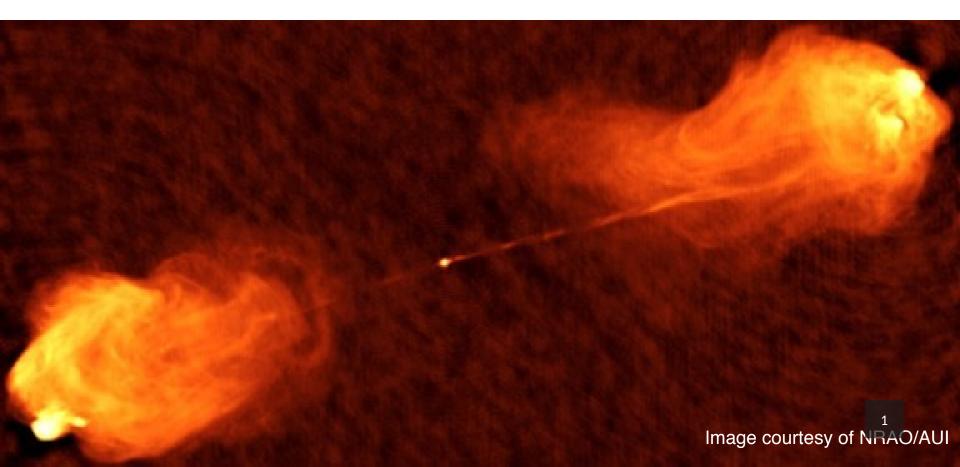


ADVANCED RADIO INTERFEROMETRIC IMAGING

Joe Callingham - Credits: J. Radcliffe, A. Offringa (ERIS 2017)



INTRODUCTION

Topics discussed:

- Recap of CLEAN
- When to use multi-scale or other deconvolution methods
- The effect of and solution to w-terms
- Multi-term deconvolution
- Self-calibration using CLEAN components
- Primary beam correction
- Mosaicing
- Direction-dependent effects during imaging

INTRODUCTION

After calibration the visibilities are represented by (+ errors):

$$V(u, v, w) = \iint \frac{I(l, m)}{\sqrt{1 - l^2 - m^2}} e^{-2\pi i (ul + vm + w(\sqrt{1 - l^2 - m^2} - 1))} dl dm$$

$$(u, v, w) \text{ interferometer's geometrical vector}$$

$$(l, m) \quad \text{sky position}$$

$$I(l, m) \quad \text{sky brightness (our 'image')}$$
Want to calculate $I(l, m)$ from $V(u, v, w)$

Nb: (1, mNb:) notation is essentially the same as (coordinates died in the previous talks

INTRODUCTION

$$V(u,v,w) = \iint \frac{I(l,m)}{\sqrt{1-l^2-m^2}} e^{-2\pi i(ul+vm+w(\sqrt{1-l^2-m^2}-1))} dldm$$

If we have a small field of view ($I \sim 0$, $m \sim 0$) then $w \rightarrow 0$:

$$V(u,v) \approx \iint I(l,m)e^{-2\pi i(ul+vm)}dldm$$

The relationship between V(u, v) and I(l, m) is?

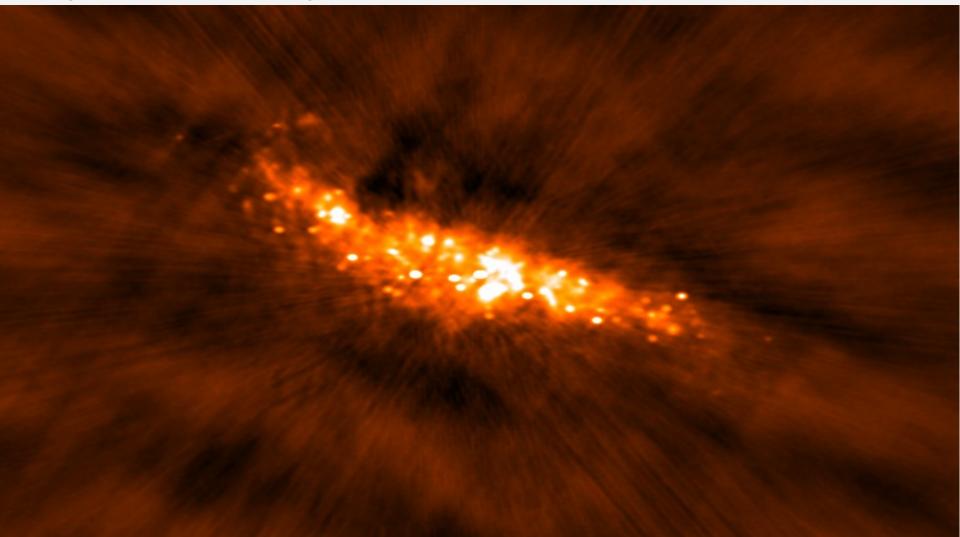


The Högbom algorithm (1974)

- 1. Find the strength and position of the brightest peak.
- 2. Subtract the dirty beam x peak strength x loop gain/damping factor position of the peak, the dirty beam B multiplied by the peak strength and a damping factor (usually termed the loop gain).
- 3. Go to 1. unless any remaining peak is below some user-specified level or number of interations reached.
- 4. Convolve the accumulated point source model with an idealized `CLEAN' beam (usually an elliptical Gaussian fitted to the central lobe of the dirty beam).
- 5. Add the residuals of the dirty image to the `CLEAN' image.

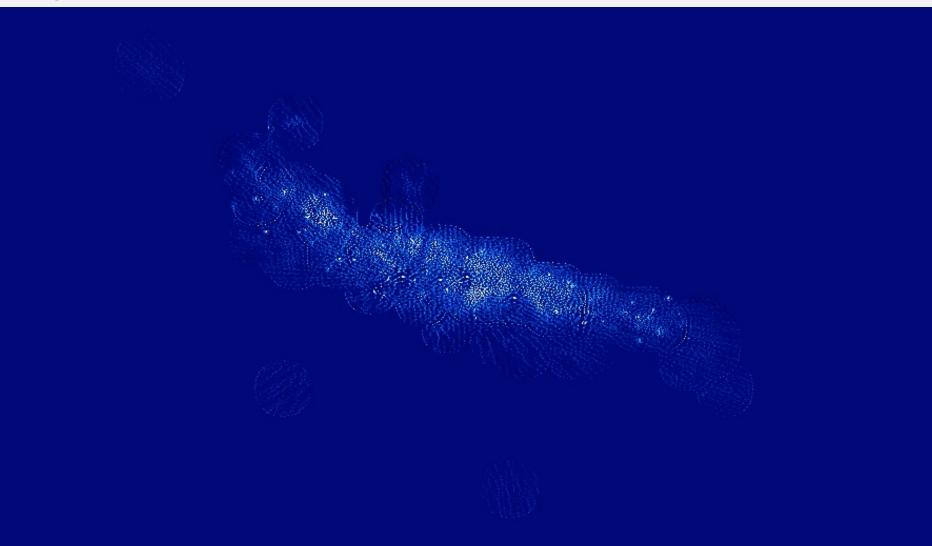
HÖGBOM CLEAN IN ACTION

Hogbom CLEANED image



CLEAN IMAGE & MODEL

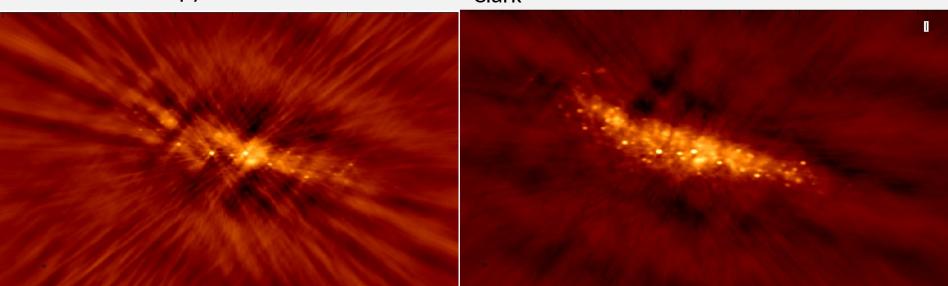
Hogbom CLEANED model

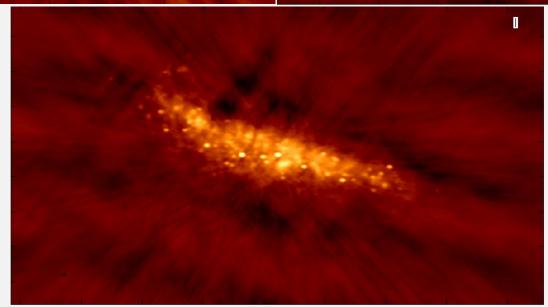


THE MANY FORMS OF CLEAN

Maximum Entropy Method

Clark





Clark-Stokes

DECONVOLVING DIFFUSE STRUCTURE

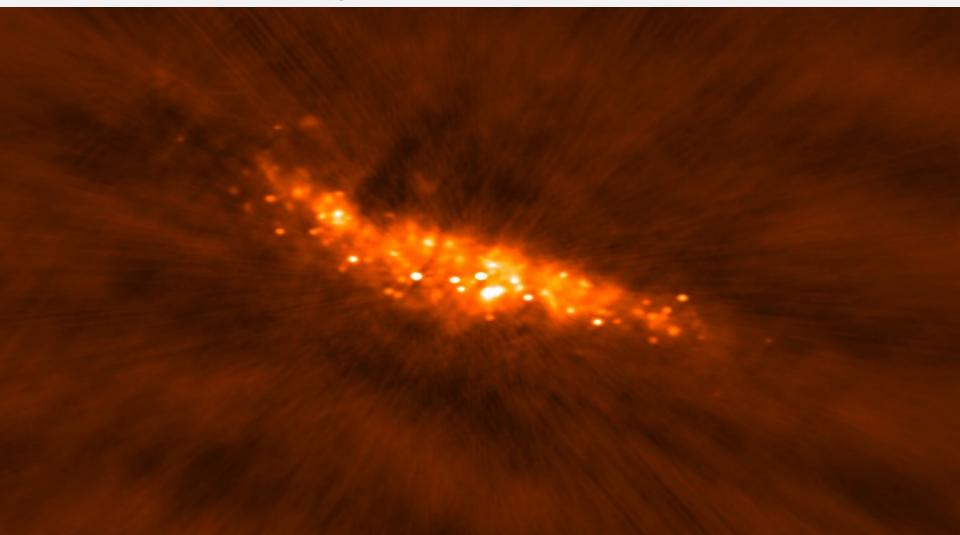
- Improved algorithm by Cornwell (2008) : "multi-scale clean"
- Fits small smooth Gaussian kernels (and delta functions) during a Högbom CLEAN iteration
- Implemented in CASA clean & tclean. Advised to use pixel scales corresponding to orders of the dirty beam size and avoid making scale too large compared to the image width/lowest spatial frequency.
- E.g. For example, if the synthesized beam is 10" FWHM and cell=2", try multiscale = [0,5,15]

deconvolver scales smallscalebias restoringbeam		<pre># Minor cycle algorithm (hogbom,clark,m # ultiscale,mtmfs,mem,clarkstokes) # List of scale sizes (in pixels) for # multi-scale algorithms # A bias towards smaller scale sizes # Restoring beam shape to use. Default # is the PSF main lobe</pre>	CASA tclean
multiscale negcomponent smallscalebias	= [0, 1, 5, 15] = -1 = 0.6	<pre># Deconvolution scales (pixels); [] = # standard clean # Stop cleaning if the largest scale # finds this number of neg components # a bias to give more weight toward # smaller scales</pre>	CASA clean

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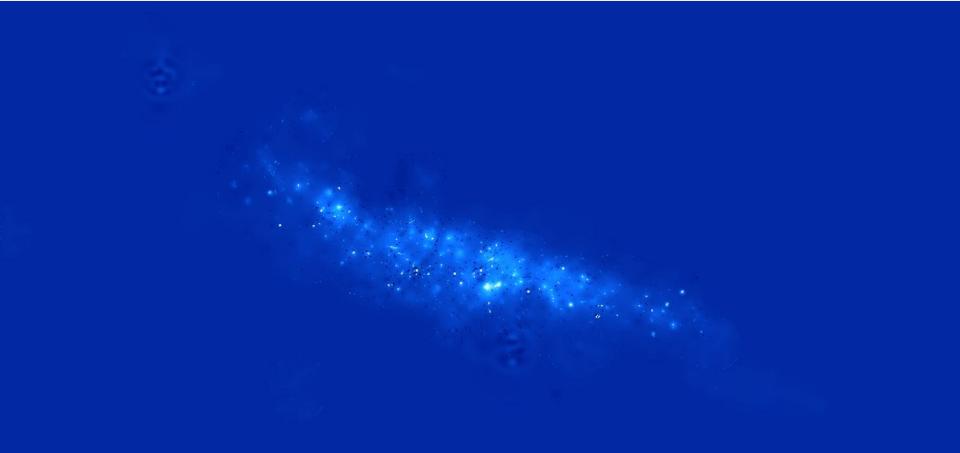
MULTI-SCALE CLEAN

Multi-scale CLEANED image



MULTI-SCALE CLEAN

Multi-scale CLEANED model



WIDE-FIELD IMAGING

2D Fourier Transform does not hold for new sensitive, wide-band, wide-field arrays

Non co-planar baselines becomes a problem i.e. l,m,w >> 0

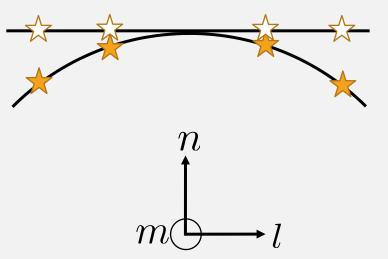
$$V(u, v, w) = \iint \frac{I(l, m)}{\sqrt{1 - l^2 - m^2}} e^{-2\pi i (ul + vm + w(\sqrt{1 - l^2 - m^2} - 1))} dl dm$$

Three-dimensional visibility fuction can be transformed to a threedimensional regional image with the three-dimensional image volume I(l, m, n) - this is not physical direction cosines.

The only non-zero values of life on the surface of a sphere of unit radius defined by $n = \sqrt{1 - l^2 - m^2}$

WIDE-FIELD IMAGING

The sky brightness consisting of a number of discrete sources \bigstar are transformed onto the surface of this sphere.



The two-dimensional image \overleftrightarrow is recovered by projection onto the tangent plane at the pointing centre

Soothow do we achieve this? Two solutions available:

- ii. Facetting split the field into multiple images and stitch them together
- iii. w-projection most used solution, effectively performs the above to recover I(l, m)

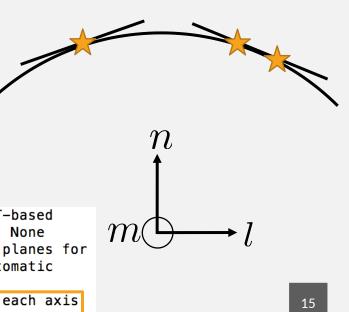
Both available in CASA! Both available in CASA!

i. FACETING

- Takes advantage of the small field approximation (I,m~0) so the image sphere is approximated by pieces of many smaller tangent planes.
- Within each sub-field, standard two-dimensional FFTs may be used.
- Errors increase quadratically away from the centre of each sub-field, but these are acceptable if enough sub-fields are selected.
- Facets can be selected so as to cover known sources.
- Facets may overlap allowing complete coverage of the primary beam

CASA clean implementation

gridmode wprojplanes	= 'wide =	field' 1	<pre># Gridding kernel for FFT-based # transforms, default='' None # Number of w-projection planes for # convolution; -1 => automatic # determination</pre>
facets	=	8	<pre># Number of facets along each axis # (main image only)</pre>



ii. w-PROJECTION

$$V(u,v,w) * \mathfrak{F}(e^{-2\pi i w(\sqrt{1-l^2-m^2}-1)}) = \iint \frac{I(l,m)}{\sqrt{1-l^2-m^2}} e^{-2\pi i (ul+vm)} dl dm$$

- Very dependent on zenith angle, co-planarity of array, field of view and resolution.
- Convolution theorem no longer works when w-terms present.
- CLEAN assumes constant PSF, but PSF changes (slightly) over the image.
- Solved with Cotton-Schwab algorithm (Schwab 1984) (used in CASA automatically).

ii. w-PROJECTION

The Cotton-Schwab + w-projection algorithm:

- 1) Make initial dirty image & central PSF Perform minor iterations:
 - Find peak
 - Subtract scaled PSF at peak with small gain
 - Repeat until highest peak ~80-90% decreased

2) Major iteration: 'Correct' residual

- Predict visibility for current model
- Subtract predicted contribution and re-image

wprojplanes = -1 # Number of w-projection planes for	CASA clean implementation
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w-PROJECTION

Source: Away from the pointing centre

No w-projection



w-projection

Small field approximation breaks and you need w-projection!

MULTI-FREQUENCY SYNTHESIS

Multi-frequency synthesis (MFS) means gridding different frequencies on the same uv grid

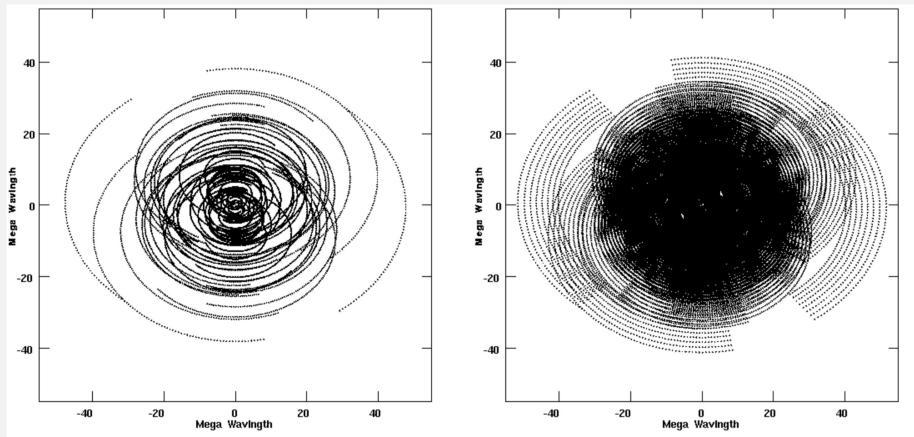
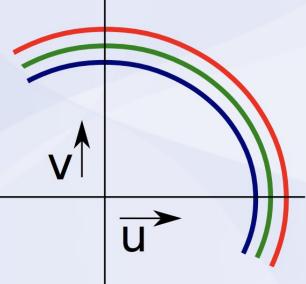


Figure 16.1: Left (a): VLBA (u, v) coverage for a full track at $\delta = 50^{\circ}$. Right (b): Using MFS observations with 8 frequencies spread over 25%.

Conway & Sault (1995)

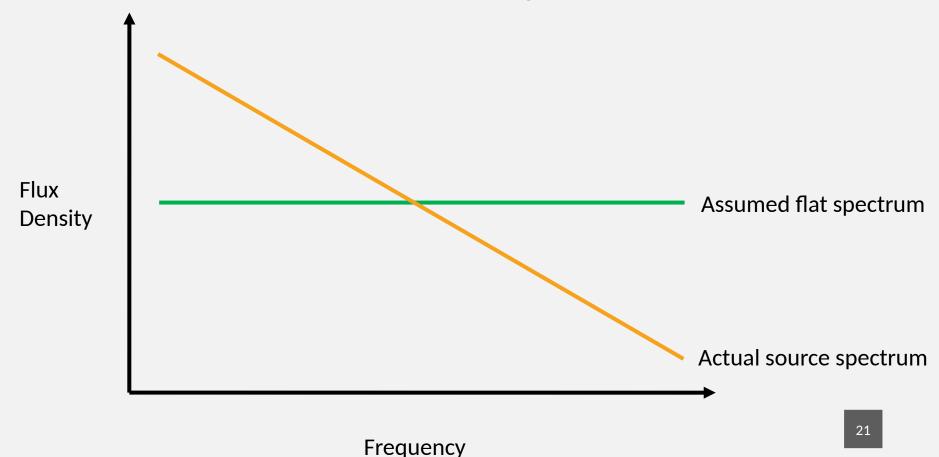
MULTI-FREQUENCY SYNTHESIS

 Multi-frequency synthesis (MFS) means gridding different frequencies on the same uv grid:



Similar but not the same! (same name often used). Also known as multiterm deconvolution (as in CASA).

Takes spectral variation into account during deconvolution



I #presents the the strais sion in terms of so Tay lary beries about out efference frequency:

$$I_{\nu}^{m} = \sum_{t=0}^{N_{t}-1} b_{\nu}^{t} I_{t}^{\text{sky}} \text{ where } b_{\nu}^{t} = \left(\frac{\nu - \nu_{0}}{\nu_{0}}\right)^{t}$$

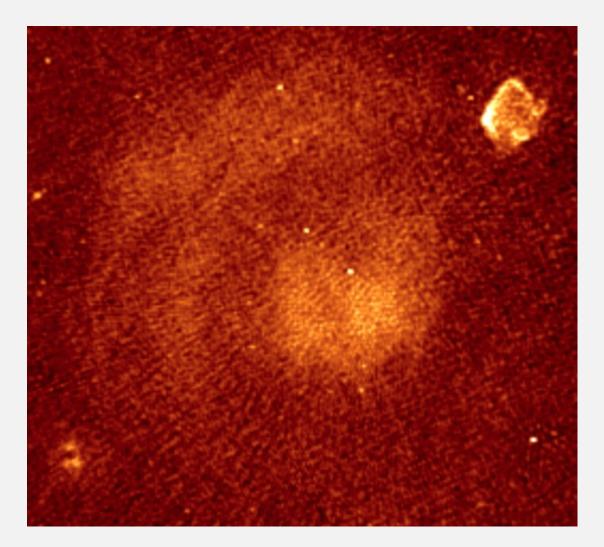
A power model is used to describe the spectral dependence of the sky. One practical choice is a power law with emission.

$$I_{\nu}^{\rm sky} = I_{\nu_0}^{\rm sky} \left(\frac{\nu}{\nu_0}\right)^{I_{\alpha}^{\rm sky} + I_{\beta}^{\rm sky} \log\left(\frac{\nu}{\nu_0}\right)}$$

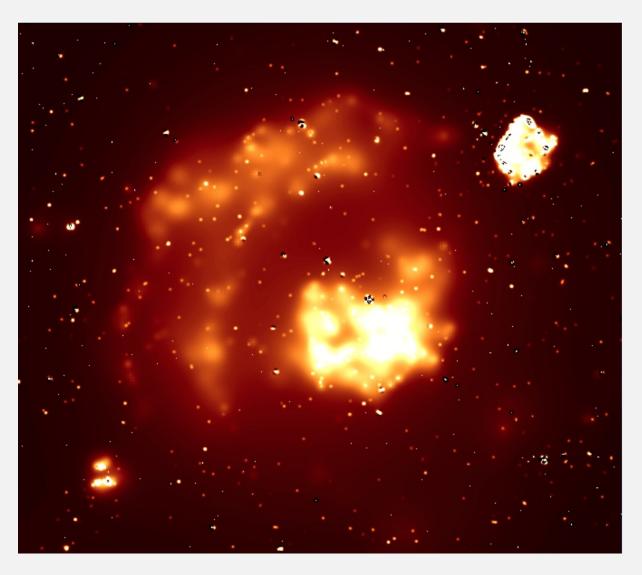
Useful for wideband, sensitive imaging. Incorporated in CASA in combination with multi-scale CLEAN as 'mtmfs'

- Recent focus on deconvolution using 'Compressed Sensing' (abbrev.
 CS but CS can mean 'Cotton-Schwab' too)
- CS methods assume the sky is 'sparse' ("solution matrix is sparse in some basis")
- Minimizes "L1-norm" (= abs sum of CLEAN components)
- Högbom clean is actually (almost) a compressed sensing method called "Matching Pursuit"
- CS considers MP to be non-ideal... but radio data is not the perfect CS case: Calibration errors, w-terms

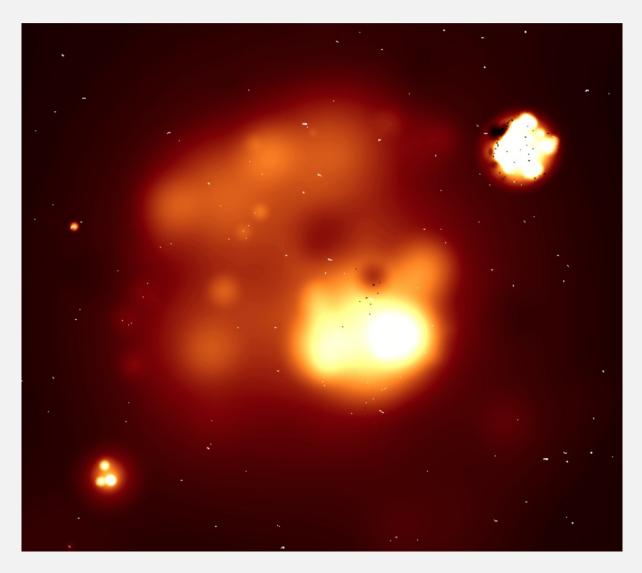
Source structure looks like (Hogborn cleaned):



Model using CS:



Model using multiscale:



- Compressed sensing does not work well with calibration artefacts
- Multi-scale is more **robust**
- On well-calibrated data:

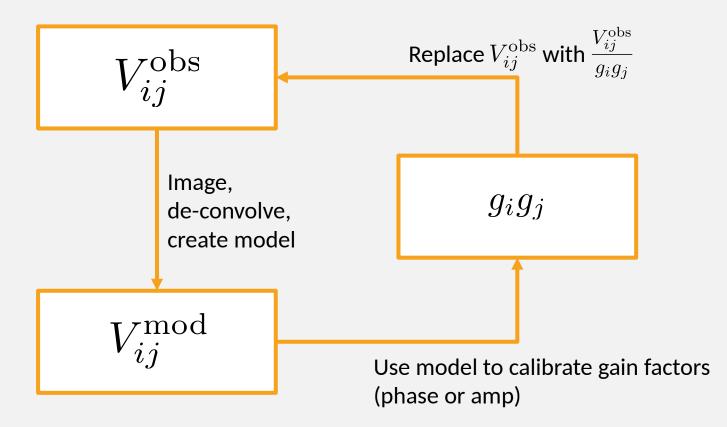
CS gives more accurate model But residuals don't improve much

 Not implemented in CASA (only available in specialised LOFAR image (AWImagerCS) or stand-alone packages e.g. Purify

SELF-CALIBRATION USING CLEAN

Self-calibration recap:

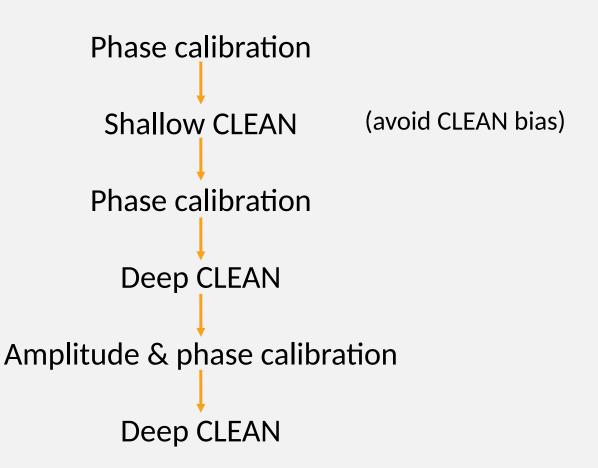
Given:
$$V_{ij}^{
m obs} = g_i g_j V_{ij}^{
m real}$$



And.. repeat until model/solution converges!

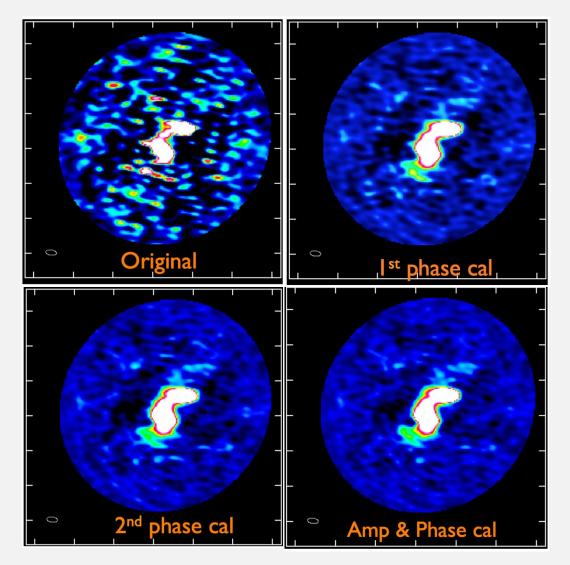
SELF-CALIBRATION USING CLEAN

- Clean components can be used as calibration model
- Often applied as:



SELF-CALIBRATION USING CLEAN

ALMA SV Data for IRAS16293 Band 6



PRIMARY BEAM CORRECTION

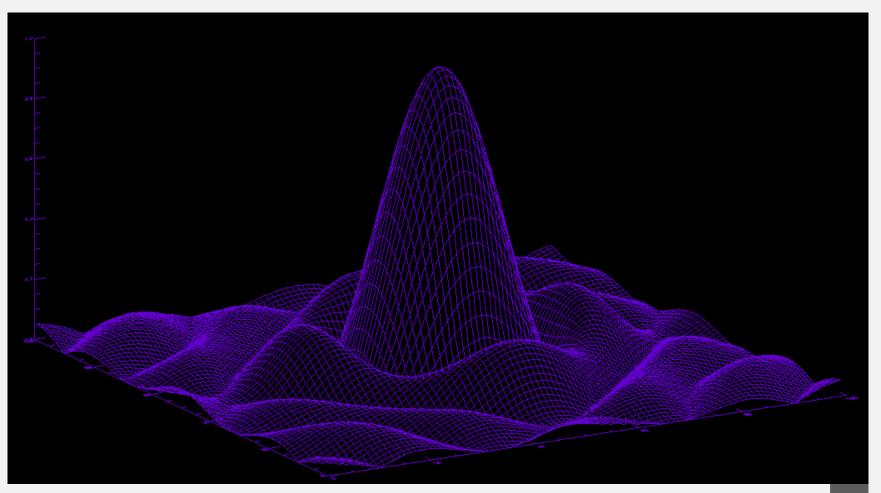
- Correction is required for the antenna response
- This is called "primary beam" correction (as opposed to the synthesized beam / psf)
- For dishes, the primary beam is ~constant but can be very complex away from the FWHM.

To correct for: multiply final image with the inverse beam!

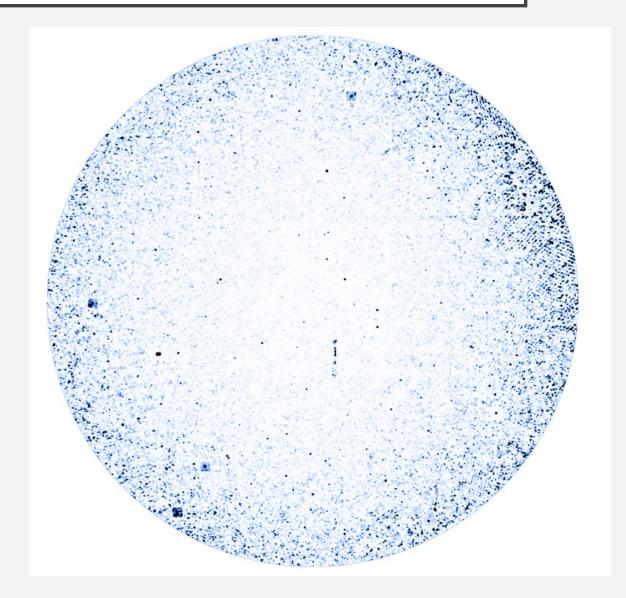
Scalar for total brightness, matrix for polarized

PRIMARY BEAM CORRECTION

Complex sidelobe structure + asymmetries!



PRIMARY BEAM CORRECTION

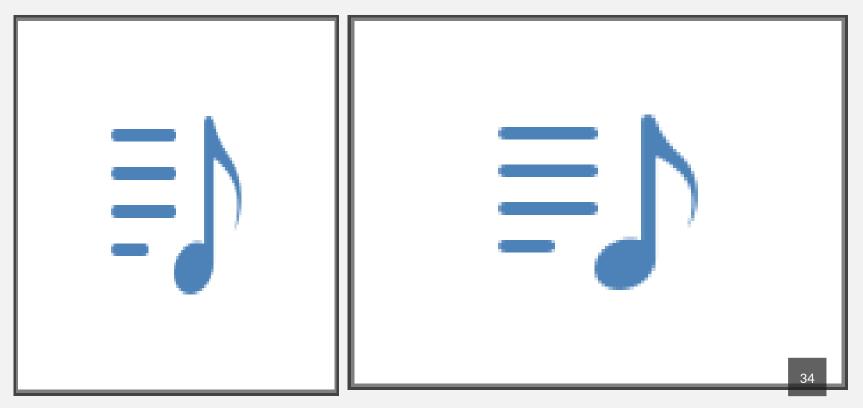


Primary beam corrected JVLA+MERLIN image of GOODS-N

Note the increased noise level towards the edge of the field

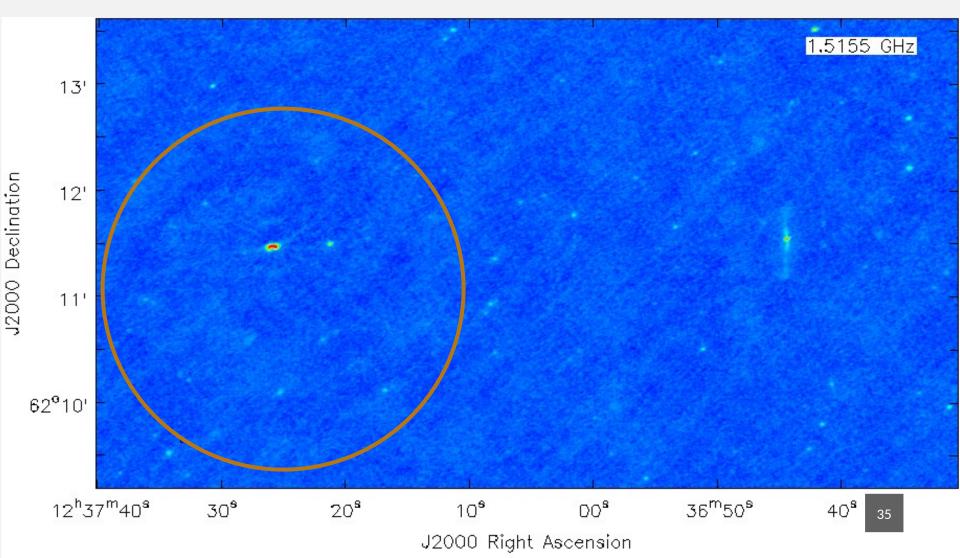
VARIABLE PRIMARY BEAMS

- Primary beam of arrays can vary with time and frequency!
- Has to be accounted for during cleaning and primary beam correction if imaging the whole primary beam (CASA has this for the JVLA + ALMA - VLBI arrays don't image the pb often!)



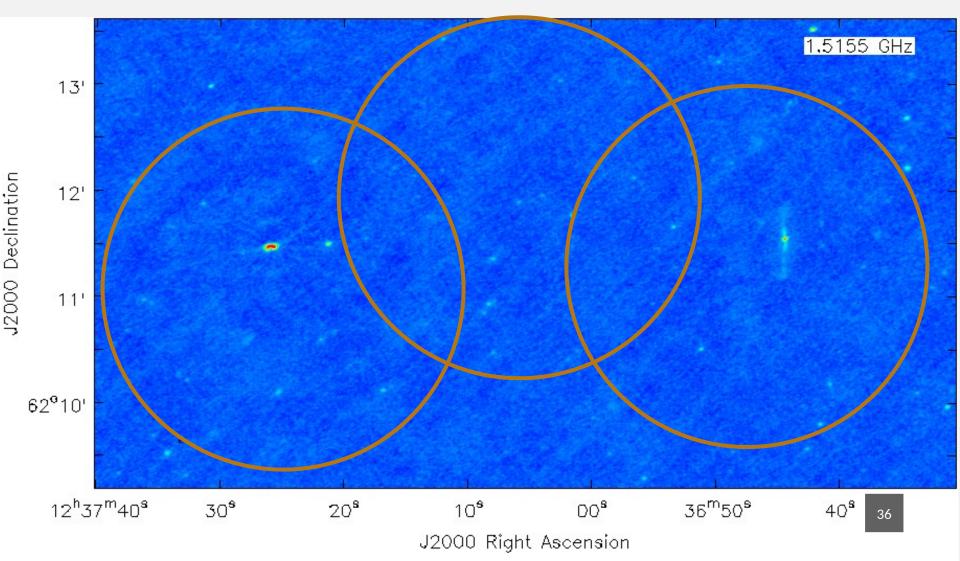
MOSAICING

What if this is our primary beam and we want to see the FR-I galaxy too?





We can use multiple pointings and combine them with correct weighting



MOSAICING

- •• Too create the massice chimage M(l,m)
- Need to we be the with $1/2^2 = 7$ (primary beam) for $B_i^2(l,m)$

$$M(l,m) = \frac{\sum_{i} B_{i}^{2}(l,m)(I_{i}(l,m)/B_{i}(l,m))}{\sum_{i} B_{i}^{2}(l,m)}$$
$$= \frac{\sum_{i} B_{i}(l,m)I_{i}(l,m)}{\sum_{i} B_{i}^{2}(l,m)}$$

SUMMARY

Topics discussed:

- CLEAN
- When to use Multi-scale or other deconvolution methods
- The effect of and solution to w-terms
- Multi-term deconvolution
- Self-calibration using CLEAN components
- Primary beam correction
- Mosaicing
- Direction-dependent effects during imaging