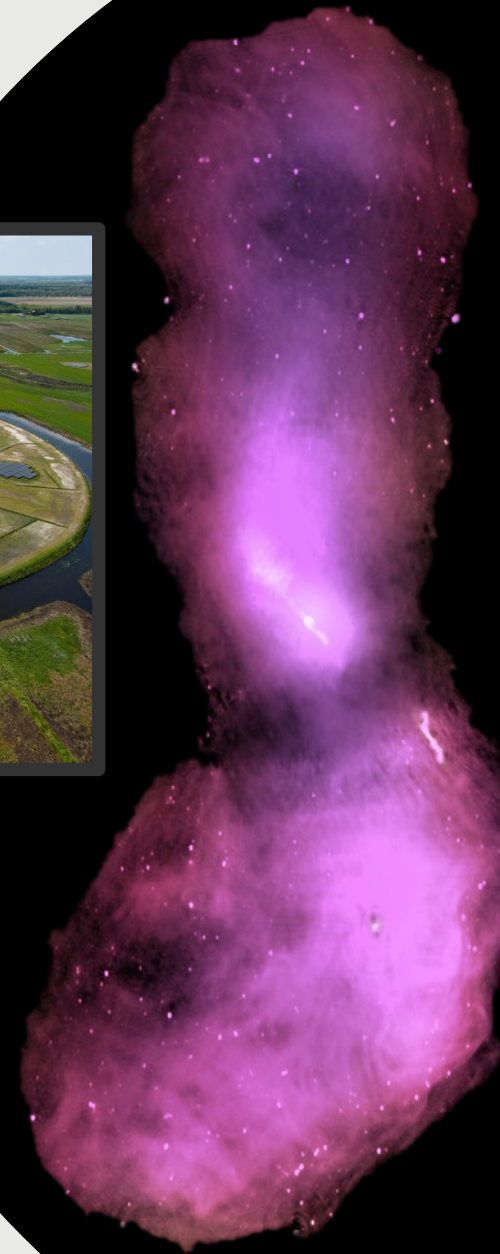


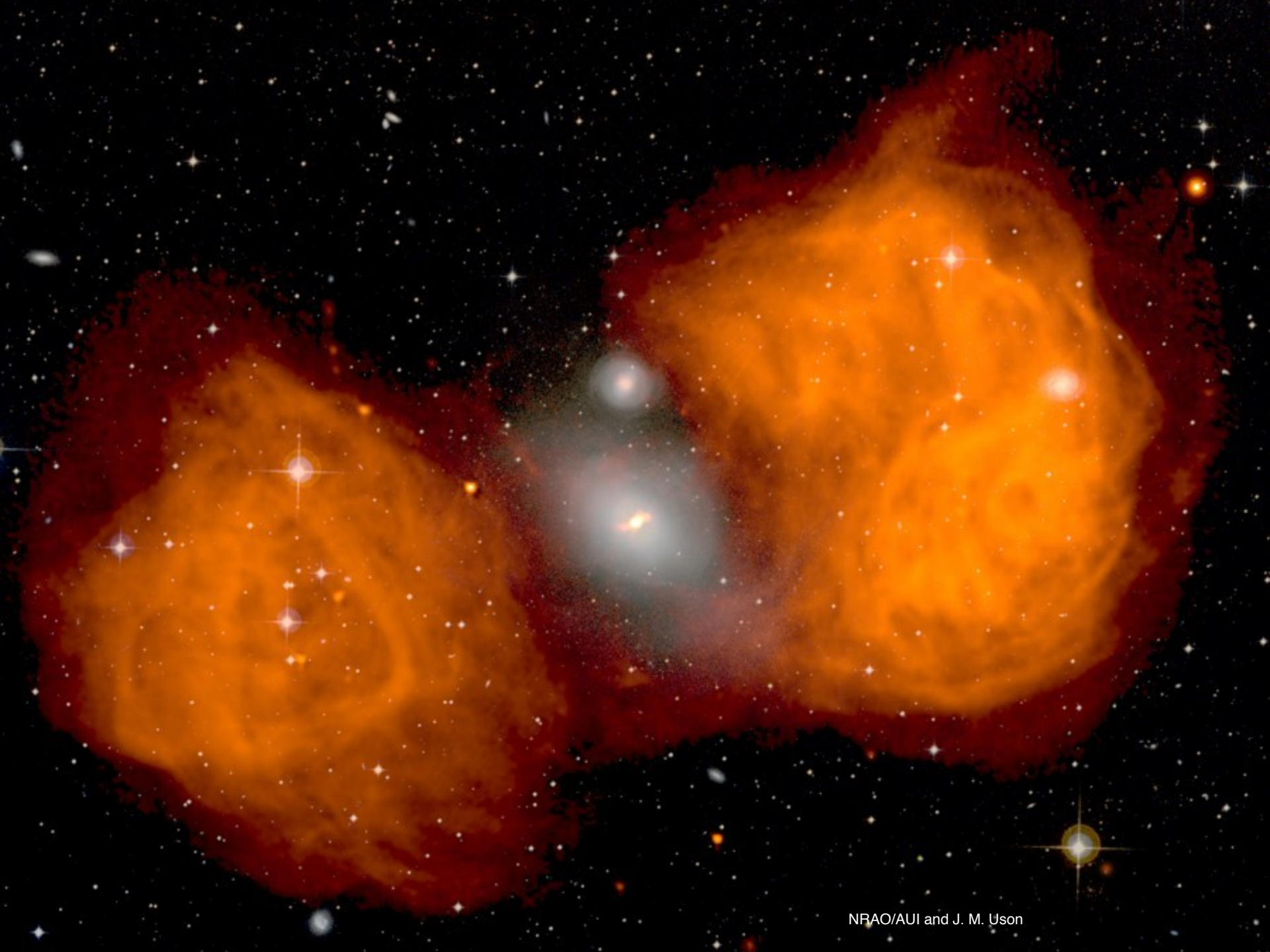


Introduction to (recap of?) Radio Interferometry

Joe Callingham (ASTRON)

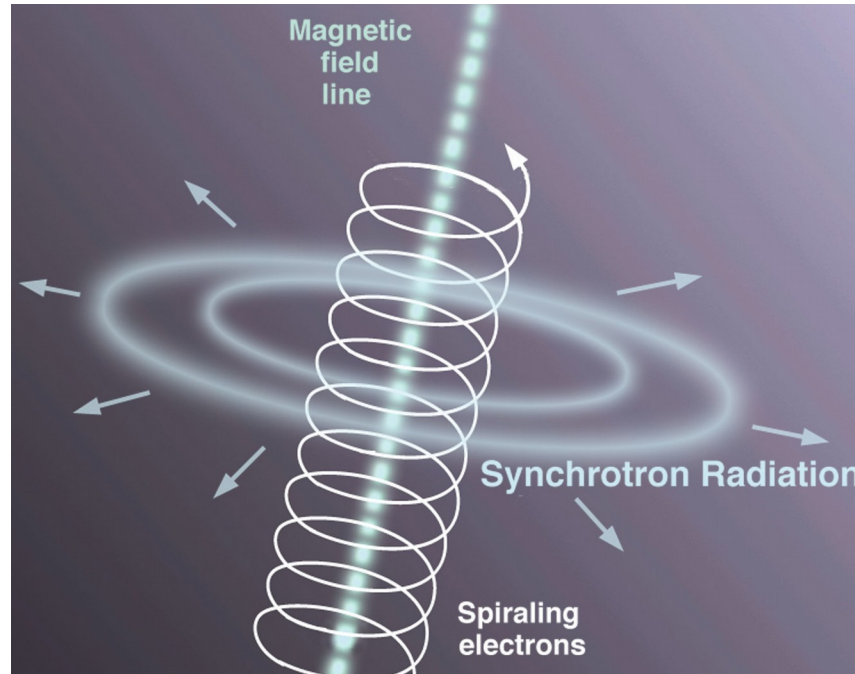
*Kenyan Radio Astronomy School,
Nairobi, Kenya
28th of May 2018*



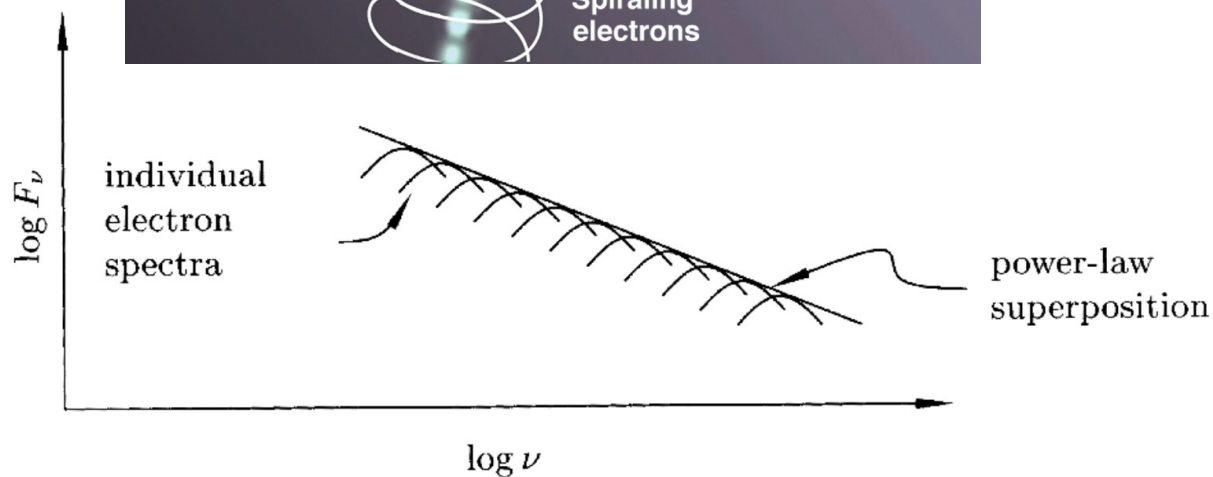


Sync my radiation

- › If the energy distribution of electrons is a power-law – the spectrum will be a power-law
- › Non-thermal
- › Most radio sources are non-thermal

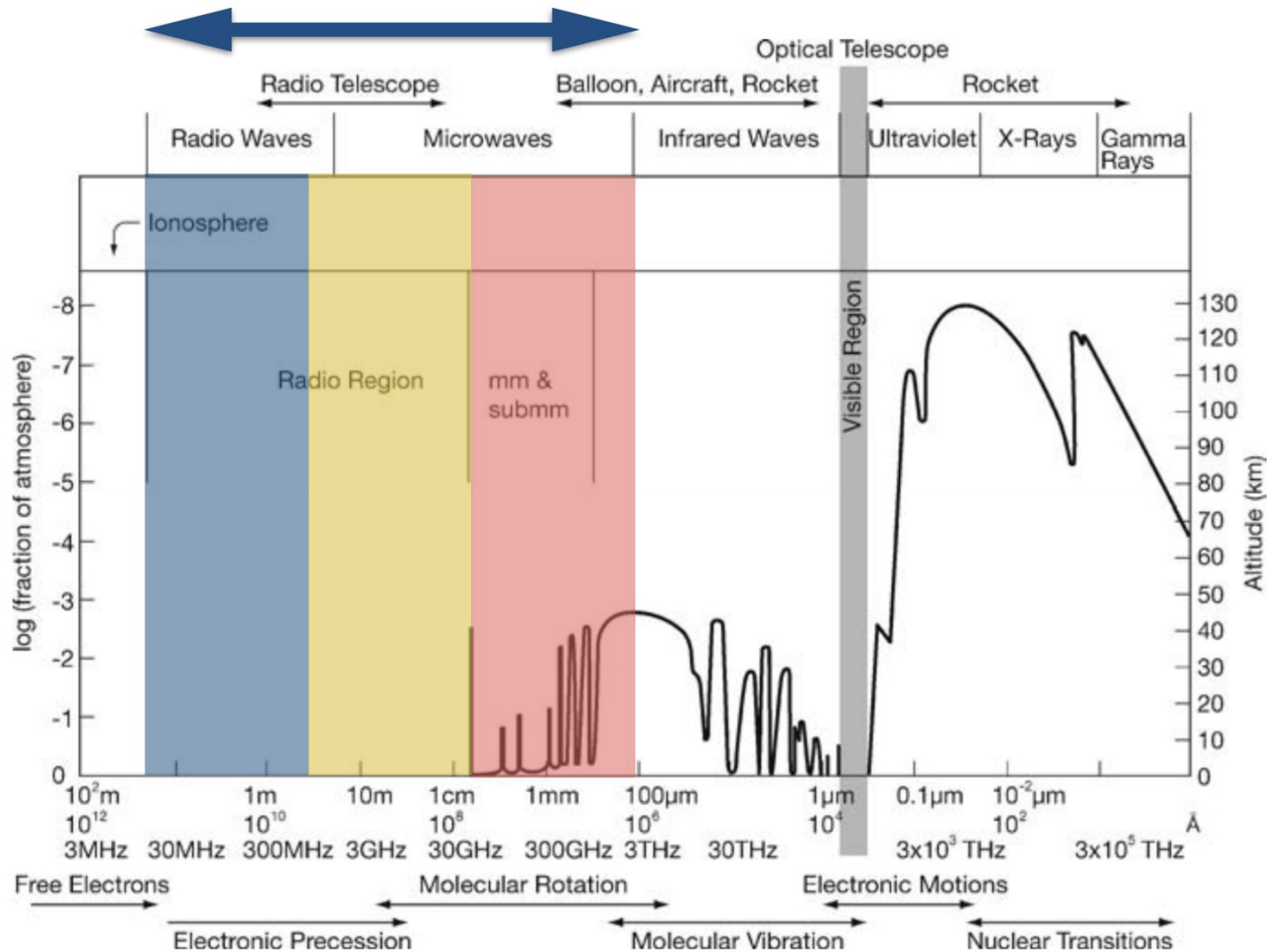


$$S_\nu = a\nu^\alpha$$



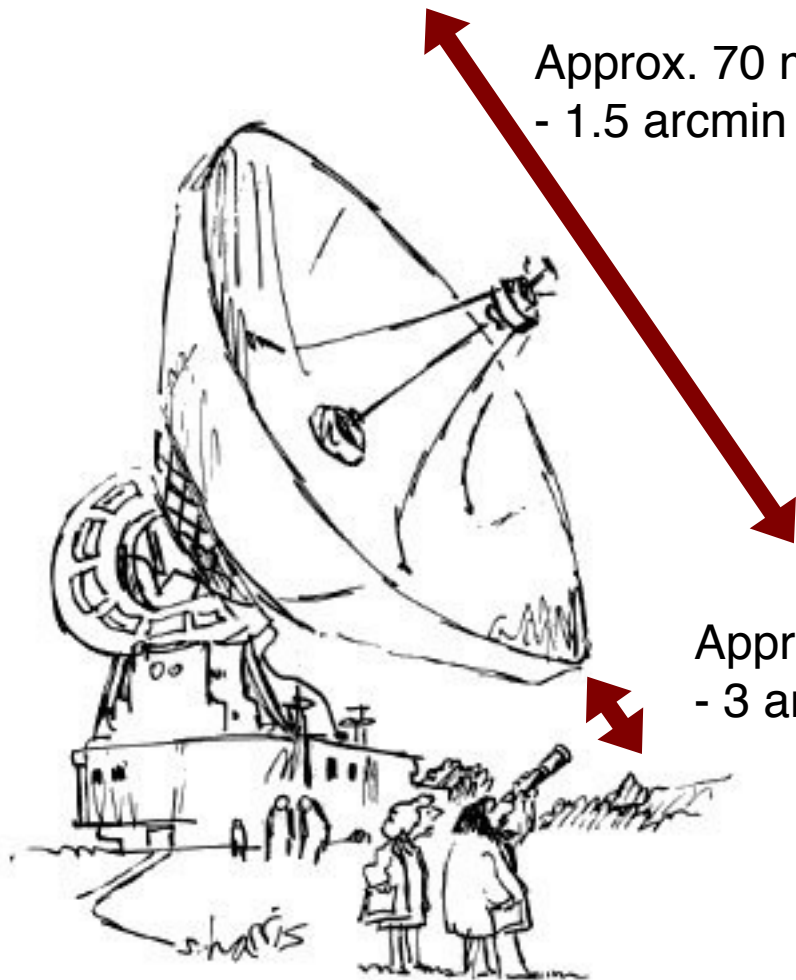
The Radio Sky

- › Radio astronomy mostly focuses in the frequency range of ~ 10 MHz to ~ 1 THz



Why does size matter?

Resolution and sensitivity



"Just checking."

$$\theta \approx \lambda / D$$

Resolution (radians)

Observing wavelength (m)

Diameter of telescope (m)

Approx. 5 mm aperture
- 3 arcsec resolution at 600 nm

$$\text{SEFD} = \frac{2kT_{\text{sys}}}{A_e}$$

When big is not big enough

ASTRON



305 m aperture – 25" resolution at 10 GHz

Human eye has 20" resolution!

Bigger is better?

ASTRON



Green Bank 300 ft Telescope - November 15, 1988

Bigger is better?

ASTRON

There is a better way!

Green Bank 300 ft Telescope - November 16, 1988



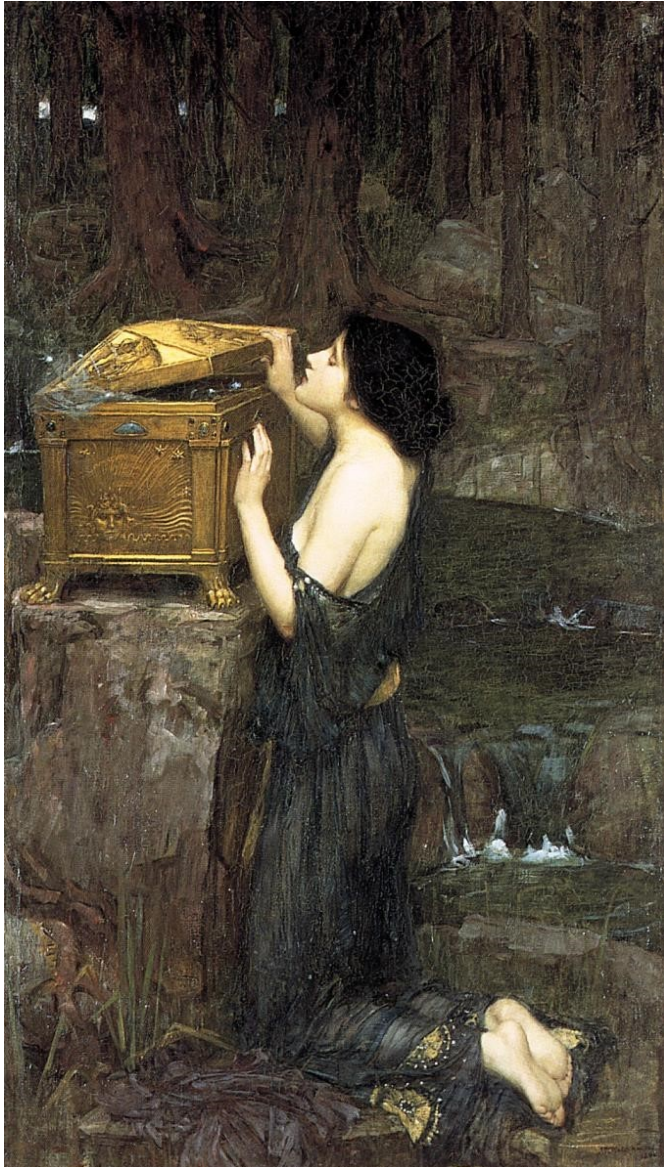
Interferometry to the rescue

$$\theta \approx \lambda/D$$

ASTRON

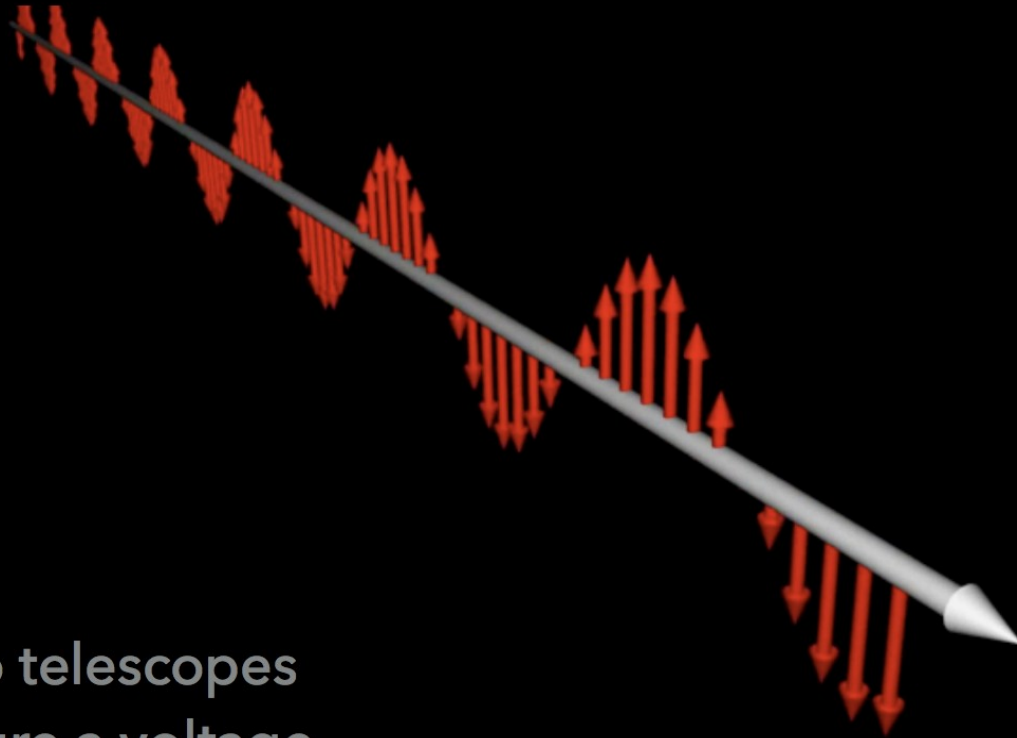


Pandora's Box



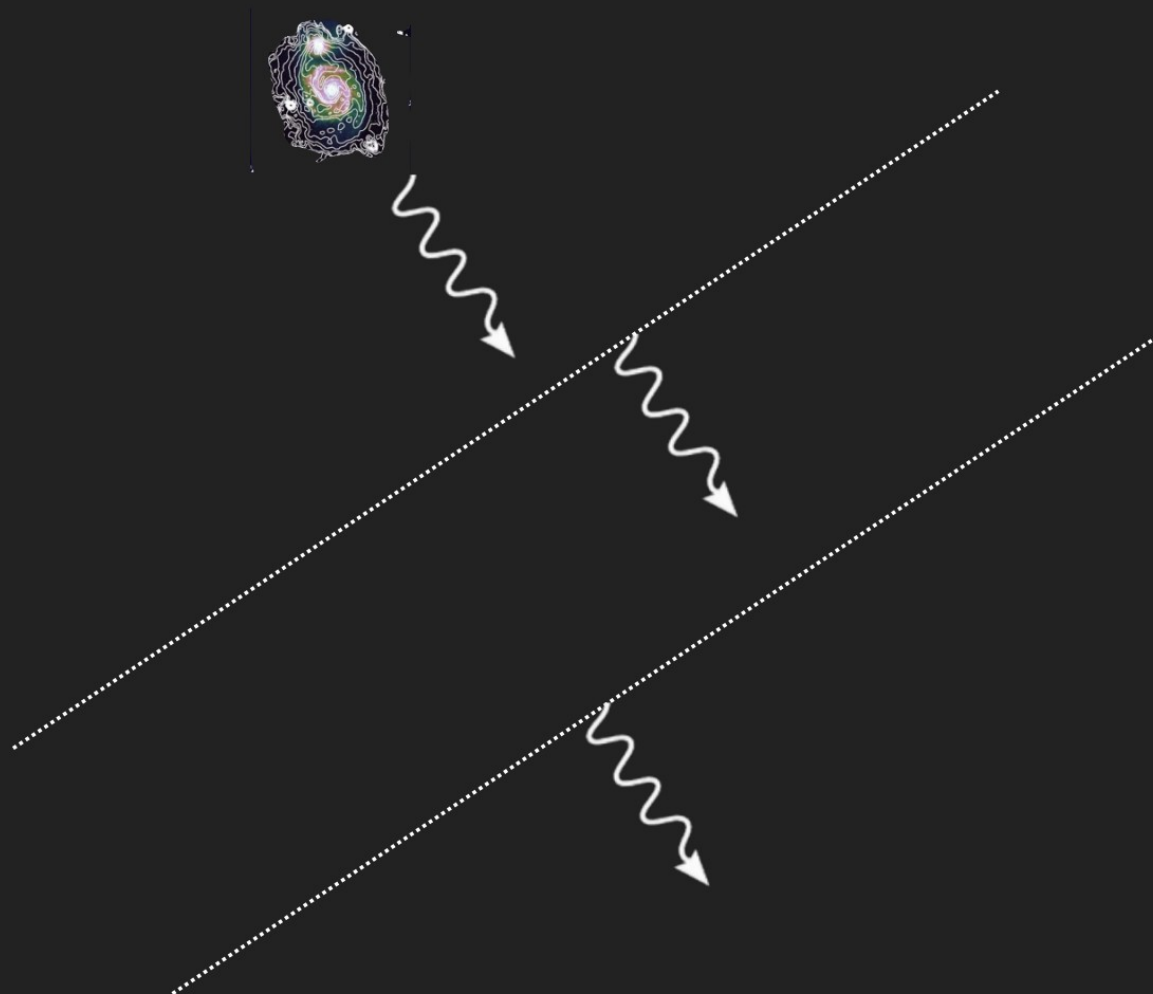
ASTRON

- › Calibration is harder
- › How do you reconstruct the image?
- › What information are you missing?
- › Loss of sensitivity



Radio telescopes
measure a voltage
due to the incident
EM radiation



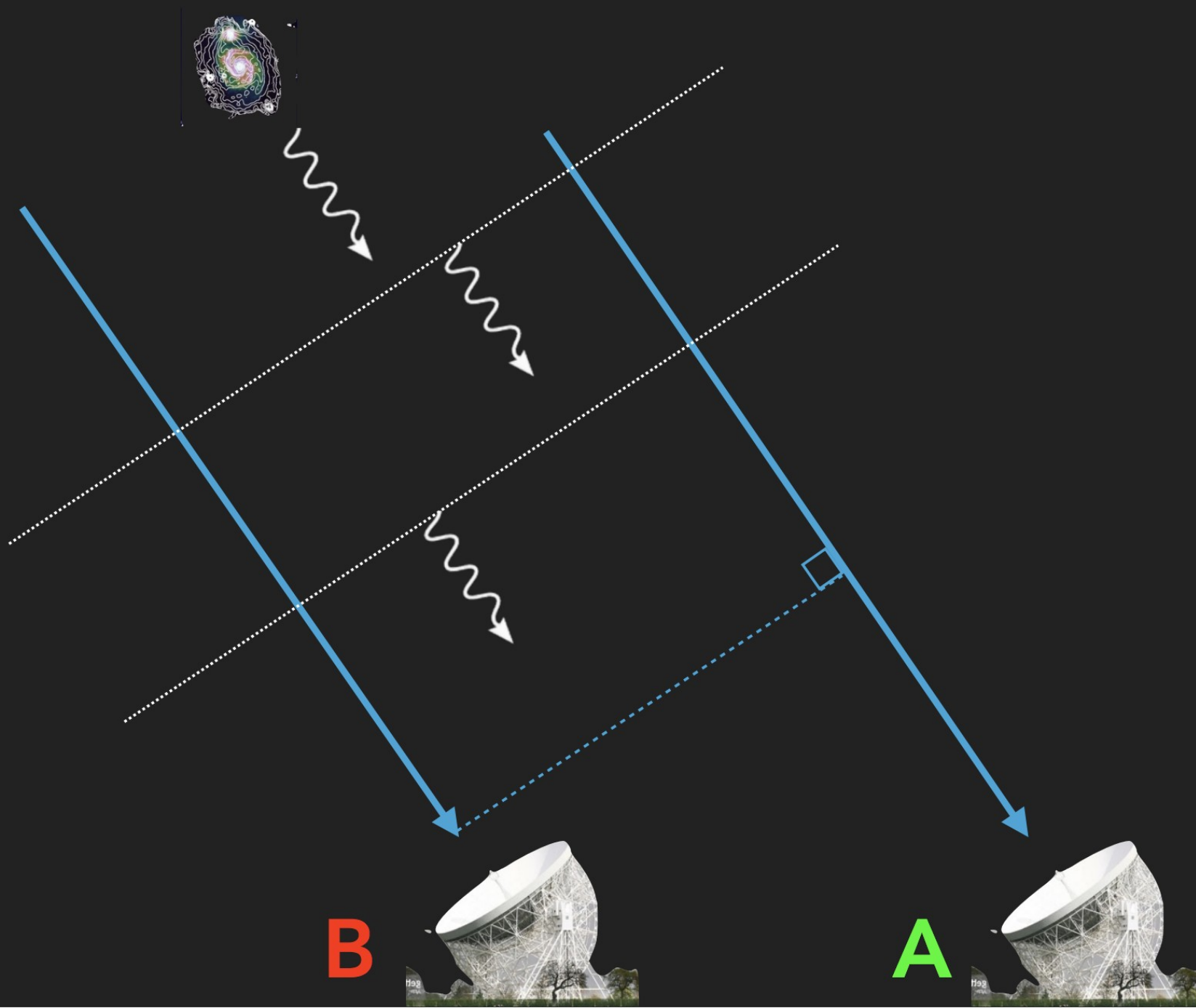


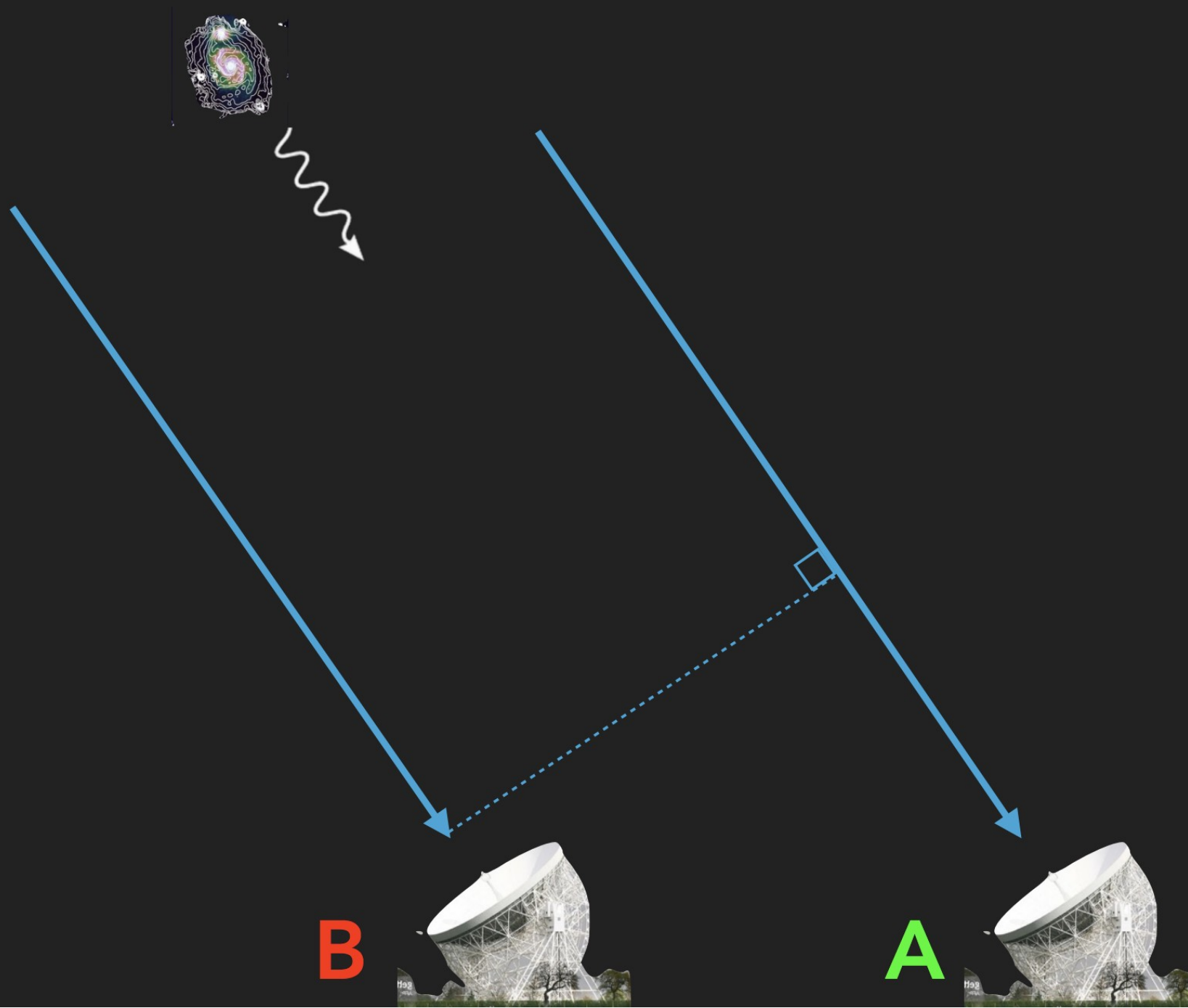
B

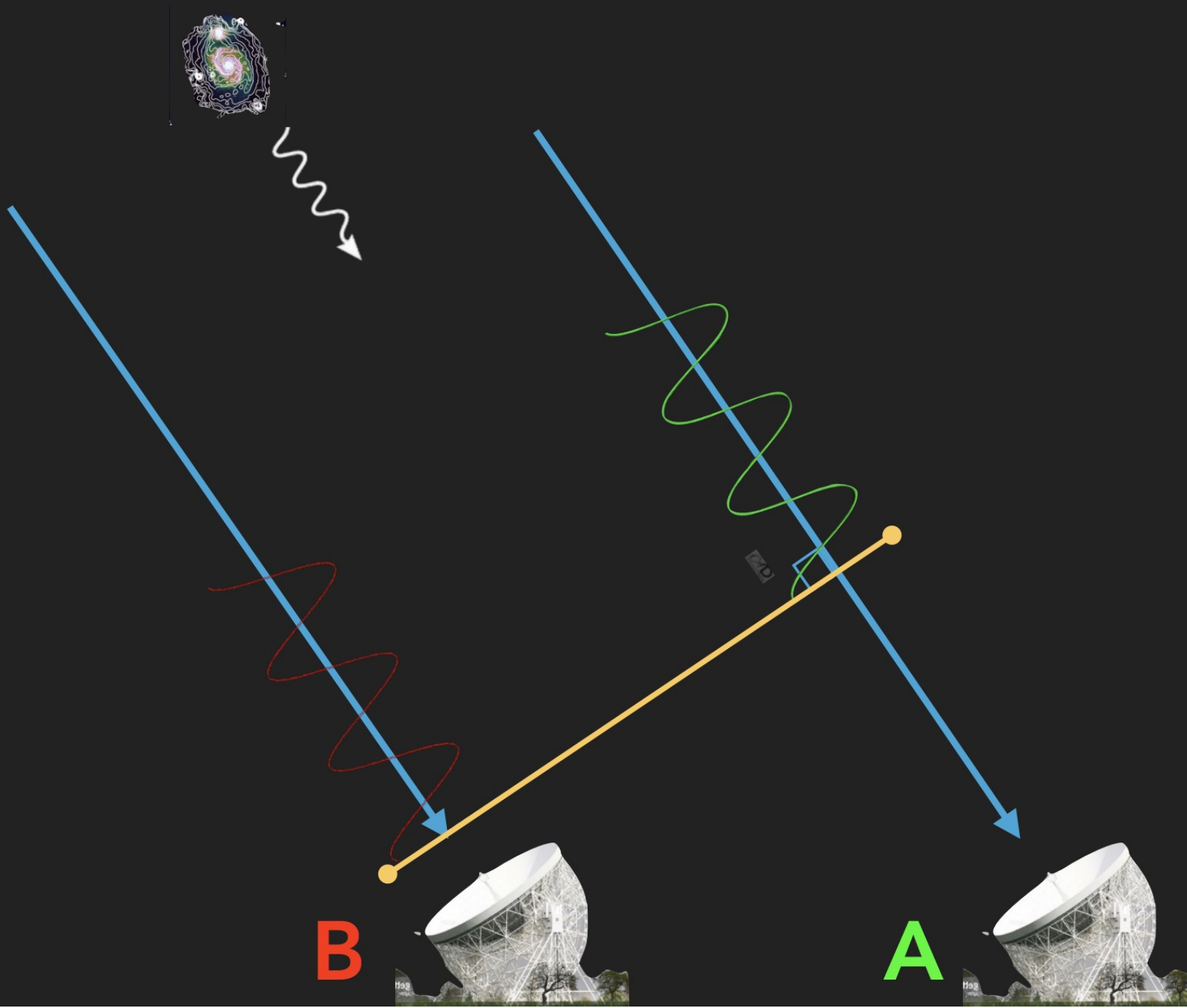


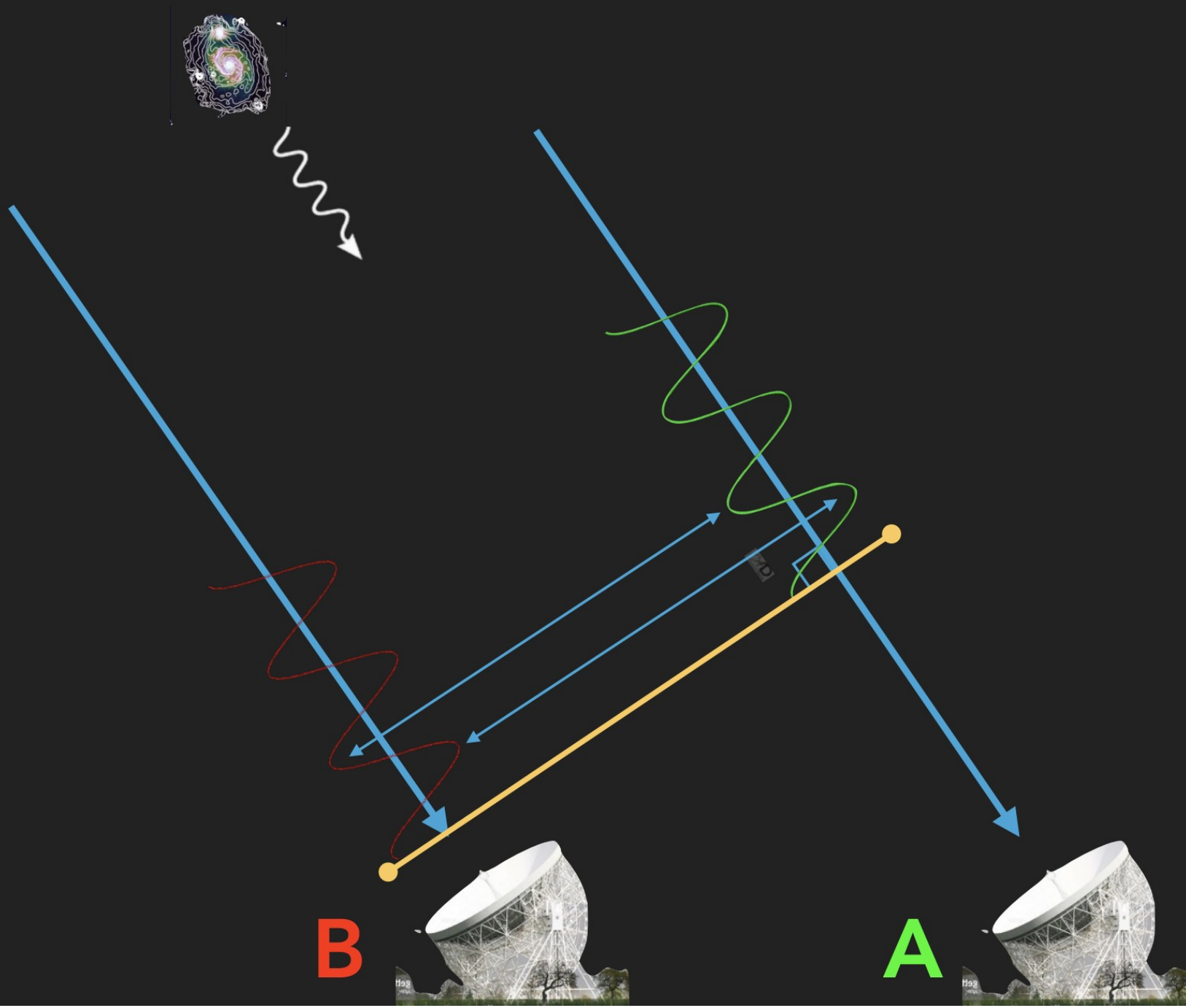
A

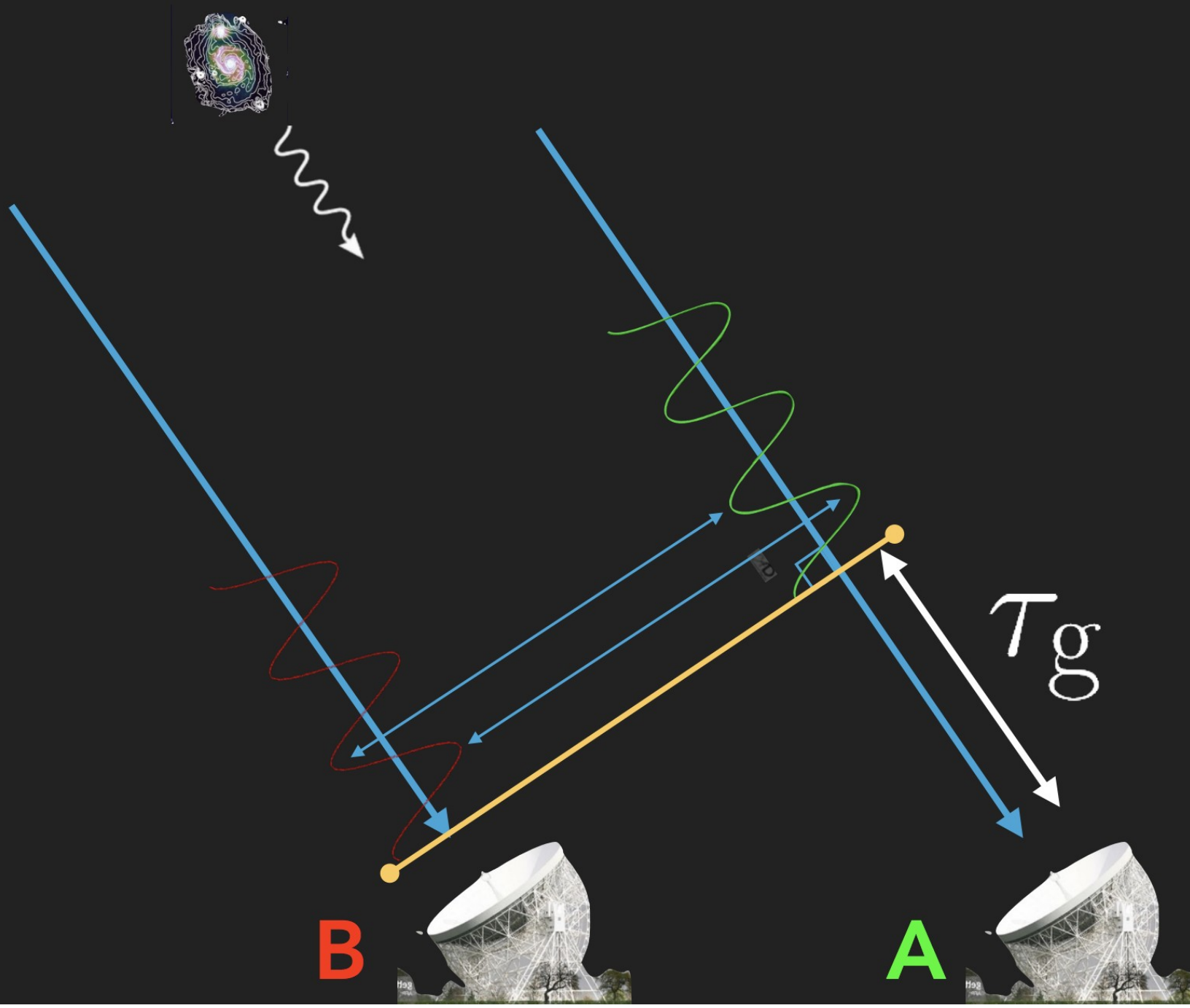




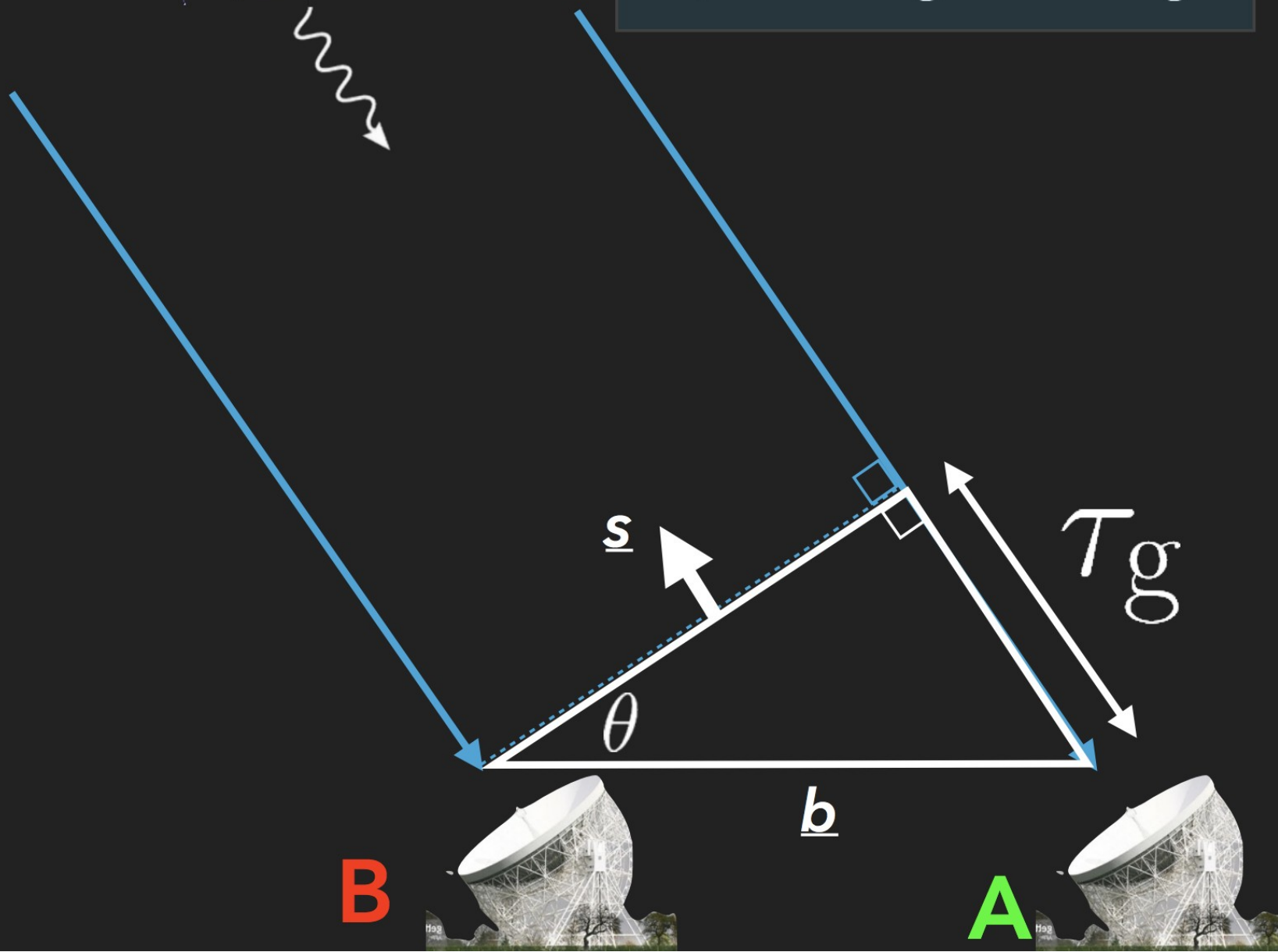


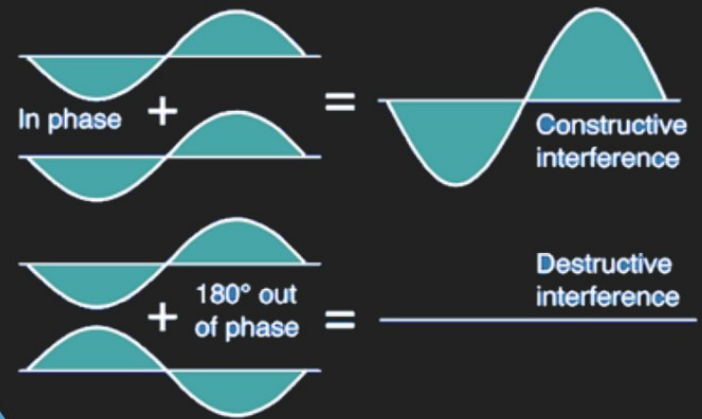






$$\tau_g = \frac{b \sin \theta}{c} = \frac{\vec{b} \cdot \vec{s}}{c}$$





$$V_B \cos \omega t$$

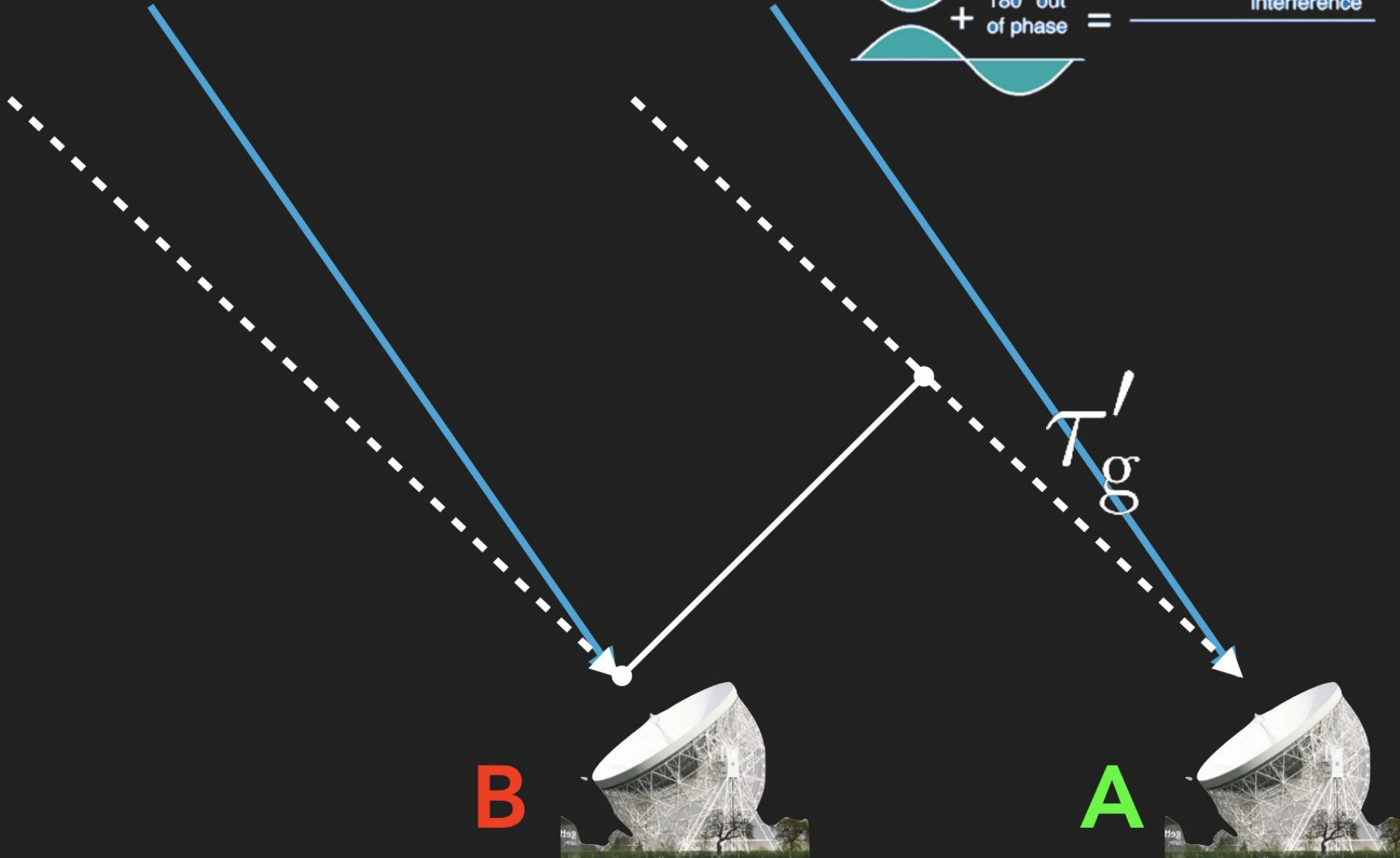
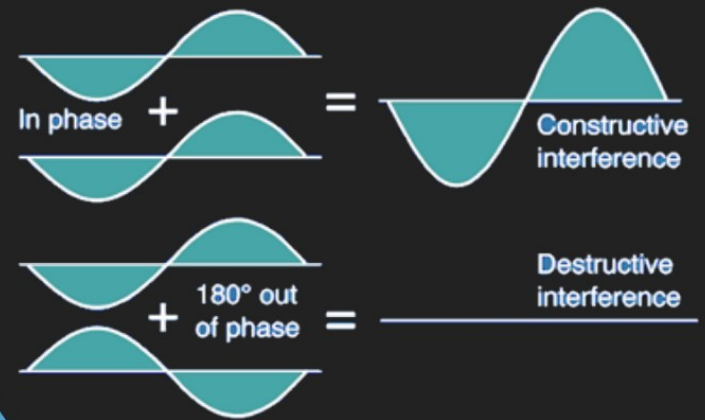
$$V_A \cos \omega(t - \tau_g)$$

B

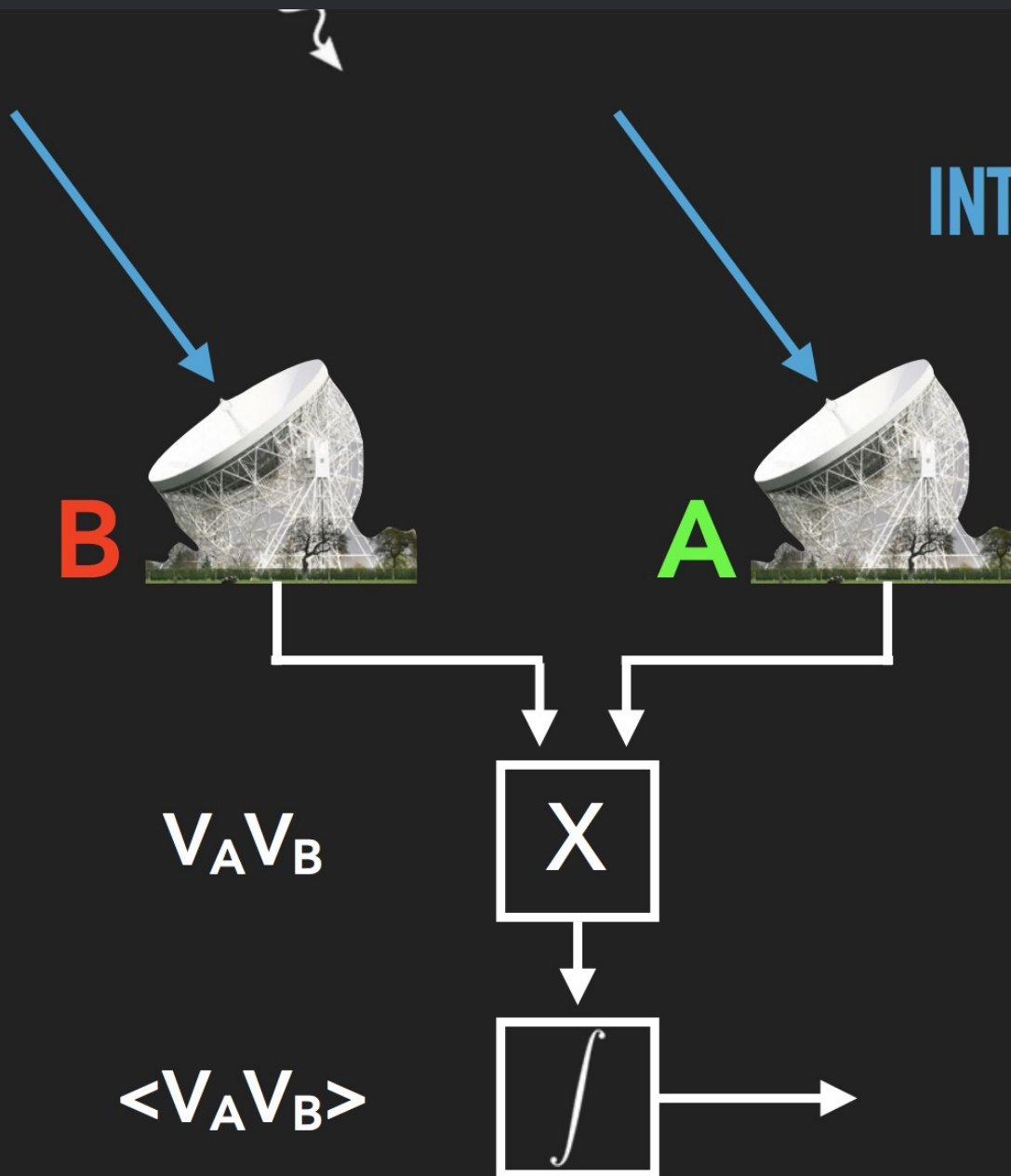


A



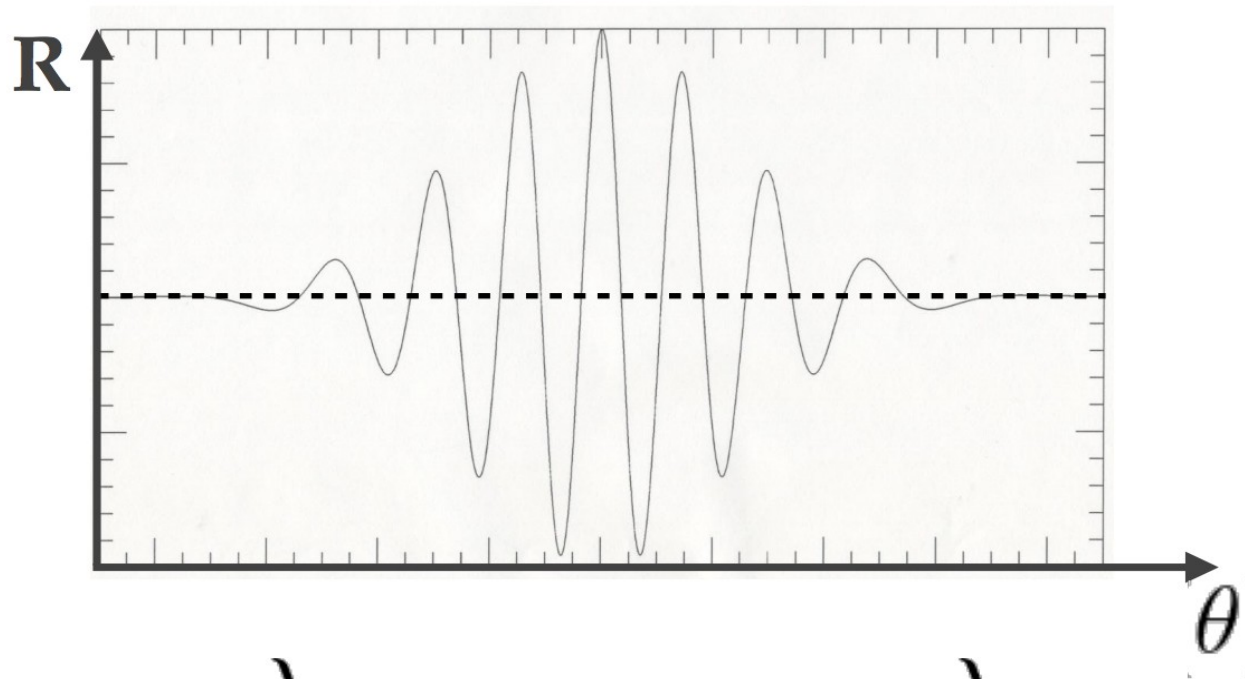


MULTIPLYING INTERFEROMETER



MULTIPLYING INTERFEROMETER

$$R \propto \langle V_A \cos \omega(t - \tau_g) \cdot V_B \cos \omega t \rangle = \frac{1}{2} V_A V_B \cos \tau_g$$

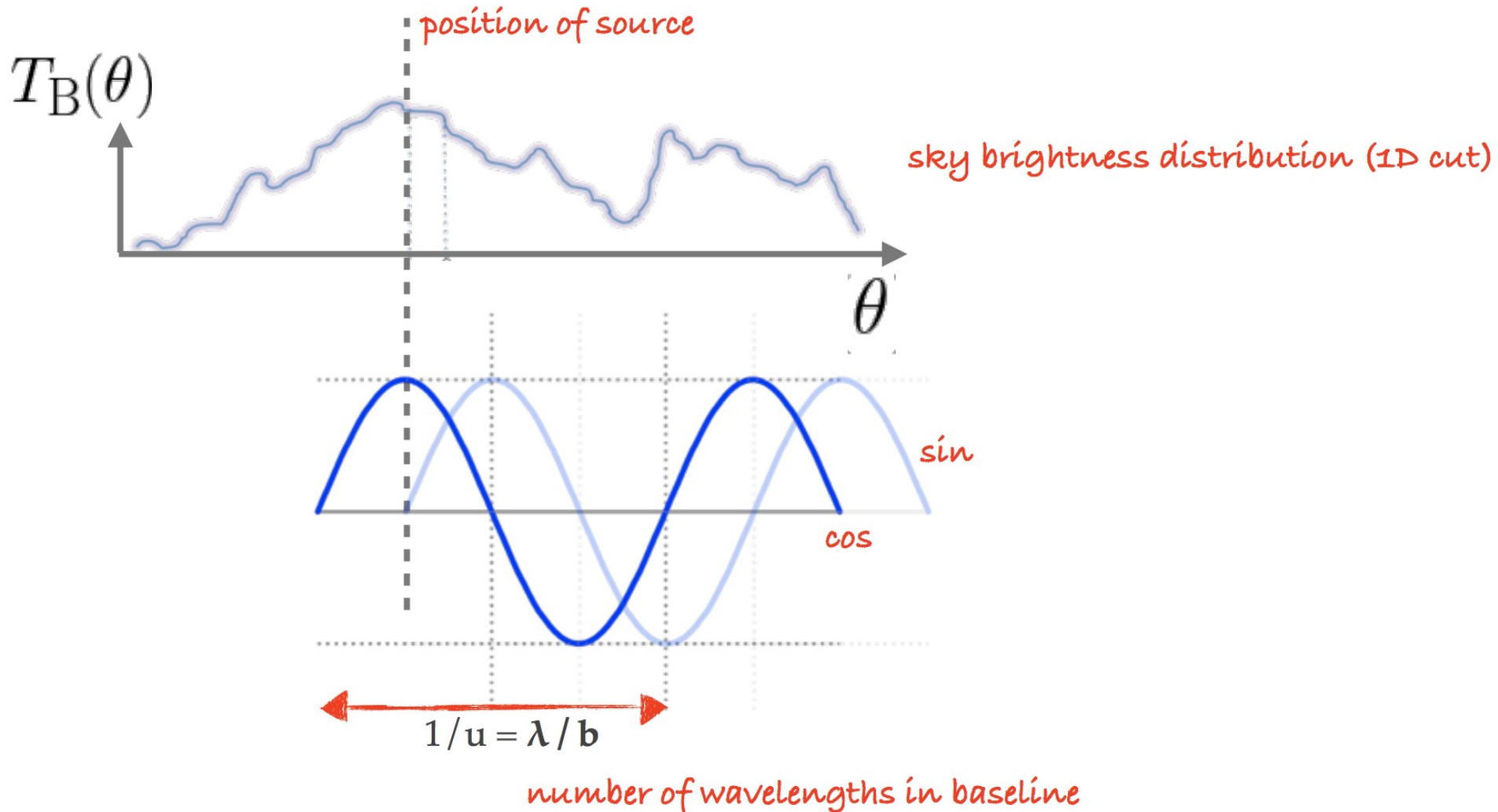


primary beam envelope: $\frac{\lambda}{D}$

fringe spacing: $\frac{\lambda}{b}$

Measuring the sky

ASTRON



Visibilities

In reality the response will be 2D, but in 1D for simplicity:

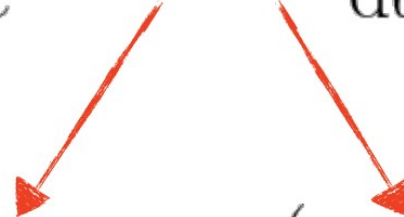
power out as a
function of
baseline

$$R_{\cos}(u) = \int_{\text{src}} B(\theta) \cos(2\pi u \theta) d\theta$$
$$R_{\sin}(u) = \int_{\text{src}} B(\theta) \sin(2\pi u \theta) d\theta$$

The sky brightness distribution is **not an even function**. If we want to reconstruct it from its Fourier components then we need **both the cos and sin terms**.

Van Cittert Zernike function

The (2-D) lateral coherence function of the radiation field in space is the Fourier Transform of the (2-D) brightness (or intensity) distribution of the source.

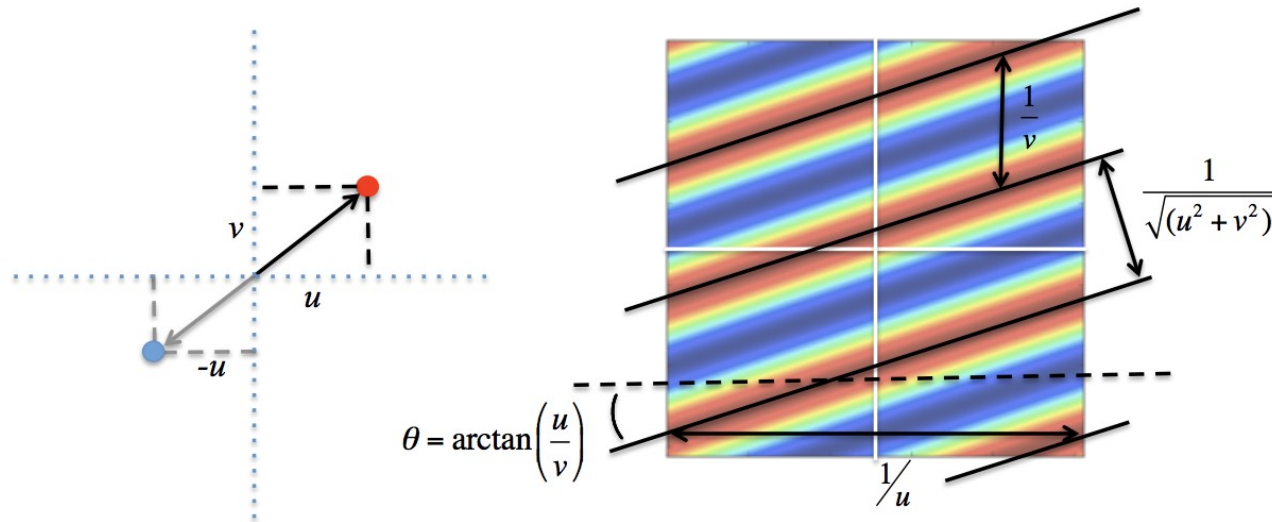
$$\langle V(x_1, t) V(x_2, t) \rangle = \int \int B(\theta, \phi) e^{-2\pi i(u\theta + v\phi)} d\theta d\phi$$

$$u = \frac{(x_1 - x_2)}{\lambda} \quad v = \frac{(y_1 - y_2)}{\lambda}$$

The Visibility Function is therefore another name for the spatial correlation function.

If we change our notation slightly, so that $V = Ae^{i\phi}$, we can write:

$$I_{meas}(l, m) = \frac{1}{M} \sum_{i=1}^M A(u_i, v_i) \cos[2\pi(u_i l + v_i m) + \phi_i]$$

FOURIER COMPONENTS



Writing the equation in this way allows us to visualise how our image is composed.

$$I_{meas}(l, m) = \frac{1}{M} \sum_{i=1}^M A(u_i, v_i) \cos[2\pi(u_i l + v_i m) + \phi_i]$$

Summary

- › The key to interferometry is the geometric delay
- › The sky is not symmetric - we need both cosine & sine waves to make a picture of it
- › Interferometers measure complex visibilities, which are the Fourier components of the sky brightness.



› Thanks to
Anna Scaife,
Ron Ekers,
and John
McKean