Medium
- Interstellar medium
- Galactic Centre (Crocker et al. 2010; Ferrière 2010)
- > Main sequence star: HD 215441  $B_0 \approx 34 \text{ kG}$ (Babcock 1960)
- White dwarf: PG 1031+234 (Schmidt et al. 1986)
- > Pulsar: PSR J1847-0130 (McLaughlin et al. 2003)
- Magnetar: SGR 1806-20 (Kouveliotou et al. 1998, Israel et al. 2005)  $B_i \approx 10^{16} \text{ G}$
- Cosmic strings (Ostriker et al. 1986)
- > Planck-mass monopoles (Duncan et al. 2000)

- B~10<sup>-30</sup> –10<sup>-20</sup> G
- $B \sim 1-10 \text{ nG}$ ?
- B~0.1-1 µG
- $B \sim 1 \, \mu G 10 \, mG$
- $B \sim 50 \ \mu G 1 \ mG$
- $B_0 \approx 10^9 \,\mathrm{G}$
- $B_0 \approx 9 \times 10^{13} \text{ G}$
- $B_0 \approx 2 \times 10^{15} \text{ G},$
- B~10<sup>30</sup> G









Magnetic filaments in Perseus A

(Yusef-Zadeh et al. 1984) Galactic Centre

#### What do you expect to see?









# Light can have a preferential direction

> Linear polaristion



#### And any angle inbetween



# Light can also be circularly polarised



#### How to describe polarisation?

- > Polarized state of light can be described by 4 parameters e.g.
  - Total power;
  - Fractional powers in horizontal and vertical linear components;
  - Phase relationship between the horizontal and vertical components.



#### **Stokes Parameters**

- > Ease of use over direct
- > Can be used for partially polarised radiation.
- > Not a vector quantity! Deals with power instead of electric field amplitudes.
- The correlator can produce ALL Stokes parameters simultaneously (not so easy in optical astronomy!)
- > Exact definition of Stokes parameters dependent on feeds of telescope.

$$I = E_x^2 + E_y^2$$
$$Q = E_x^2 - E_y^2$$
$$U = 2E_x E_y \cos(\delta)$$
$$V = 2E_x E_y \sin(\delta)$$

- For monochromatic waves
- I : total intensity
- Q : linear
- U : linear
- V:circular
- $|^2 = Q^2 + U^2 + V^2$

# How to measure polarisation – linear feeds



## How to measure polarisation – circular feeds



#### **Measurement of Stokes**

- > Conceptually use many feeds to measure the different orthogonal polarizations
- > At radio frequencies voltages can be measured and correlated!

I = XX + YY,Q = XX - YY,U = XY + YX,iV = XY - YX.

where XX is  $\langle E_0 E_0 \rangle$  and YY is  $\langle E_{90} \overline{E_{90}} \rangle$  ("parallel hand" correlations) and XY is  $\langle E_0 \overline{E_{90}} \rangle$  and YX is  $\langle E_{90} \overline{E_0} \rangle$  ("cross hand" correlations).

#### Making stokes images

- > Each antenna measures two orthogonal polarizations X and Y.
- > For every baseline, form all four possible correlations XX, YY, XY, YX.
- > Calibration and other tricks
- > Appropriately combine the four correlations to get four Stokes "visibilities".
- Perform standard imaging with these Stokes visibilities to make Stokes images.

#### **Talking about the Jones**

> Jones matrices are "antenna based"

> Antenna gain:

$$\begin{pmatrix} g_x & 0 \\ 0 & g_y \end{pmatrix}$$

> Polarization leakage:

$$\begin{pmatrix} 1 & d_x \\ d_y & 1 \end{pmatrix}$$

$$\begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}$$

> Rotation:

#### Leakage

For real-world feeds, the feed will respond both to the desired polarization, and to a small degree the orthogonal polarization:

$$E'_X = E_X + d_x E_Y$$
$$E'_Y = E_Y + d_y E_X$$

 The leakage ("d term") is typically ~10<sup>-2</sup>. It is caused by alignment error, feed ellipticity, etc. Generic linear model (will suit practically anything).

#### **Rotation and parallactic angle**



#### **Rotation and parallactic angle**

- > Alt-az mount
- For a conventional alt-az mount, the sky rotates relative to the antenna feed -``parallactic angle rotation''
- > Instrumental polarization (leakage) will be in the frame of the antenna
- > Astronomical polarization will be in the frame of the sky.
- Instrumental and astronomical characteristics can be decoupled if the your observation spans a good range of parallactic angles.

#### **Depolarisation**

- > Depolarization = loss of polarimetric signal.
- Caused by the system polarimetric response not being constant (i.e. varying spatially, with time, across bandwidth etc etc) smearing out the polarimetric signal.
- Calibrated interferometers generally have very low depolarization (in polarimetric jargon, a system with no depolarization is called "pure").

#### Sync my radiation

- If the energy distribution of electrons is a power-law the spectrum will be a power-law
- > Non-thermal
- Most radio sources are non-thermal



# Some of the quanities we measure with polarisation

>

 Rotation measures – provide integrated magnetic fields through Faraday rotation of linear polarisation – integral along the line of sight of the electron density and line-of-sight magnetic field

$$\mathrm{RM} = 0.81 \int_{\mathrm{source}}^{\mathrm{observer}} n_e(l) B_{\parallel} \, dl \, \mathrm{rad} \, \mathrm{m}^{-2}.$$

> Polarisation vectors – provide field strength and direction in plane of sky through computation of measured Stokes Q and U to obtain linear polarisation and polarisation angle  $P = \sqrt{U^2 + Q^2} = Q - \frac{1}{4} \tan^{-1} \left( U \right)$ 

Gradient of Stokes Q and U – provide direct imaging of interstellar turbulence –  
changing of magnetic field orientation with gas motions
$$|\nabla \mathbf{P}| = \sqrt{\left(\frac{\partial Q}{\partial x}\right)^2 + \left(\frac{\partial U}{\partial y}\right)^2 + \left(\frac{\partial Q}{\partial y}\right$$

 Circular polarisation from synchrotron emission (it has a small, <0.1% Stokes I, component in Stokes V) – provide direct measurement of field strength and direction

$$m_{\rm c} = \epsilon_{\alpha}^{\nu} \left(\frac{\nu_{B\perp}}{\nu}\right)^{0.5} \frac{B_{\rm u,los}}{B_{\perp}^{\rm rms}}$$

#### Conclusions

- Huge amount of information in polarised light an something radio astronomy (since we store phase) is uniquely suited to exploit
- It is hard... instrumental calibration, weak signals, depolarisation, many structures between us and the source
- > Worth doing, but make sure your know your instrument and calibrators!

