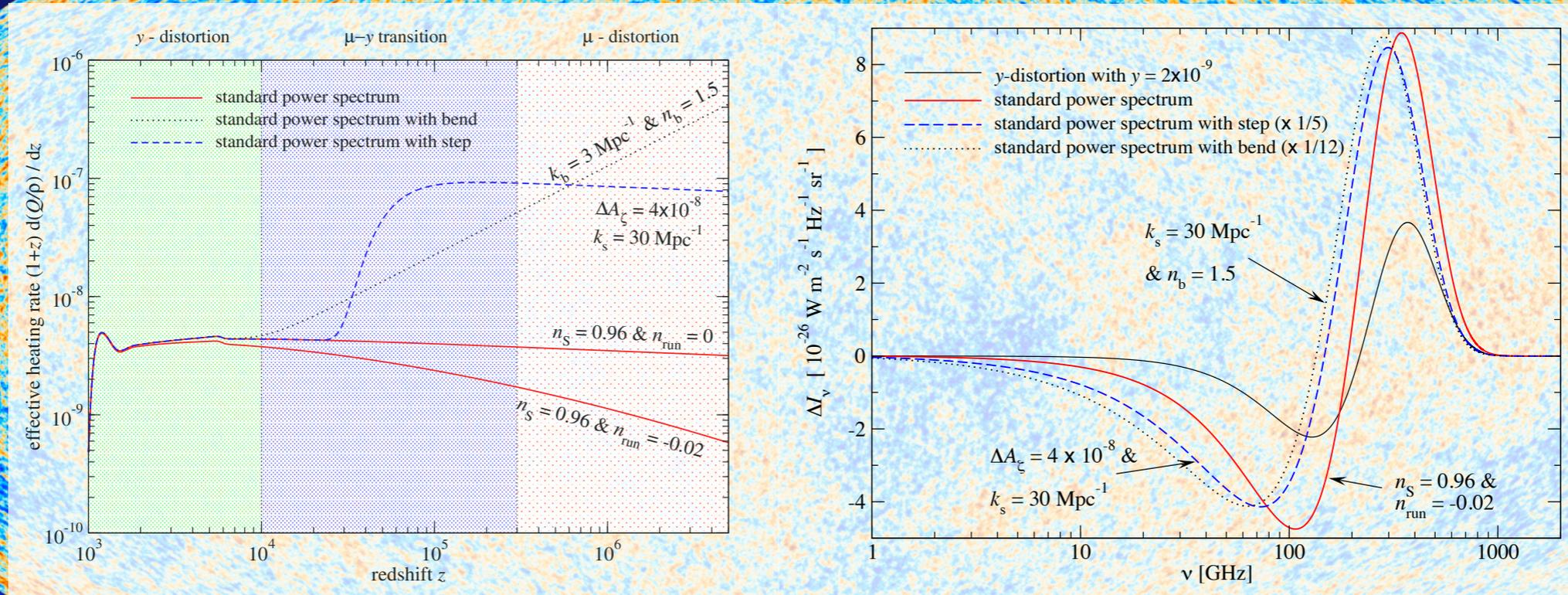


CMB Spectral Distortions as New Probe of Early-Universe Physics

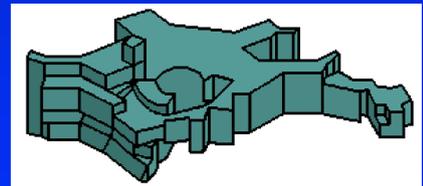


JOHNS HOPKINS
UNIVERSITY

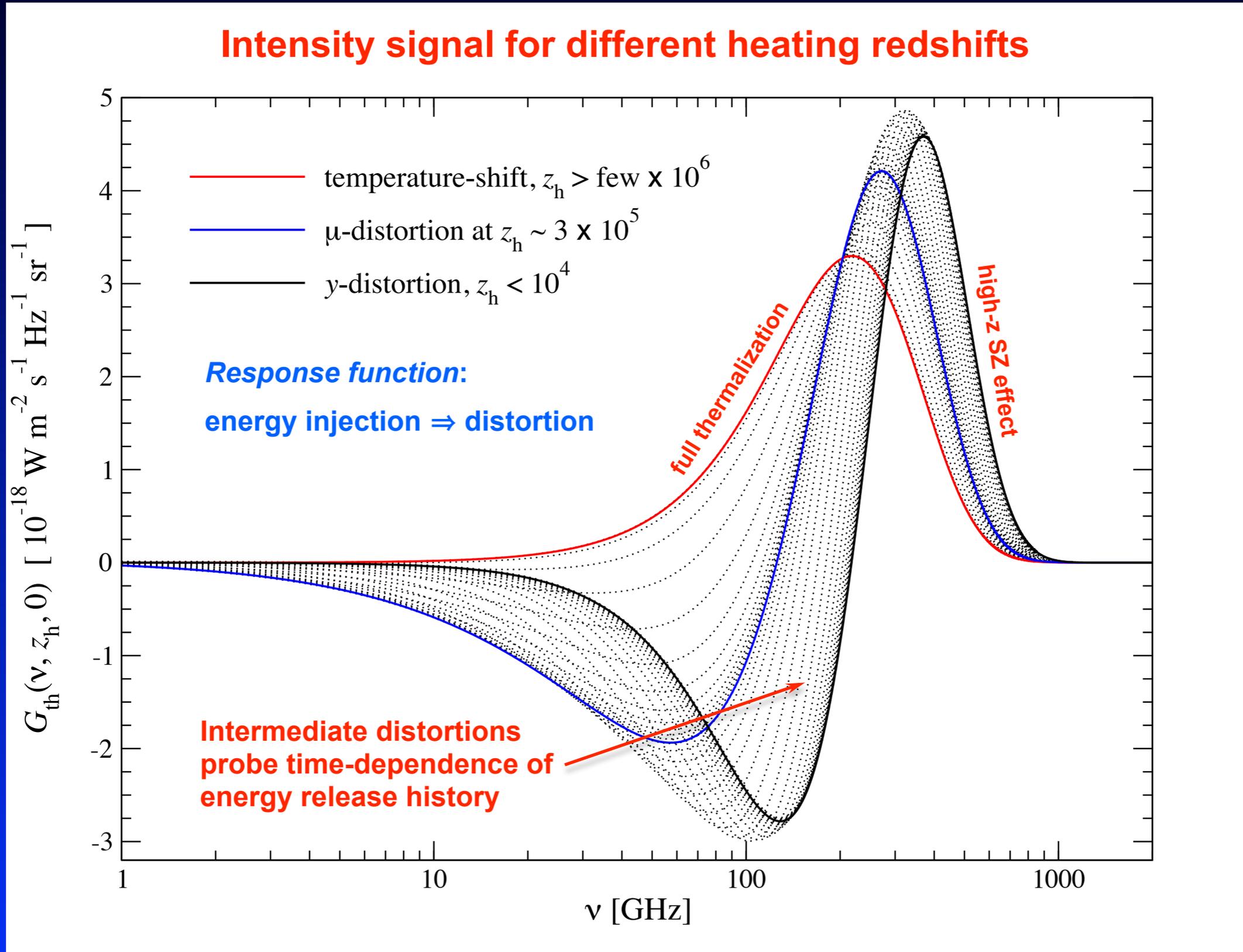
Jens Chluba

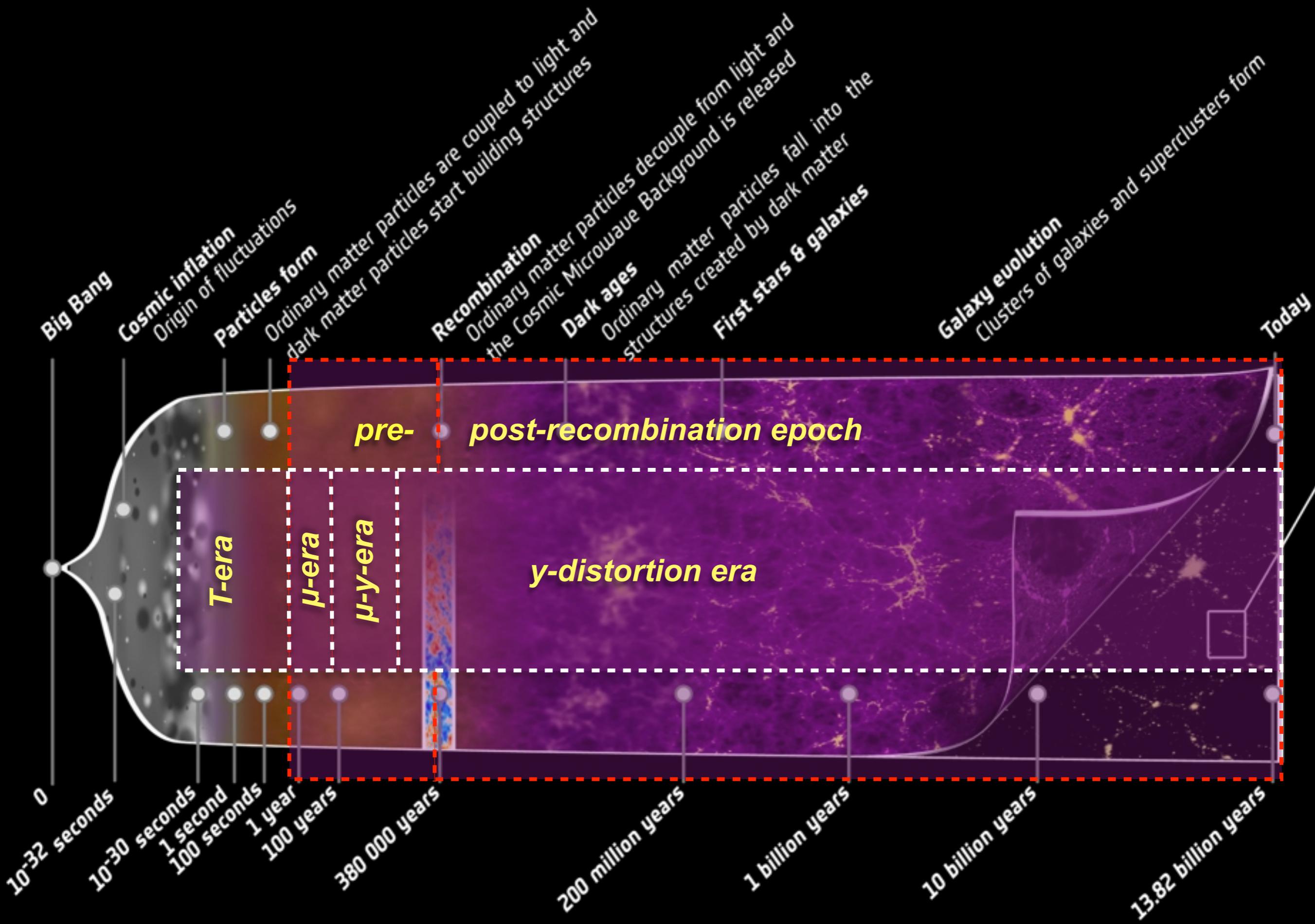
Lecture II: *Science with CMB Spectral Distortions*

Les Houches, August 2nd, 2013



What does the spectrum look like after energy injection?





Main Goals for this Lecture

- Convince you that future CMB distortions science will be *extremely* exciting!
- Provide an overview for different sources of early-energy release
- Show why the CMB spectrum is a *complementary* probe of inflation physics and particle physics

Physical mechanisms that lead to spectral distortions

- *Cooling by adiabatically expanding ordinary matter:* $T_\gamma \sim (1+z) \leftrightarrow T_m \sim (1+z)^2$
(JC, 2005; JC & Sunyaev 2011; Khatri, Sunyaev & JC, 2011)
 - continuous *cooling* of photons until redshift $z \sim 150$ via Compton scattering
 - due to huge heat capacity of photon field distortion very small ($\Delta\rho/\rho \sim 10^{-10}$ - 10^{-9})
 - Heating by *decaying or annihilating* relic particles
 - How is energy transferred to the medium?
 - lifetimes, decay channels, neutrino fraction, (at low redshifts: environments), ...
 - *Evaporation of primordial black holes & superconducting strings*
(Carr et al. 2010; Ostriker & Thompson, 1987; Tashiro et al. 2012)
 - rather fast, quasi-instantaneous but also extended energy release
 - *Dissipation of primordial acoustic modes & magnetic fields*
(Sunyaev & Zeldovich, 1970; Daly 1991; Hu et al. 1994; Jedamzik et al. 2000)
 - *Cosmological recombination*
-
- Signatures due to first supernovae and their remnants
(Oh, Cooray & Kamionkowski, 2003)
 - Shock waves arising due to large-scale structure formation
(Sunyaev & Zeldovich, 1972; Cen & Ostriker, 1999)
 - SZ-effect from clusters; effects of reionization (Heating of medium by X-Rays, Cosmic Rays, etc)

„high“ redshifts

„low“ redshifts

pre-recombination epoch

post-recombination

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Standard sources of distortions

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Standard sources of distortions

too little time...

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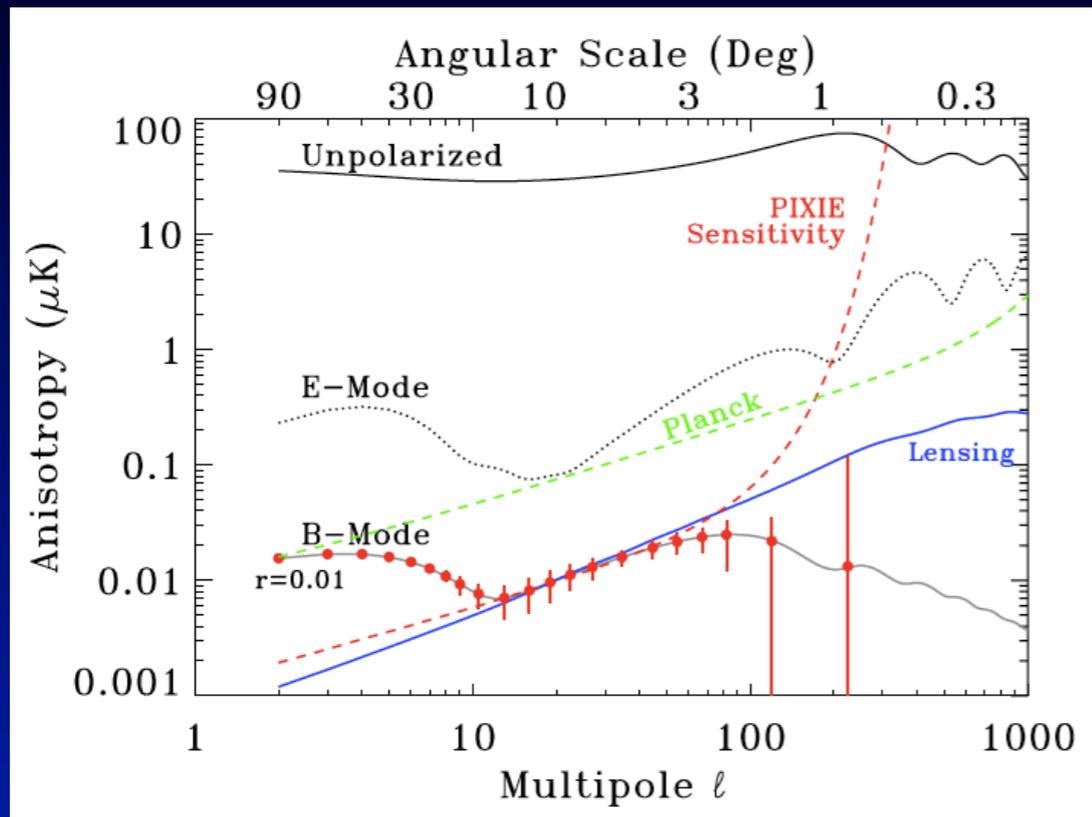
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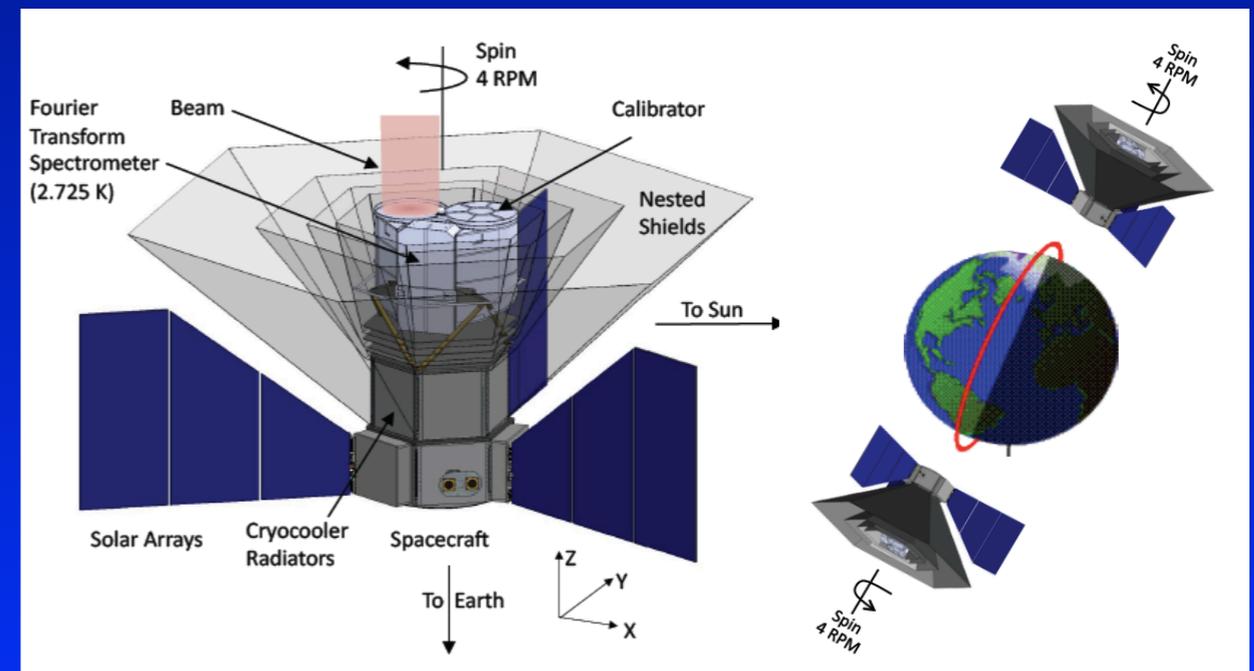
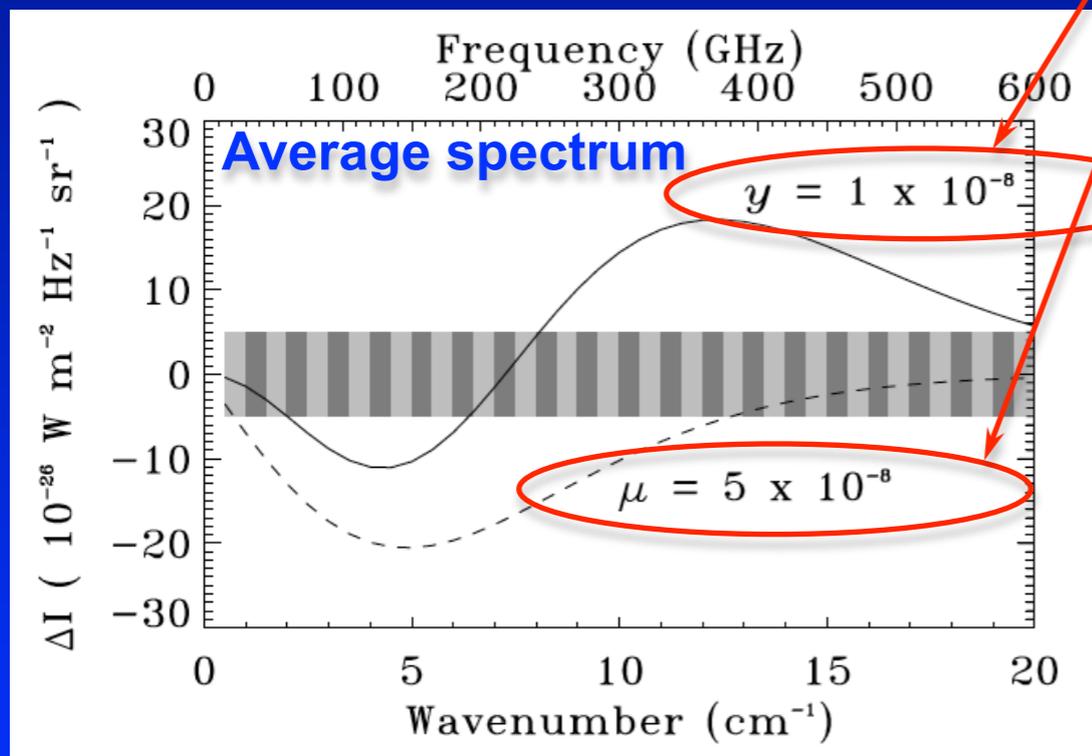
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PIXIE: Primordial Inflation Explorer

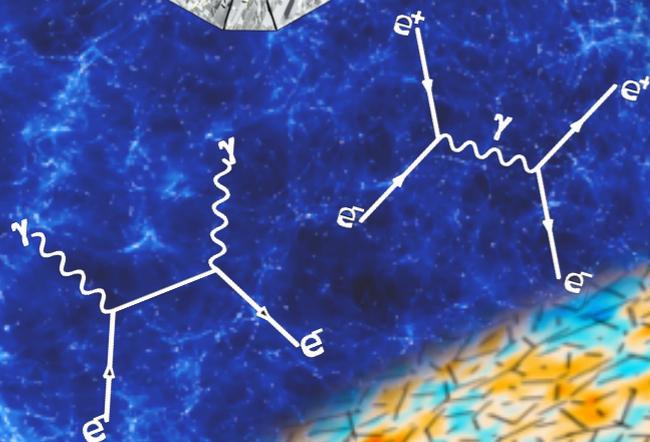
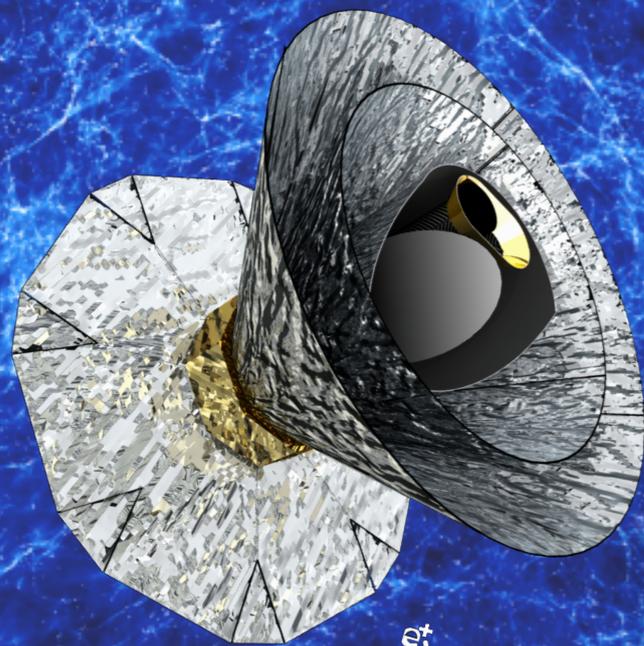


- 400 spectral channel in the frequency range 30 GHz and 6THz ($\Delta\nu \sim 15\text{GHz}$)
- about 1000 (!!!) times more sensitive than COBE/FIRAS
- B-mode polarization from inflation ($r \approx 10^{-3}$)
- improved limits on μ and y
- was proposed 2011 as NASA EX mission (i.e. cost ~ 200 M\$)



PRISM

Probing cosmic structures and radiation with the ultimate polarimetric spectro-imaging of the microwave and far-infrared sky



Spokesperson: Paolo de Bernardis
e-mail: paolo.debernardis@roma1.infn.it — tel: + 39 064 991 4271

Instruments:

- L-class ESA mission
- White paper, May 24th, 2013
- Imager:
 - polarization sensitive
 - 3.5m telescope [arcmin resolution at highest frequencies]
 - 30GHz-6THz [30 broad ($\Delta\nu/\nu\sim 25\%$) and 300 narrow ($\Delta\nu/\nu\sim 2.5\%$) bands]
- Spectrometer:
 - FTS similar to PIXIE
 - 30GHz-6THz ($\Delta\nu\sim 15$ & 0.5 GHz)

Some of the science goals:

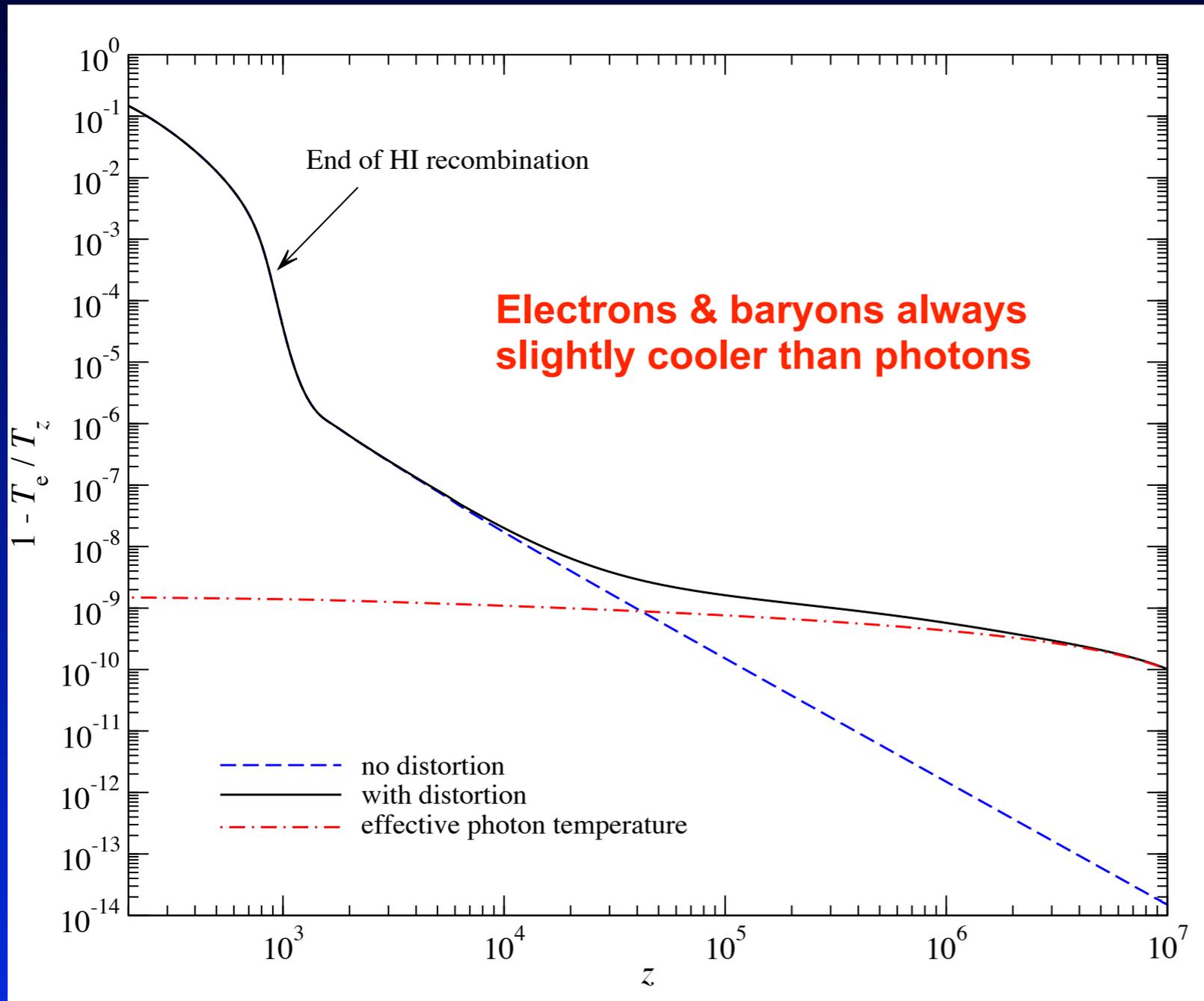
- B-mode polarization from inflation ($r \approx 5 \times 10^{-4}$)
- count all SZ clusters $> 10^{14} M_{\text{sun}}$
- CIB/large scale structure
- Galactic science
- *CMB spectral distortions*

Sign up at:

<http://www.prism-mission.org/>

Adiabatically cooling ordinary matter

Spectral distortion caused by the cooling of ordinary matter



- adiabatic expansion
 $\Rightarrow T_\gamma \sim (1+z) \leftrightarrow T_m \sim (1+z)^2$
- photons continuously *cooled / down-scattered* since day one of the Universe!
- Compton heating balances adiabatic cooling
 $\Rightarrow \frac{da^4 \rho_\gamma}{a^4 dt} \simeq -Hk\alpha_h T_\gamma \propto (1+z)^6$
- at high redshift same scaling as annihilation ($\propto N_X^2$)
 \Rightarrow *cancellation* possible

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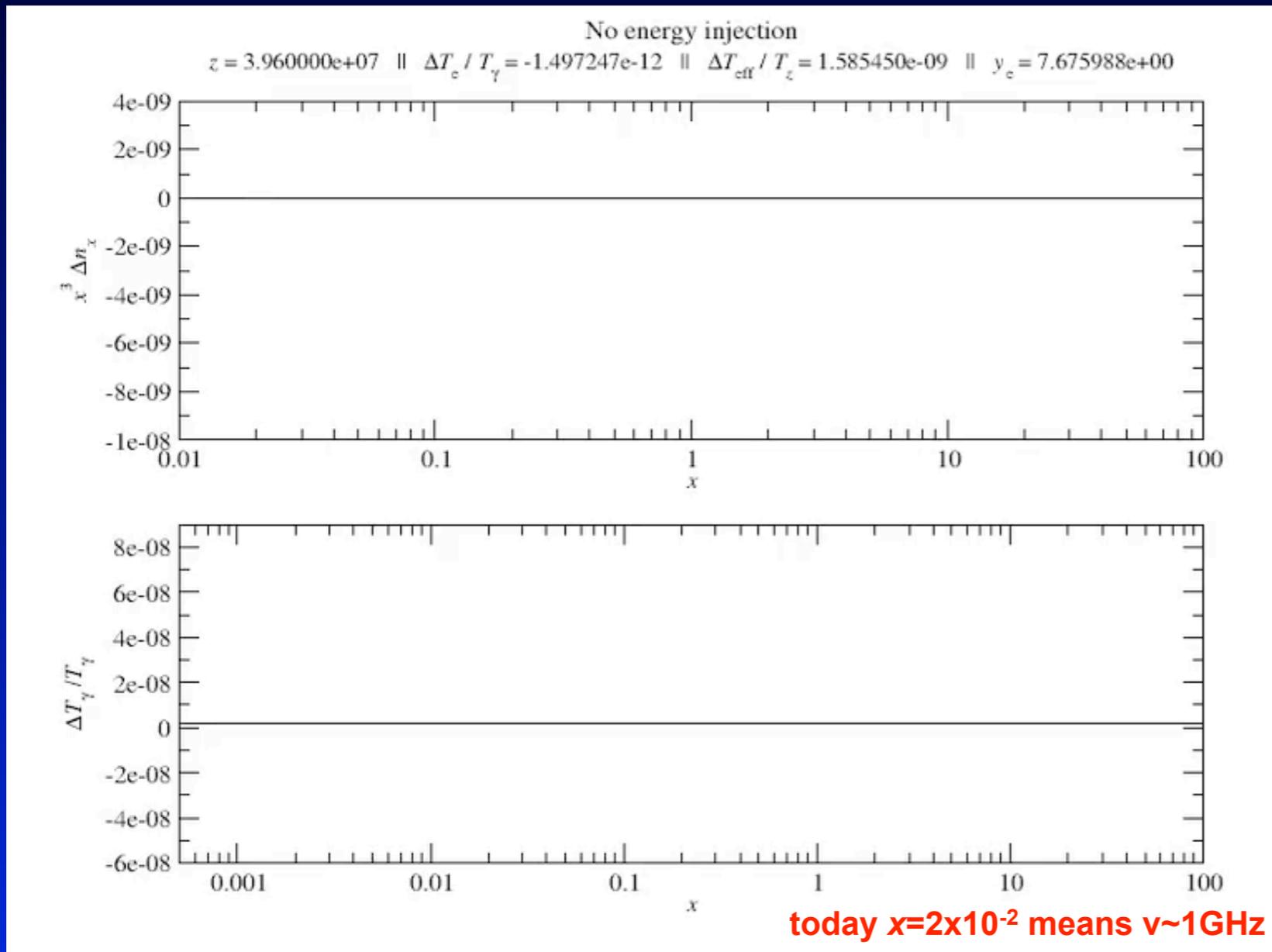
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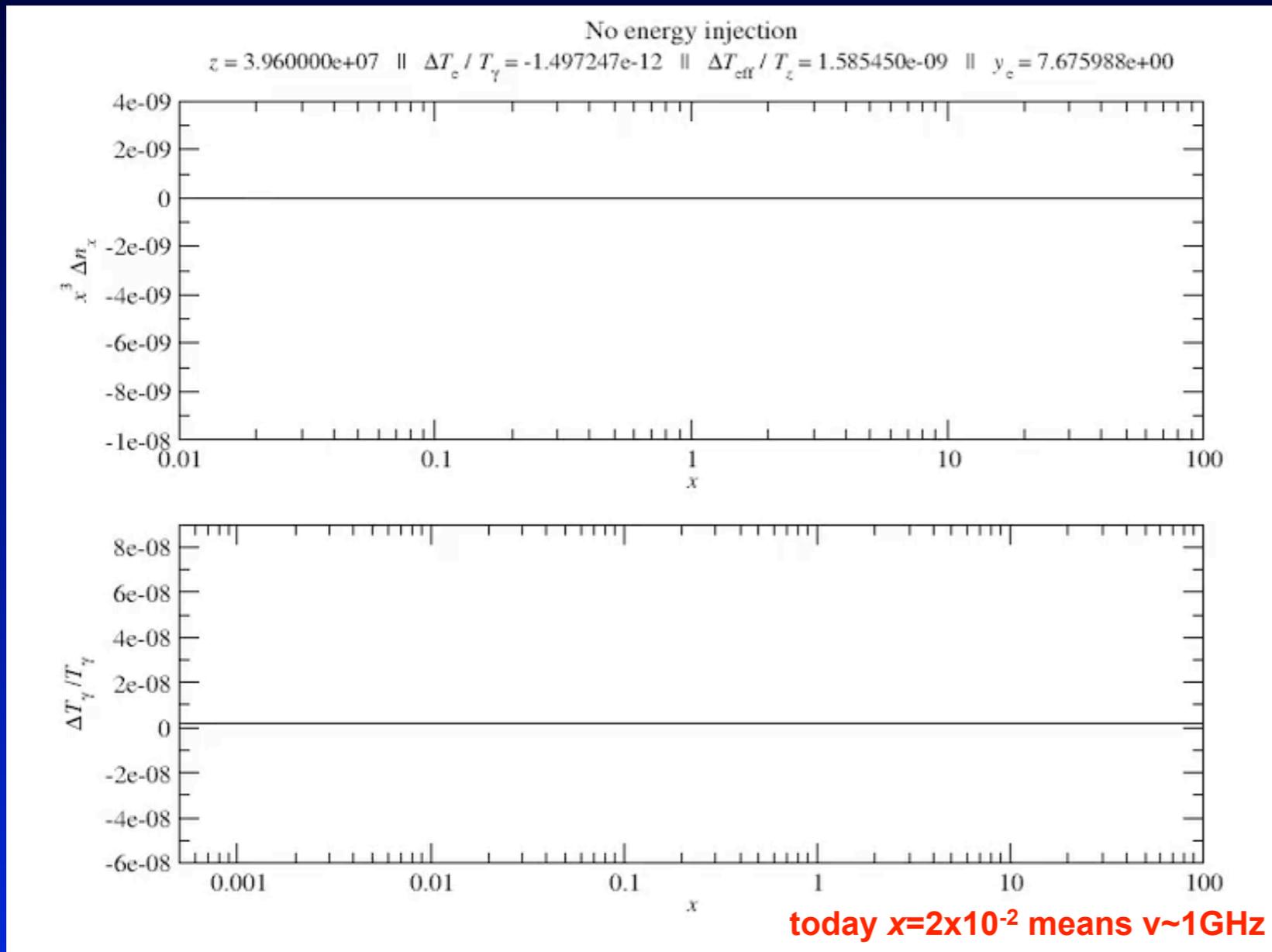
today $x=2 \times 10^{-2}$ means $\nu \sim 1\text{GHz}$

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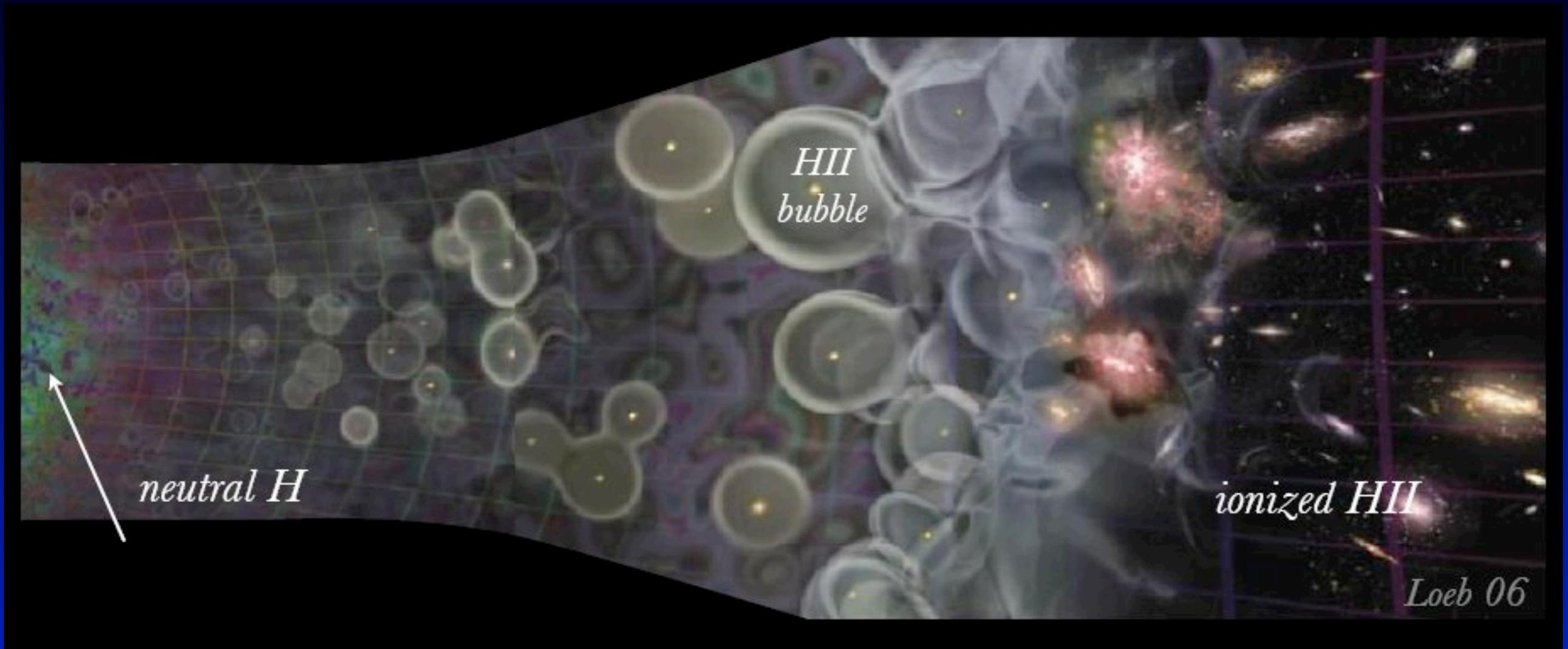


$$\mu \simeq 1.4 \left. \frac{\Delta \rho_\gamma}{\rho_\gamma} \right|_\mu \approx -3 \times 10^{-9} \quad y \simeq \frac{1}{4} \left. \frac{\Delta \rho_\gamma}{\rho_\gamma} \right|_y \approx -6 \times 10^{-10}$$

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- photons continuously *cooled / down-scattered* since day one of the Universe!
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- at high redshift same scaling as annihilation ($\propto N_X^2$)
 \Rightarrow *cancellation* possible
- *negative* μ and y distortion
- late free-free absorption at very low frequencies
- Distortion a few times below PIXIE's sensitivity

Reionization and structure formation

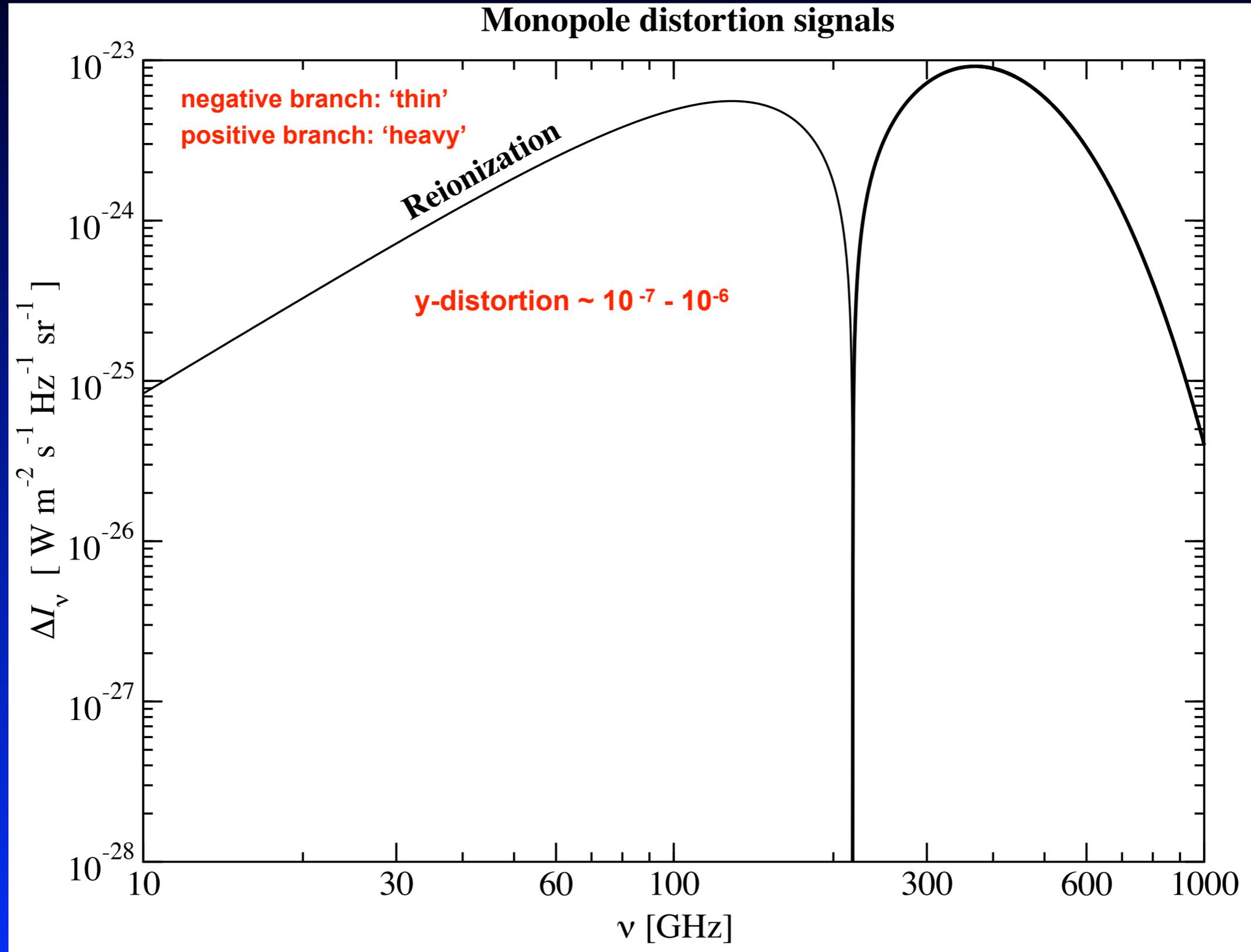
Simple estimates for the distortion



- Gas temperature $T \approx 10^4$ K $\implies y \approx \frac{kT_e}{m_e c^2} \approx 2 \times 10^{-7}$
- Thomson optical depth $\tau \approx 0.1$
- second order Doppler effect $y \approx \text{few} \times 10^{-8}$
- structure formation / SZ effect (e.g., Refregier et al., 2003) $y \approx \text{few} \times 10^{-7} - 10^{-6}$

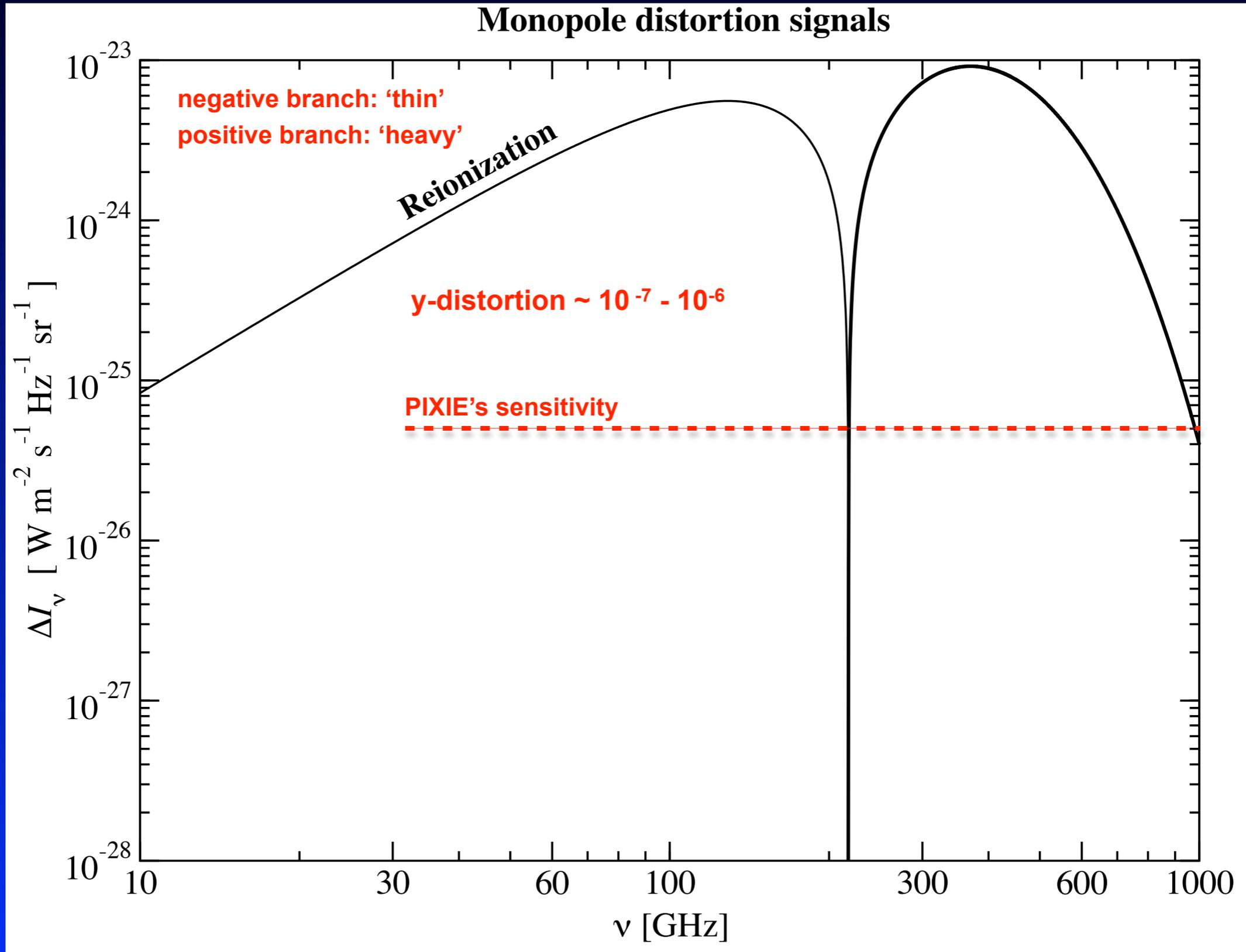
Average CMB spectral distortions

Absolute value of Intensity signal



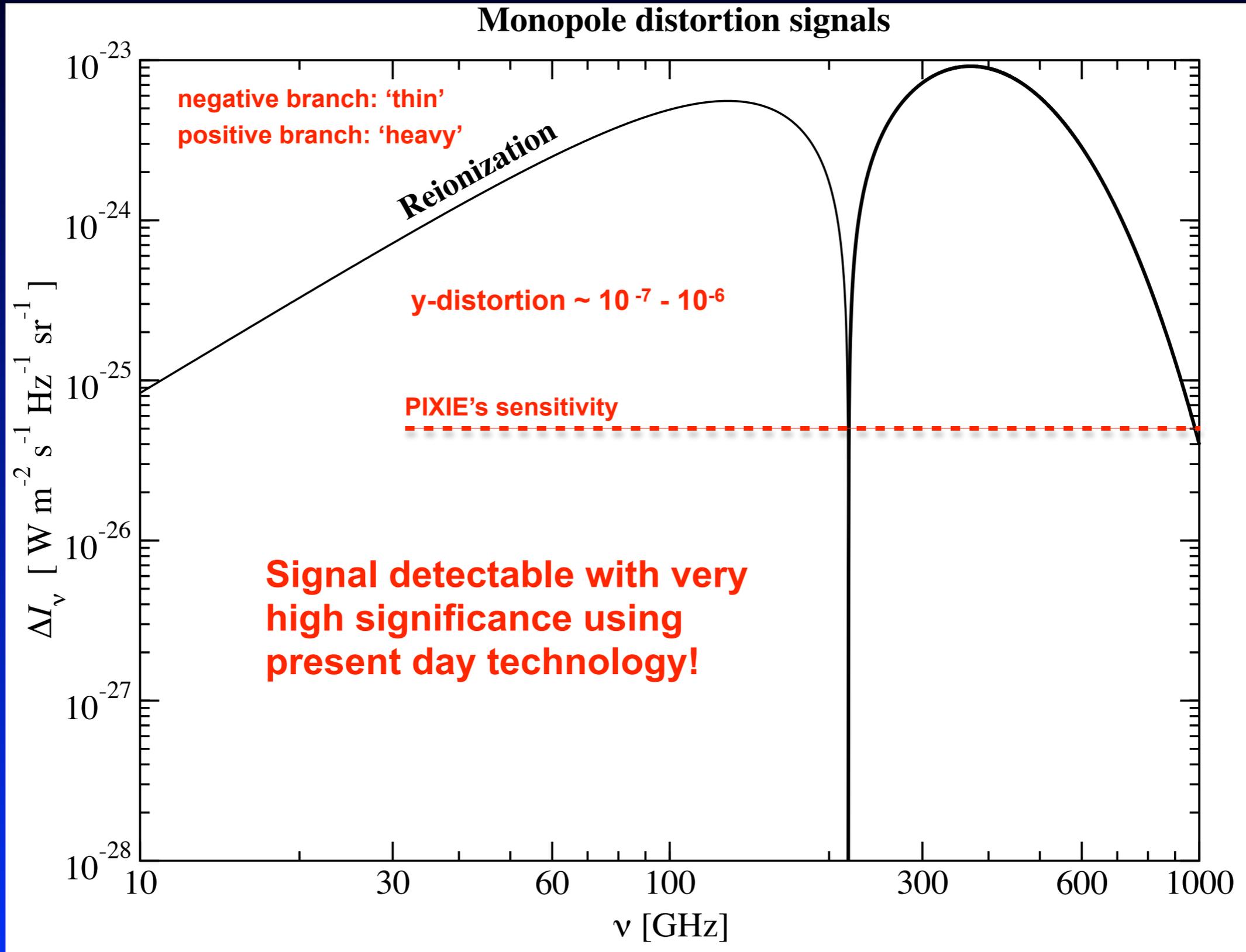
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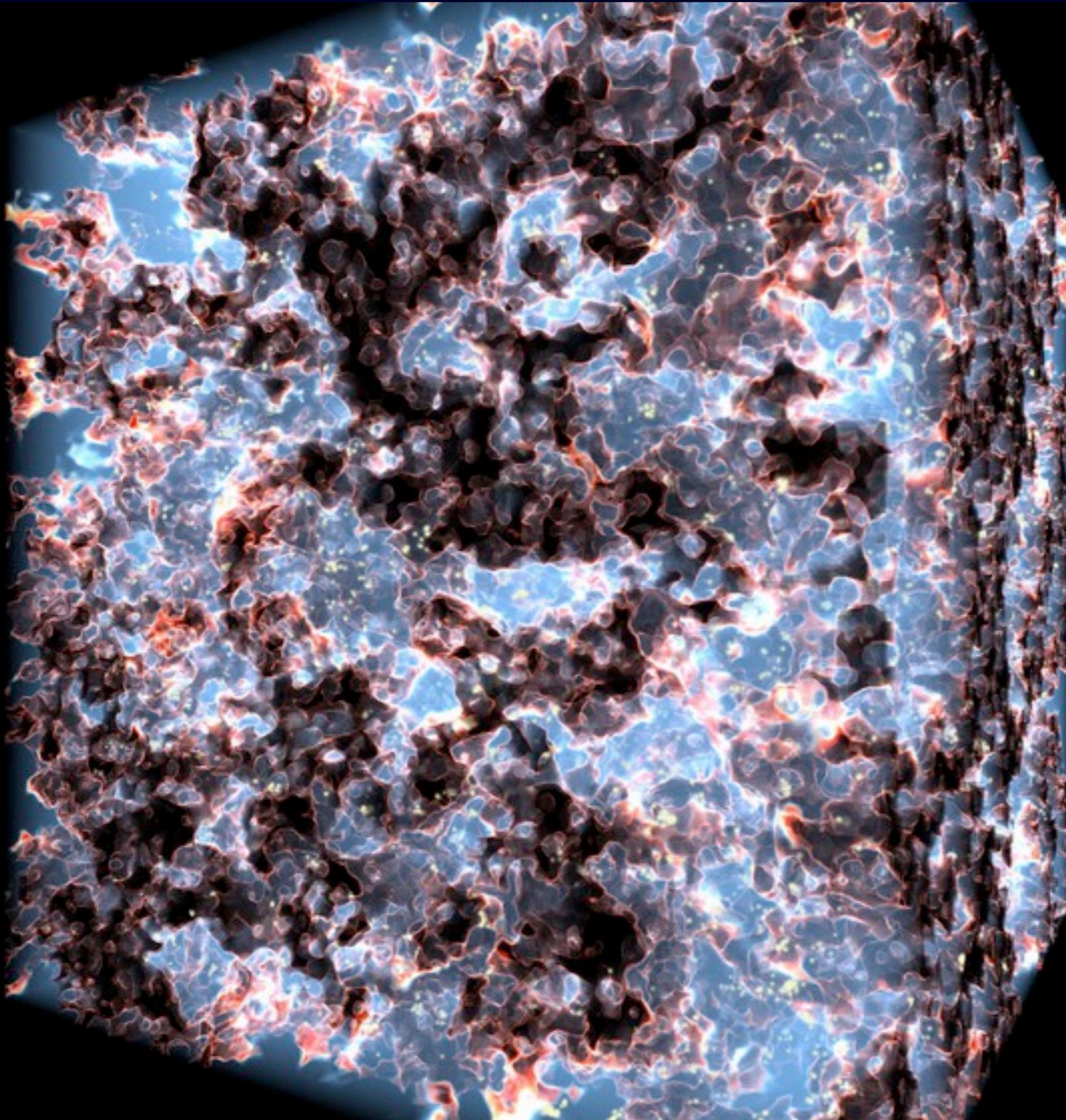


Average CMB spectral distortions

Absolute value of Intensity signal



Fluctuations of the γ -parameter at large scales

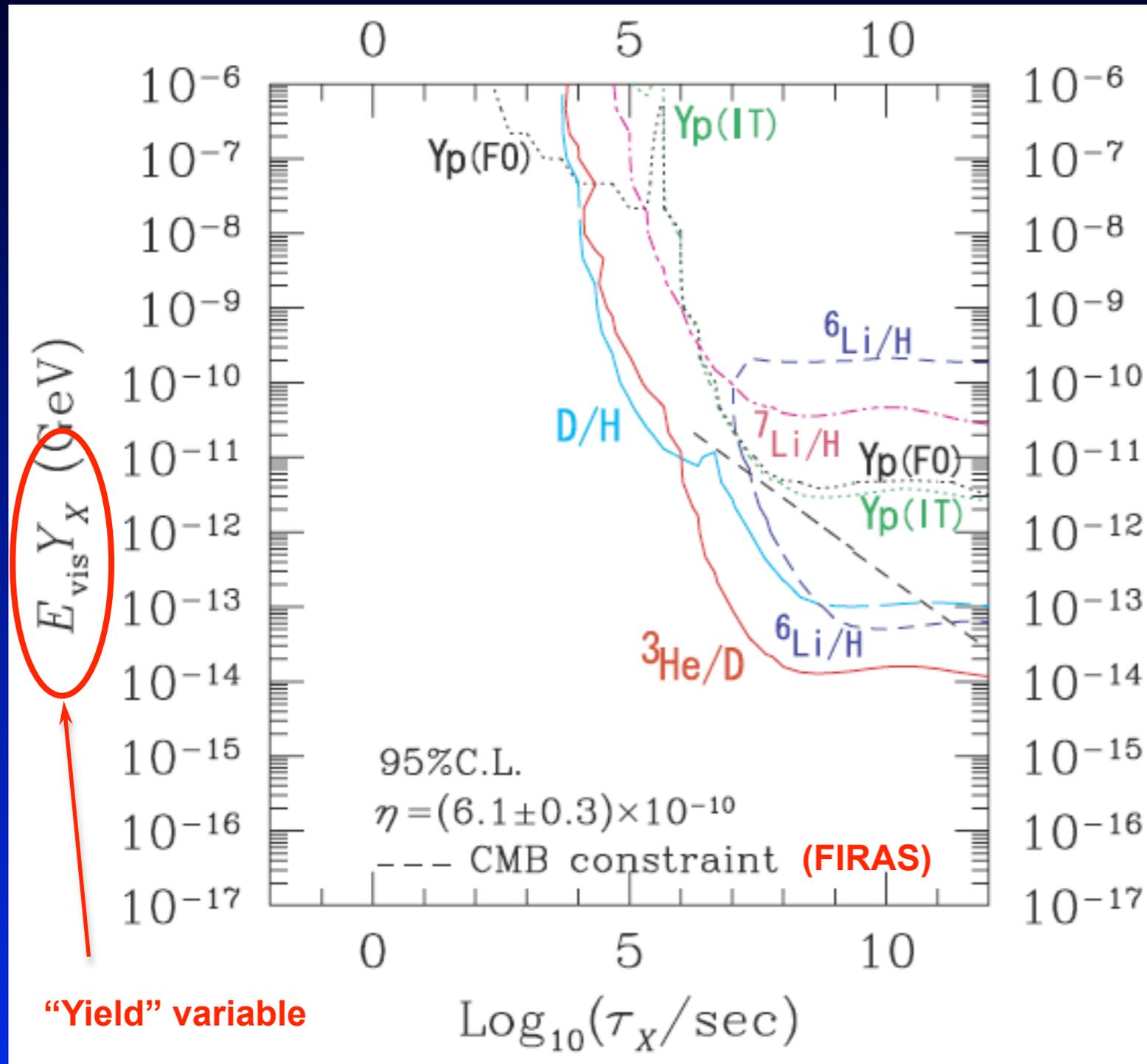


- spatial variations of the optical depth and temperature cause small-spatial variations of the γ -parameter at different angular scales
- could tell us about the reionization sources and structure formation process
- additional independent piece of information!

Example:
Simulation of reionization process
(1Gpc/h) by *Alvarez & Abel*

Decaying particles

Constraints from measurements of light elements



- Yield variable \Rightarrow parametrizes the total energy release relative to total entropy density of the Universe

$$Y_X \simeq N_X/S$$

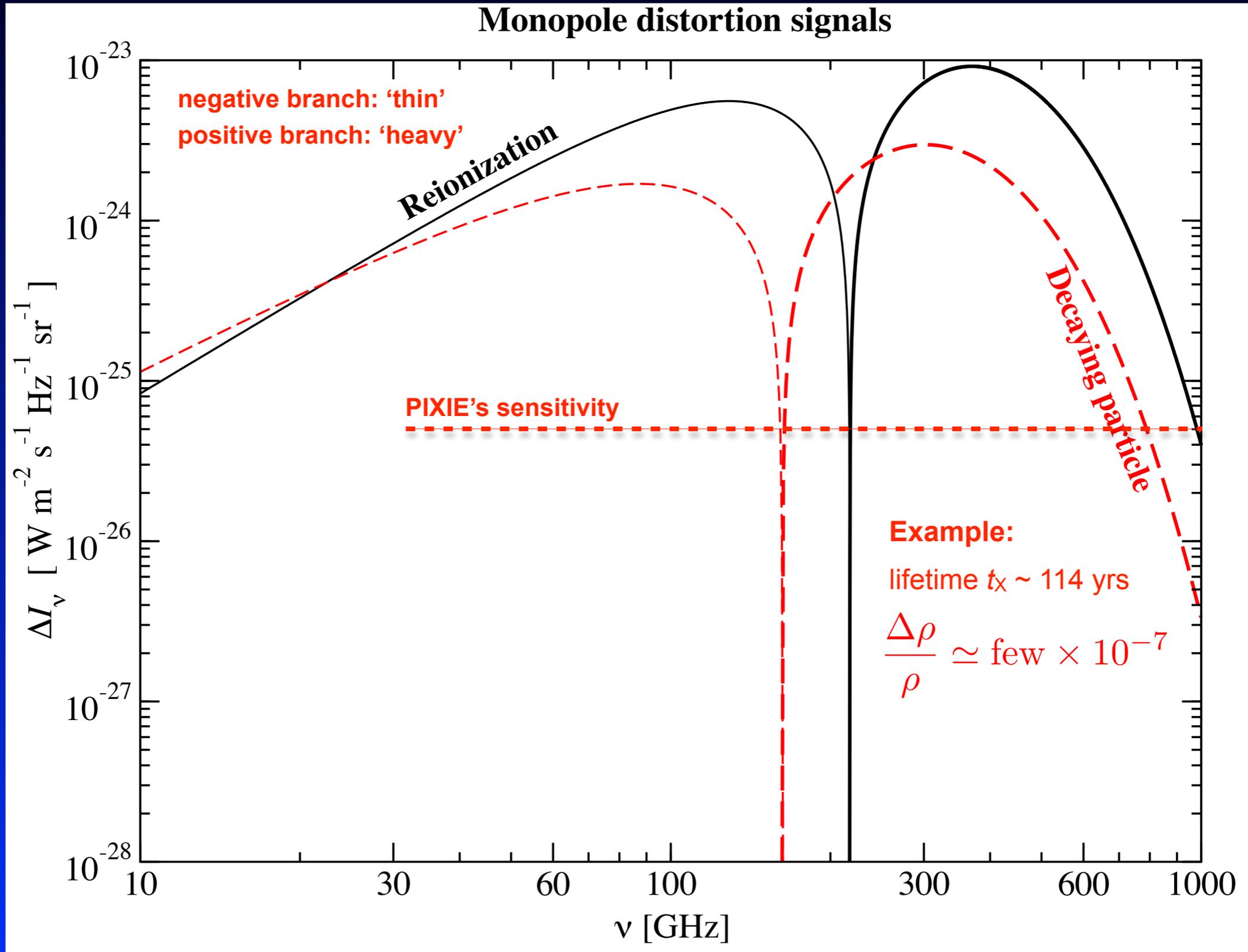
- E_{vis} hides physics of energy deposition (decay channels, neutrino fraction, etc.)
- current CMB limit rather weak....

Energy release by decaying particles

- Energy release rate $\frac{d(Q/\rho_\gamma)}{dz} \approx \frac{f^* M_X c^2}{H(z)(1+z)} \frac{N_X(z)}{\rho_\gamma(z)} \Gamma_X e^{-\Gamma_X t}$
- For computations: $f_X = f^* M_X c^2 N_X / N_H$ and $\varepsilon_X = \frac{f_X}{z_X}$
- Efficiency factor f^* contains all the physics describing the cascade of decay products
- At high redshift deposited energy goes into heat
- Around recombination and after things become more complicated
(Slatyer et al. 2009; Cirelli et al. 2009; Huts et al. 2009; Slatyer et al. 2013)
 \Rightarrow *branching ratios into heat, ionizations, and atomic excitation*

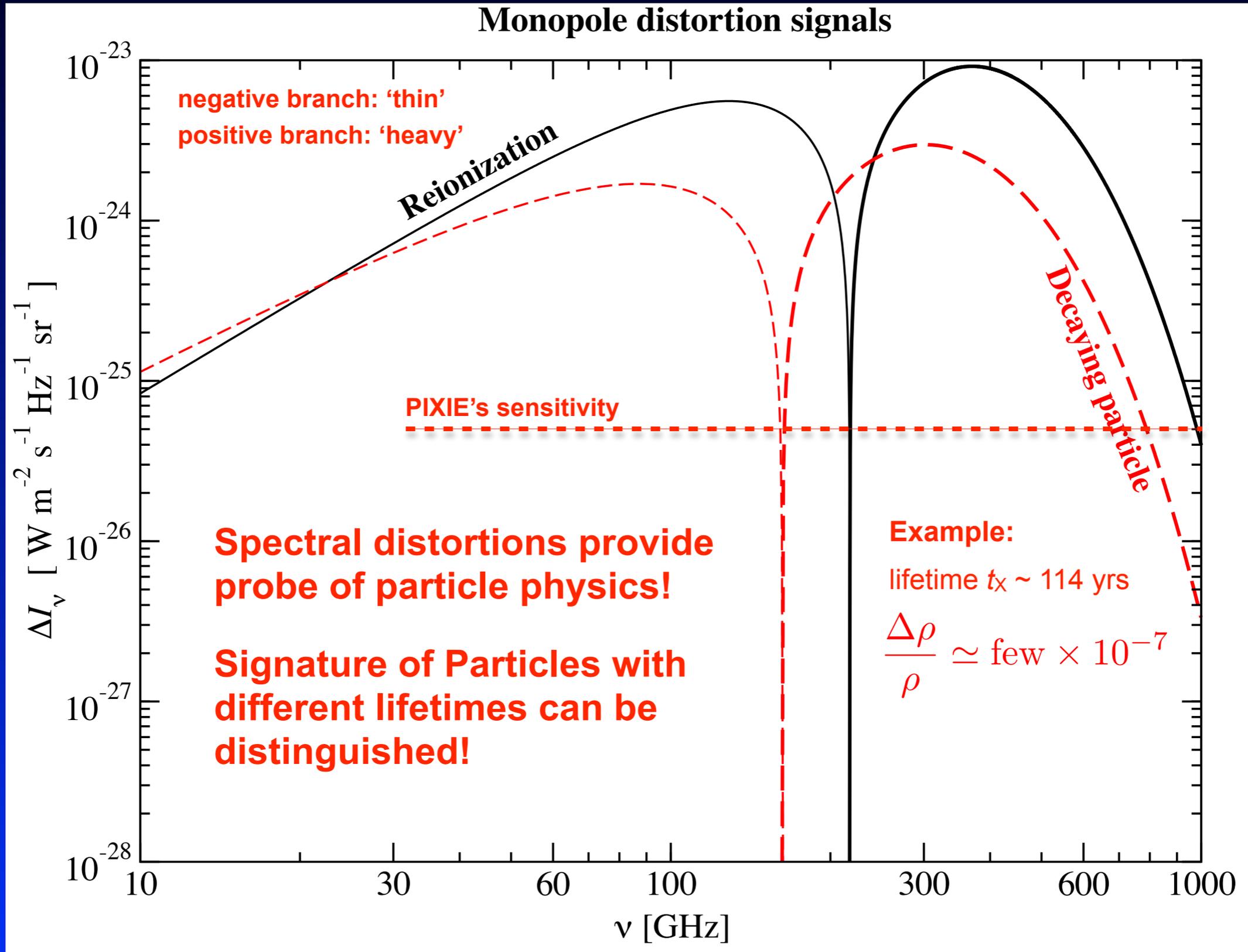
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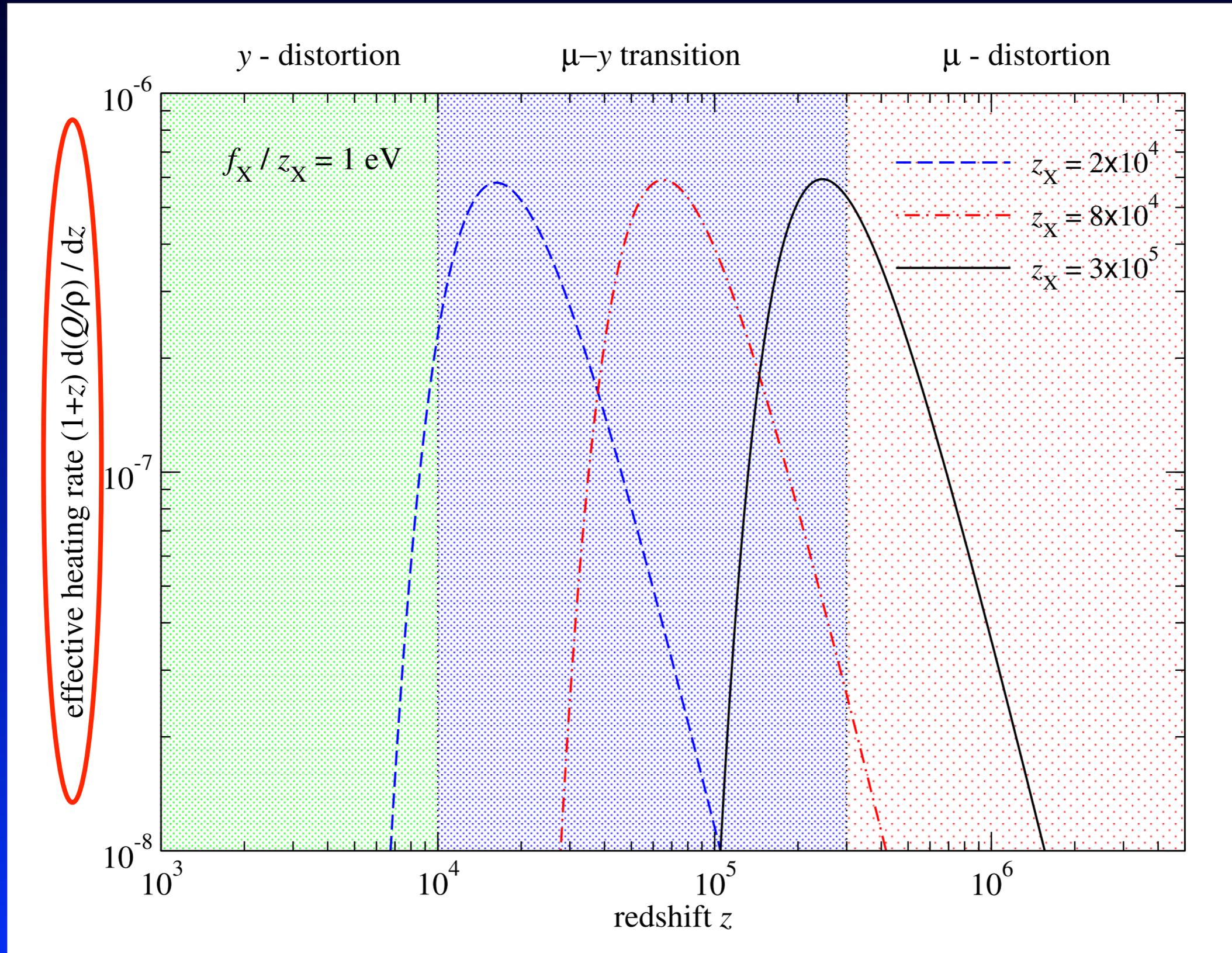


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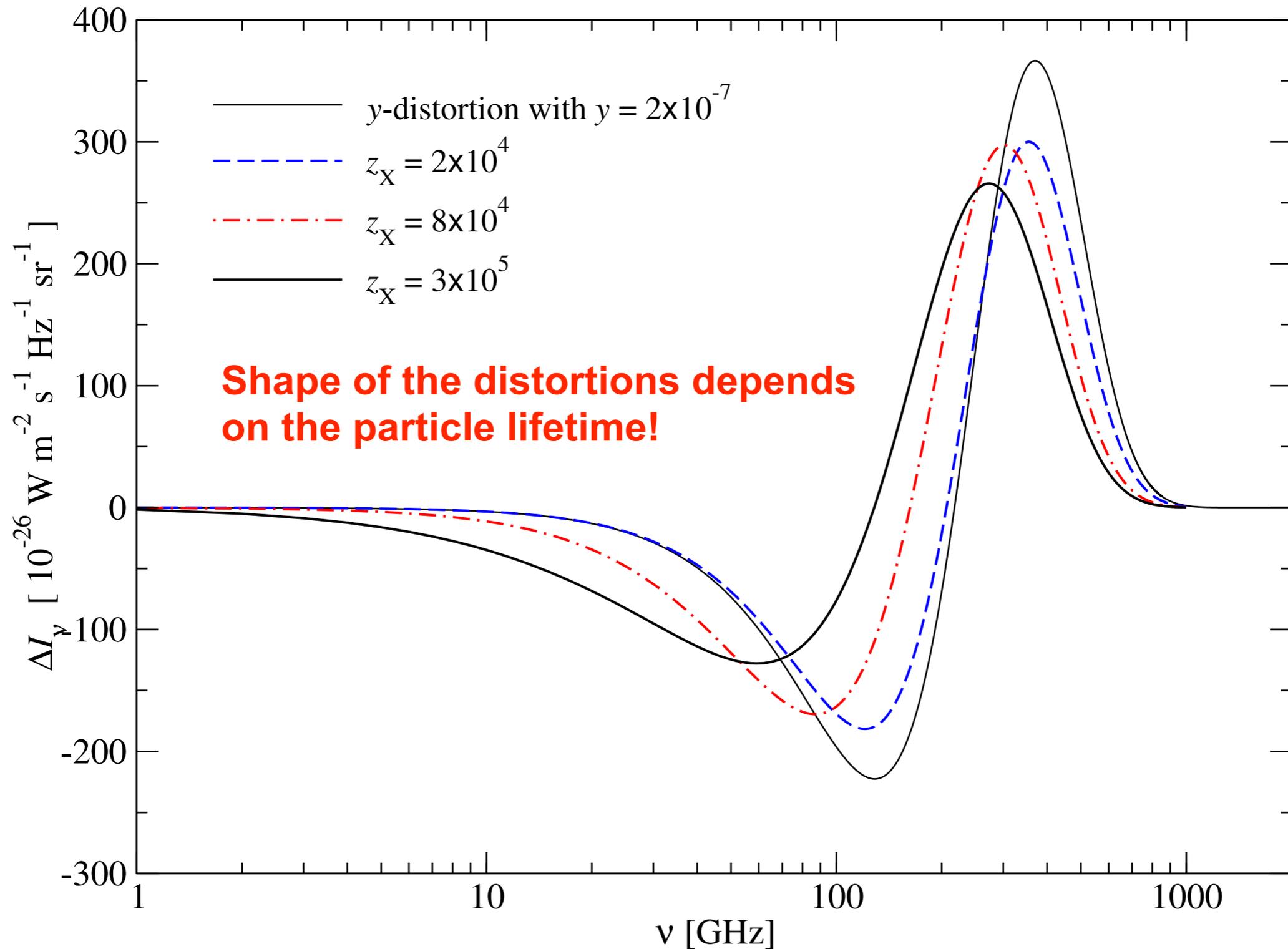
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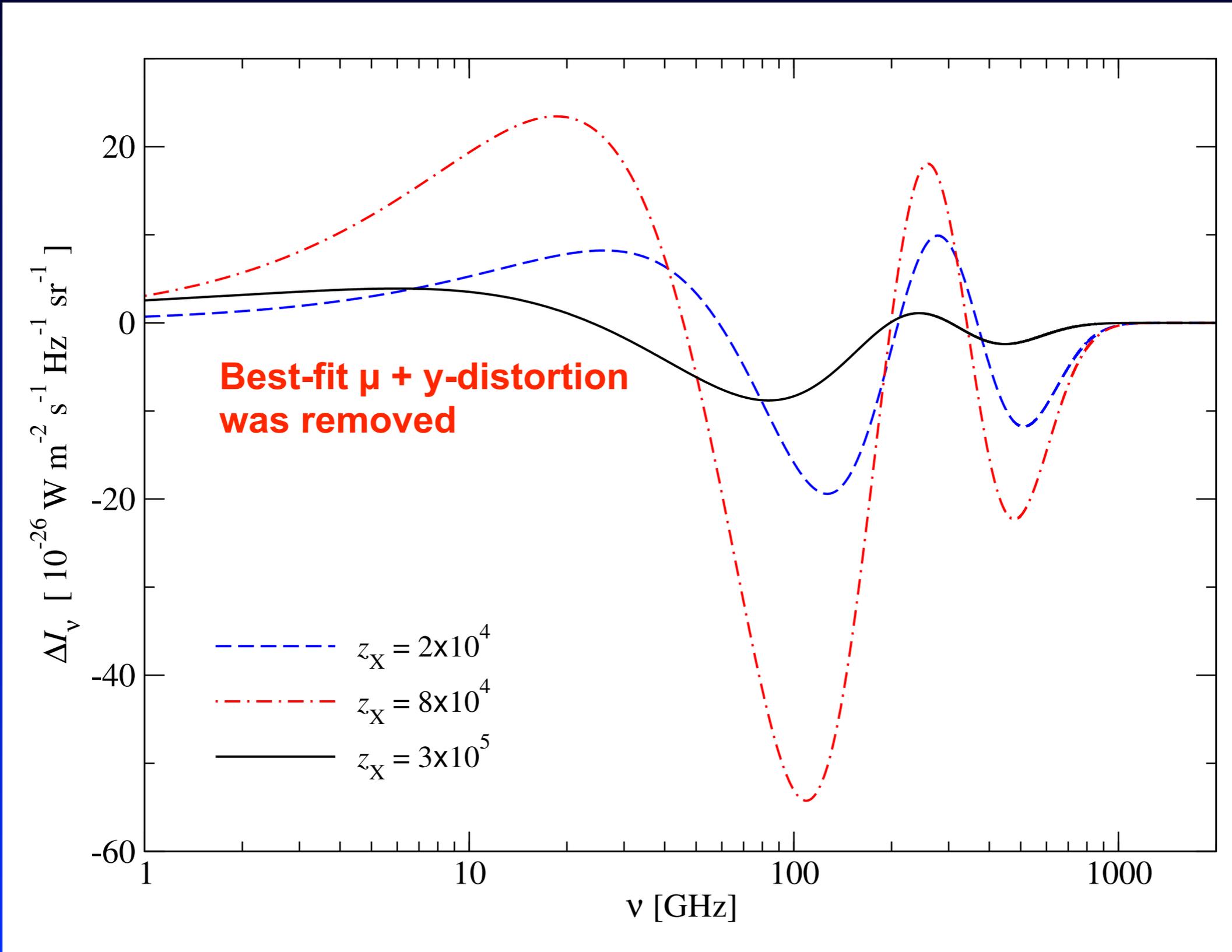
Decaying particle scenarios



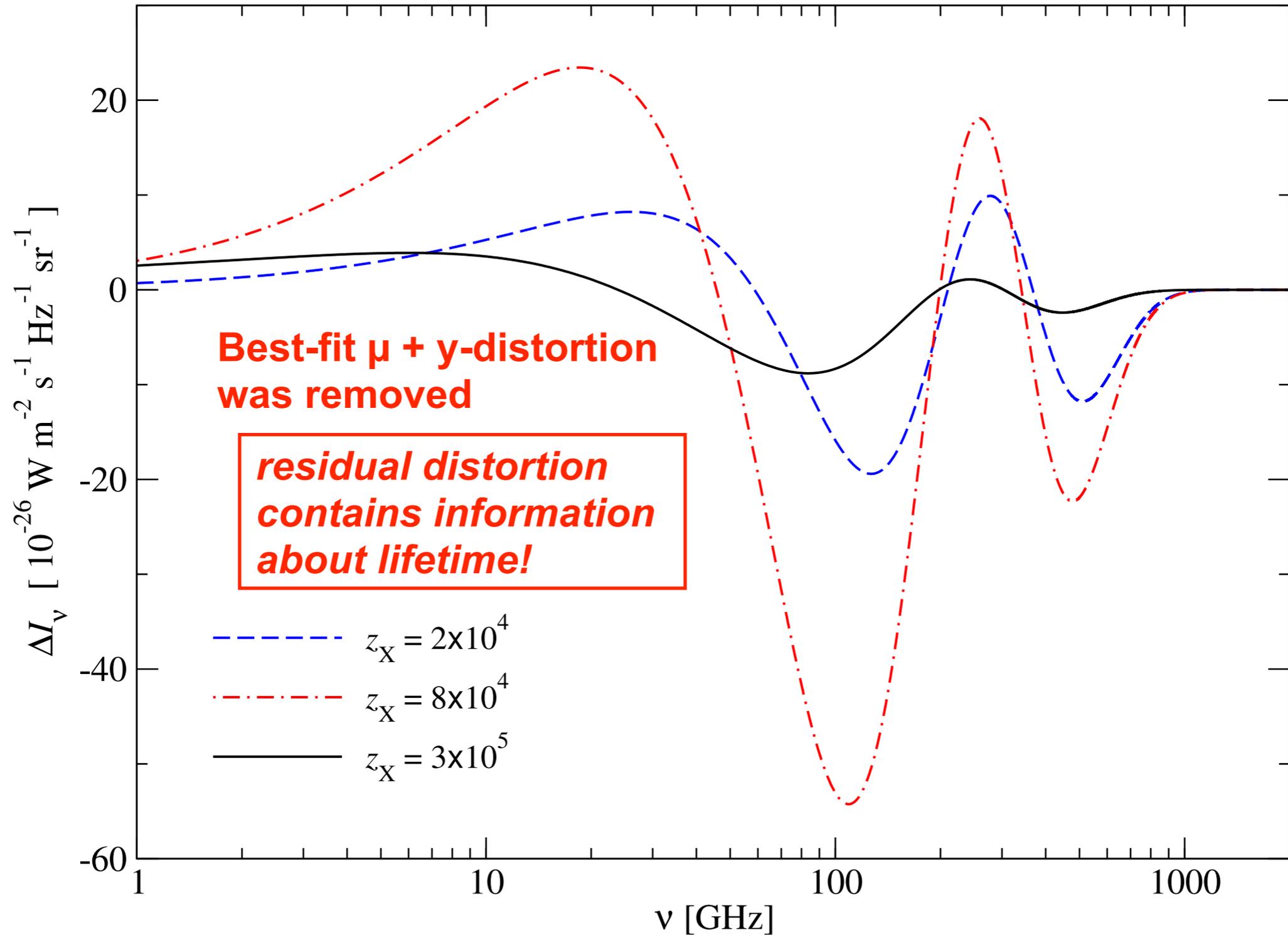
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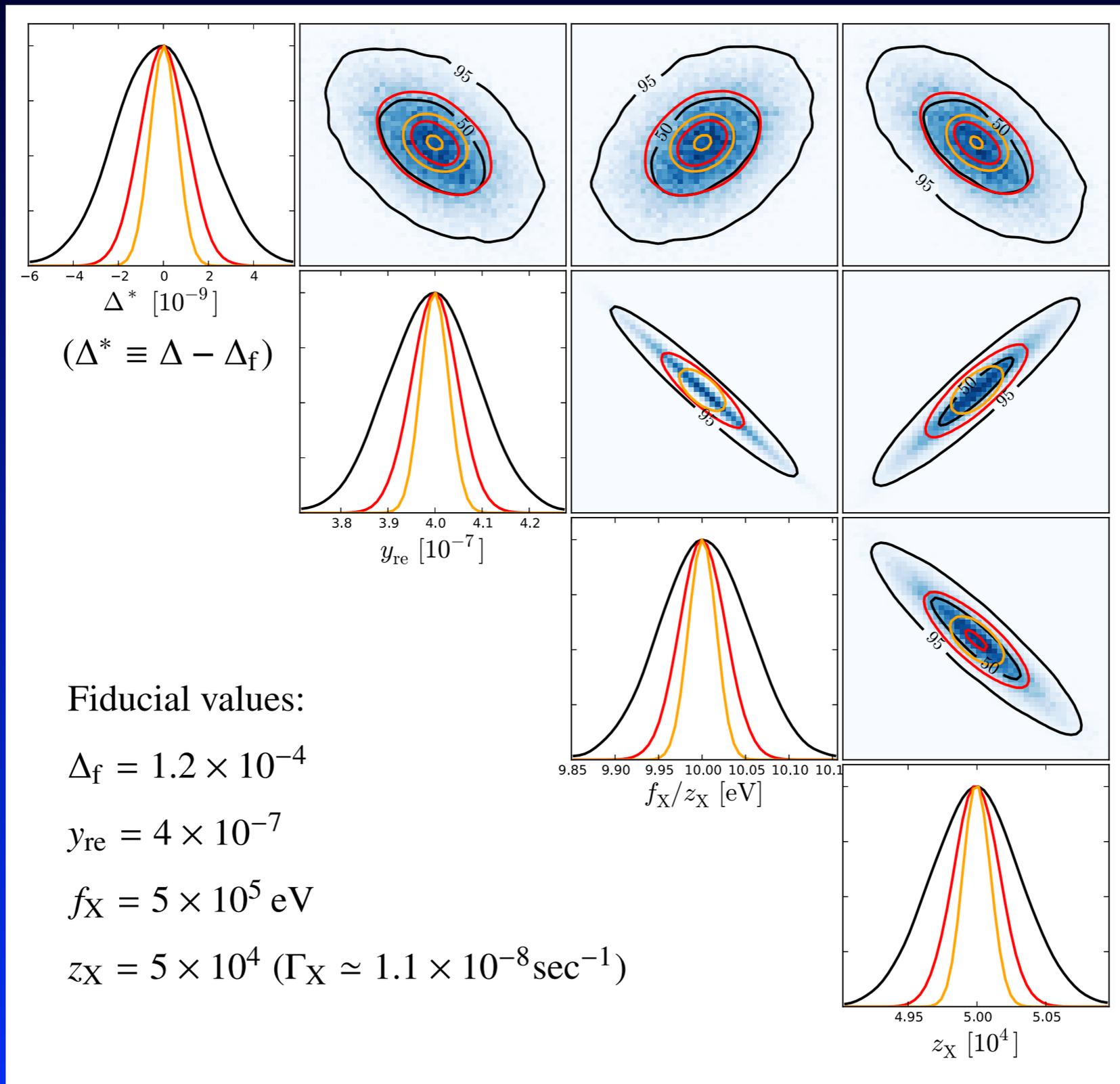
Decaying particle scenarios (information in residual)



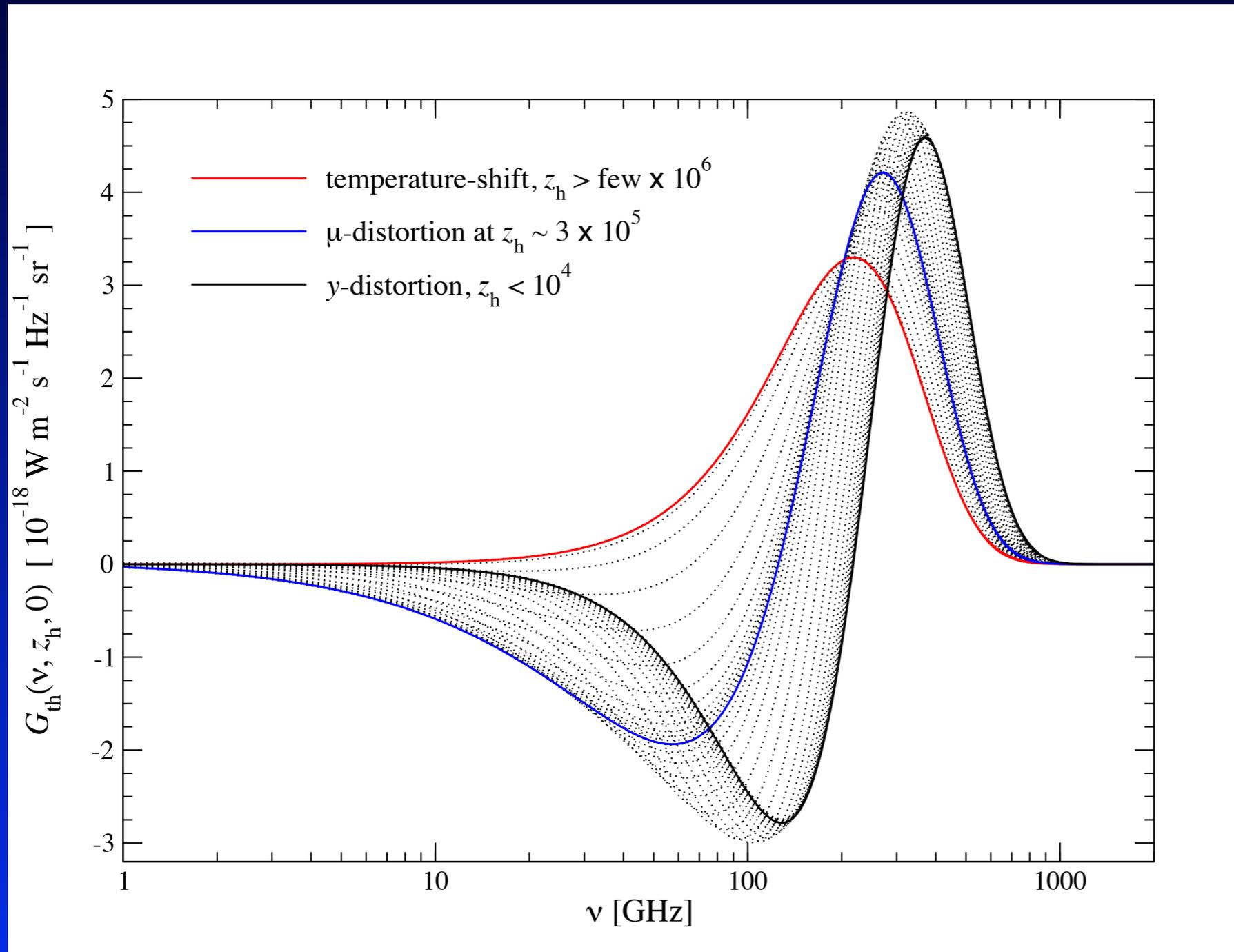
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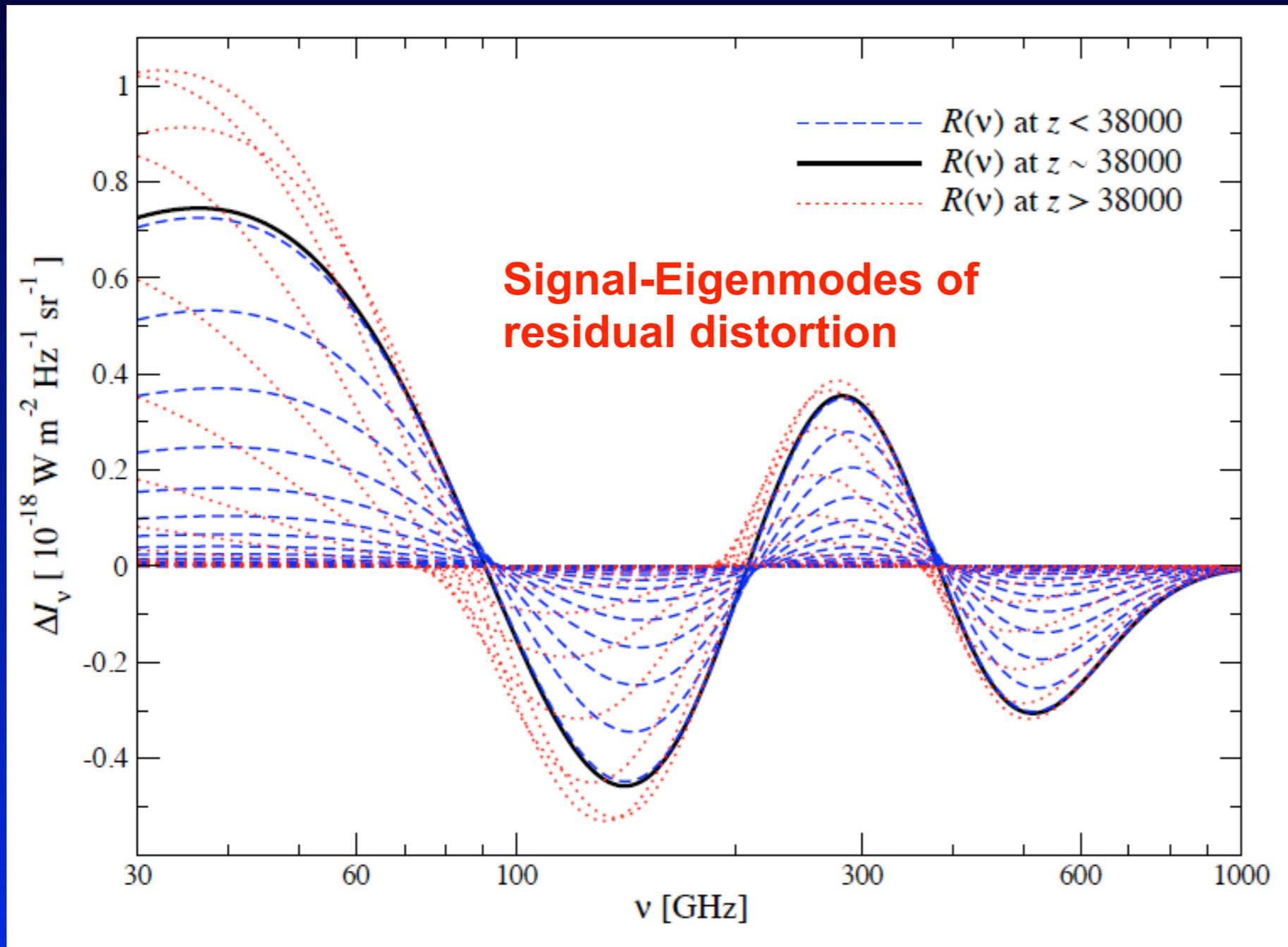


Using signal eigenmodes to compress the distortion data



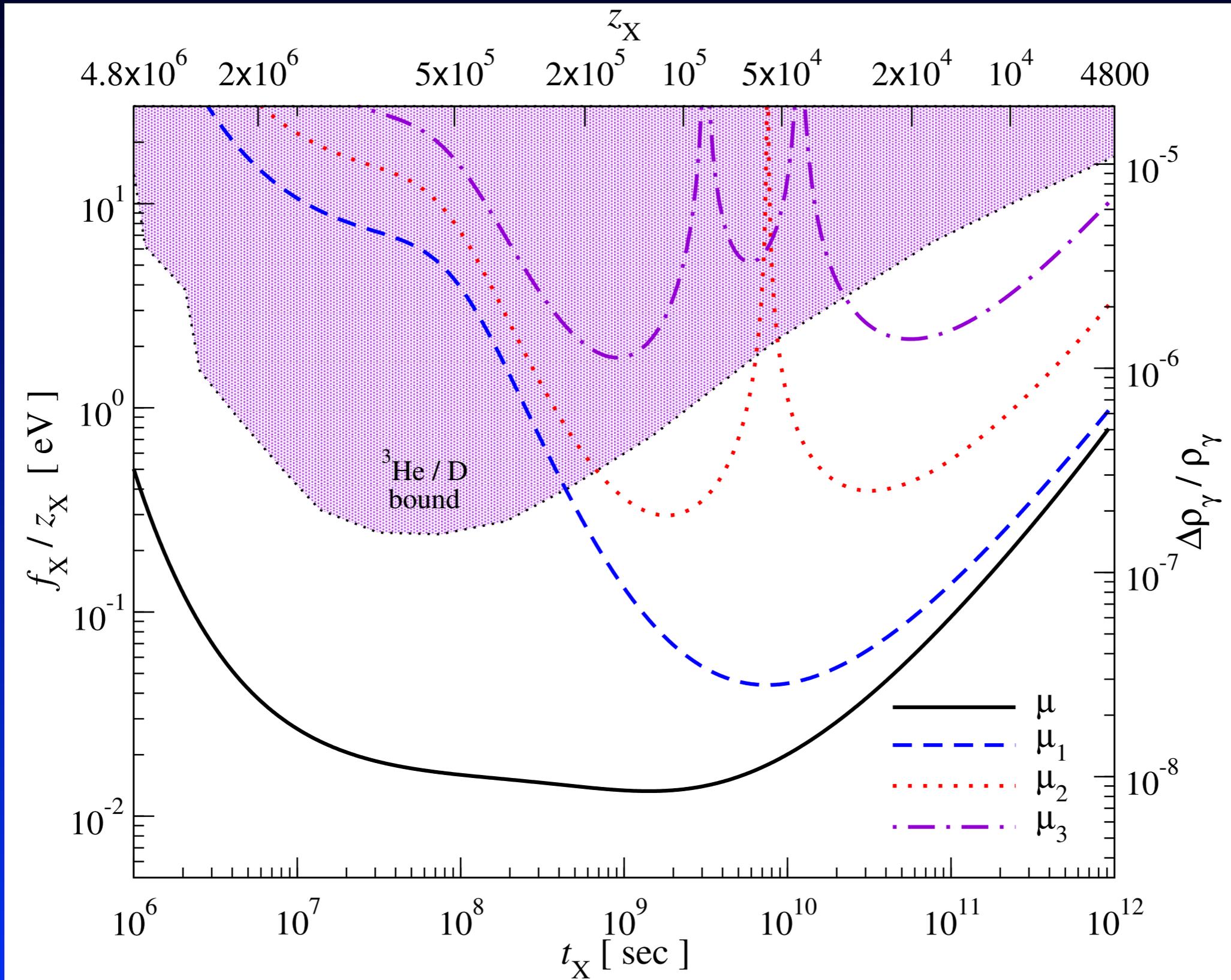
- *Principle component decomposition* of the distortion signal
- compression of the useful information given instrumental settings

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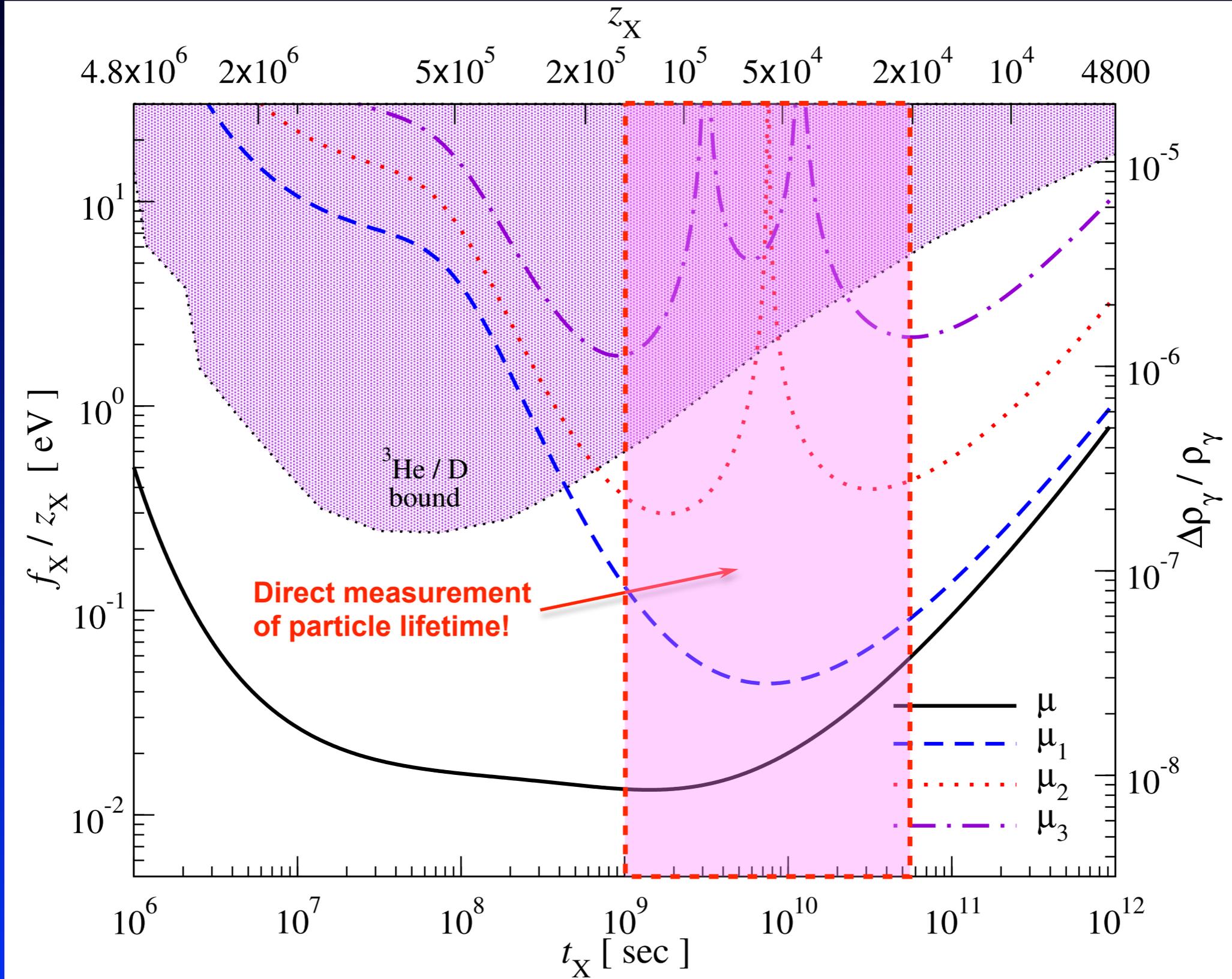


- *Principle component decomposition* of the distortion signal
- compression of the useful information given instrumental settings
- new set of observables
 $p = \{y, \mu, \mu_1, \mu_2, \dots\}$
- model-comparison + forecasts of errors very simple!

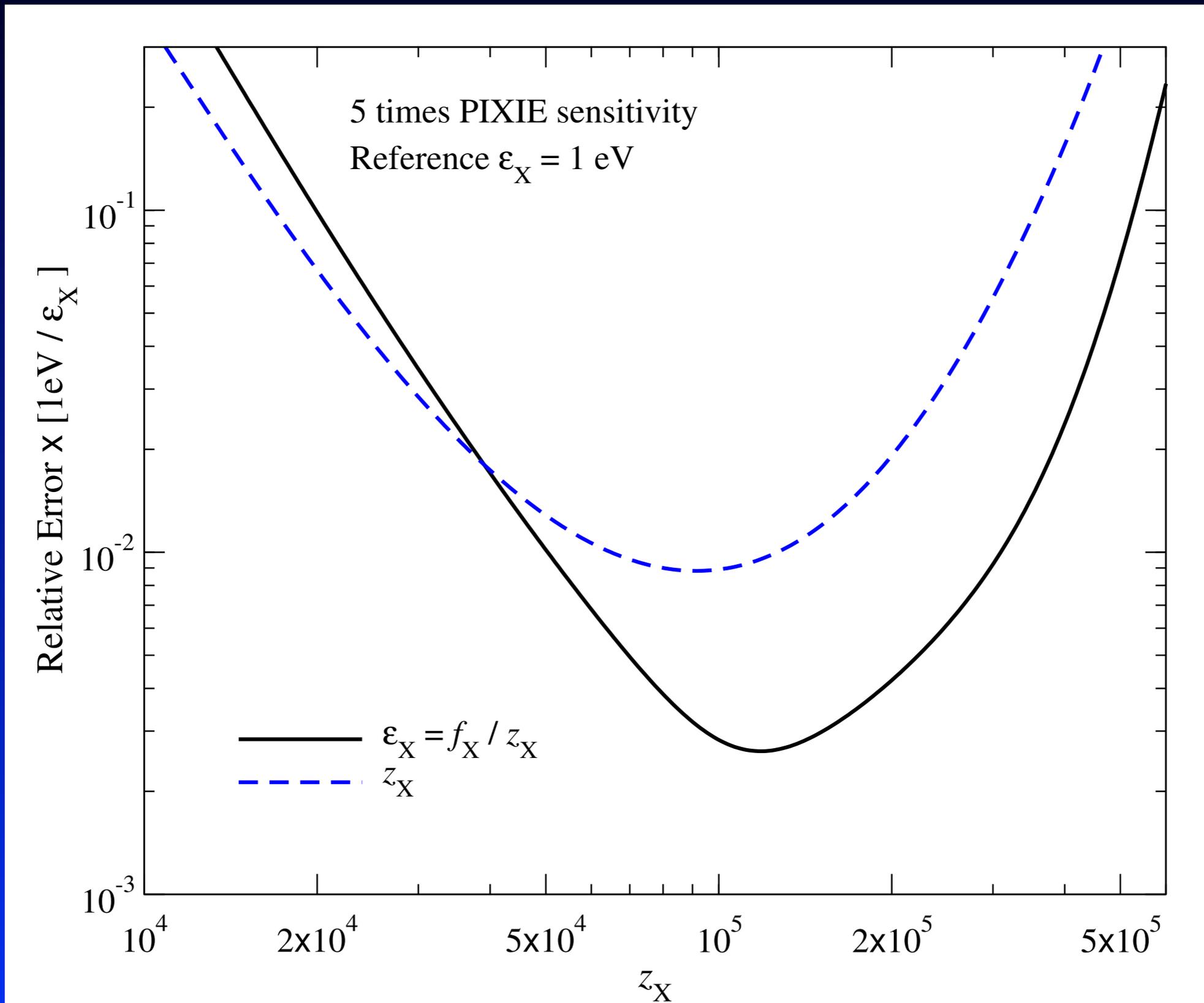
Decaying particle 1σ -detection limits for PIXIE



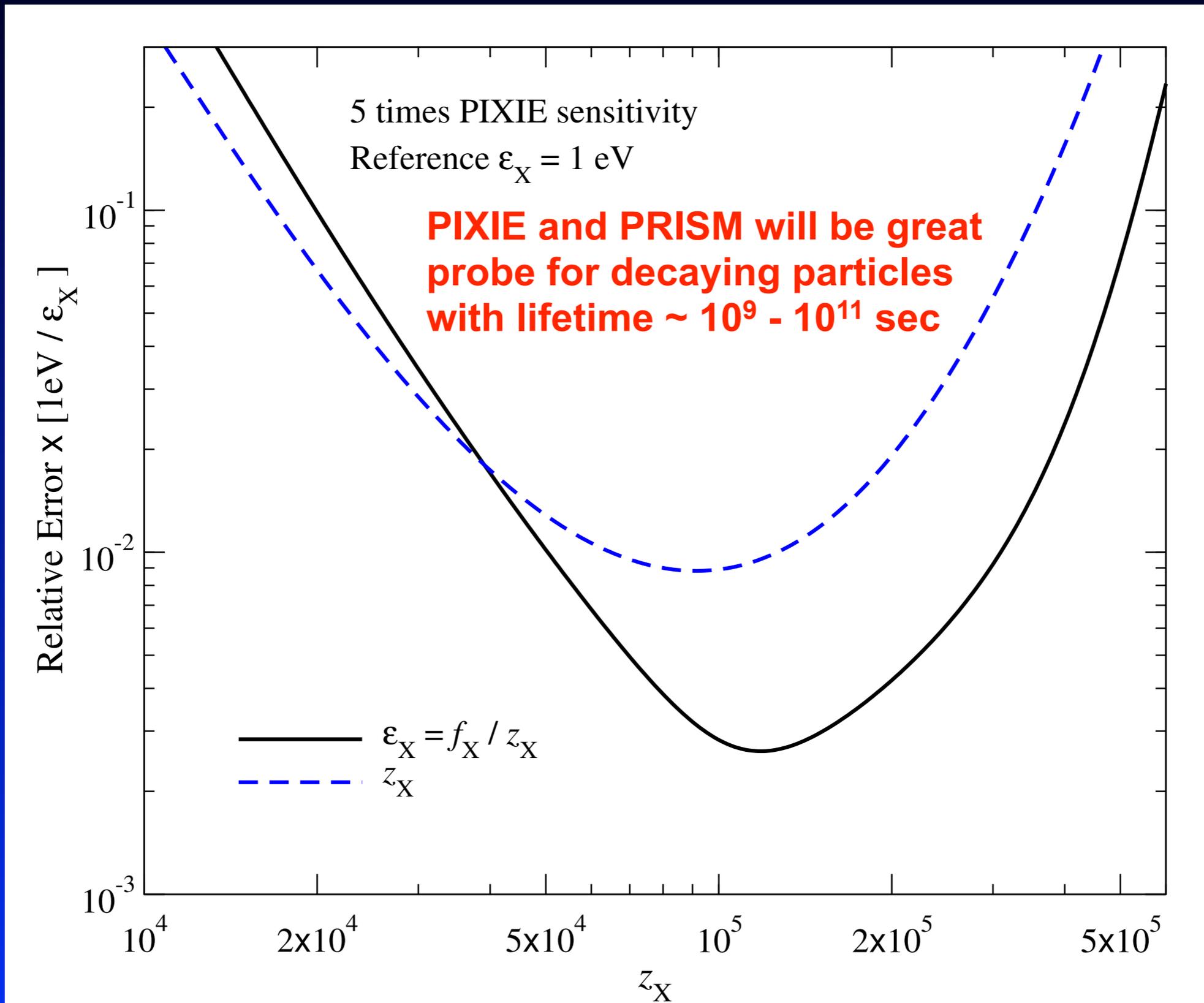
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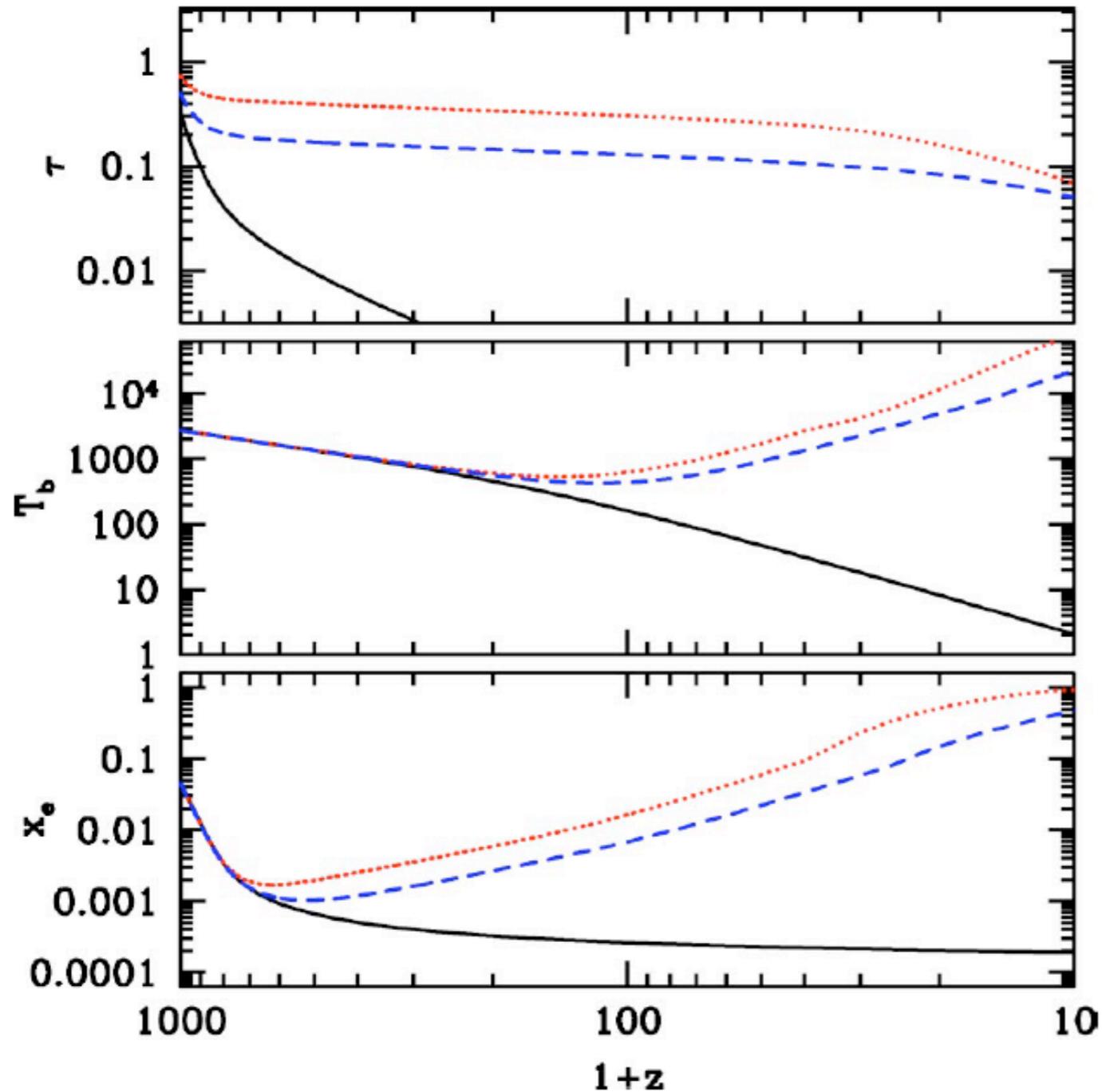
Decaying particle error forecasts



Decaying particle error forecasts

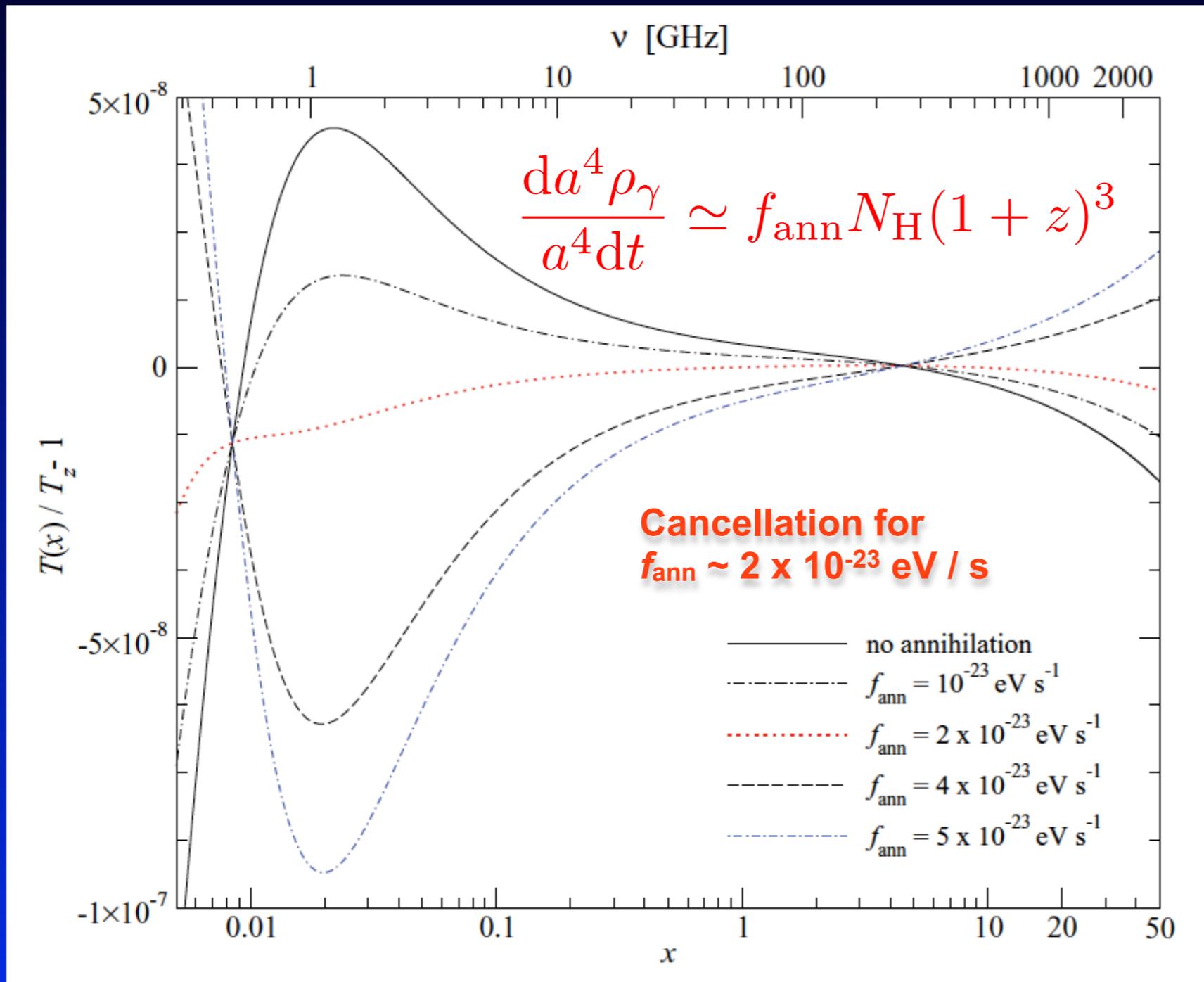


Decaying particle during & after recombination



- Modify recombination history
- this changes Thomson visibility function and thus the CMB temperature and polarization power spectra
- \Rightarrow CMB anisotropies allow probing particles with lifetimes $\gtrsim 10^{12}$ sec
- CMB spectral distortions provide complementary probe!

Cancellation of cooling by heating from annihilation



- $f_{\text{ann}} \equiv$ annihilation efficiency (Padmanabhan & Finkbeiner, 2005; JC 2010)

- CMB anisotropy constraint

$$f_{\text{ann}} \lesssim 2 \times 10^{-23} \text{ eV s}^{-1}$$

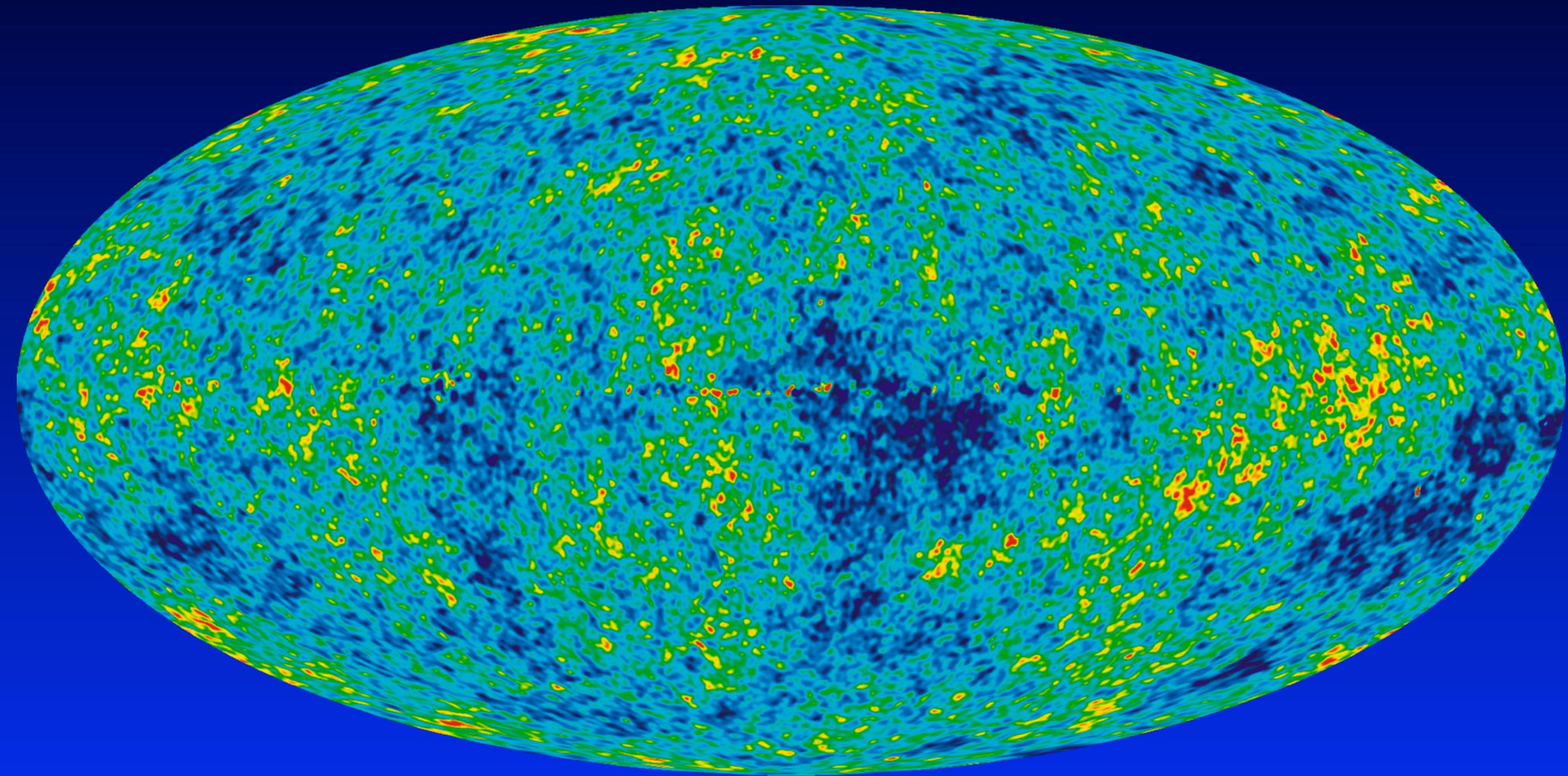
(Galli et al., 2009; Slatyer et al., 2009; Huetsi et al., 2009, 2011)

- Limit from Planck satellite will be roughly *6 times stronger* → more precise prediction for the distortion will be possible
- uncertainty dominated by particle physics
- limits from PIXIE/PRISM several times weaker, *but* independent

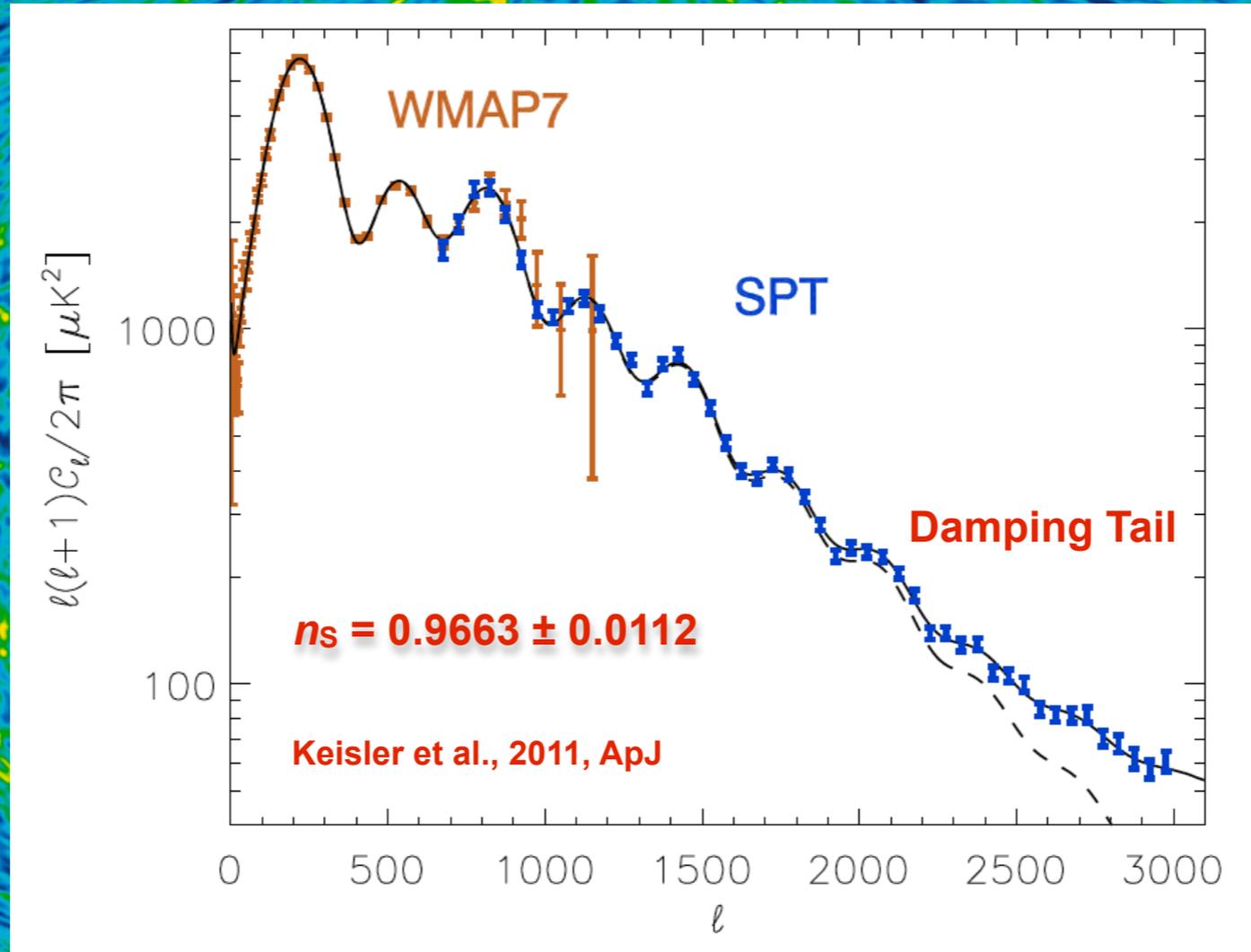
$$f_{\text{ann}} = 1.1 \times 10^{-24} \frac{100 \text{ GeV}}{M_X c^2} \left[\frac{\Omega_X h^2}{0.11} \right]^2 \frac{\langle \sigma v \rangle}{3 \times 10^{-26} \text{ cm}^3 / \text{ s}}$$

The dissipation of small-scale acoustic modes

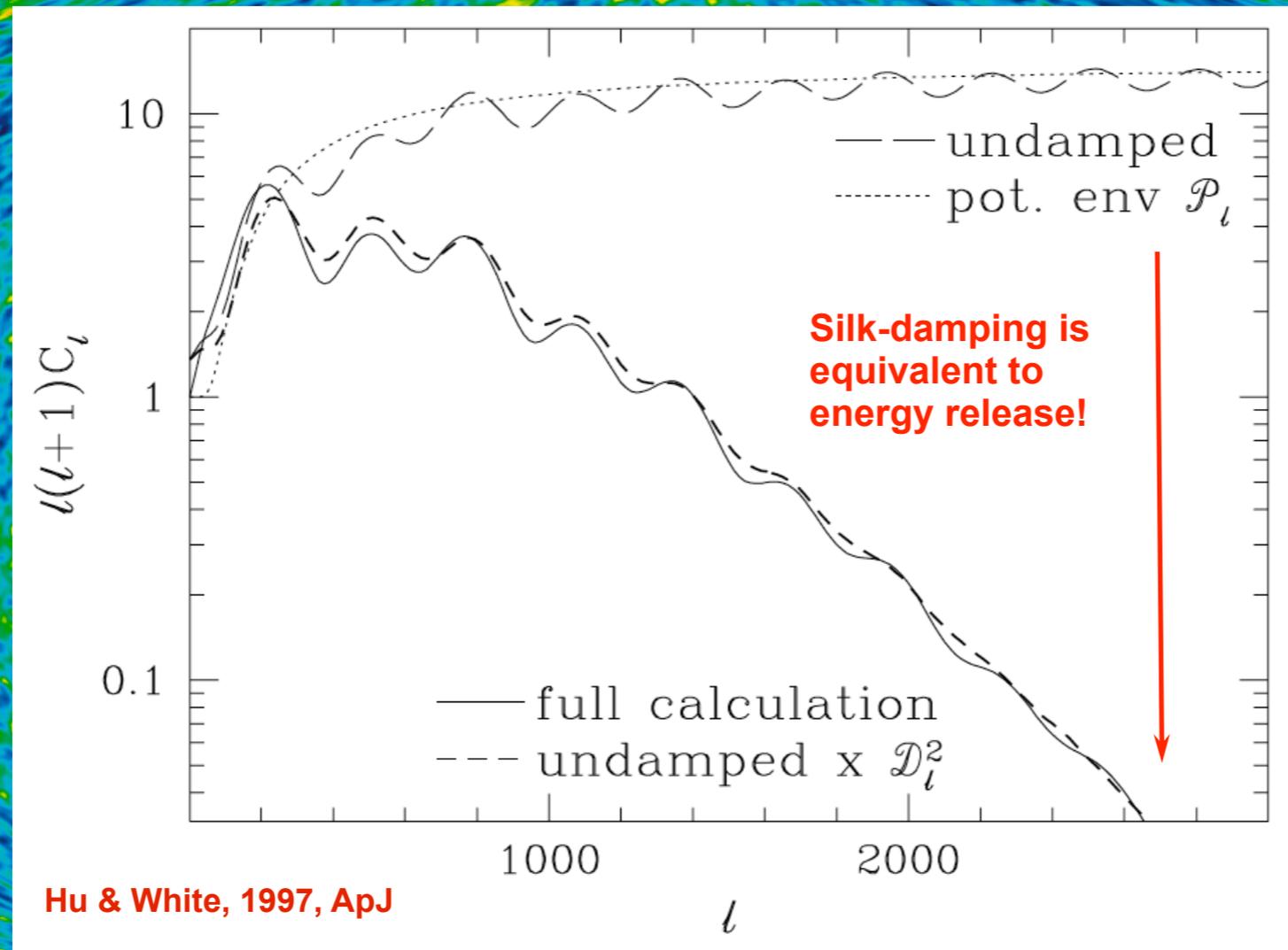
Dissipation of small-scale acoustic modes



Dissipation of small-scale acoustic modes



Dissipation of small-scale acoustic modes



Energy release caused by dissipation process

‘Obvious’ dependencies:

- *Amplitude* of the small-scale power spectrum
- *Shape* of the small-scale power spectrum
- *Dissipation scale* $\rightarrow k_D \sim (H_0 \Omega_{\text{rel}}^{1/2} N_{e,0})^{1/2} (1+z)^{3/2}$ at early times

not so ‘obvious’ dependencies:

- *primordial non-Gaussianity* in the squeezed limit
(Pajer & Zaldarriaga, 2012; Ganc & Komatsu, 2012)
- *Type* of the perturbations (adiabatic \leftrightarrow isocurvature)
(Barrow & Coles, 1991; Hu et al., 1994; Dent et al, 2012, JC & Grin, 2012)
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CMB Spectral distortions provide probe of Inflation physics!!!

Dissipation of acoustic modes: 'classical treatment'

- energy stored in plane sound waves

$$\text{Landau \& Lifshitz, 'Fluid Mechanics', \S 65} \Rightarrow Q \sim c_s^2 \rho (\delta\rho/\rho)^2$$

- expression for normal ideal gas where ρ is '*mass density*' and c_s denotes '*sounds speed*'

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- expression for normal ideal gas where ρ is '*mass density*' and c_s denotes '*sounds speed*'
- photon-baryon fluid with baryon loading $R \ll 1$

$$(c_s/c)^2 = [3(1+R)]^{-1} \sim 1/3$$

$$\rho \rightarrow \rho_Y = a_R T^4$$

$$\delta\rho/\rho \rightarrow 4(\delta T_0/T) \equiv 4\Theta_0 \leftarrow \text{only perturbation in the monopole accounted for}$$

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$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt = -16/3 d\langle \Theta_0^2 \rangle / dt$$

'minus' because *decrease* of Θ at small scales means *increase* for average spectrum

can be calculated using first order perturbation theory

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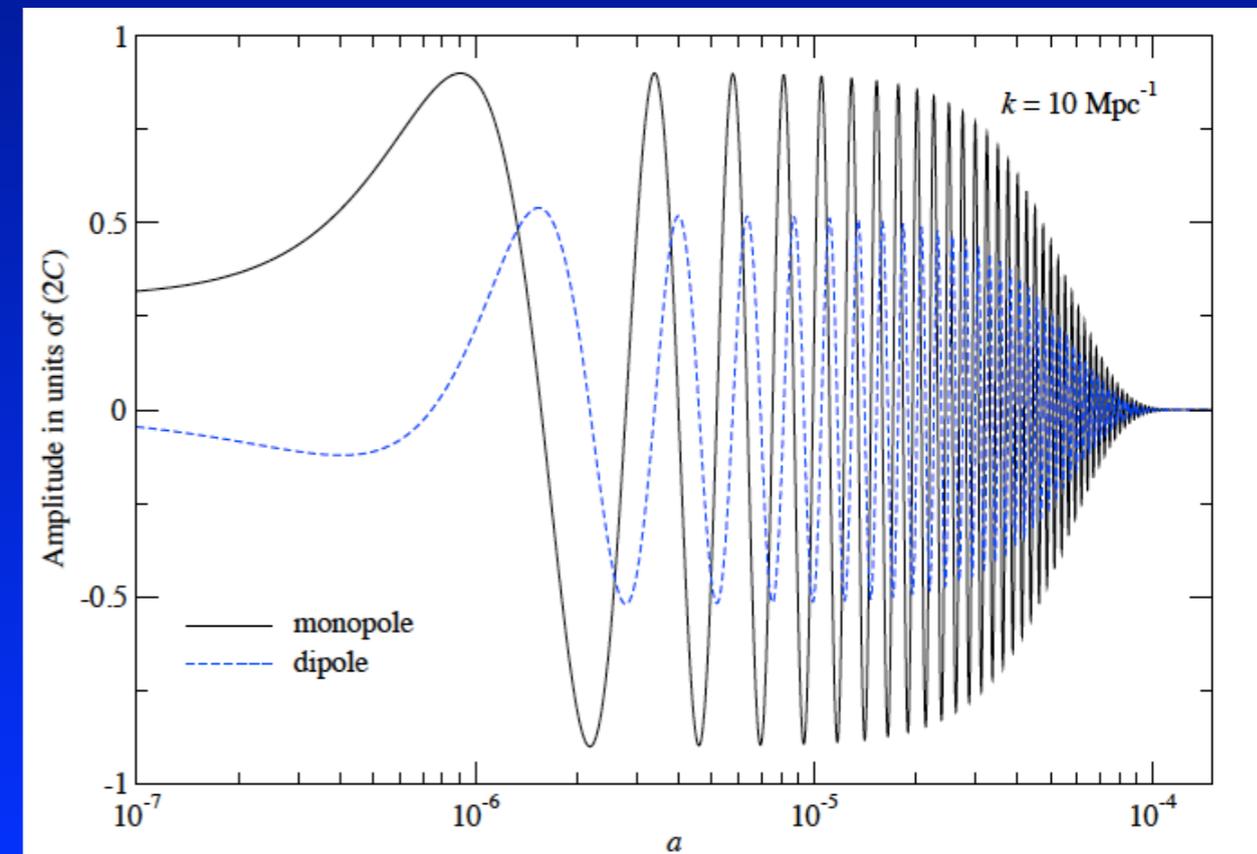
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- photon-baryon fluid with baryon loading $R \ll 1$

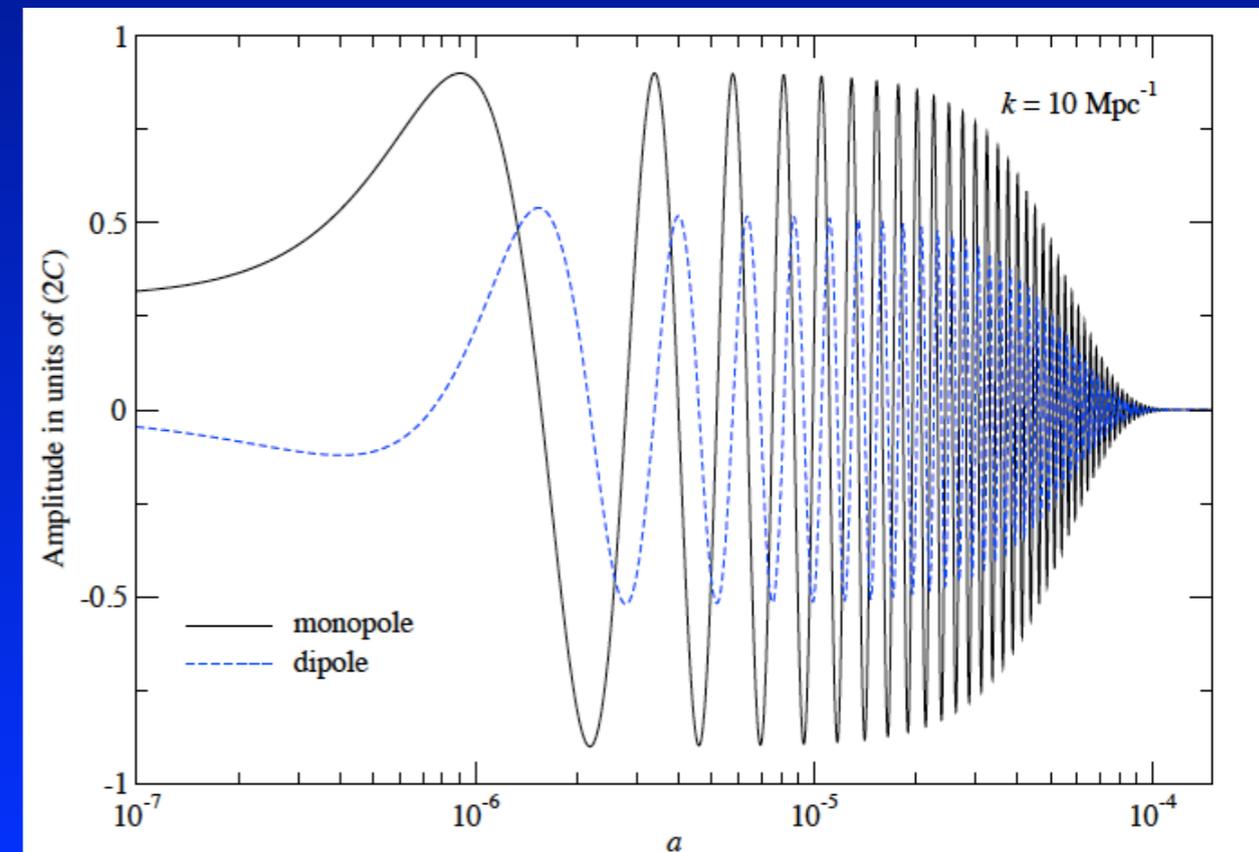
$$(c_s/c)^2 = [3(1+R)]^{-1} \sim 1/3$$

$$\rho \rightarrow \rho_Y = a_R T^4 \quad \Rightarrow \quad (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt = -16/3 d\langle \Theta_0^2 \rangle / dt$$

$$\delta\rho/\rho \rightarrow 4(\delta T_0/T) \equiv 4\Theta_0$$

- Simple estimate does *not* capture all the physics of the problem:

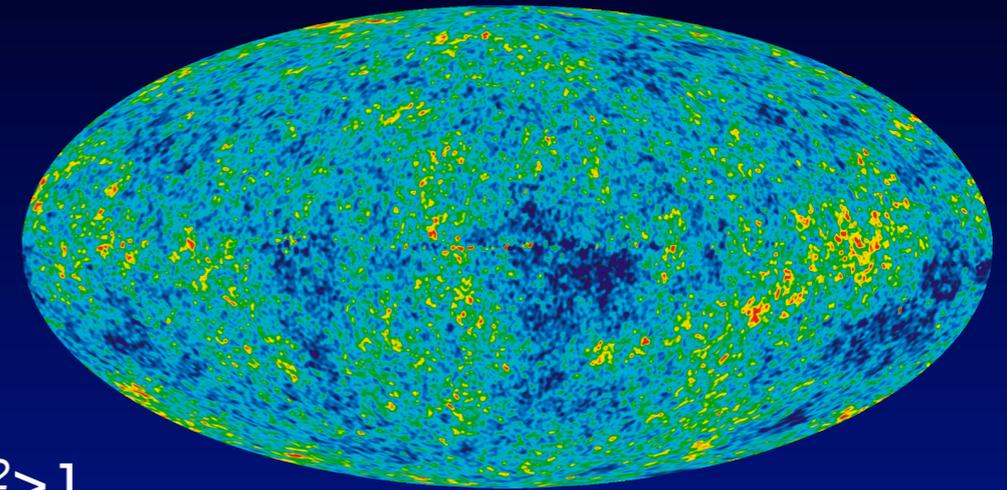
- ▶ *total energy release is 9/4 ~ 2.25 times larger!*
- ▶ *only 1/3 of the released energy goes into distortions*



Dissipation of acoustic modes: 'microscopic picture'

- after inflation: photon field has spatially varying temperature T
- average energy stored in photon field at any given moment

$$\langle \rho_\gamma \rangle = a_R \langle T^4 \rangle \approx a_R \langle T \rangle^4 [1 + 4 \underbrace{\langle \Theta \rangle}_{=0} + 6 \langle \Theta^2 \rangle]$$



E.g., our snapshot at $z=0$

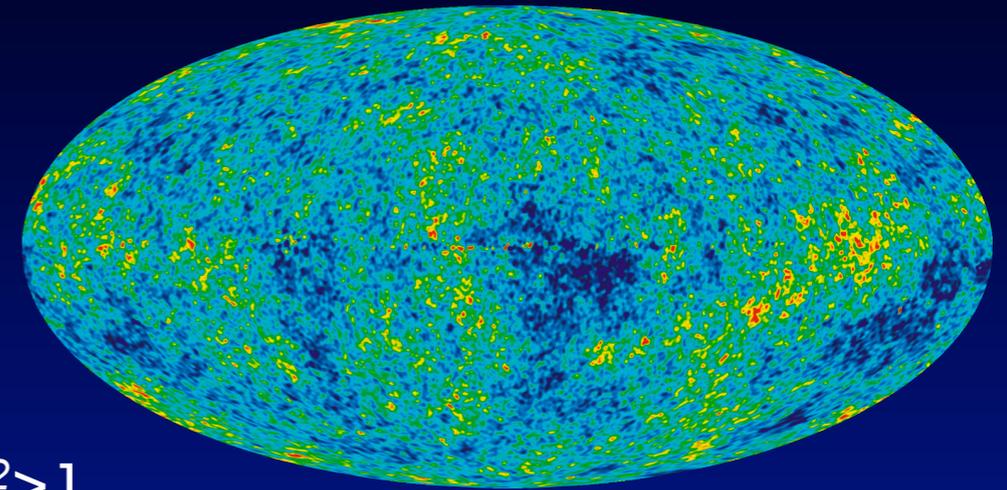
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$$\Rightarrow (a^4 \rho_\gamma)^{-1} da^4 Q_{ac}/dt = -6 d\langle \Theta^2 \rangle/dt$$

- Monopole actually **drops** out of the equation!
- In principle *all* higher multipoles contribute to the energy release



E.g., our snapshot at $z=0$

Dissipation of acoustic modes: 'microscopic picture'

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$$\langle \rho_Y \rangle = a_R \langle T^4 \rangle \approx a_R \langle T \rangle^4 [1 + 4\langle \Theta \rangle + 6\langle \Theta^2 \rangle]_{\Theta=0}$$

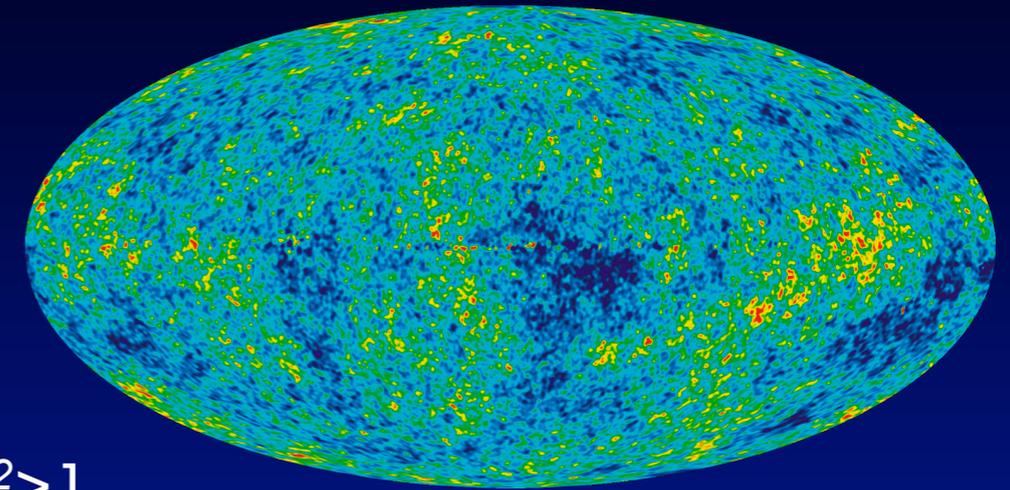
$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt = -6 d\langle \Theta^2 \rangle/dt$$

- Monopole actually **drops** out of the equation!
- In principle **all** higher multipoles contribute to the energy release
- At high redshifts ($z \geq 10^4$):

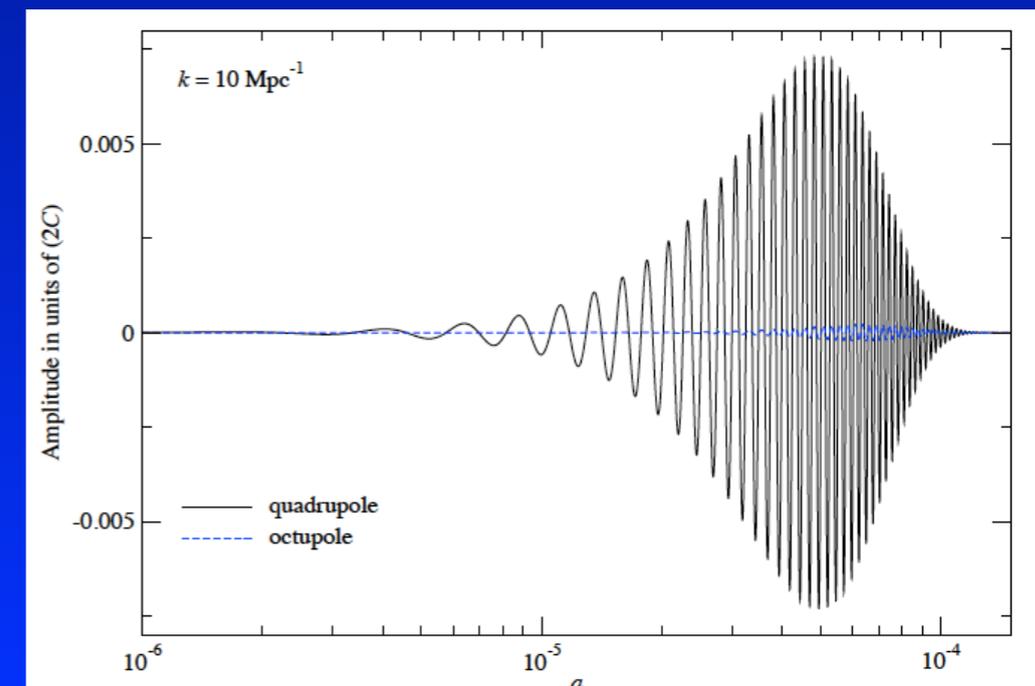
- ▶ *net (gauge-invariant) dipole and contributions from higher multipoles are negligible*
- ▶ *dominant term caused by quadrupole anisotropy*

$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt \approx -12 d\langle \Theta_0^2 \rangle/dt$$

9/4 larger than classical estimate

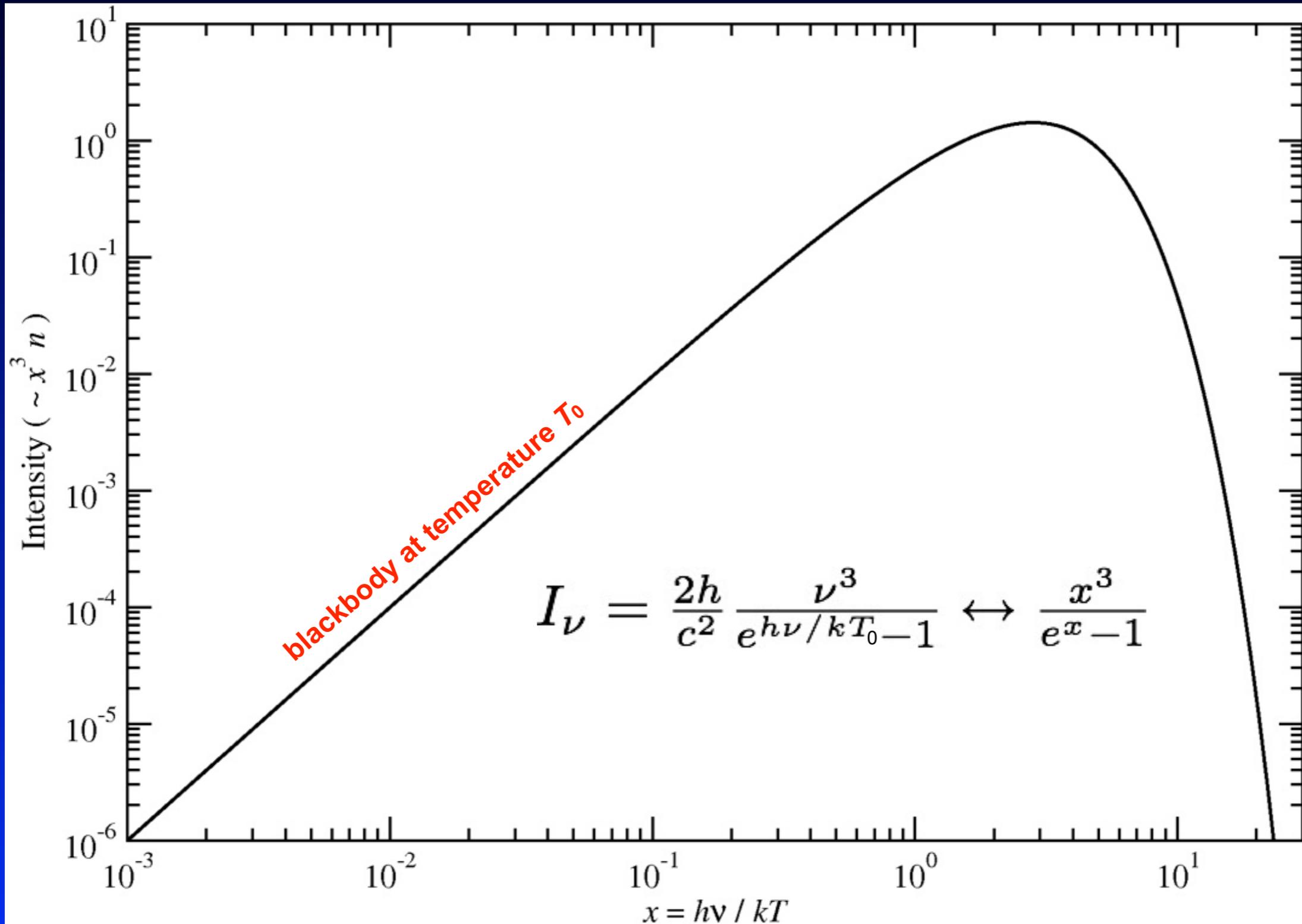


E.g., our snapshot at $z=0$

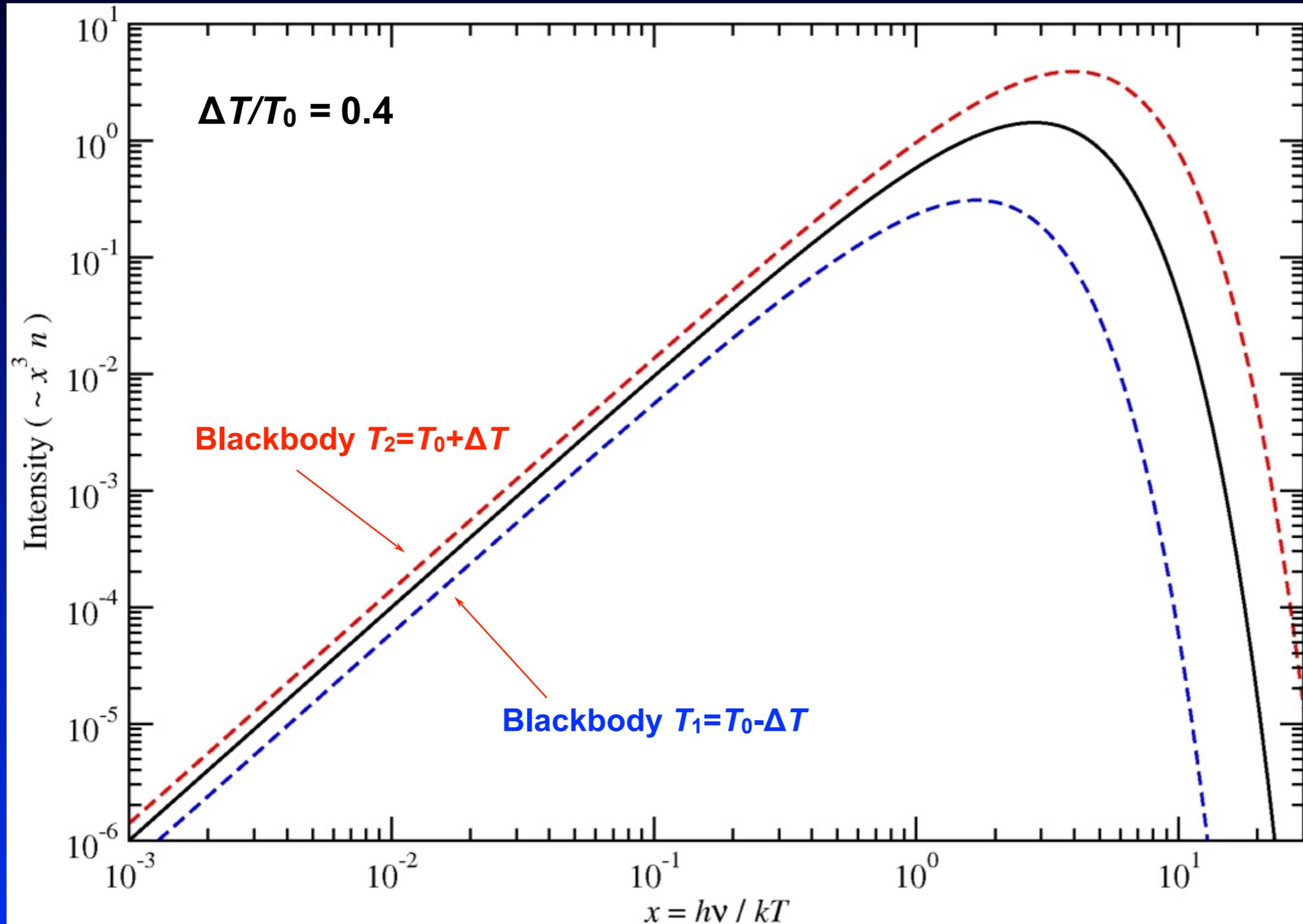


Where does the 2:1 ratio come from?

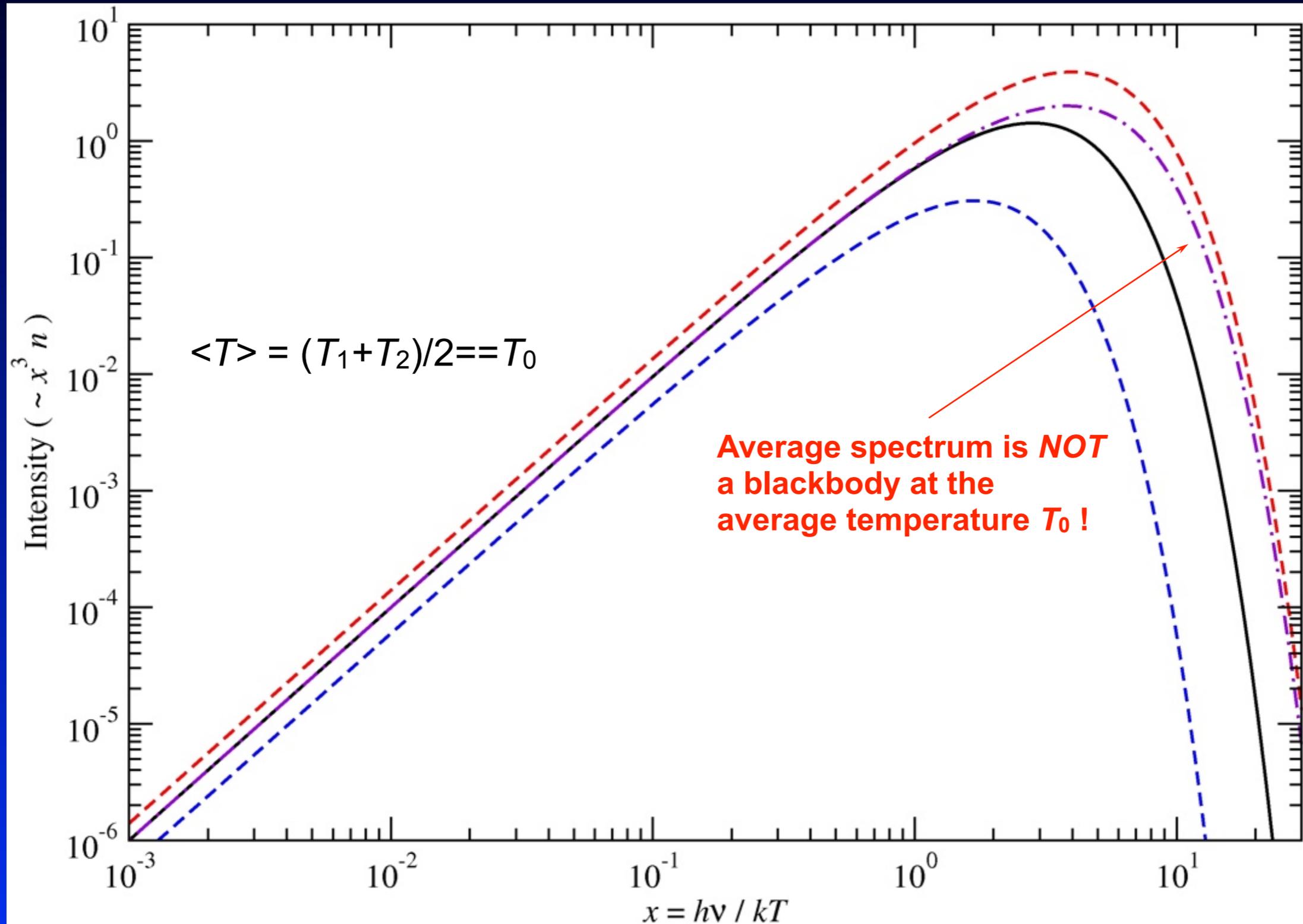
Superpositions of blackbody spectra



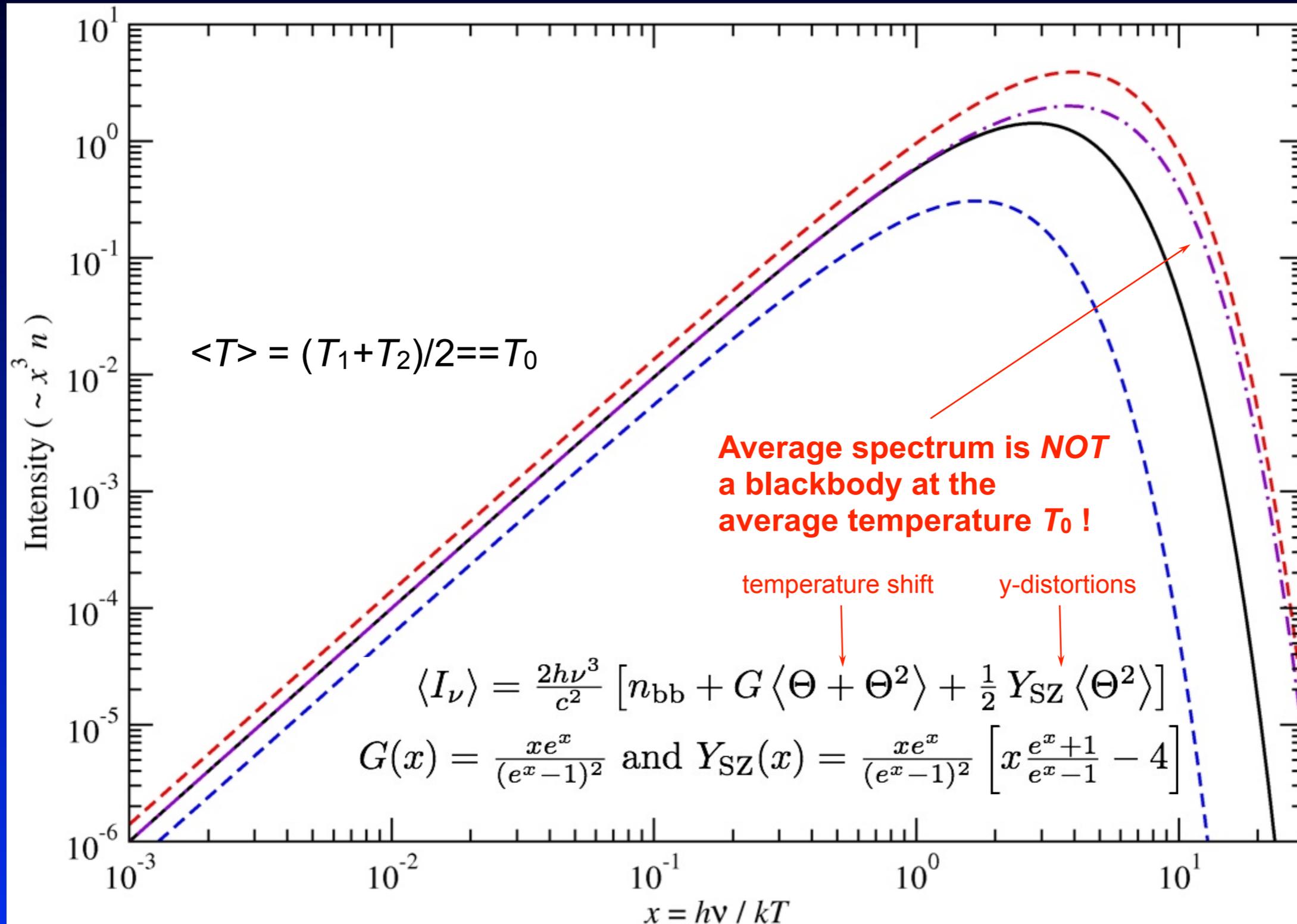
Superpositions of blackbody spectra



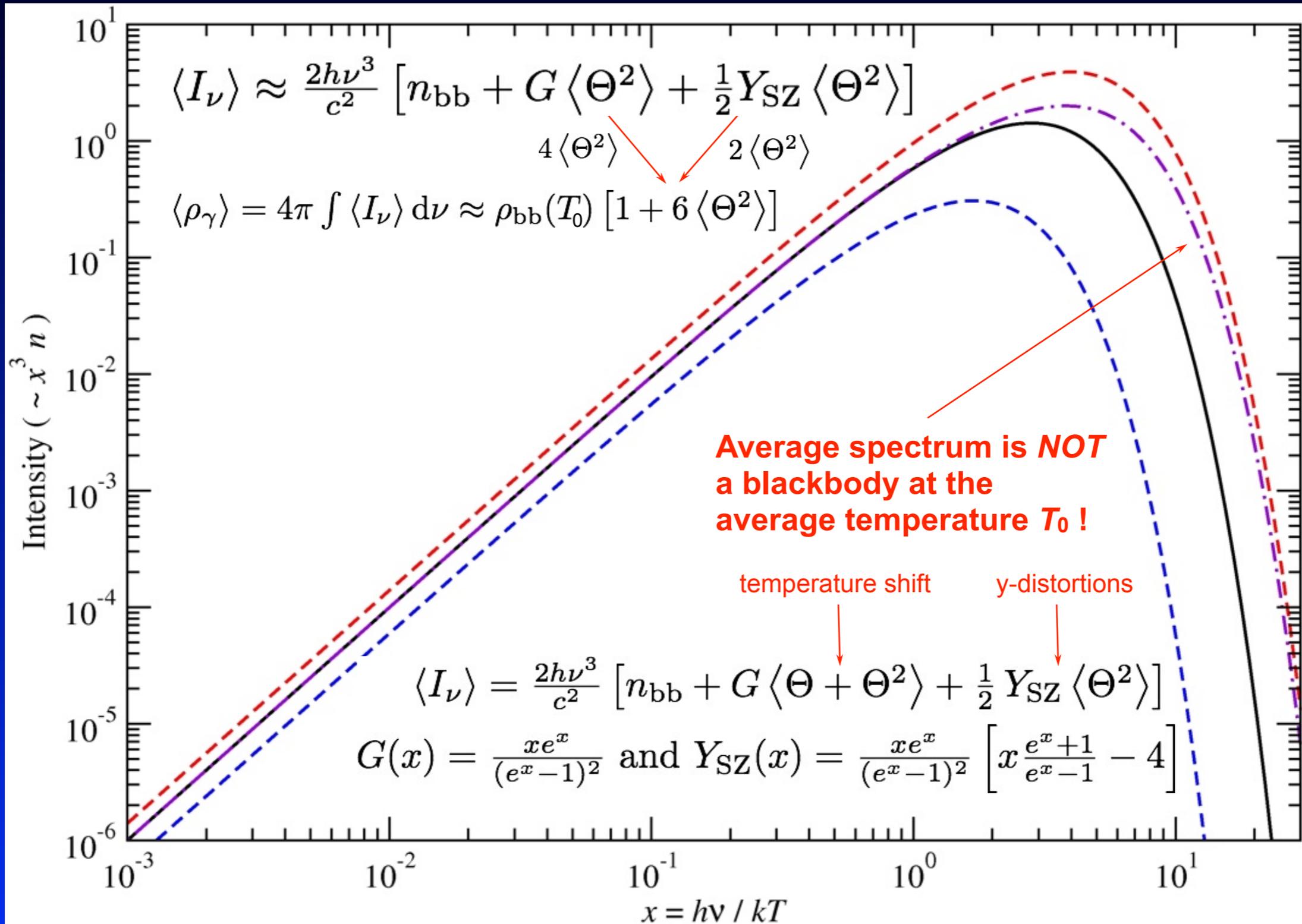
Superpositions of blackbody spectra



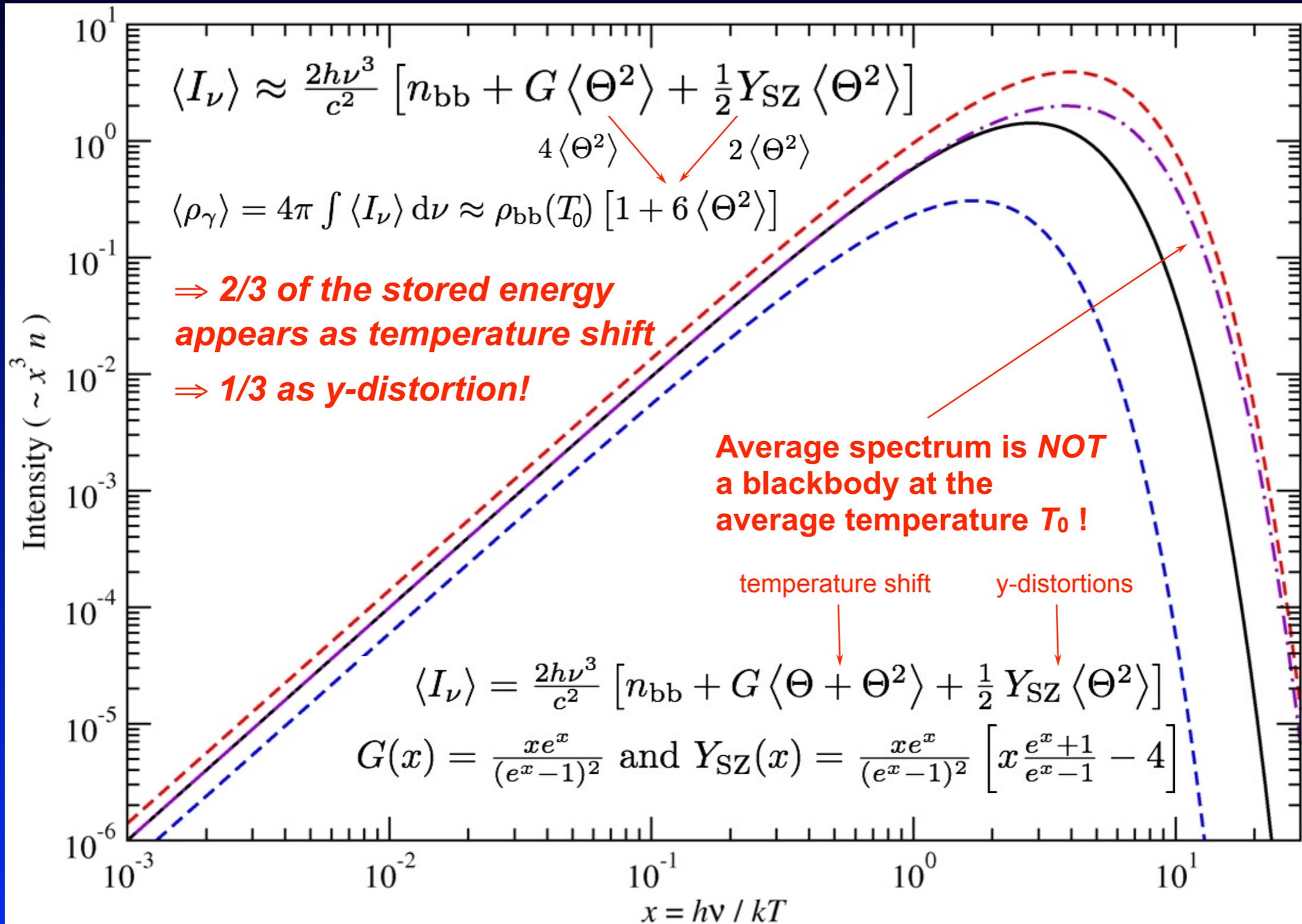
Superpositions of blackbody spectra



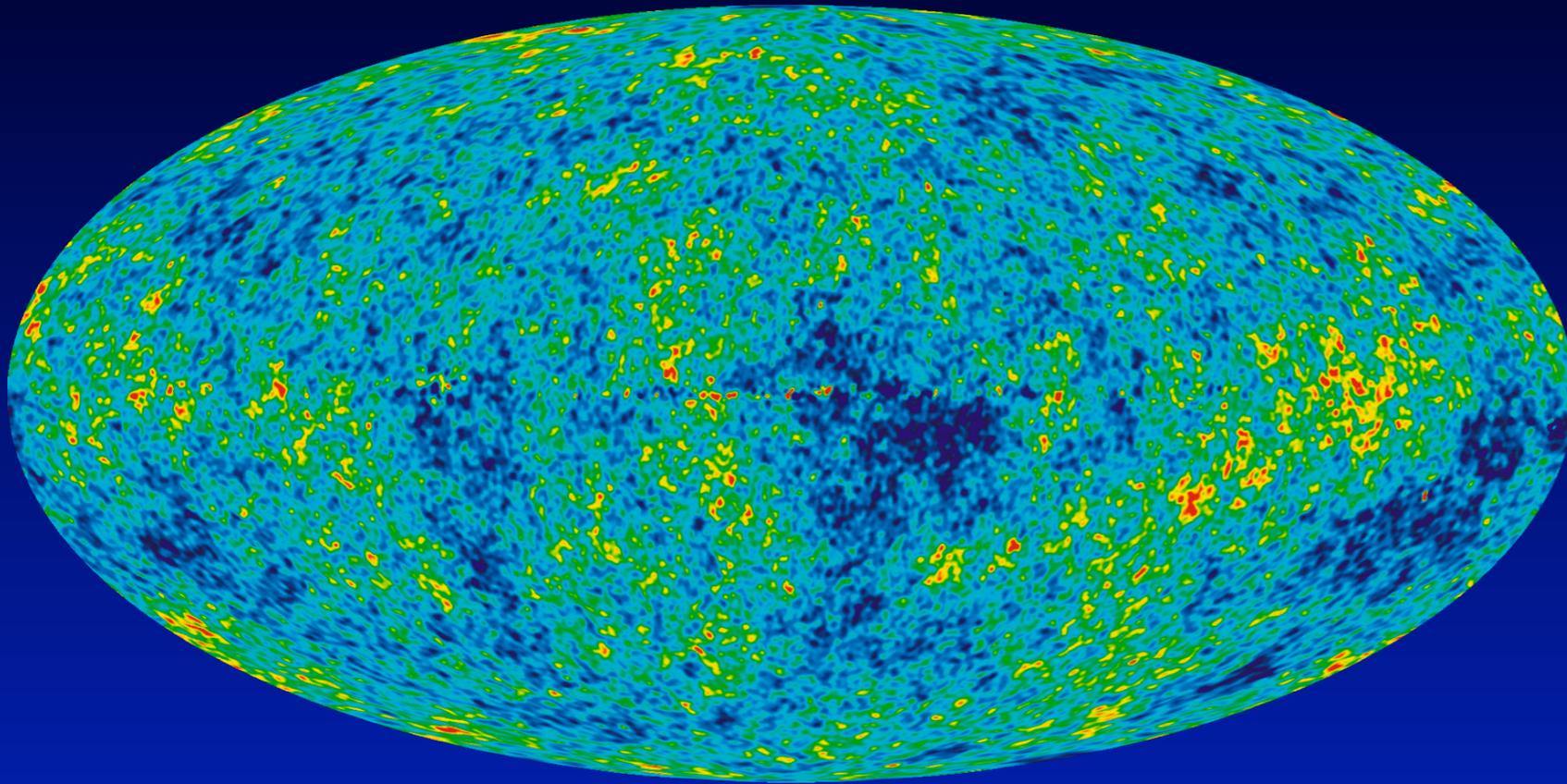
Superpositions of blackbody spectra



Superpositions of blackbody spectra



Distortion caused by superposition of blackbodies



- average spectrum

$$\Rightarrow y \simeq \frac{1}{2} \left\langle \left(\frac{\Delta T}{T} \right)^2 \right\rangle \approx 8 \times 10^{-10}$$

$$\Delta T_{\text{sup}} \simeq T \left\langle \left(\frac{\Delta T}{T} \right)^2 \right\rangle \approx 4.4 \text{ nK}$$

- known with very high precision

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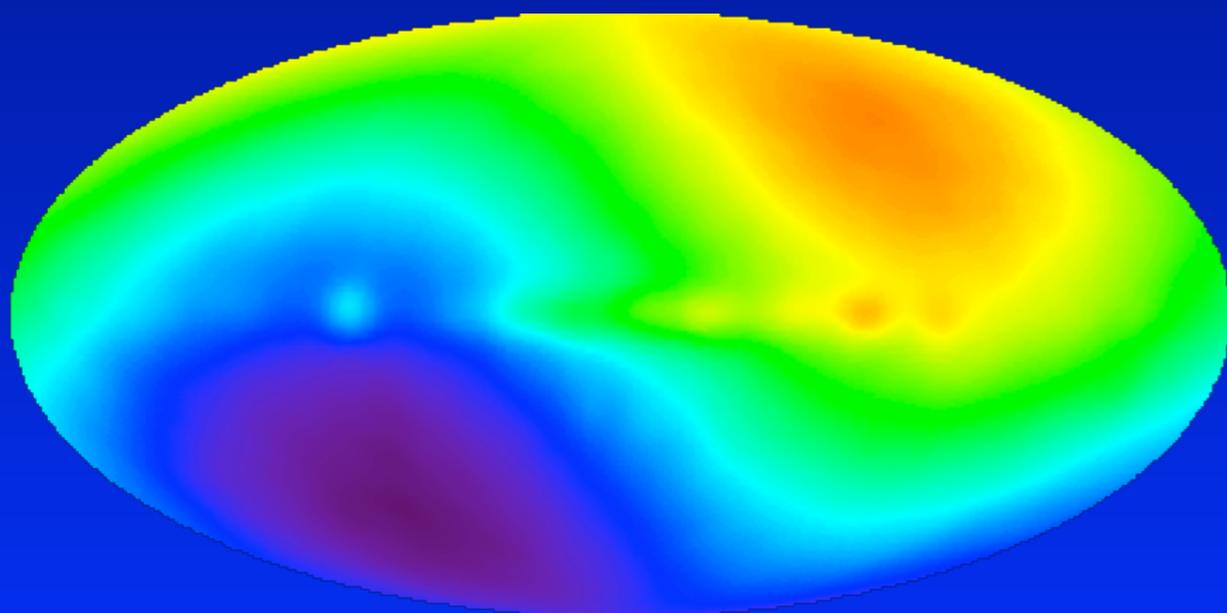
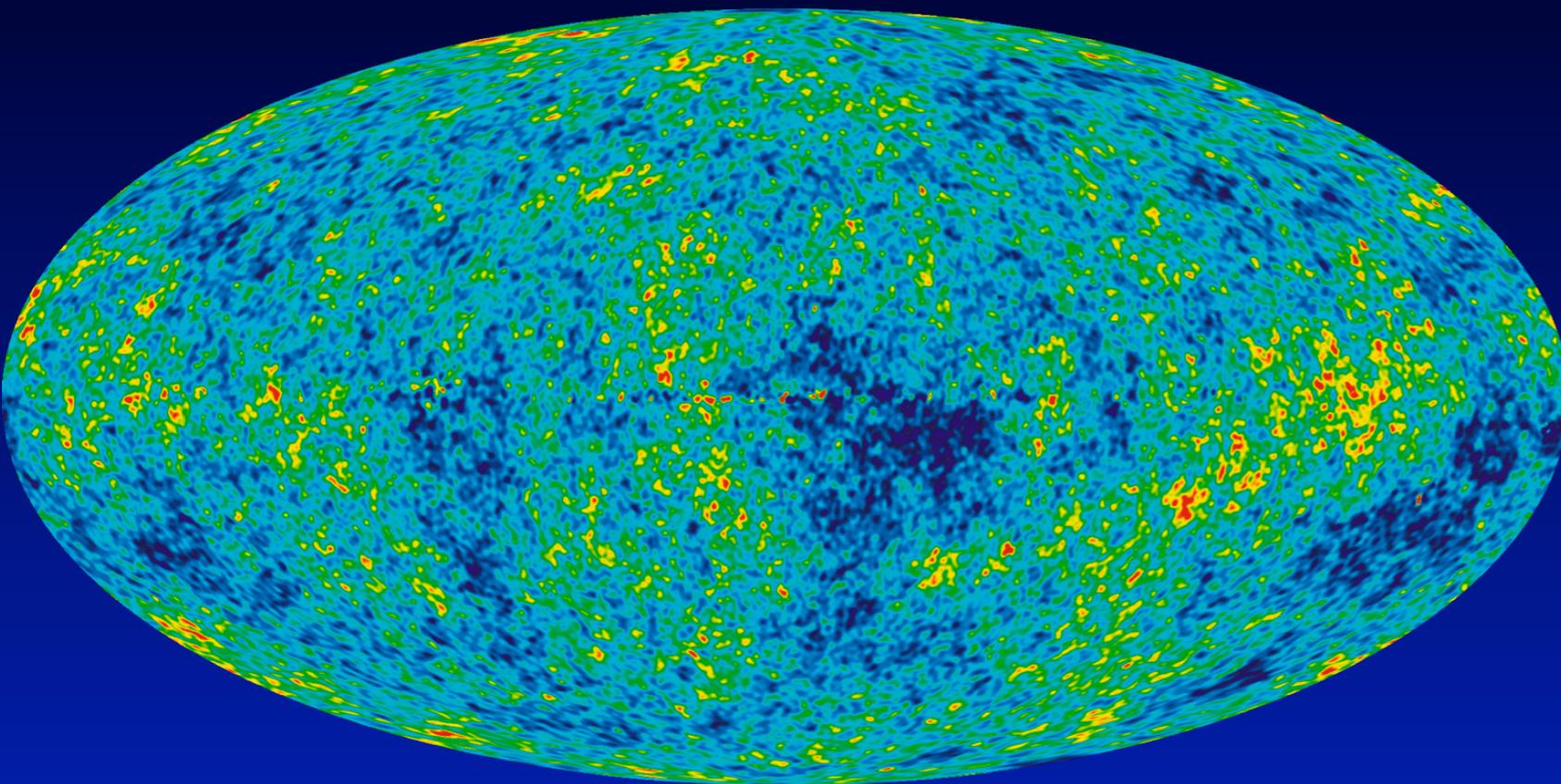
- known with very high precision

- CMB dipole ($\beta_c \sim 1.23 \times 10^{-3}$)

$$\Rightarrow y \simeq \frac{\beta_c^2}{6} \approx 2.6 \times 10^{-7}$$

$$\Delta T_{\text{sup}} \simeq T \frac{\beta_c^2}{3} \approx 1.4 \mu\text{K}$$

- electrons are up-scattered
- can be taken out at the level of $\sim 10^{-9}$



Effective energy release caused by damping effect

- Effective heating rate from full 2x2 Boltzmann treatment (JC, Khatri & Sunyaev, 2012)

$$\frac{1}{a^4 \rho_\gamma} \frac{da^4 Q_{ac}}{dt} = 4\sigma_T N_e c \left\langle \frac{(3\Theta_1 - \beta)^2}{3} + \frac{9}{2}\Theta_2^2 - \frac{1}{2}\Theta_2(\Theta_0^P + \Theta_2^P) + \sum_{l \geq 3} (2l + 1)\Theta_l^2 \right\rangle$$

$$\Theta_l = \frac{1}{2} \int \Theta(\mu) P_l(\mu) d\mu$$

gauge-independent dipole

effect of polarization

higher multipoles

$$\langle XY \rangle = \int \frac{k^2 dk}{2\pi^2} P(k) X(k) Y(k)$$

Primordial power spectrum

Effective energy release caused by damping effect

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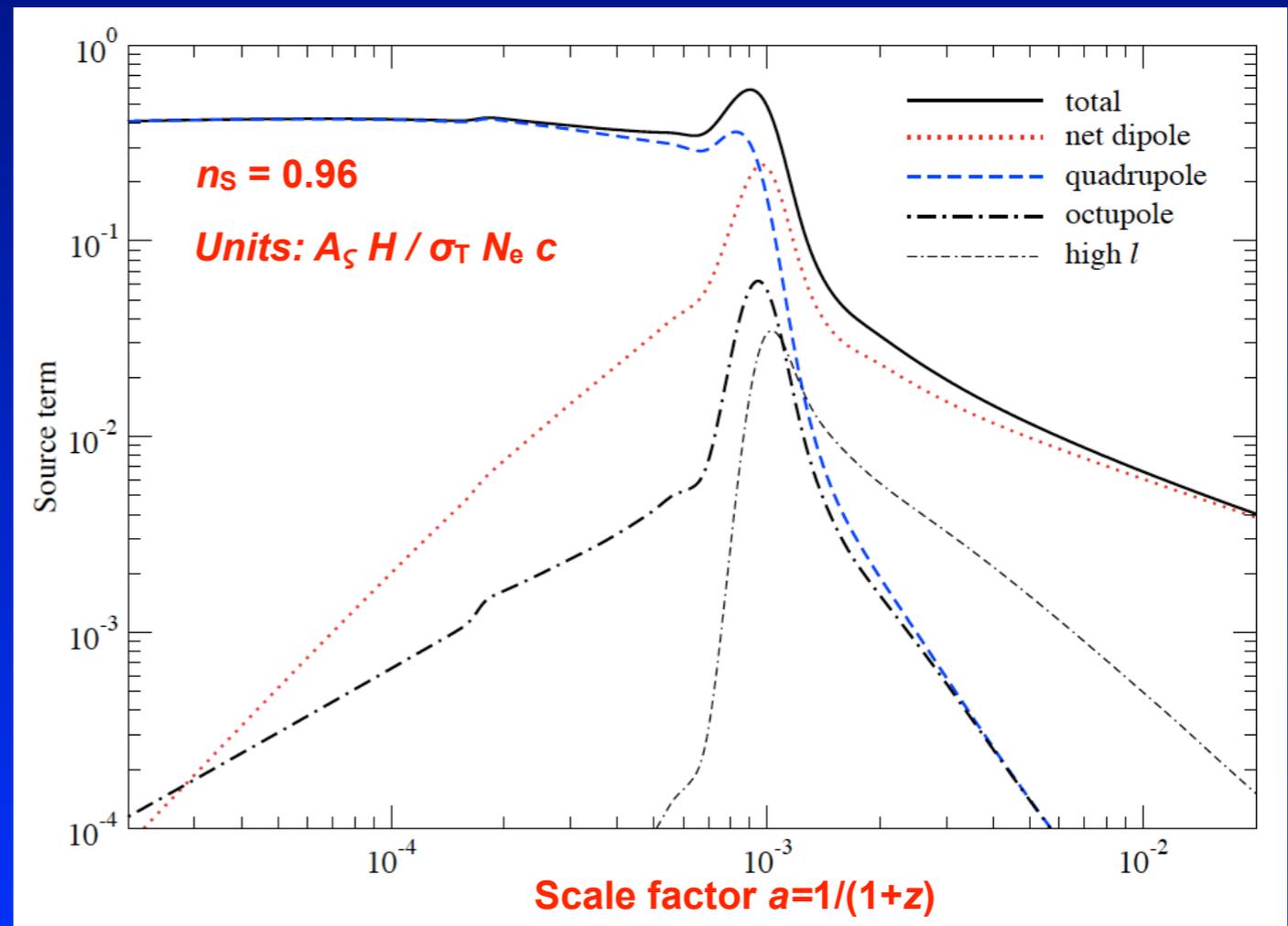
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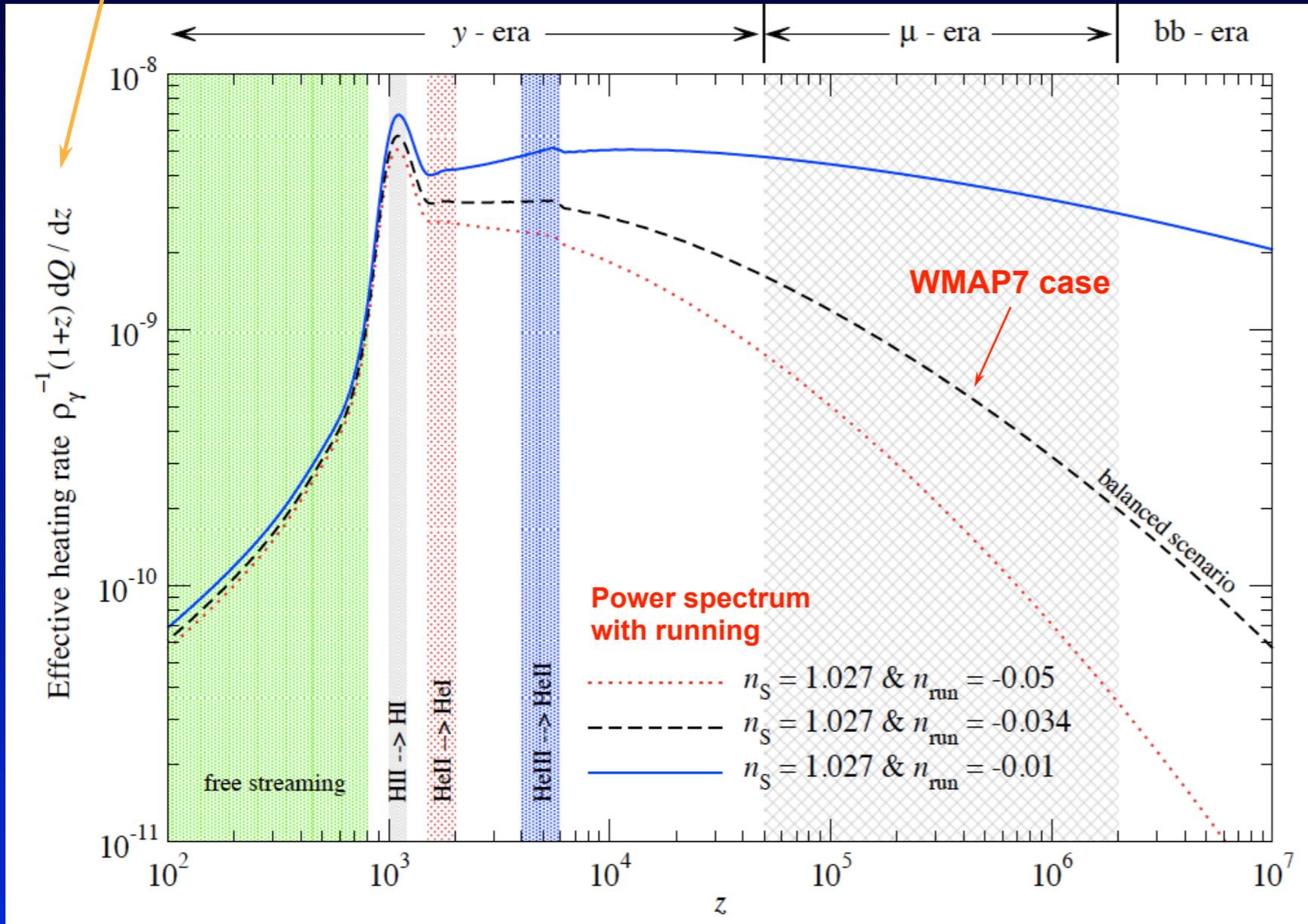
Primordial power spectrum

- quadrupole dominant at high z
- net dipole important only at low redshifts
- polarization ~5% effect
- contribution from higher multipoles rather small



Our computation for the effective energy release

scaled such that constant for $n_s = 1$



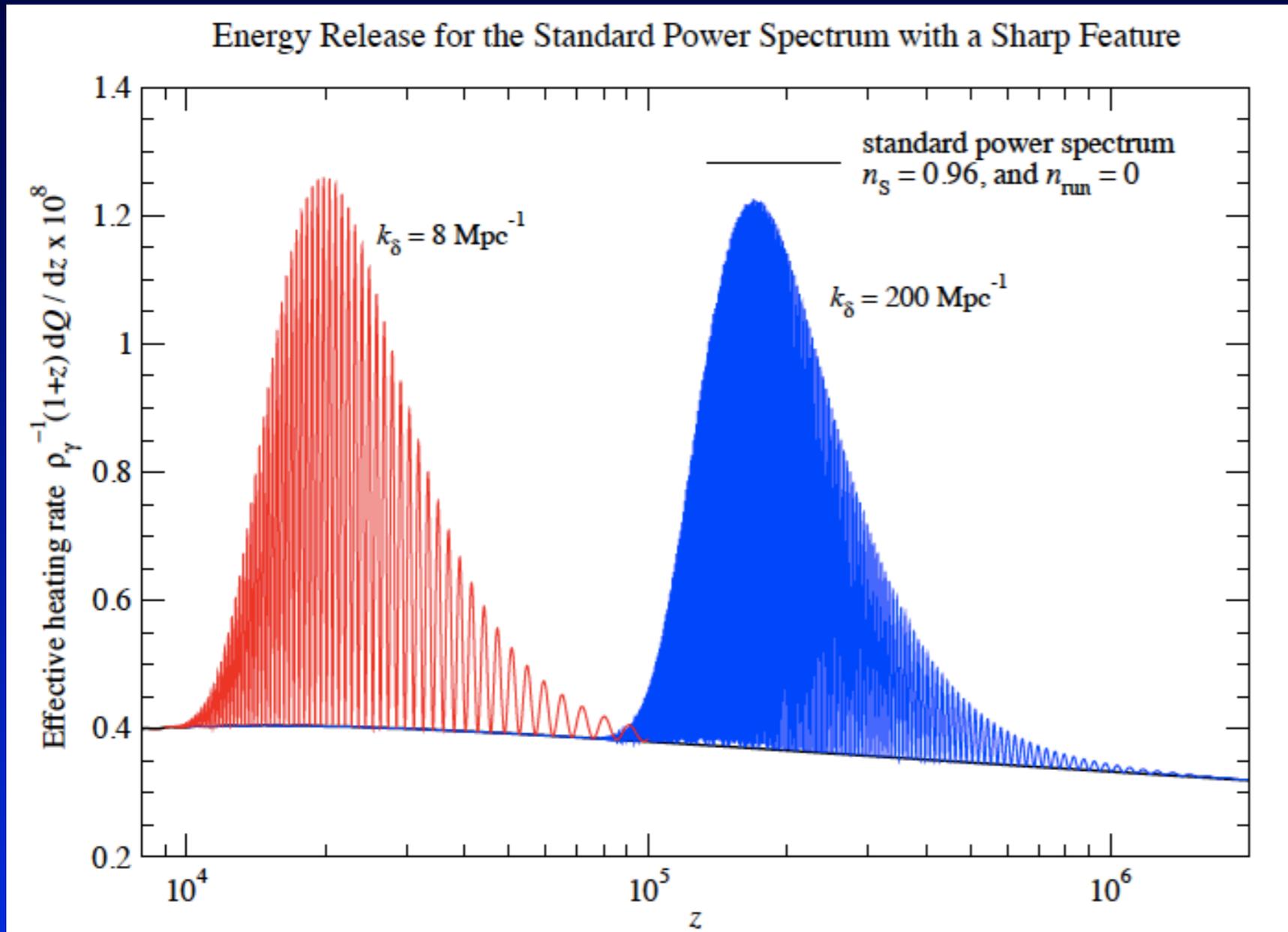
- Our 2. order perturbation calculation showed that the *classical* picture was slightly inconsistent
- Amplitude of the distortion depends on the small-scale power spectrum
- Computation carried out with **CosmoTherm** (JC & Sunyaev 2011)

JC, Khatri & Sunyaev, 2012

$$P_\zeta(k) = 2\pi^2 A_\zeta k^{-3} (k/k_0)^{n_s - 1 + \frac{1}{2} n_{run} \ln(k/k_0)}$$

Primordial power spectrum of curvature perturbations is input for the calculation

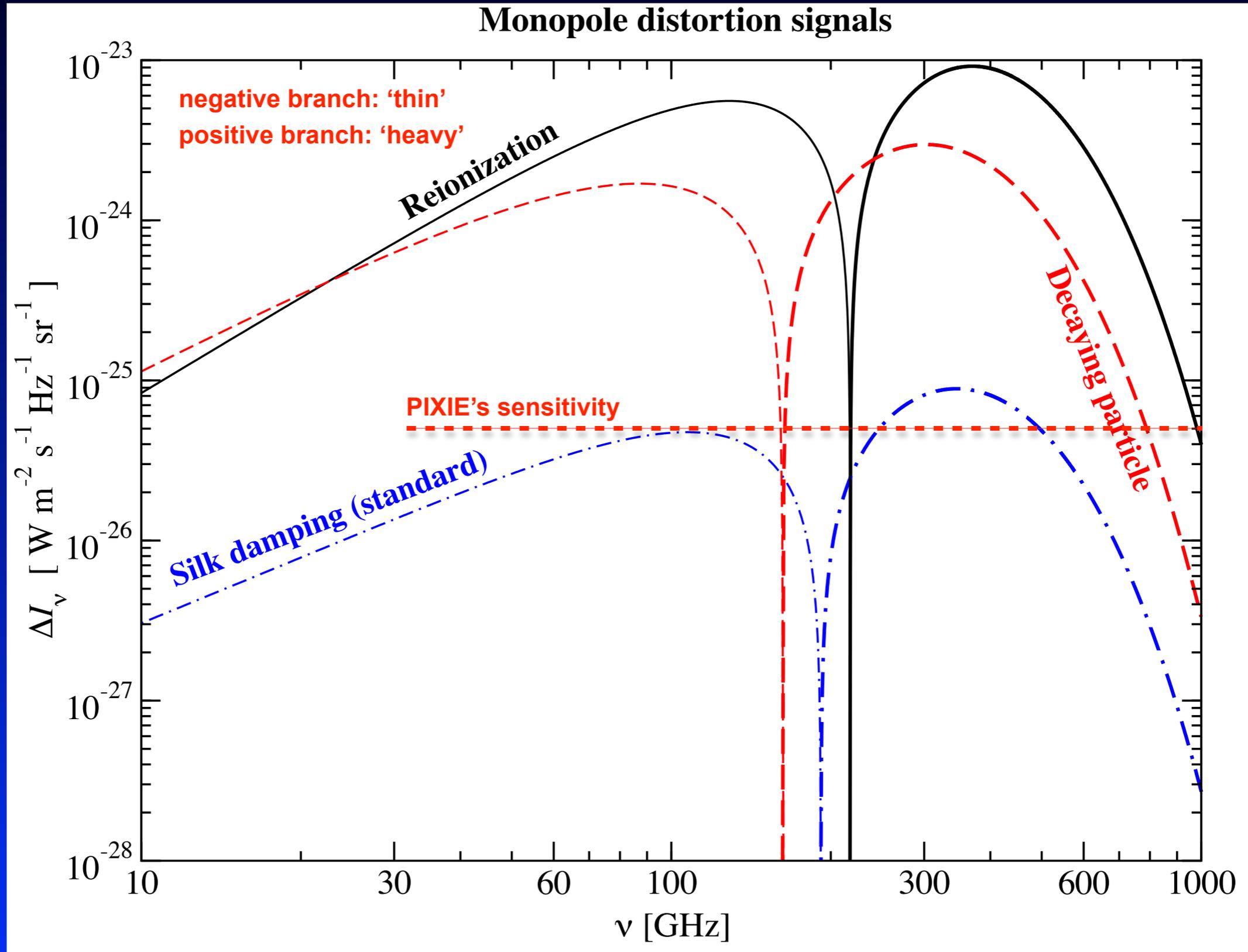
Which modes dissipate in the μ and y -eras?



- Single mode with wavenumber k dissipates its energy at $z_d \sim 4.5 \times 10^5 (k \text{ Mpc}/10^3)^{2/3}$
- Modes with wavenumber $50 \text{ Mpc}^{-1} < k < 10^4 \text{ Mpc}^{-1}$ dissipate their energy during the μ -era
- Modes with $k < 50 \text{ Mpc}^{-1}$ cause y -distortion

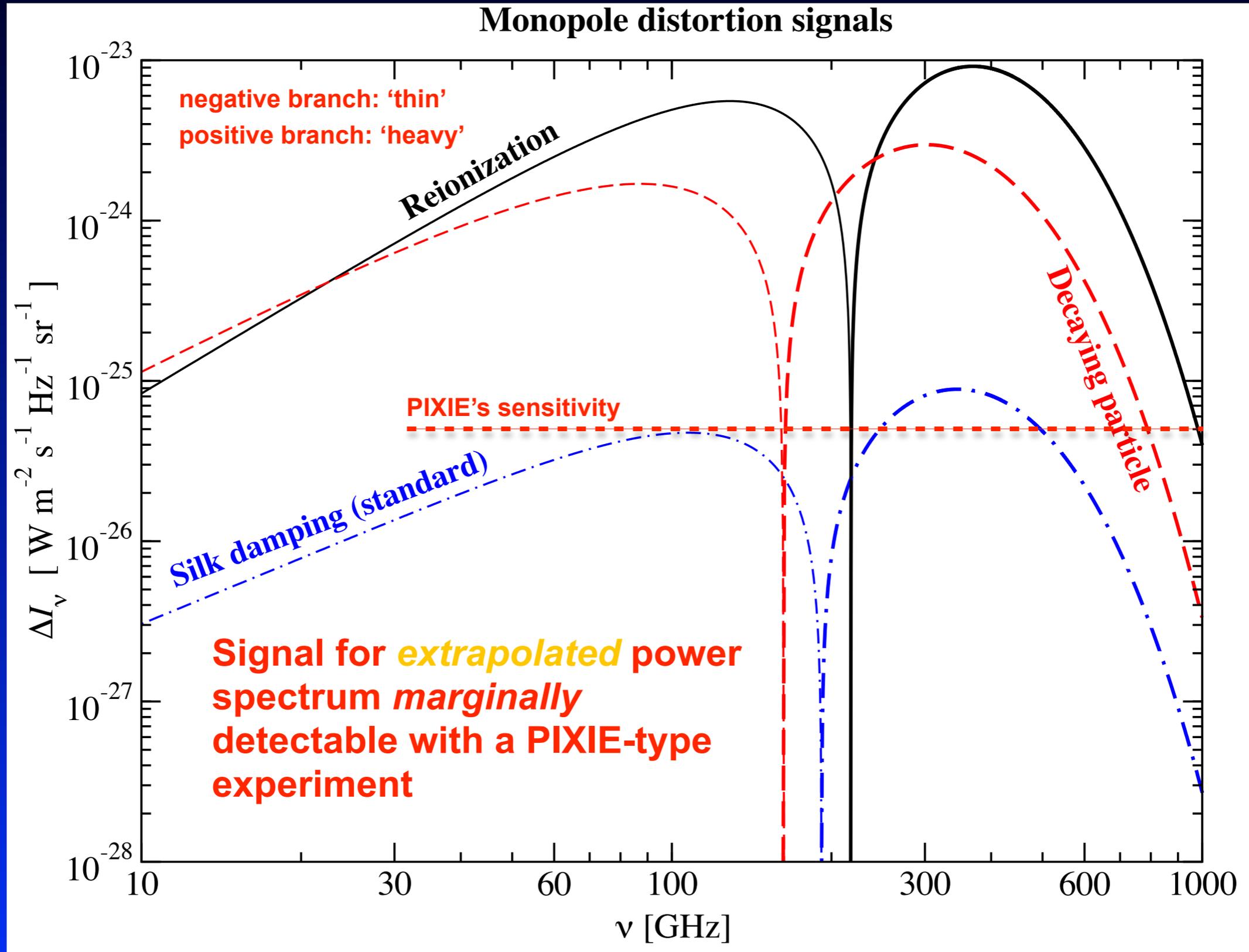
Average CMB spectral distortions

Absolute value of Intensity signal



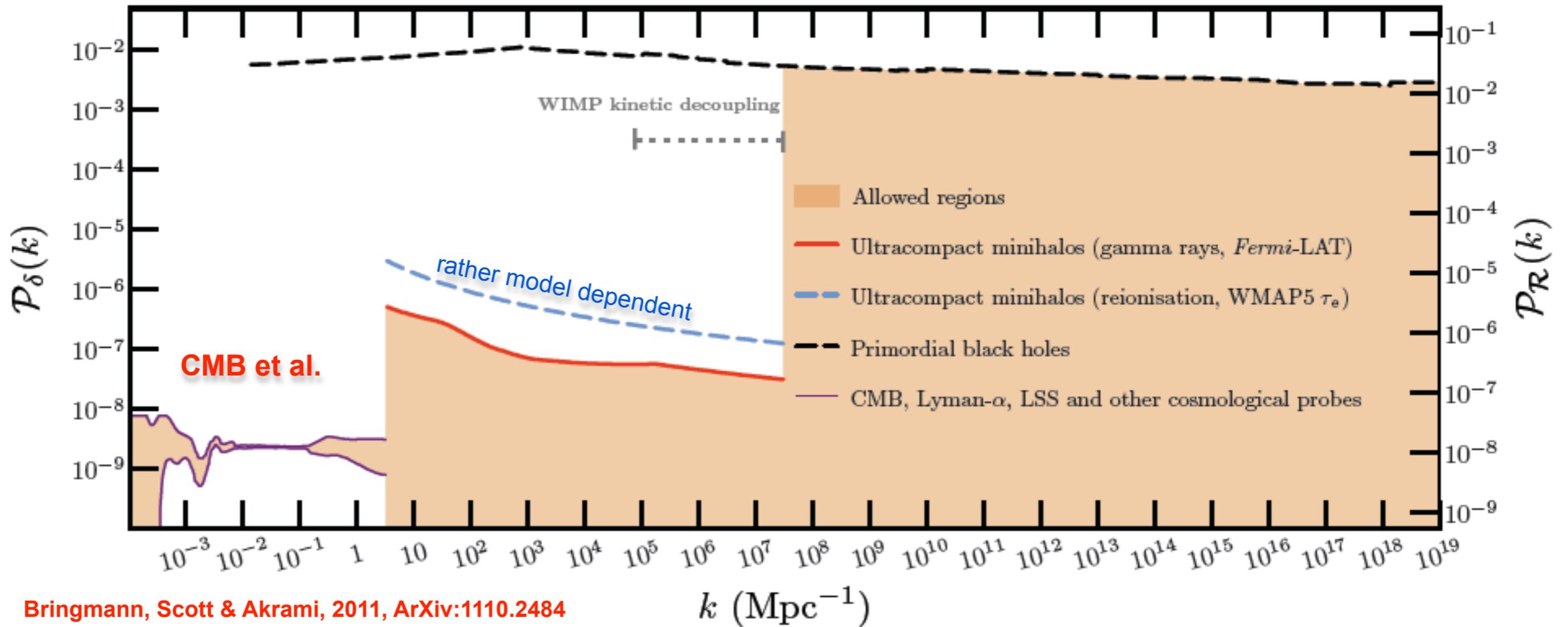
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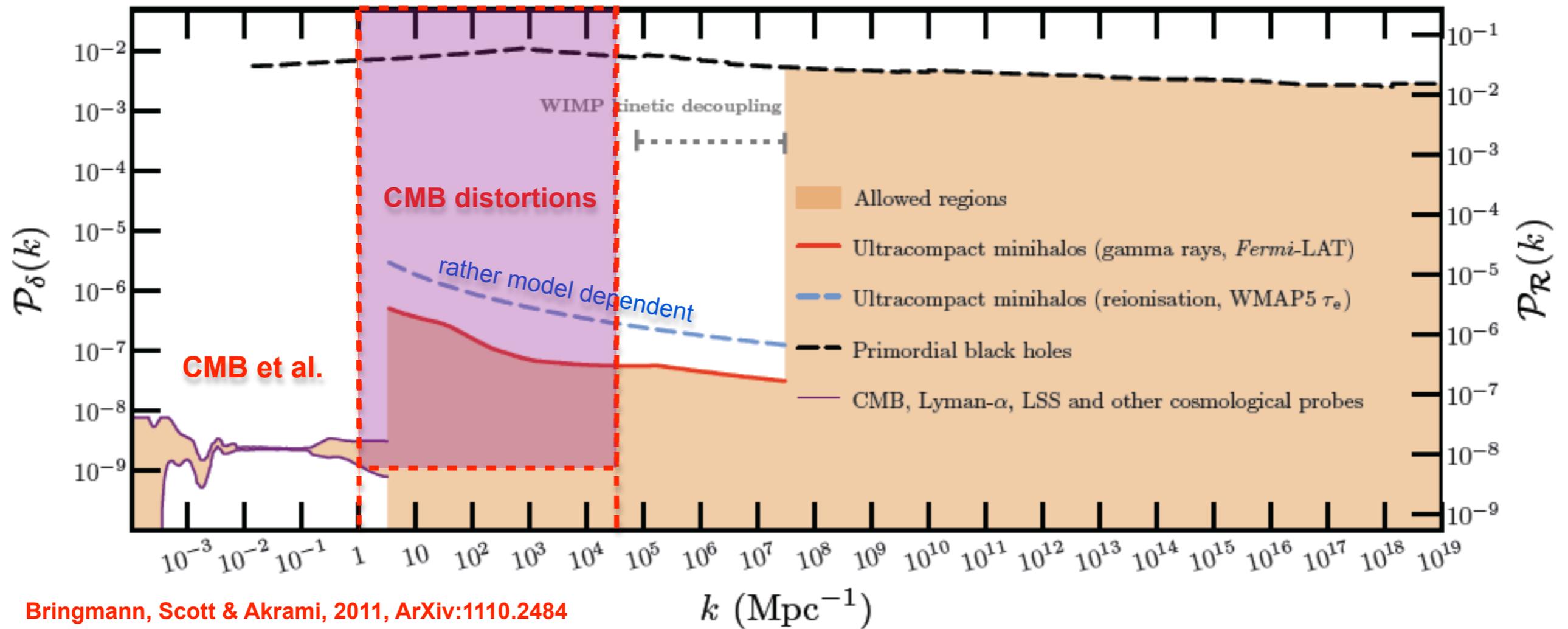
But this is not all that one could look at !!!

Power spectrum constraints



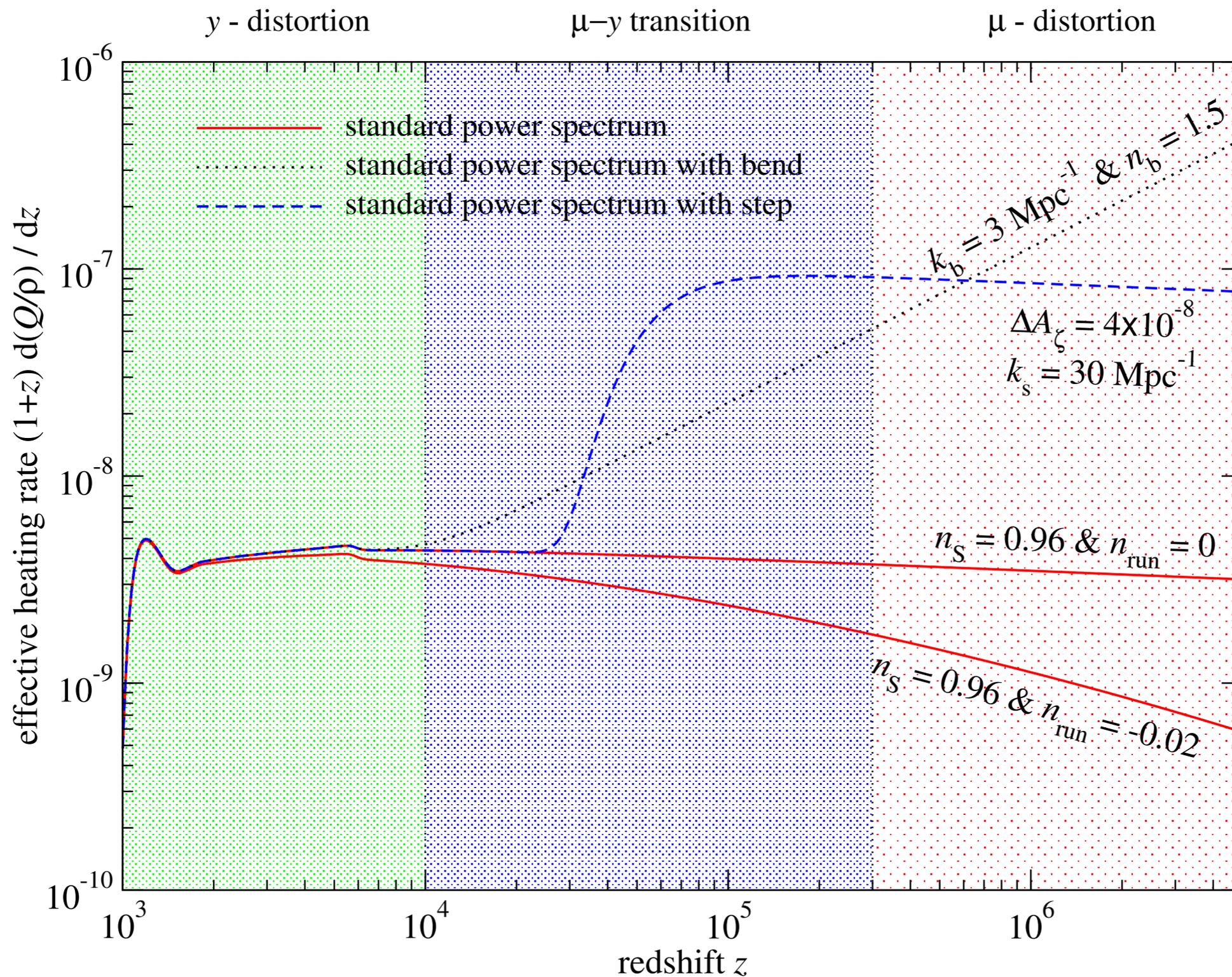
- Amplitude of power spectrum rather uncertain at $k > 3 \text{ Mpc}^{-1}$
- improving limits at smaller scales would constrain inflationary models

Power spectrum constraints

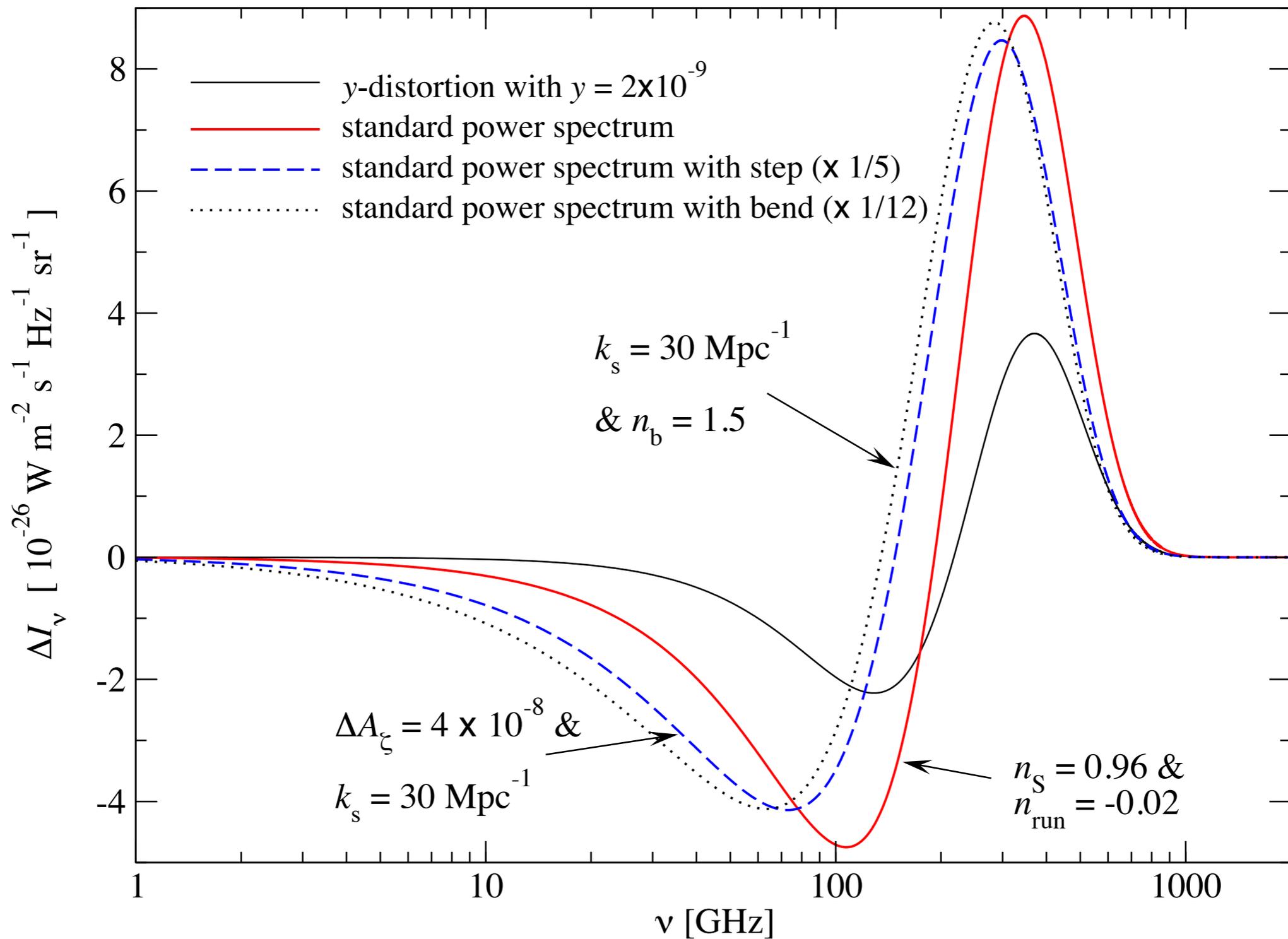


- Amplitude of power spectrum rather uncertain at $k > 3 \text{ Mpc}^{-1}$
- improving limits at smaller scales would constrain inflationary models
- CMB spectral distortions could allow extending our lever arm to $k \sim 10^4 \text{ Mpc}^{-1}$
- See JC, Erickcek & Ben-Dayan, 2012 for constraints on more general $P(k)$

Probing the small-scale power spectrum

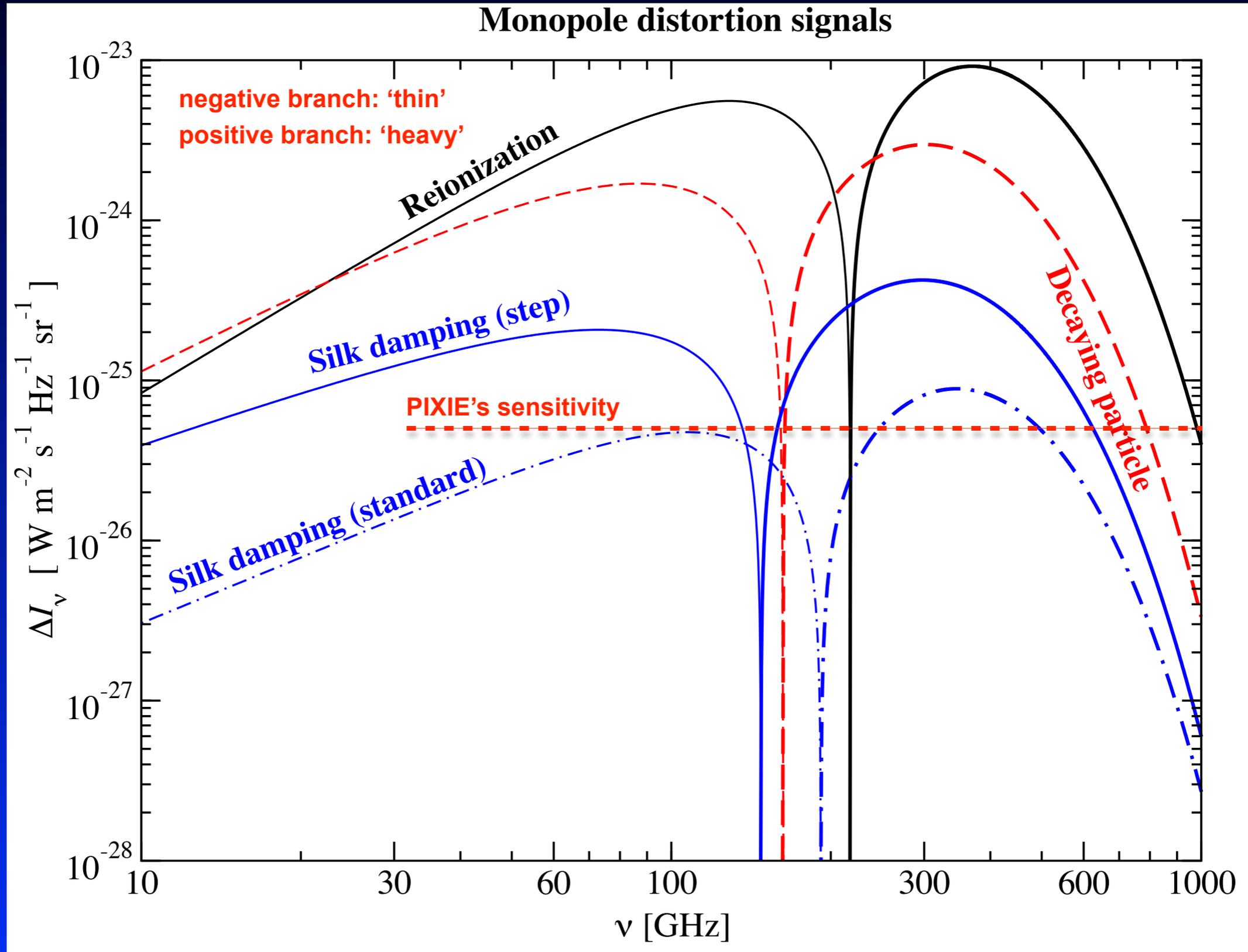


Probing the small-scale power spectrum



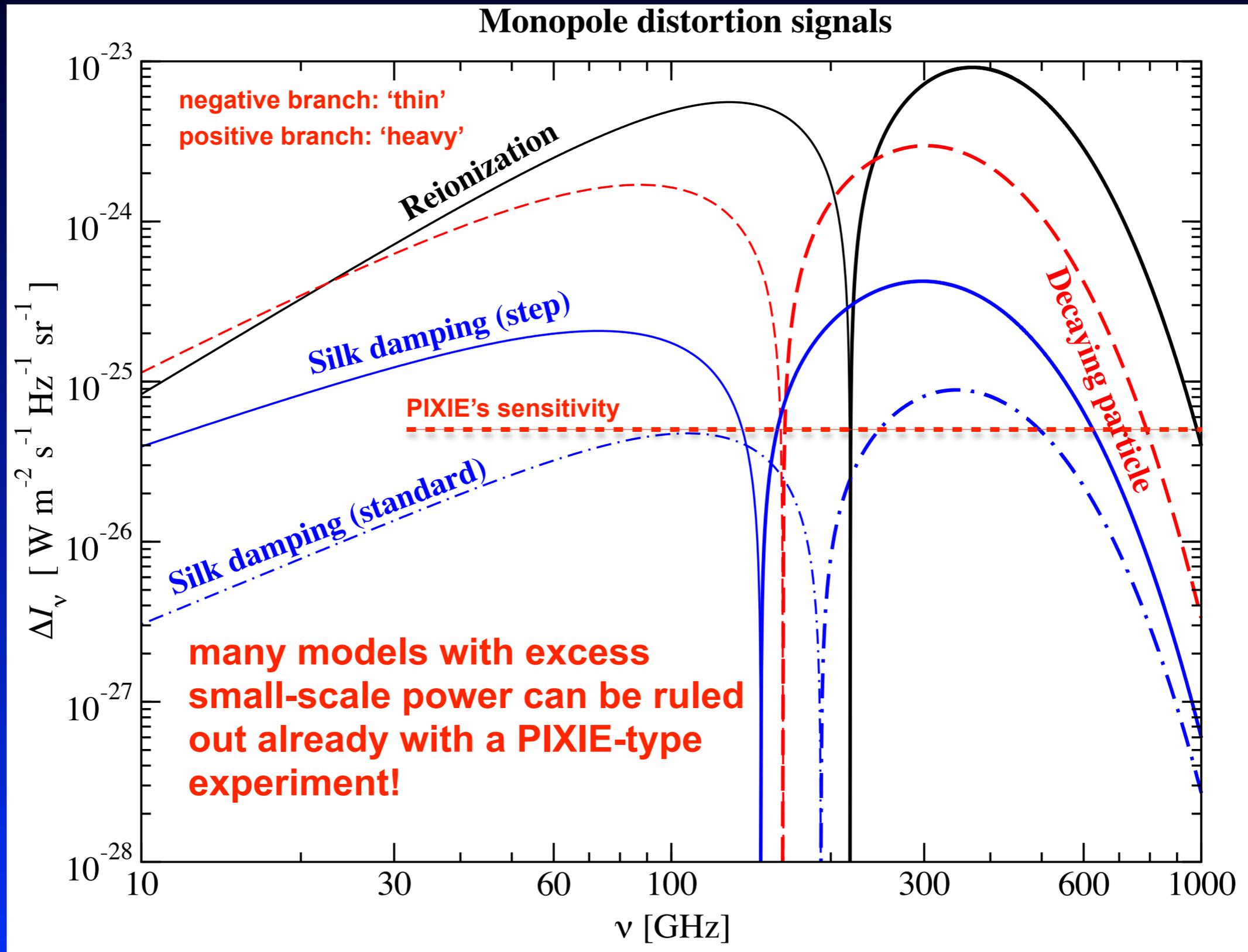
Average CMB spectral distortions

Absolute value of Intensity signal

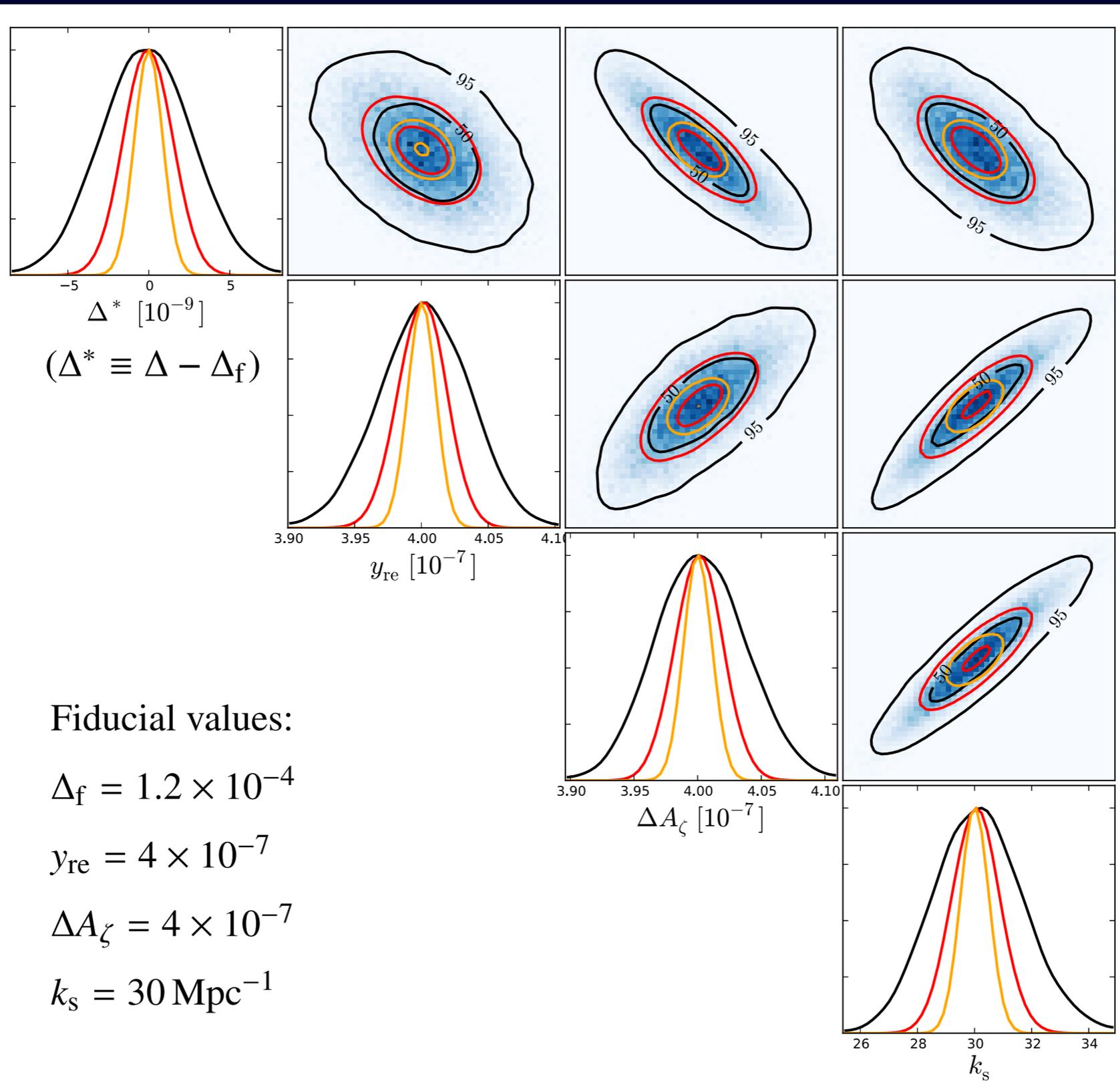


Average CMB spectral distortions

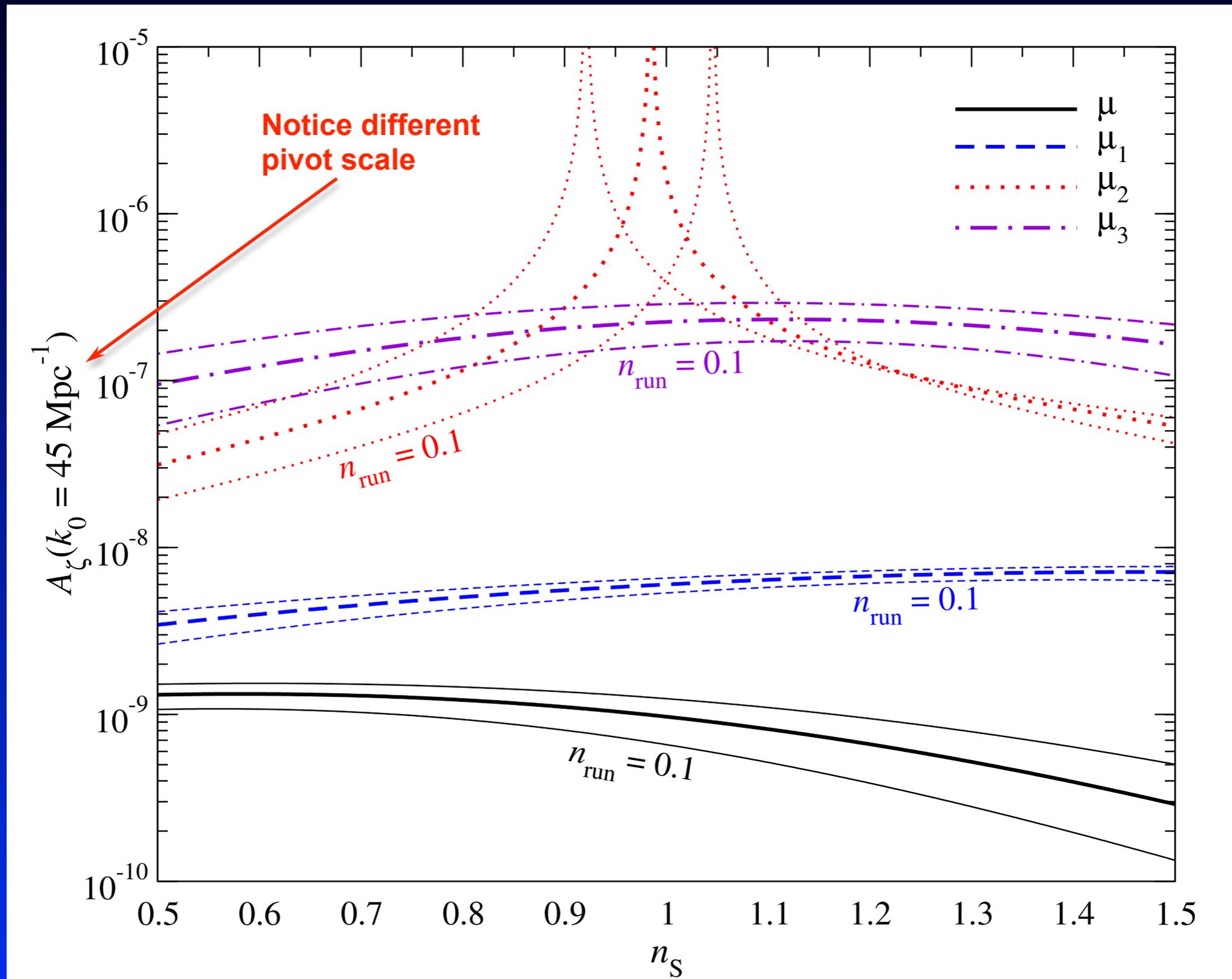
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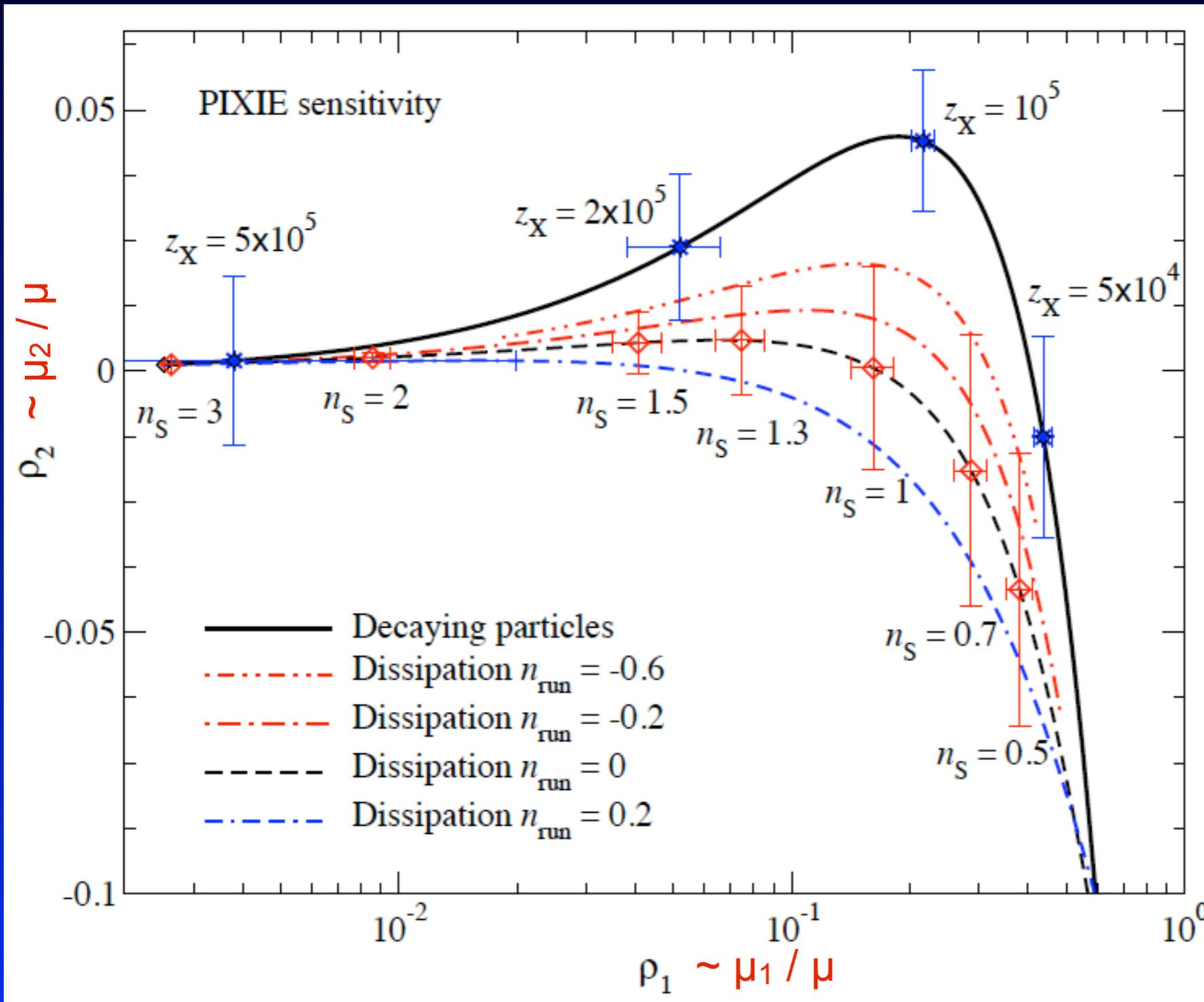
Probing the small-scale power spectrum



Dissipation scenario: 1σ -detection limits for PIXIE

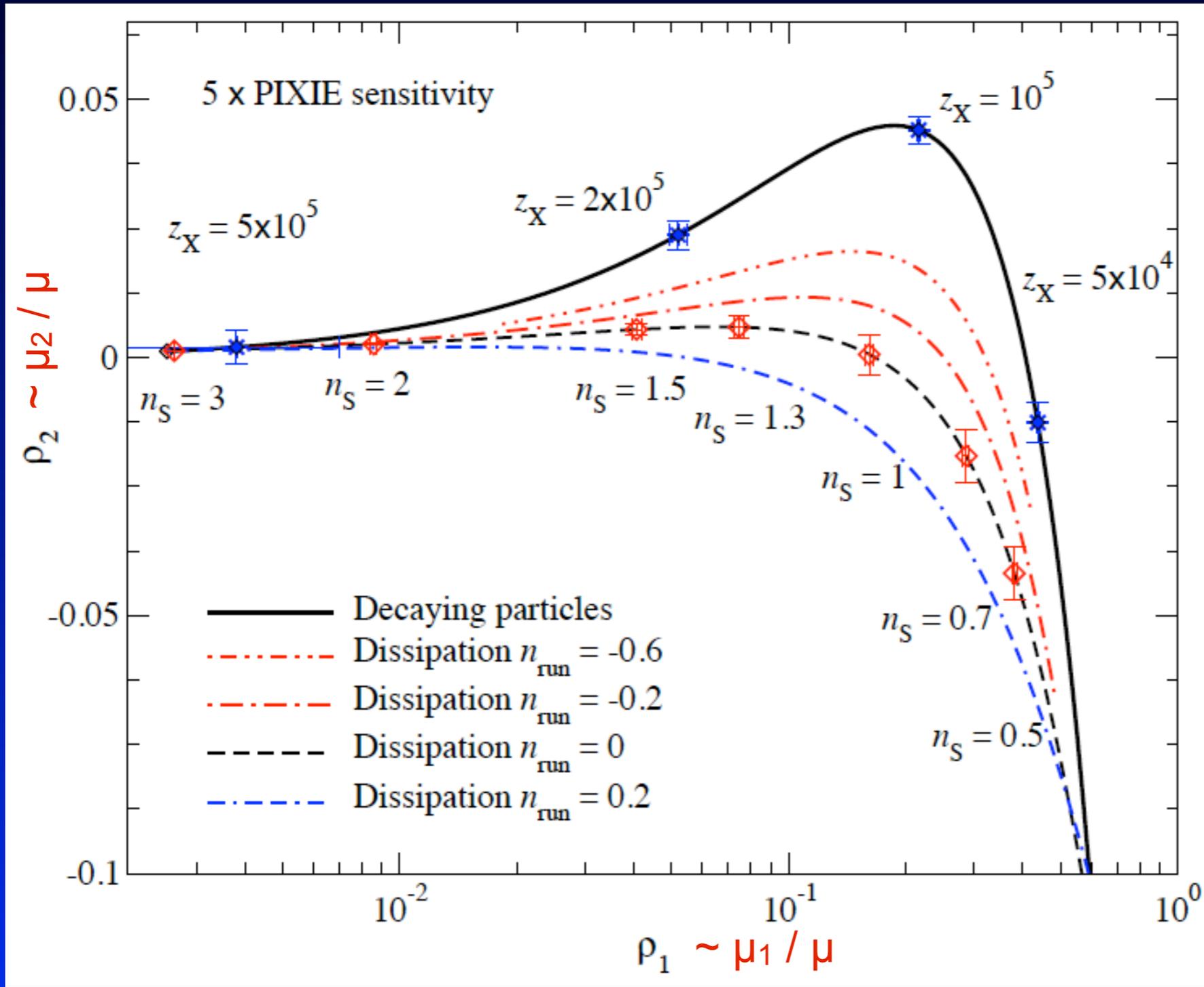


Distinguishing dissipation and decaying particle scenarios



- measurement of μ , μ_1 & μ_2
- trajectories of decaying particle and dissipation scenarios differ!
- scenarios can in principle be distinguished

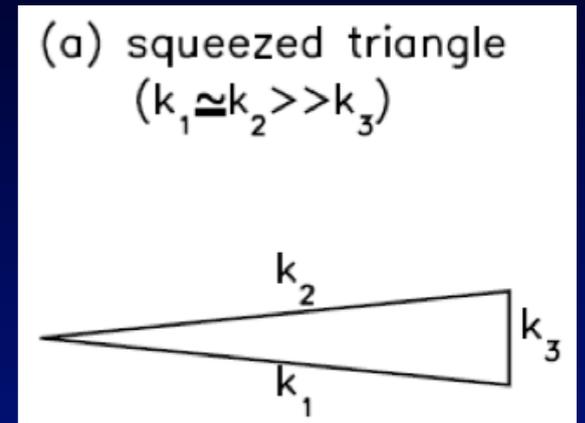
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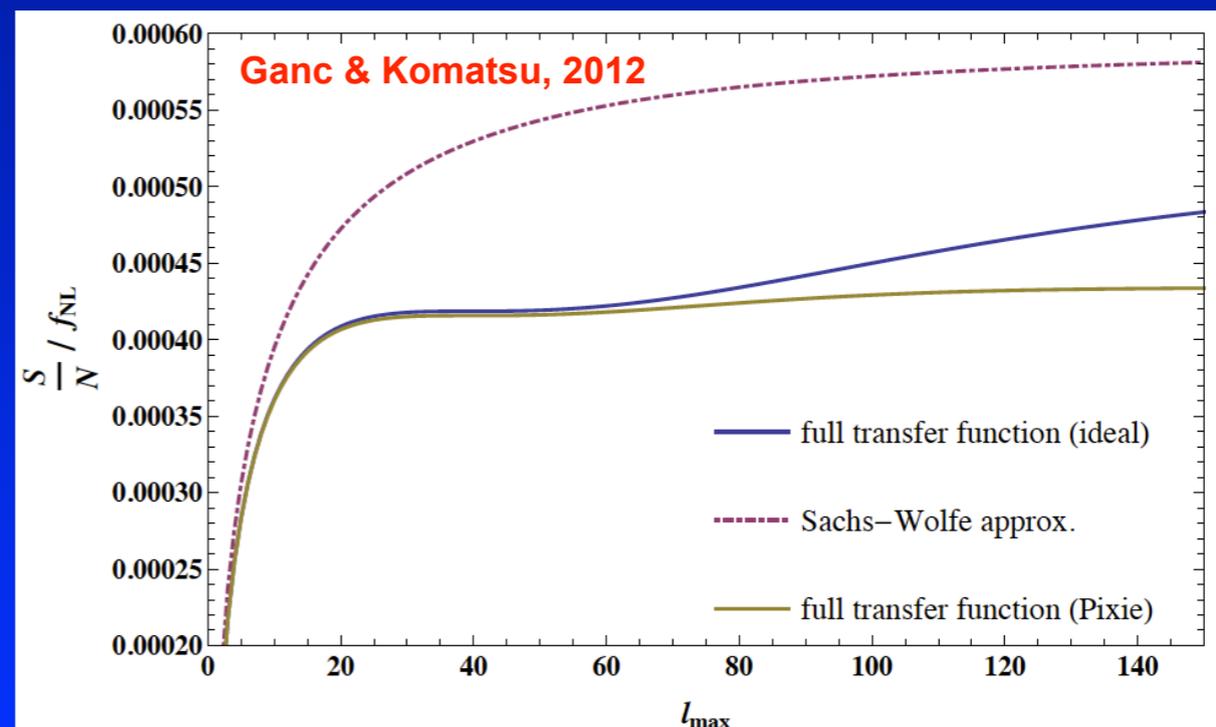
Modified μ -distortion in the squeezed limit

- Modes that dissipate energy have $k_1 \approx k_2 \gg k_3$
- Non-Gaussian power spectrum \rightarrow presence of positive long-wavelength mode enhances small-scale power
- More small-scale power \rightarrow larger μ -distortion
- \rightarrow Spatially varying μ -distortion caused by non-Gaussianity!
(Pajer & Zaldarriaga, 2012; Ganc & Komatsu, 2012)
- Non-vanishing μ -T correlation at large scales
- Might be detectable with PIXIE-type experiment for $f_{\text{NL}} > 10^3$

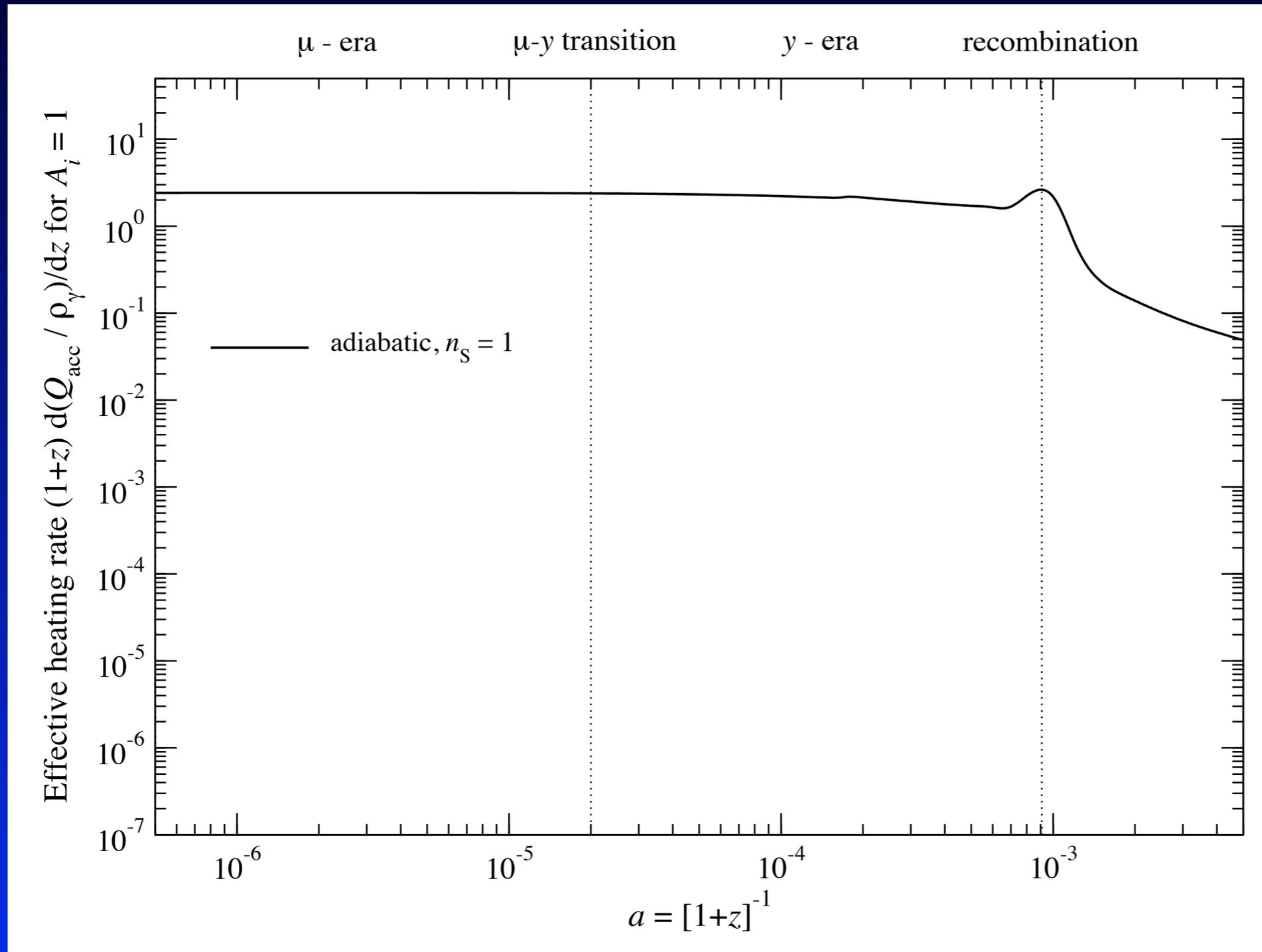


Requirements

- precise cross-calibration of frequency channels
- higher angular resolution does not improve cumulative S/N



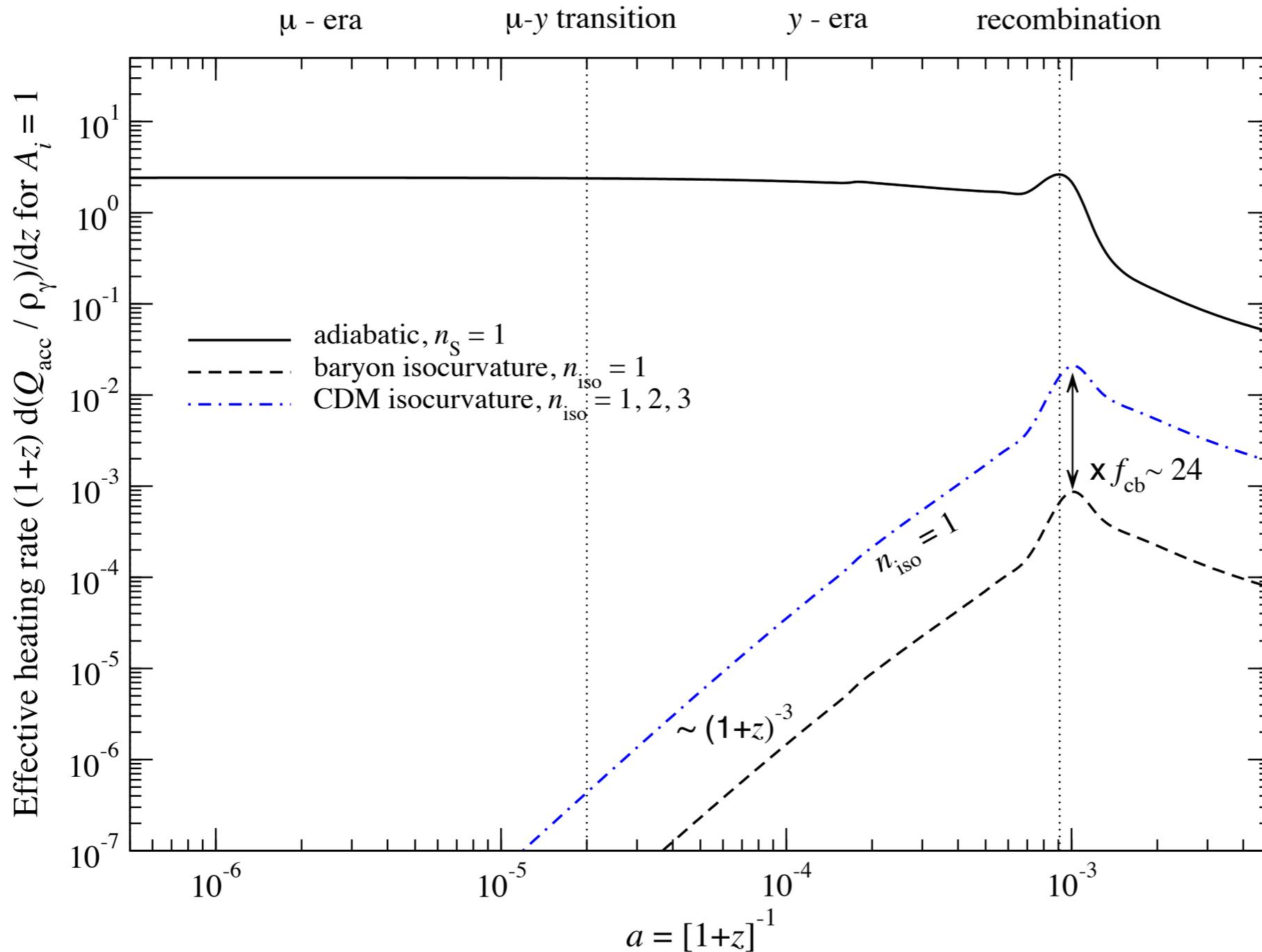
Dependence of heating rate on the perturbation type



- Adiabatic modes: heating rate $\sim 1/z$ at high z

$$P_i(k) = 2\pi^2 A_i k^{-3} (k/k_0)^{n_i-1}$$

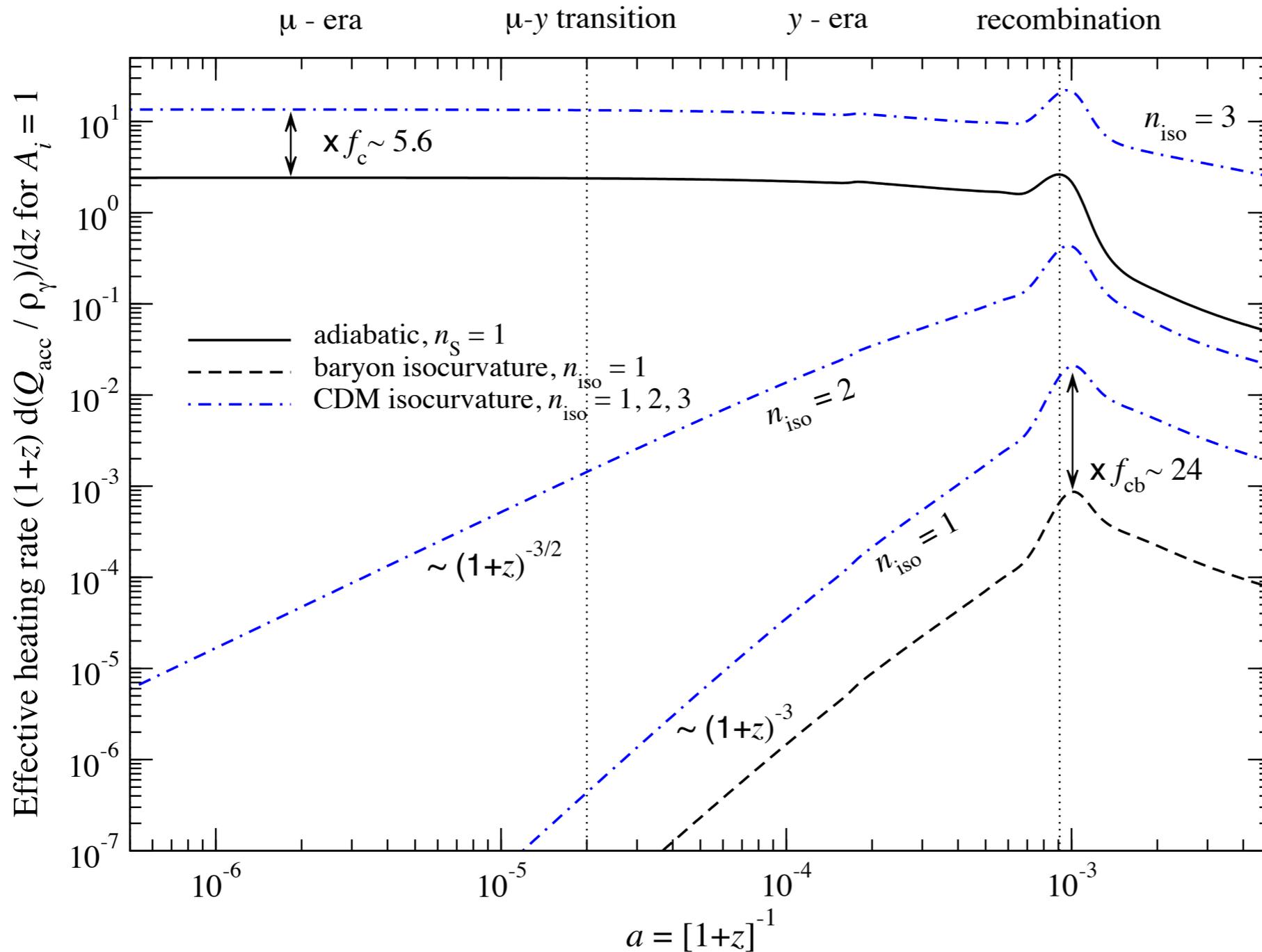
Dependence of heating rate on the perturbation type



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 $A \sim k/k_{\text{eq}}$
 during radiation dominated epoch

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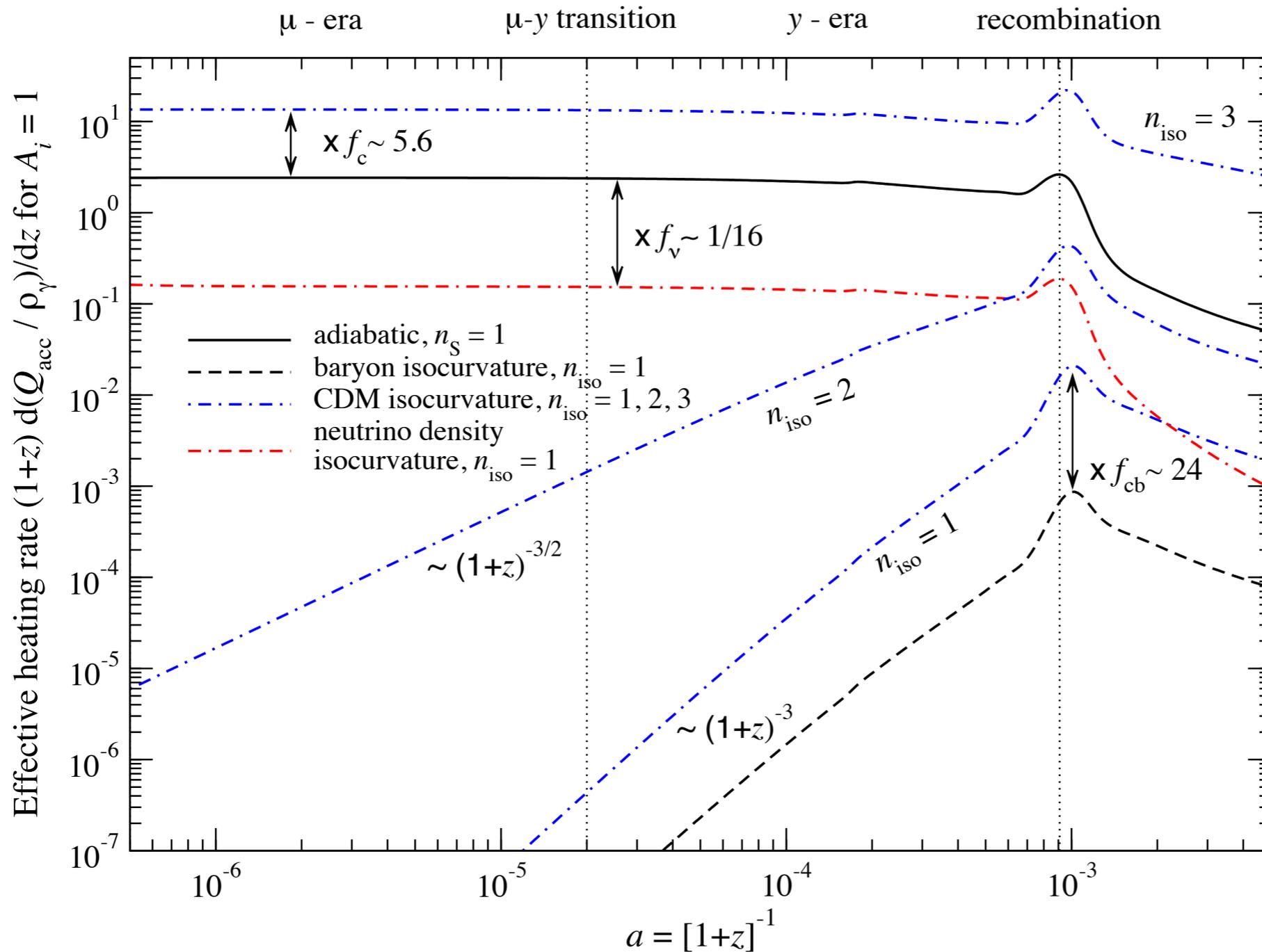
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- $n_{\text{iso}} \sim 3 \Rightarrow$ heating rate $\sim 1/z$

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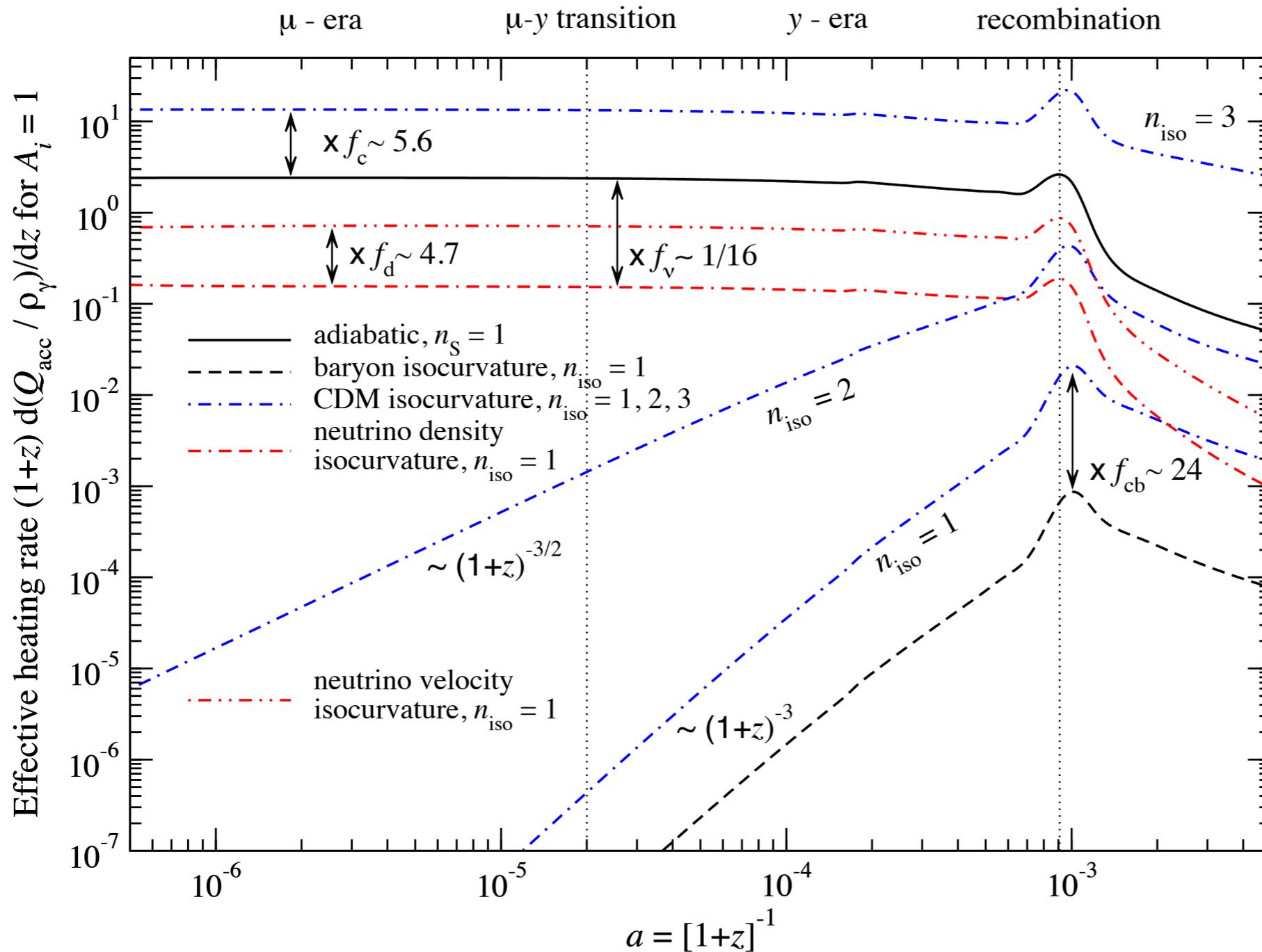
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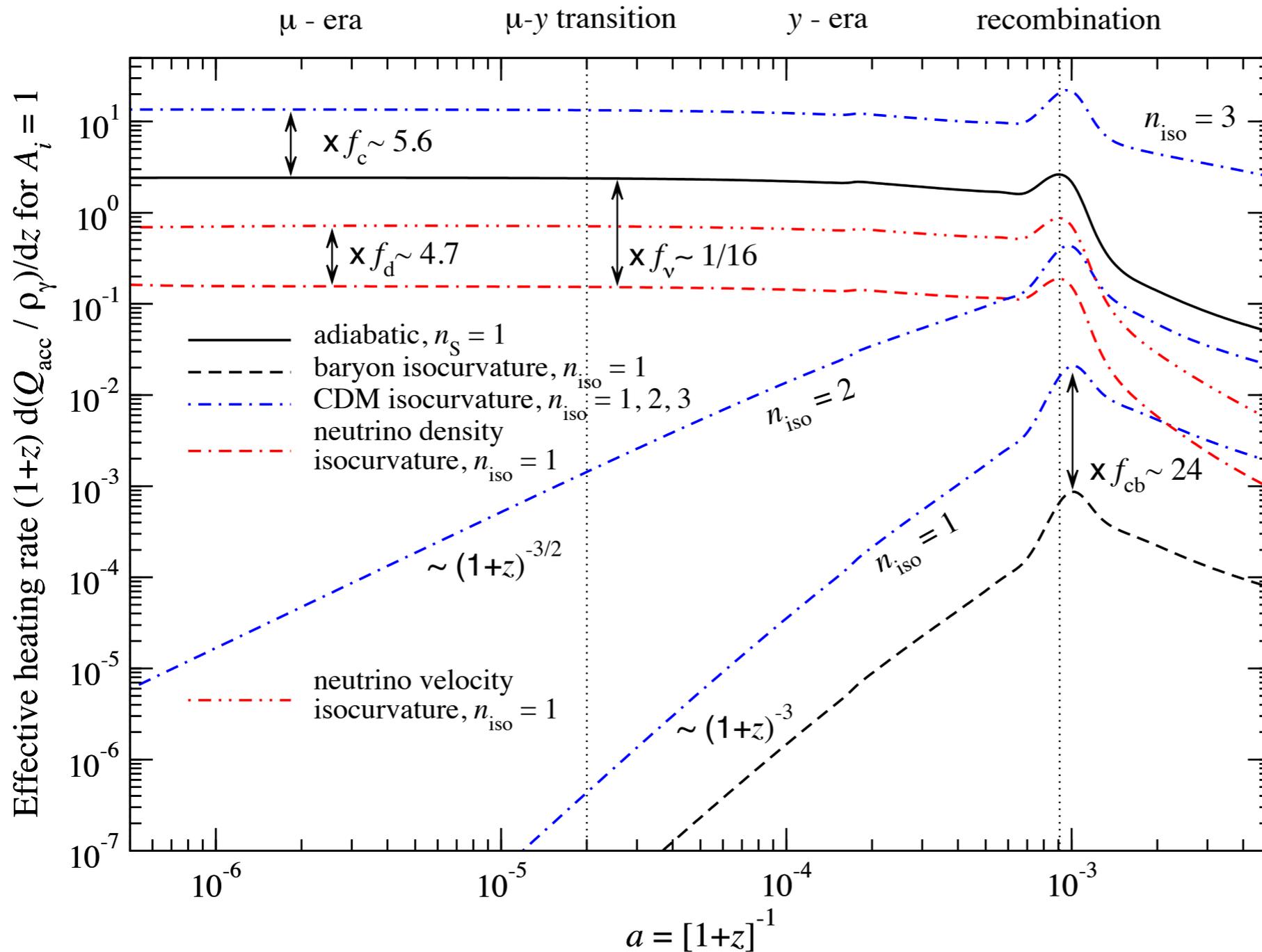
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- neutrino isocurvature modes very similar to adiabatic modes
- compensated isocurvature modes: practically no heating

$$P_i(k) = 2\pi^2 A_i k^{-3} (k/k_0)^{n_i-1}$$

The cosmological recombination radiation

Simple estimates for hydrogen recombination

Hydrogen recombination:

- per recombined hydrogen atom an energy of ~ 13.6 eV in form of photons is released
 - at $z \sim 1100 \rightarrow \Delta\varepsilon/\varepsilon \sim 13.6 \text{ eV } N_b / (N_\gamma 2.7kT_r) \sim 10^{-9} - 10^{-8}$
- recombination occurs at redshifts $z < 10^4$
- At that time the *thermalization* process doesn't work anymore!
- There should be some *small* spectral distortion due to additional Ly- α and 2s-1s photons!
- (Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278; Peebles, 1968, ApJ, 153, 1)
- In 1975 **Viktor Dubrovich** emphasized the possibility to observe the recombinational lines from $n > 3$ and $\Delta n \ll n$!

First recombination computations completed in 1968!



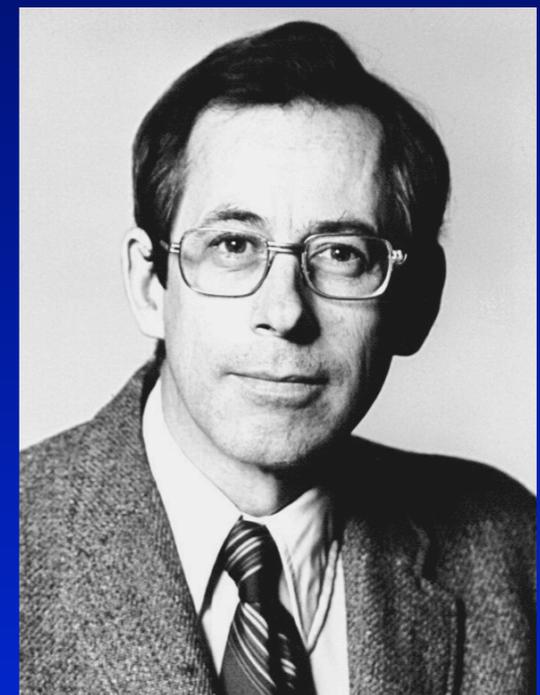
Yakov Zeldovich

Moscow

Princeton



Rashid Sunyaev

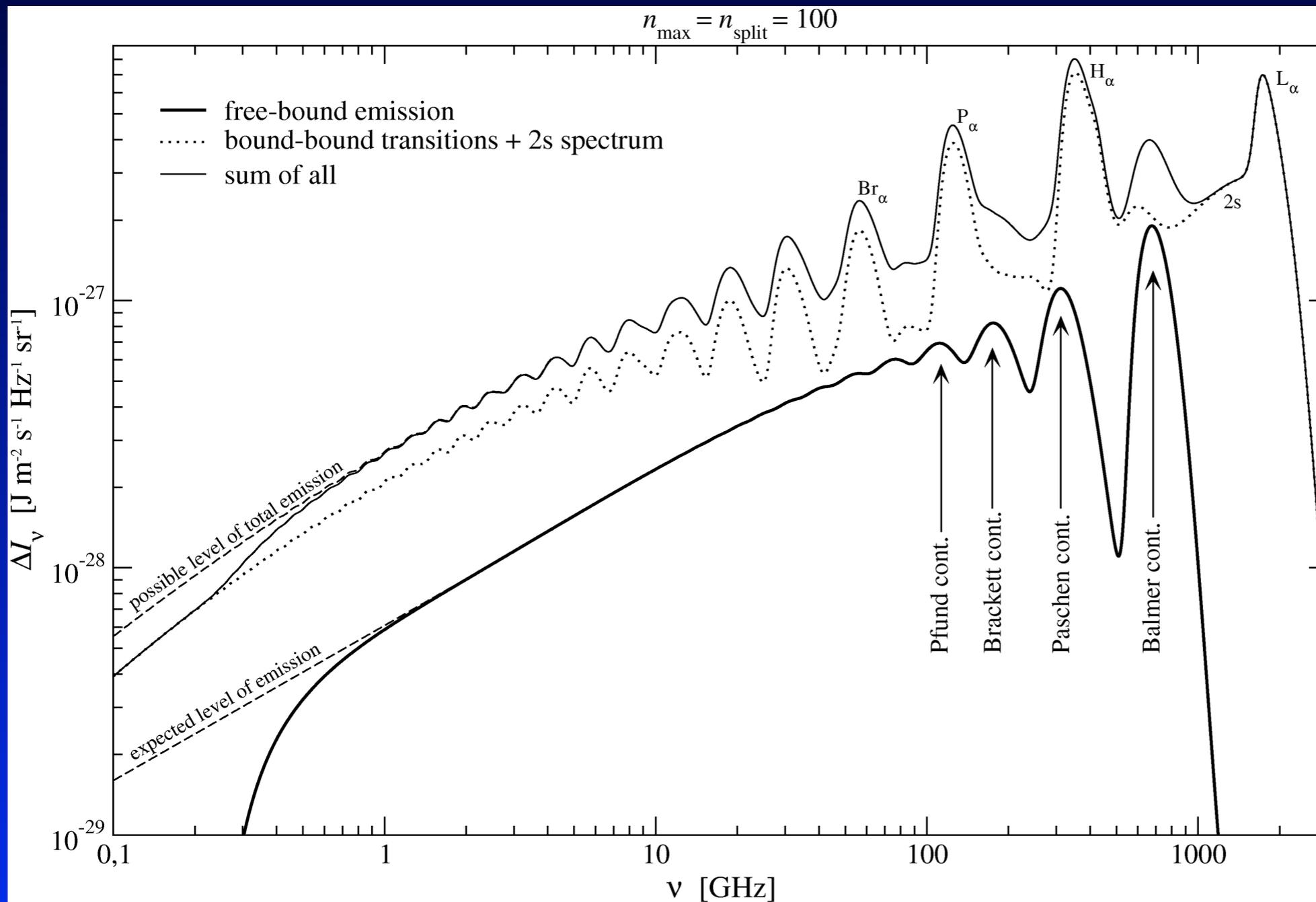


Jim Peebles



Vladimir Kurt
(UV astronomer)

100-shell hydrogen atom and continuum CMB spectral distortions



bound-bound & 2s:

- at $\nu > 1\text{GHz}$: distinct features
- slope ~ 0.46

free-bound:

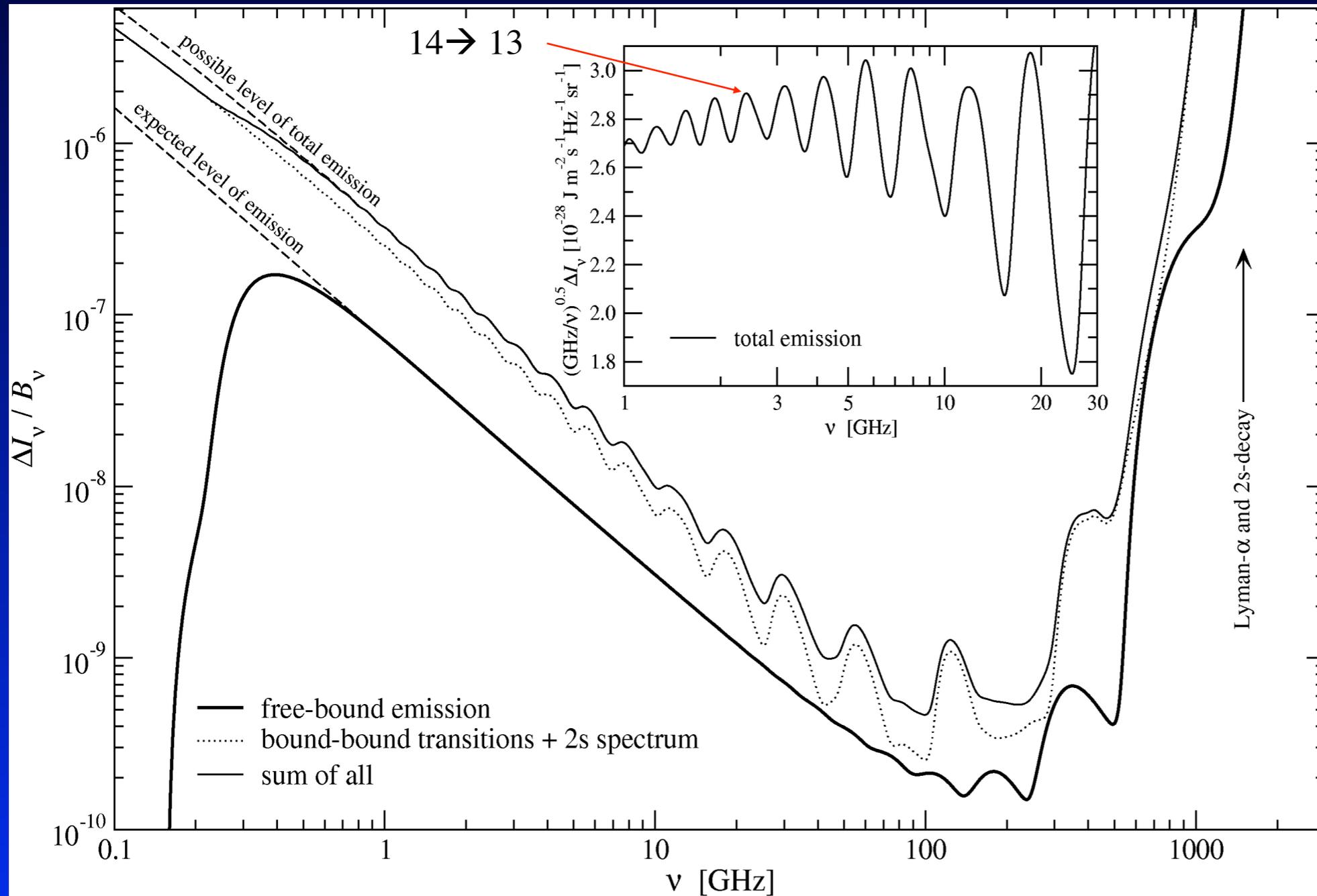
- only a few features distinguishable
- slope ~ 0.6

Total:

- f-b contributes $\sim 30\%$ and more
- Balmer cont. $\sim 90\%$
- Balmer: 1γ per HI
- in total 5γ per HI

100-shell hydrogen atom and continuum

Relative distortions



Wien-region:

- L_α and 2s distortions are very strong
- but CIB more dominant

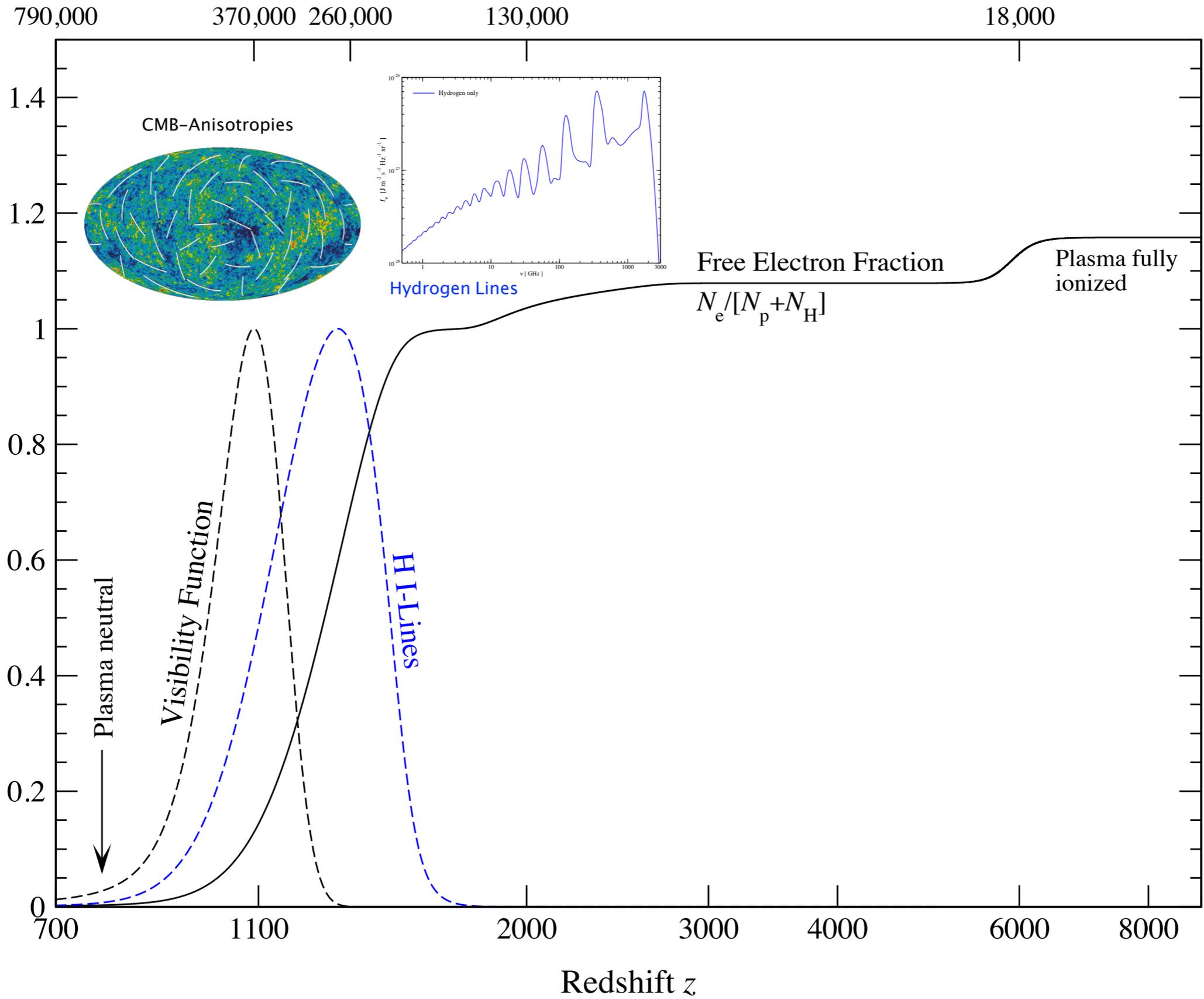
@ CMB maximum:

- relative distortions extremely small
- strong ν -dependence

RJ-region:

- relative distortion exceeds level of $\sim 10^{-7}$ below $\nu \sim 1$ -2 GHz
- oscillatory frequency dependence with ~ 1 -10 percent-level amplitude:
- *hard to mimic by known foregrounds or systematics*

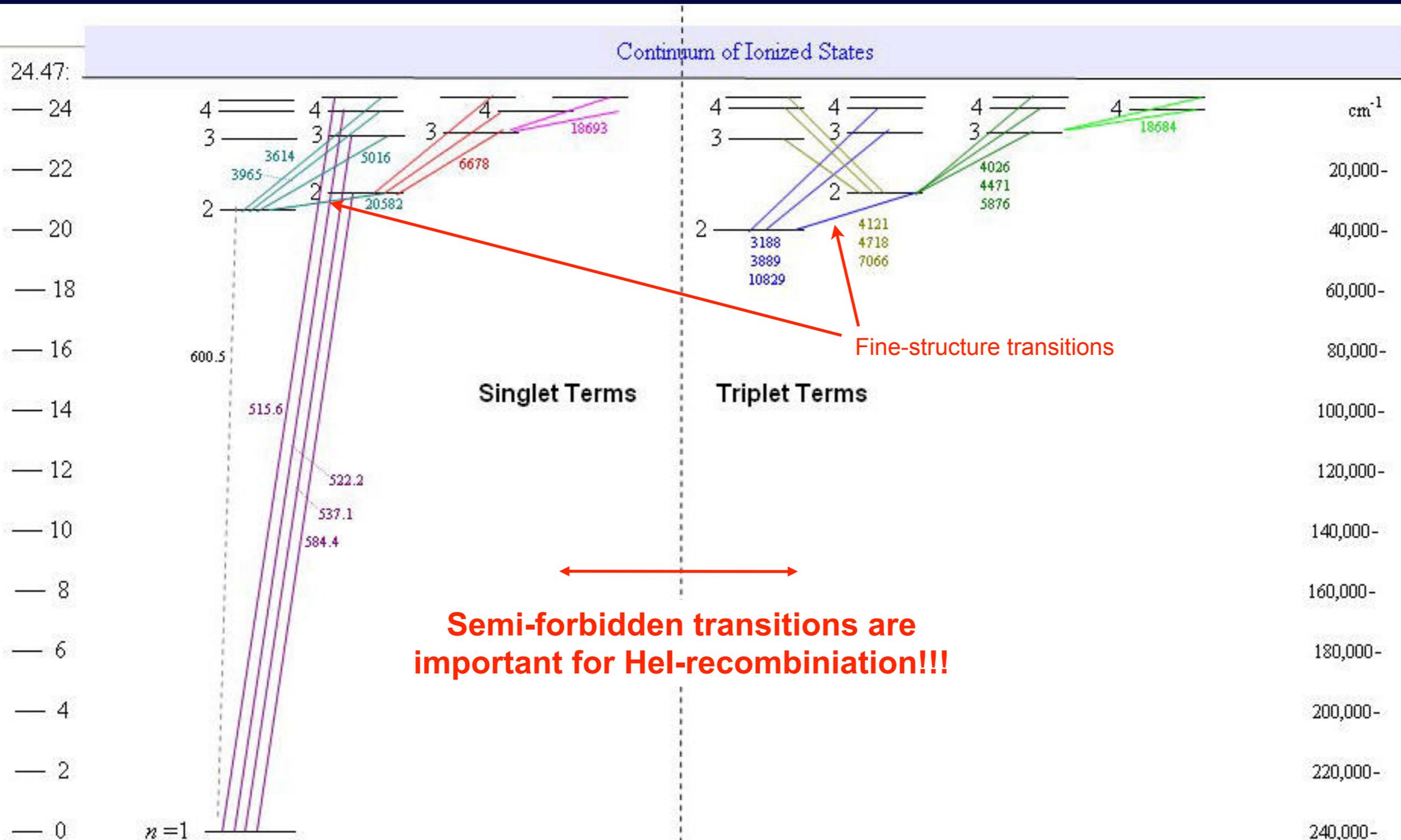
Cosmological Time in Years



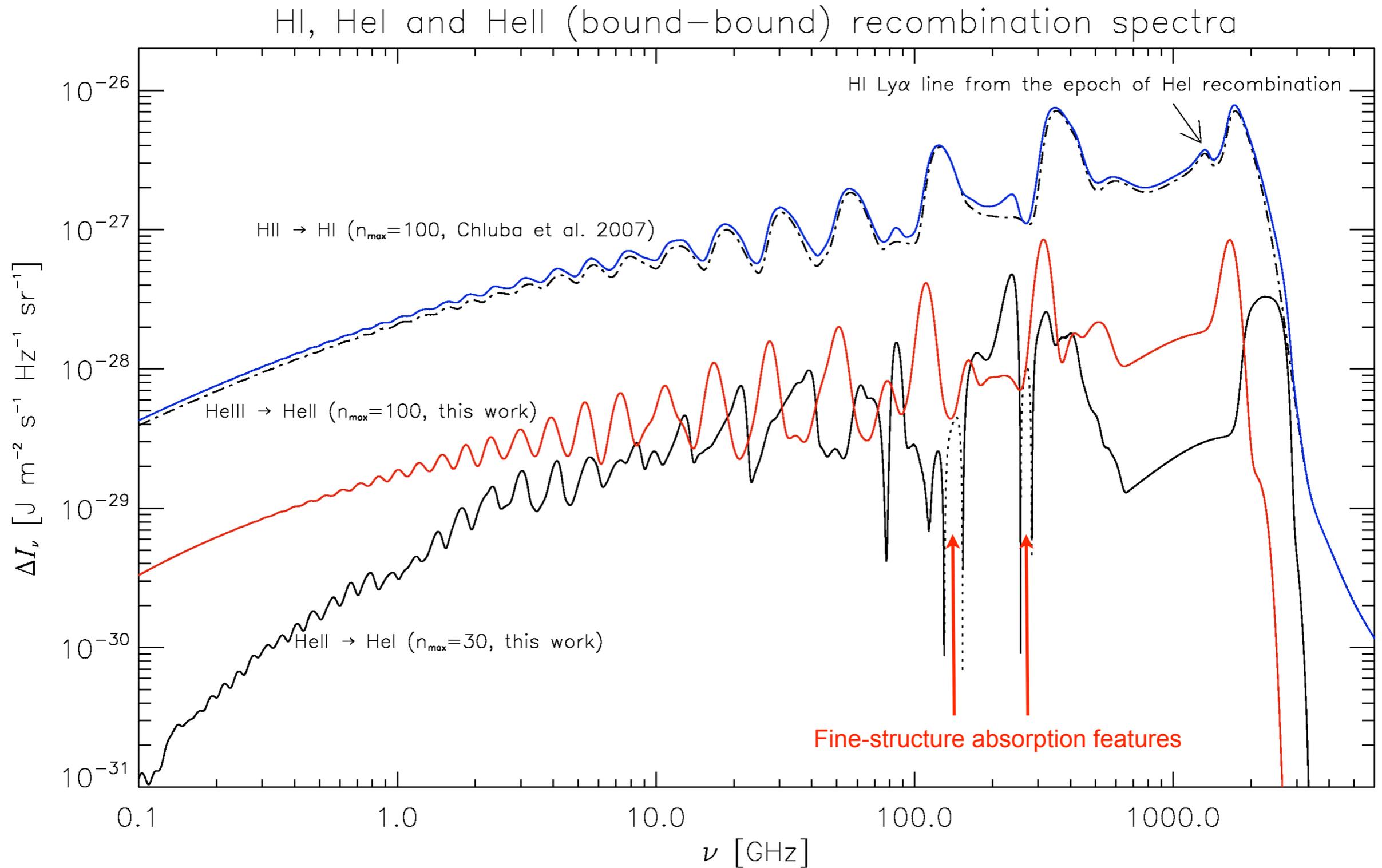
What about the contributions from helium recombination?

- Nuclear reactions: $Y_p \sim 0.24 \leftrightarrow N_{\text{HeI}} / N_{\text{H}} \sim 8 \%$
 - expected photon number rather small
- **BUT:**
 - (i) two epochs of He recombination
HeII → HeI at $z \sim 6000$ and HeII → HeI at $z \sim 2500$
 - (ii) Helium recombinations faster
 - more *narrow* features with *larger* amplitude
 - (iii) non-trivial superposition
 - local amplification possible
 - (iv) **reprocessing** of HeII & HeI photons by HeI and HI
 - increases the number of helium-related photons
 - May opens a way to **directly** measure the primordial (pre-stellar!!!) helium abundance!

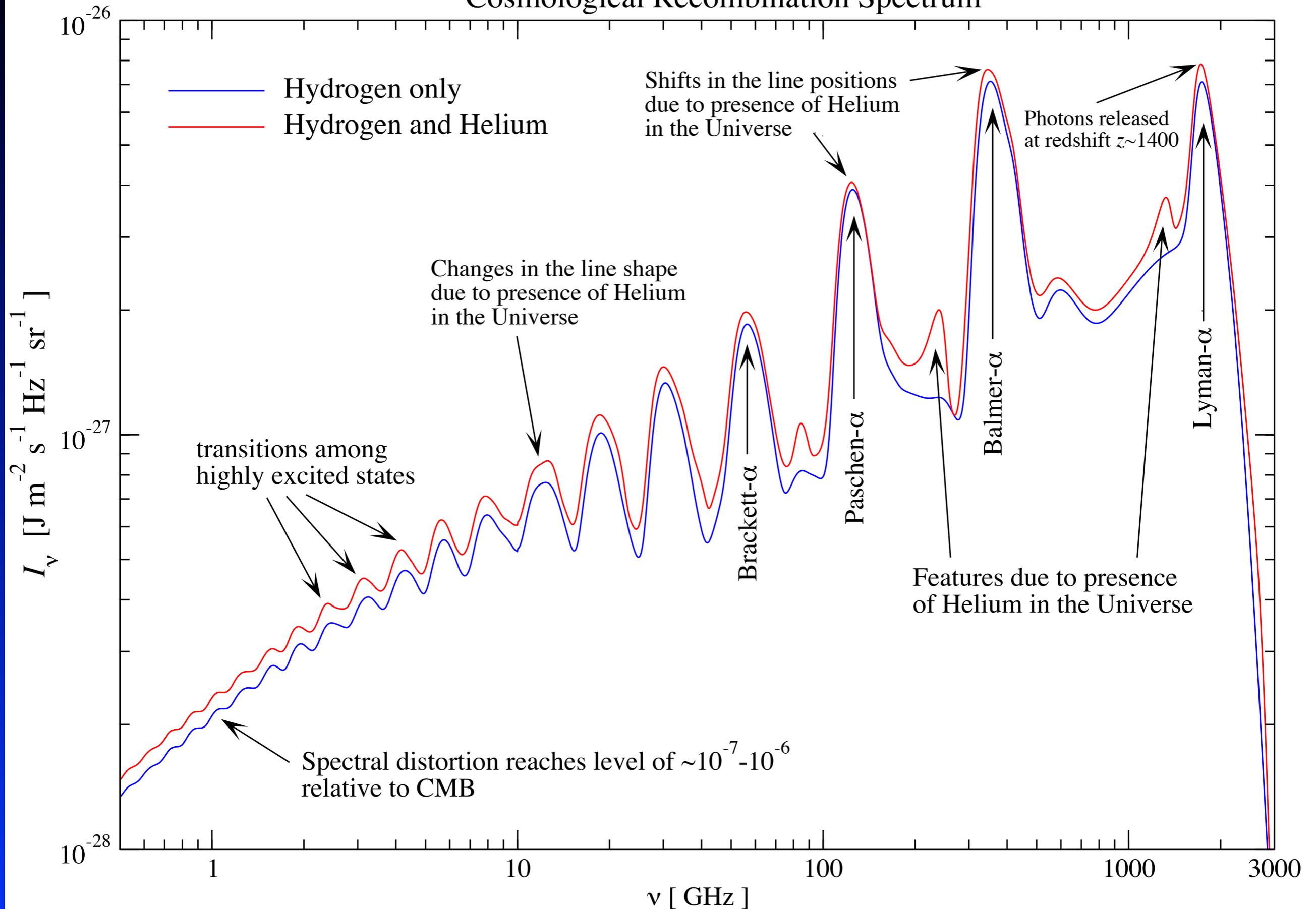
Grotrian diagram for neutral helium



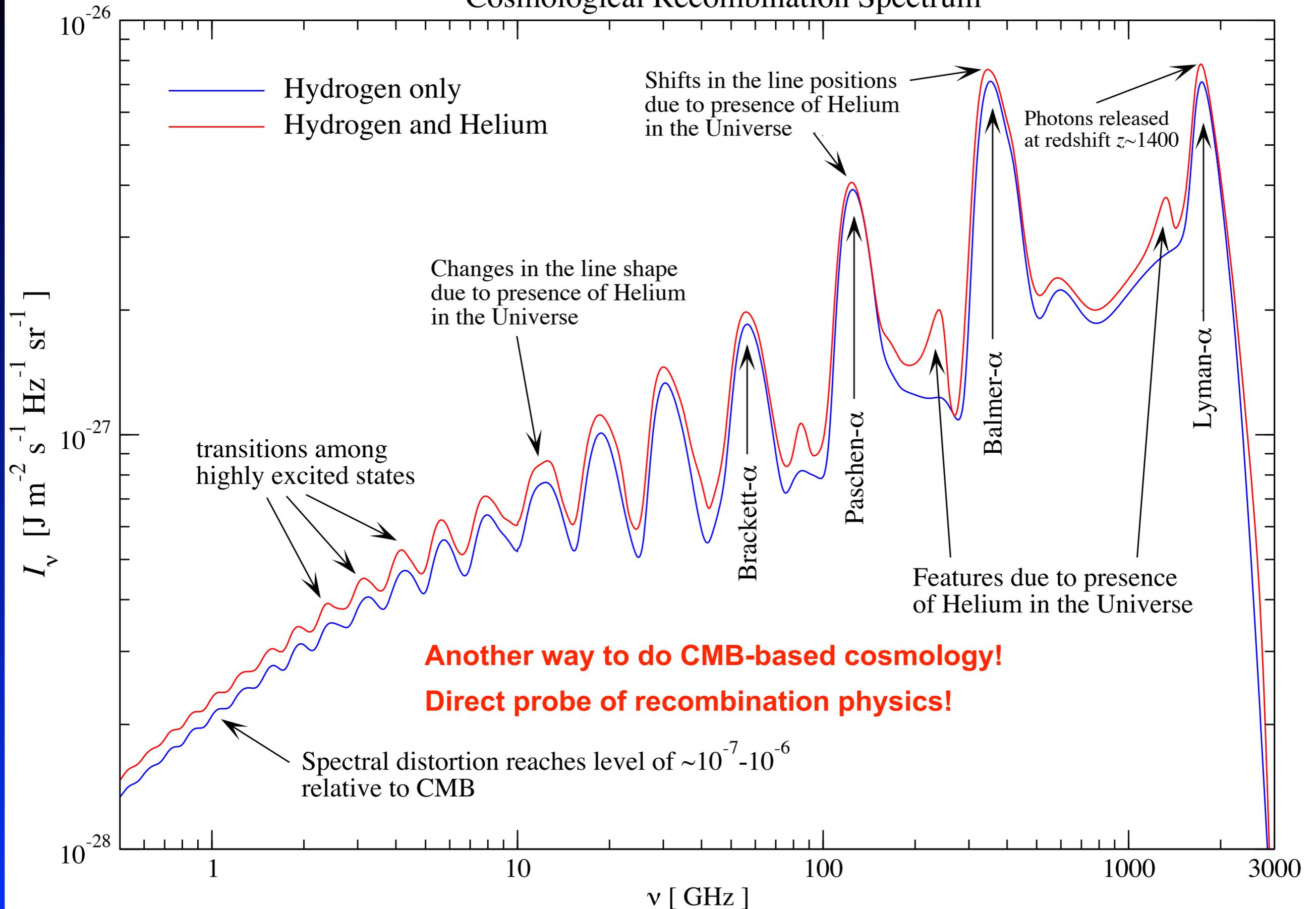
Helium contributions to the cosmological recombination spectrum



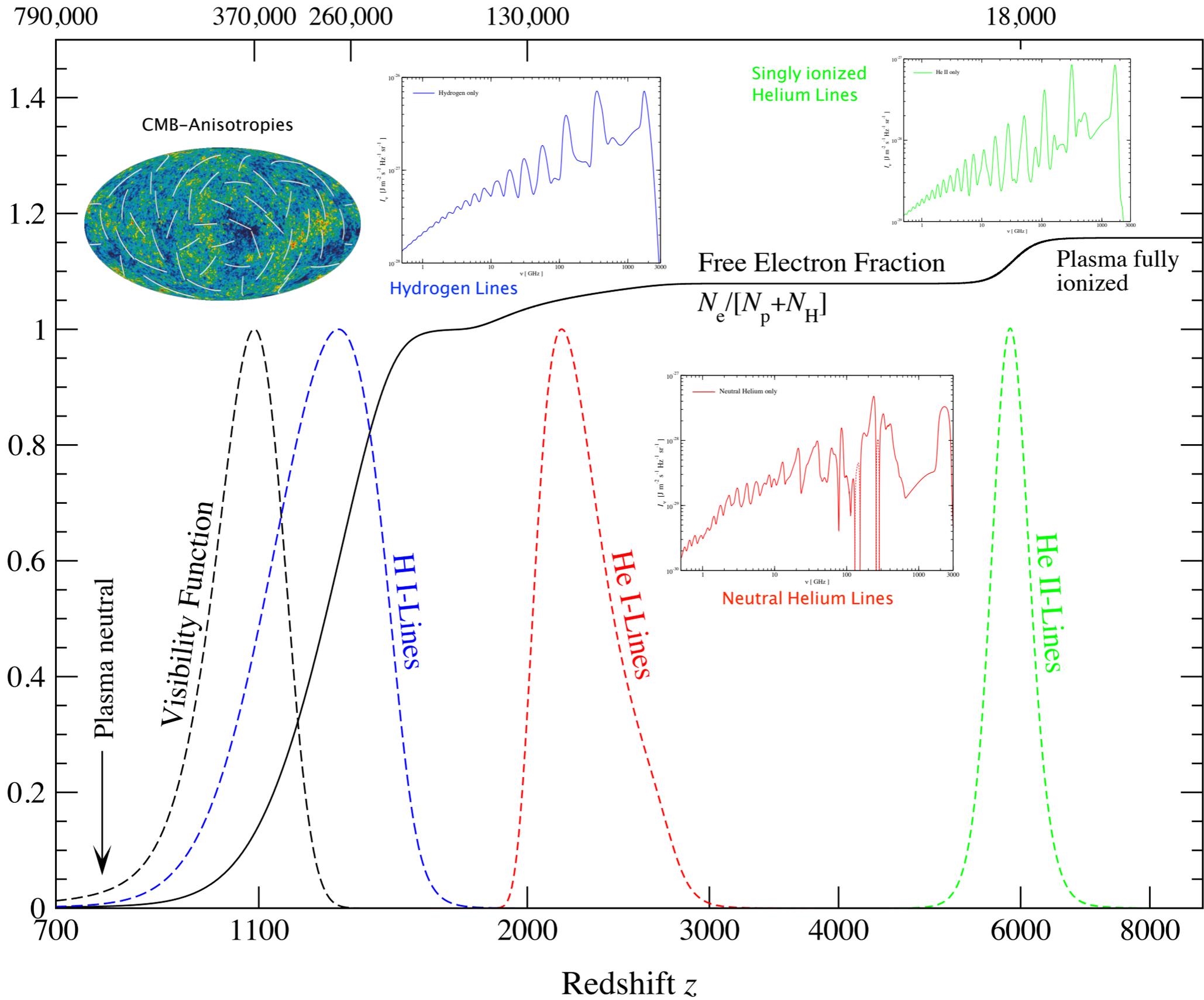
Cosmological Recombination Spectrum



Cosmological Recombination Spectrum



Cosmological Time in Years

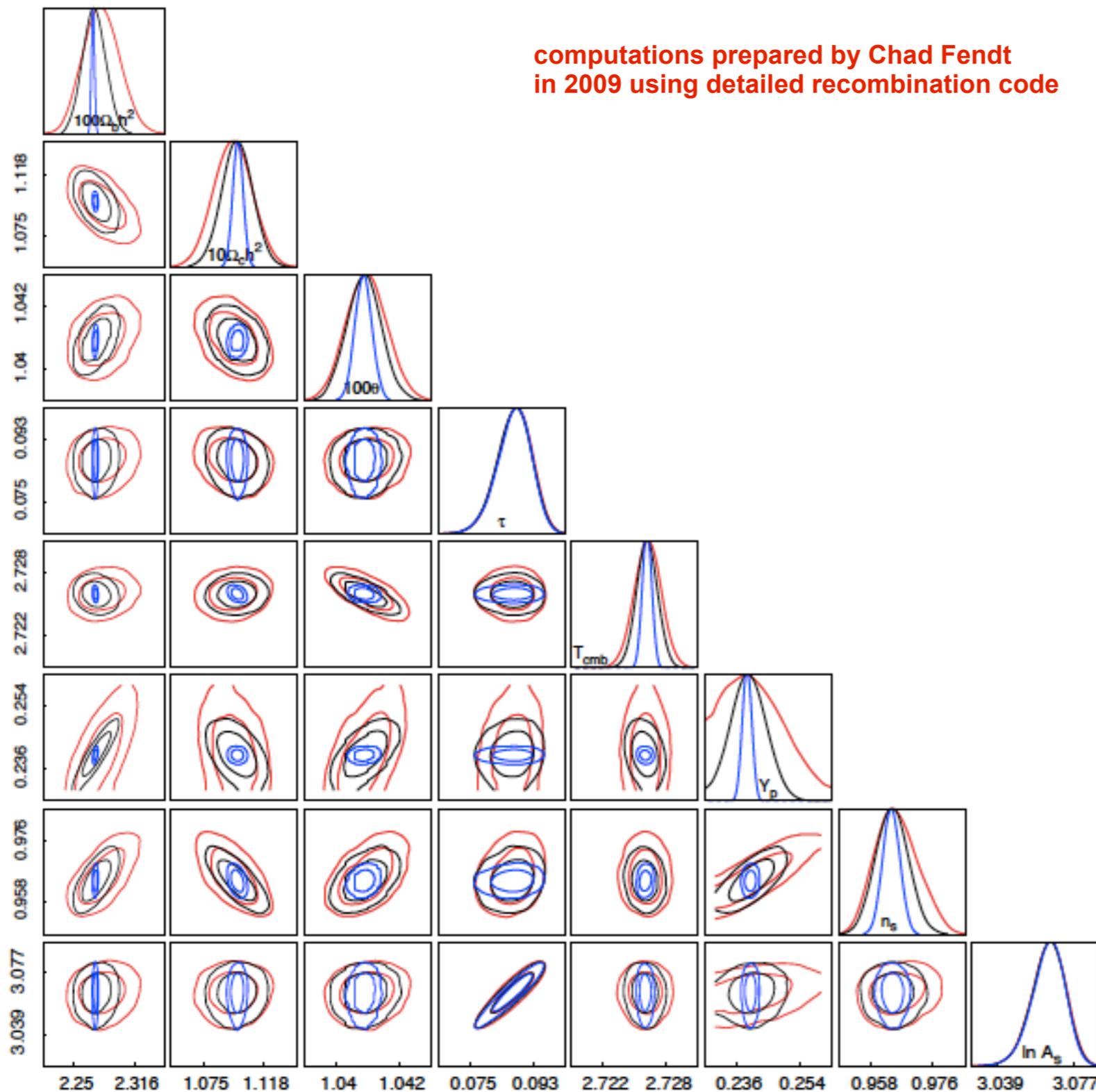


What would we actually learn by doing such hard job?

Cosmological Recombination Spectrum opens a way to measure:

- the specific *entropy* of our universe (related to $\Omega_b h^2$)
- the CMB *monopole* temperature T_0
- *the pre-stellar abundance of helium* Y_p
- *If recombination occurs as we think it does, then the lines can be predicted with very high accuracy!*
- *In principle allows us to directly check our understanding of the standard recombination physics*

computations prepared by Chad Fendt
in 2009 using detailed recombination code

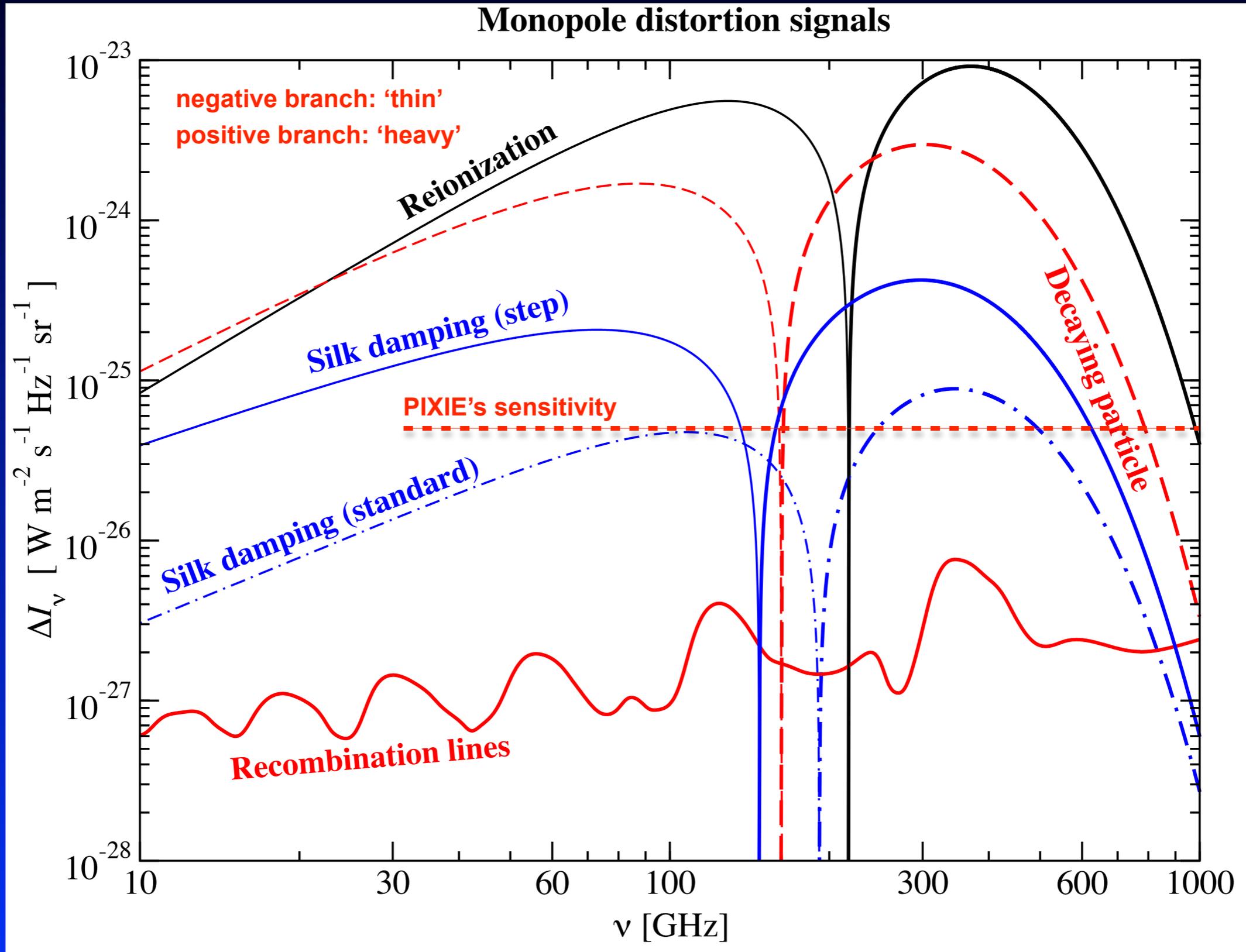


- CMB based cosmology alone
- Spectrum helps to break some of the parameter degeneracies
- Planning to provide a module that computes the recombination spectrum in a fast way
- detailed forecasts: which lines to measure; how important is the absolute amplitude; how accurately one should measure; best frequency resolution;

Figure 7.3: The 1 and 2 dimensional marginalized parameter posterior using the CMB spectral distortions. All three cases constrain the CMB power spectrum using a Gaussian likelihood based on Planck noise levels. The black line adds constraints due to a 10% measurement of the spectral distortions, while the blue line assumes a 1% measurement. The red line does not include the data from the spectral distortions.

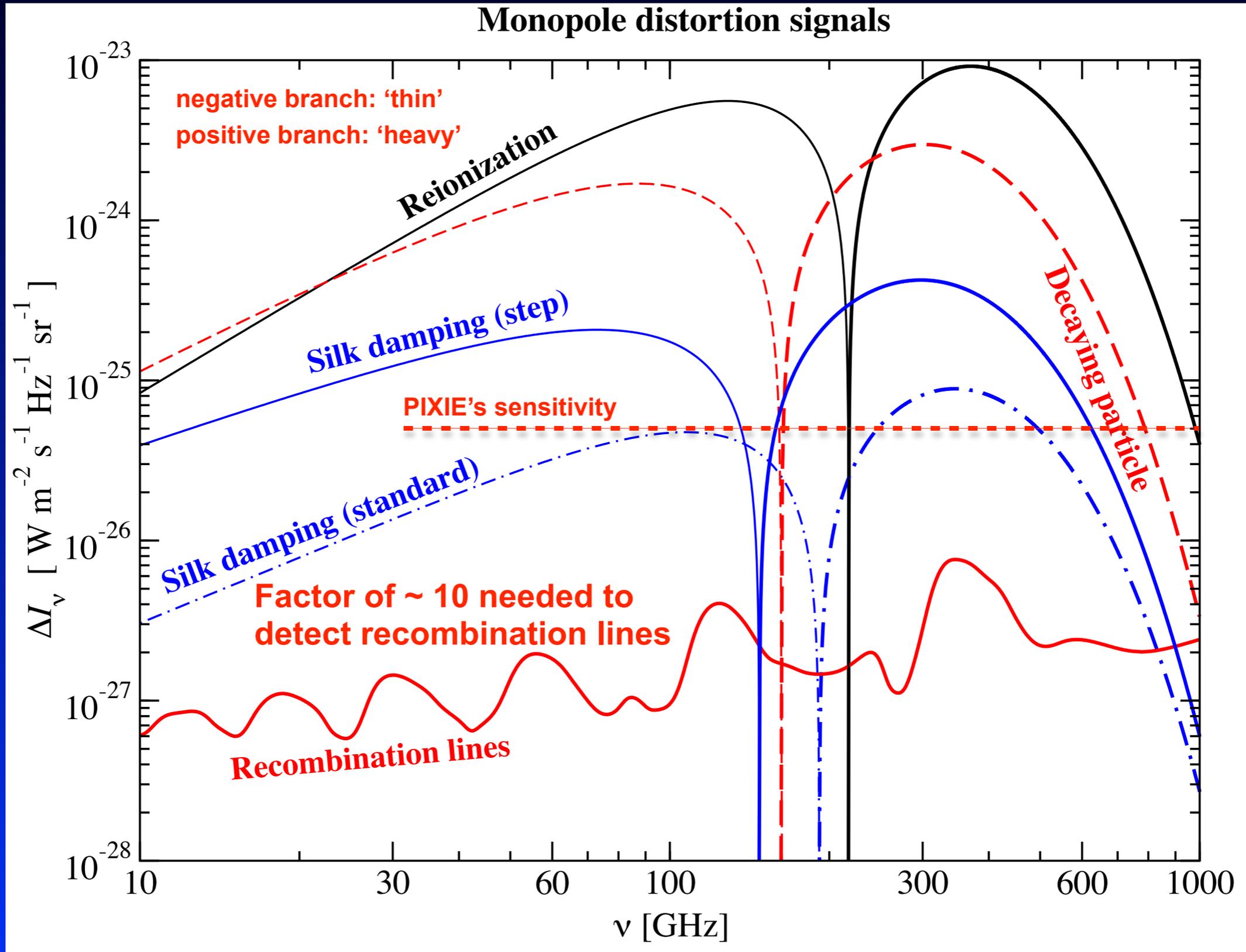
Average CMB spectral distortions

Absolute value of Intensity signal



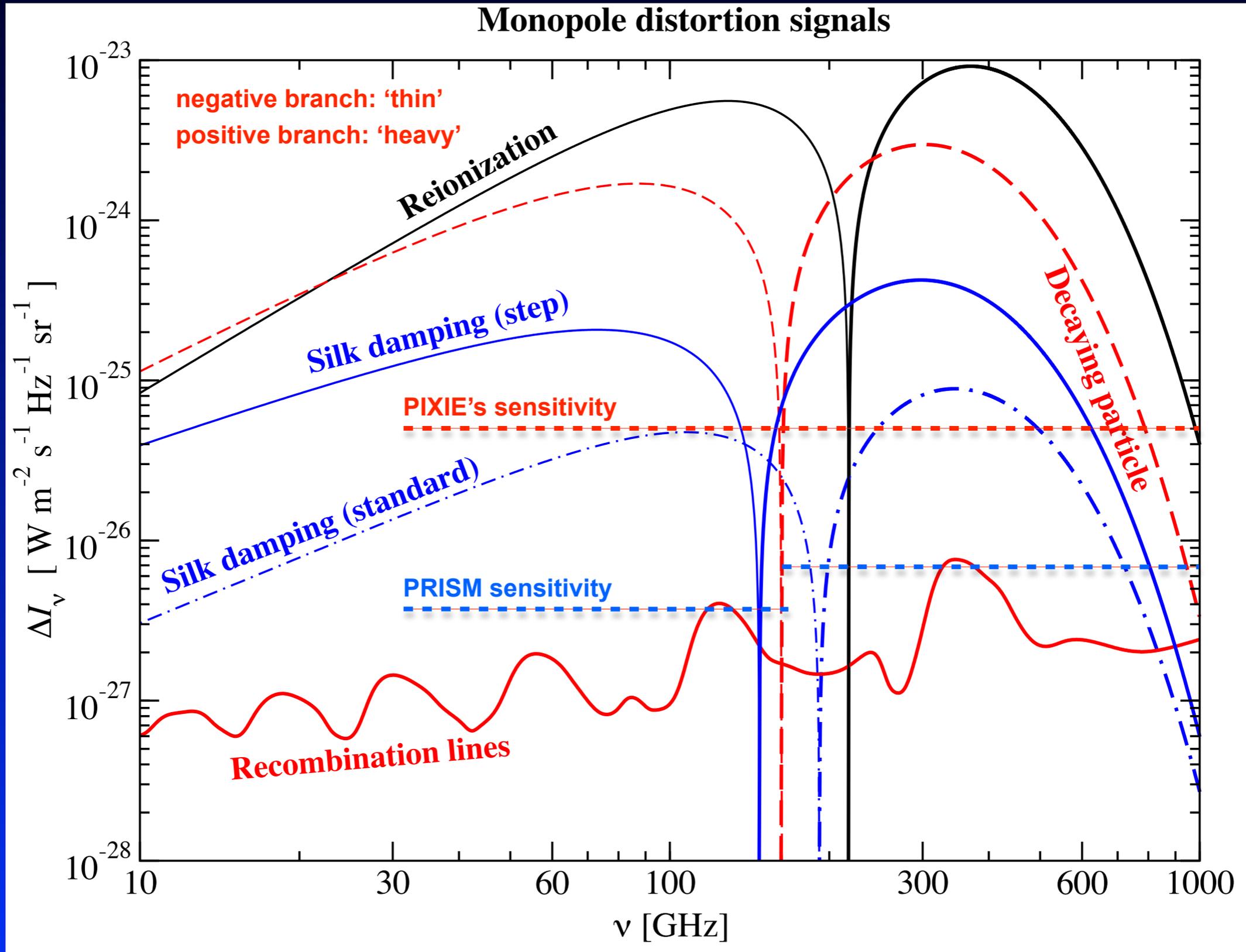
Average CMB spectral distortions

Absolute value of Intensity signal



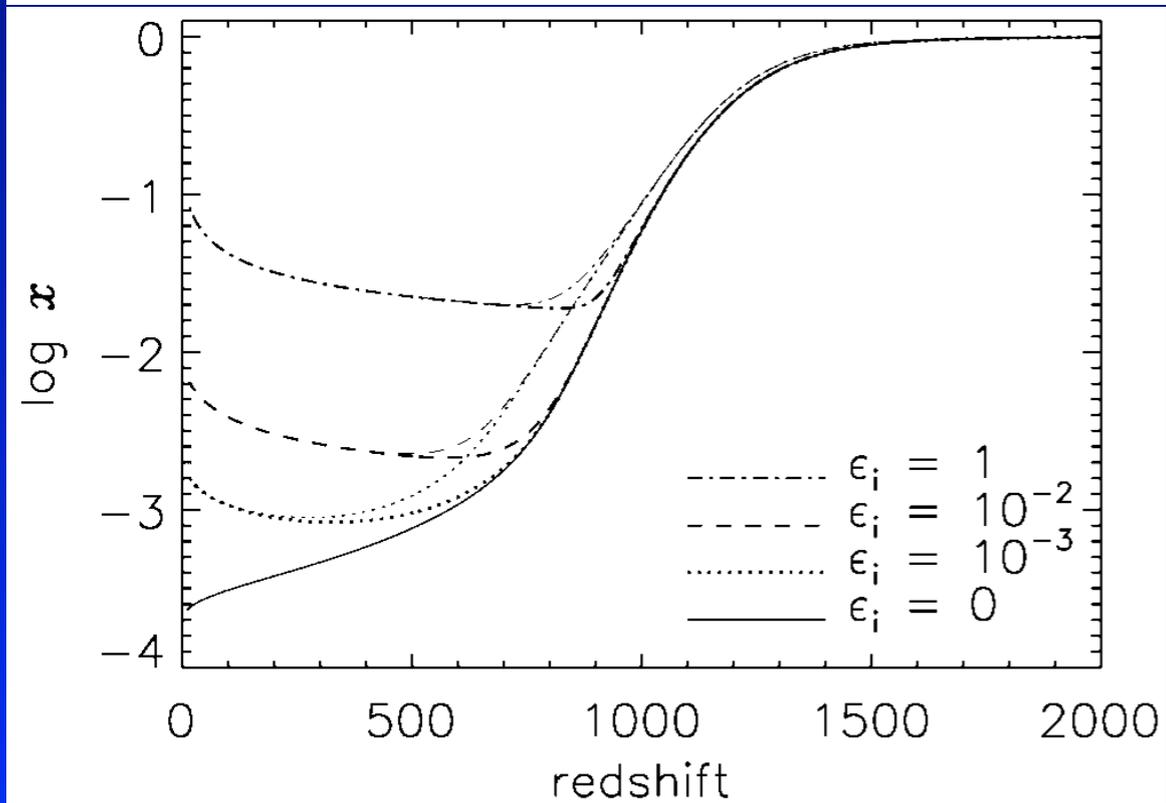
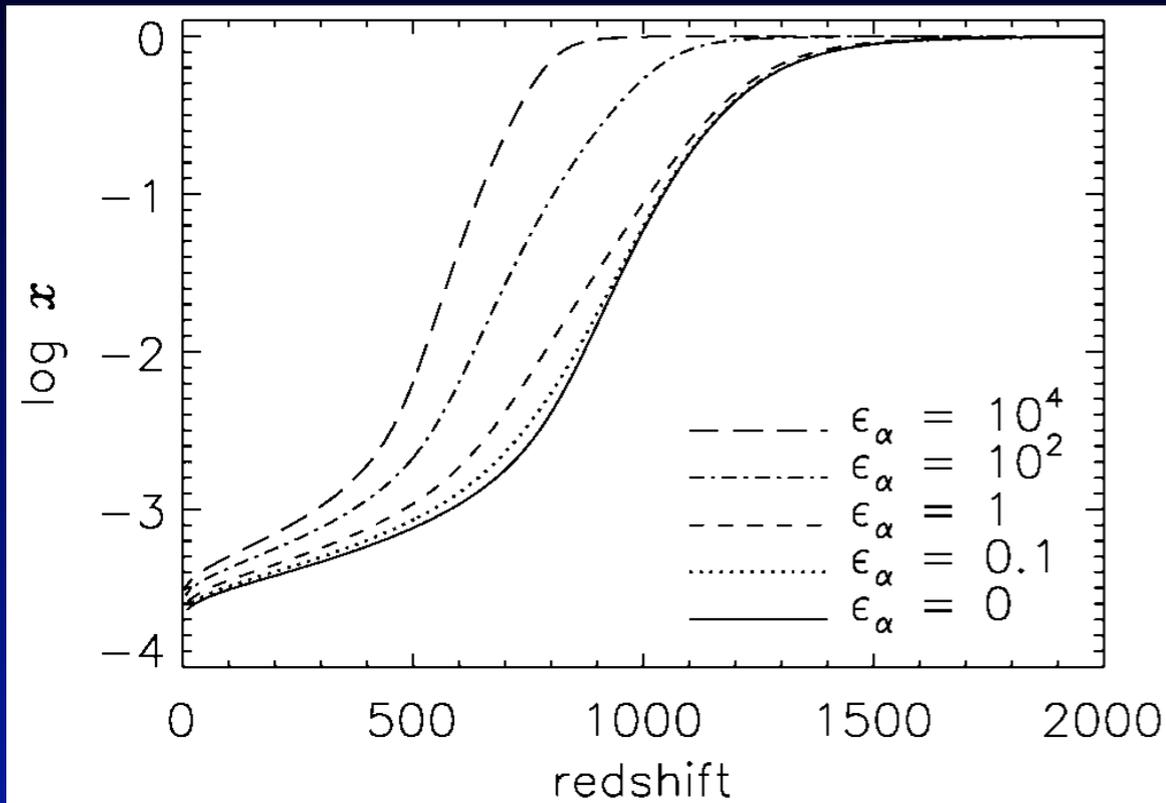
Average CMB spectral distortions

Absolute value of Intensity signal



But this is again not all!

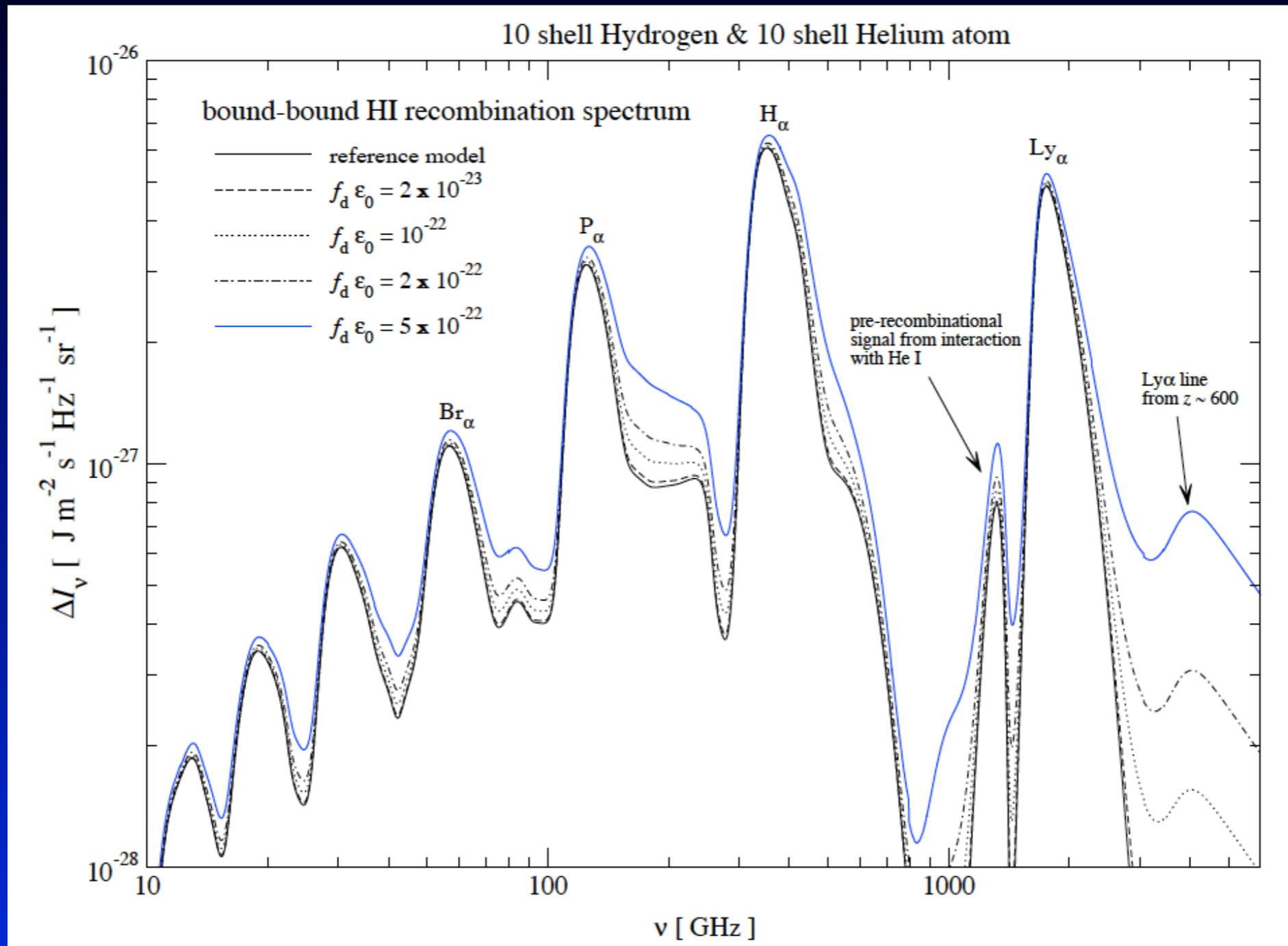
Extra Sources of Ionizations or Excitations



- ,Hypothetical' source of extra photons parametrized by ϵ_α & ϵ_i
- Extra **excitations** \Rightarrow delay of Recombination
- Extra **ionizations** \Rightarrow affect 'freeze out' tail
- This affects the Thomson visibility function
- From WMAP $\Rightarrow \epsilon_\alpha < 0.39$ & $\epsilon_i < 0.058$ at 95% confidence level (Galli et al. 2008)

- Extra **ionizations & excitations** should also lead to **additional photons** in the recombination radiation!!!
- This in principle should allow us to check for such sources at $z \sim 1000$

Dark matter annihilations / decays



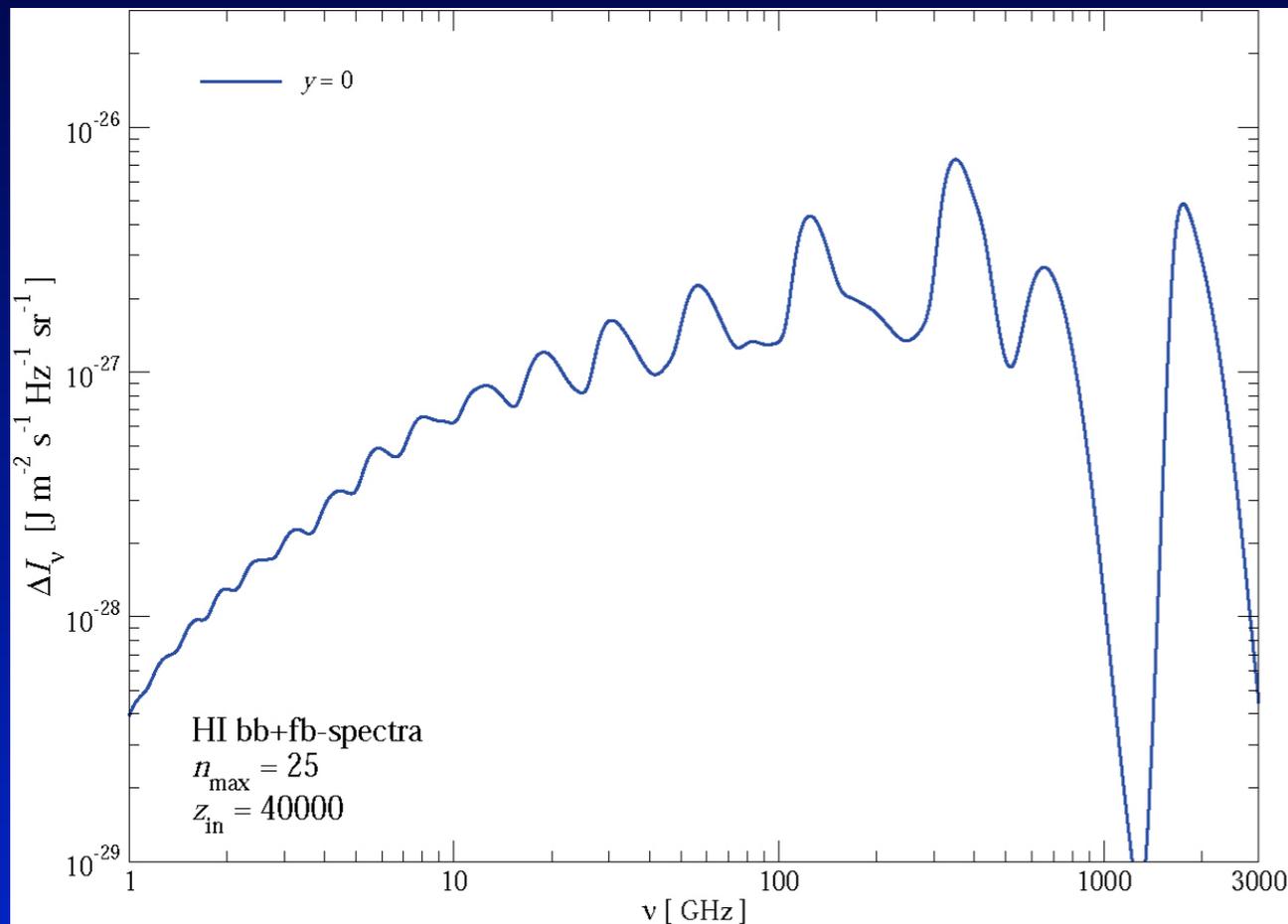
JC, 2009, arXiv:0910.3663

- Additional photons at all frequencies
- Broadening of spectral features
- Shifts in the positions

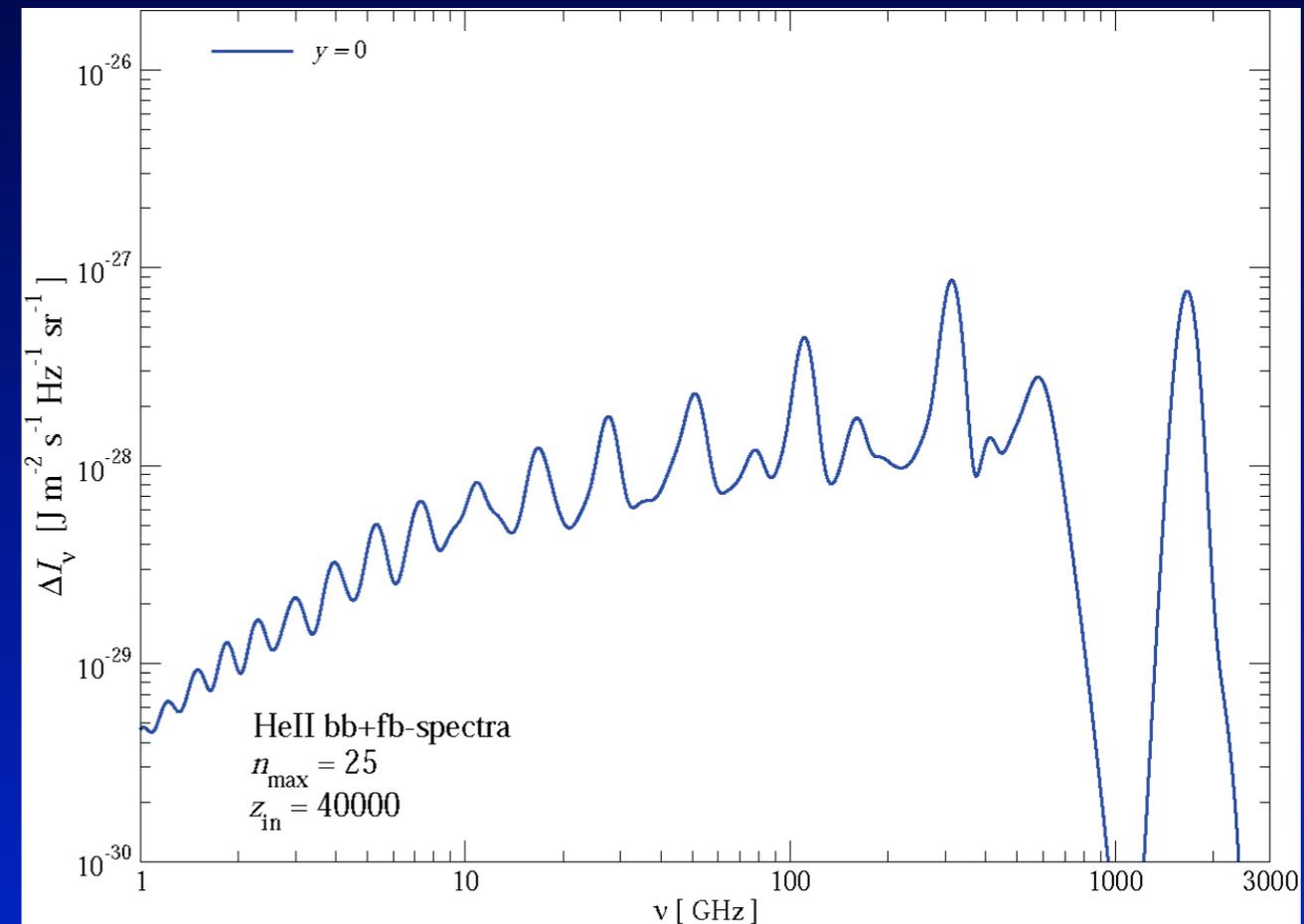
CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on y*

Hydrogen



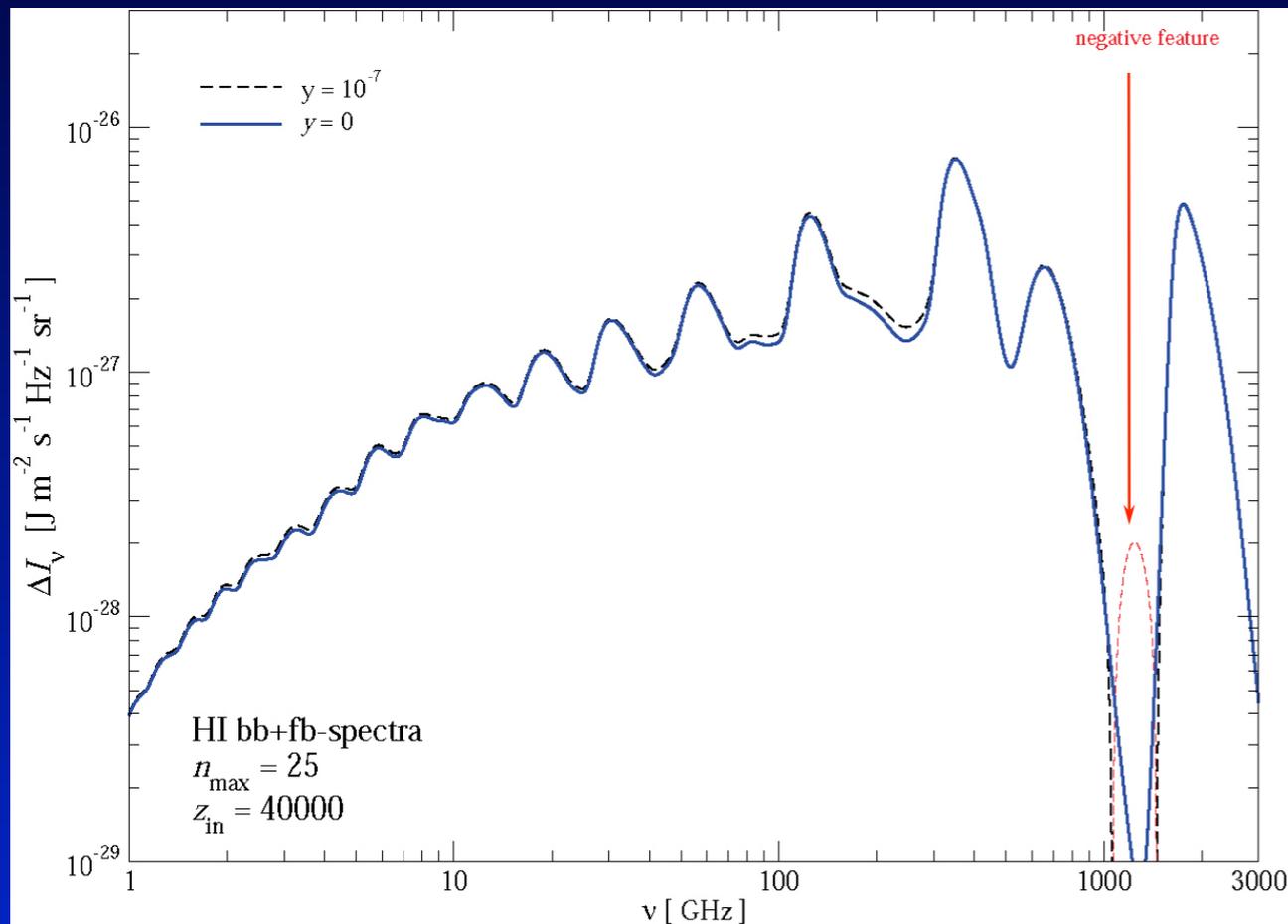
Helium +



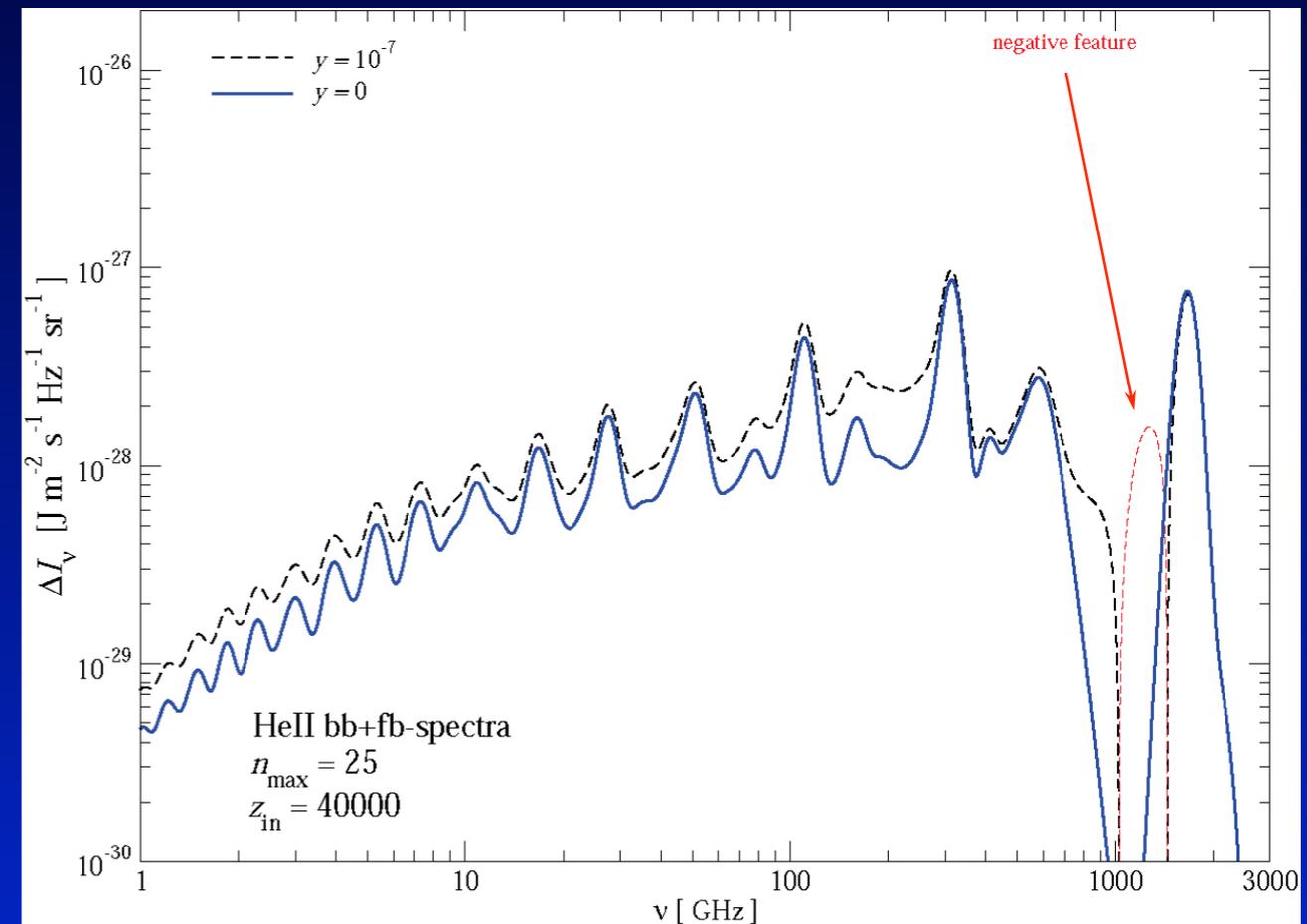
CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on y*

Hydrogen



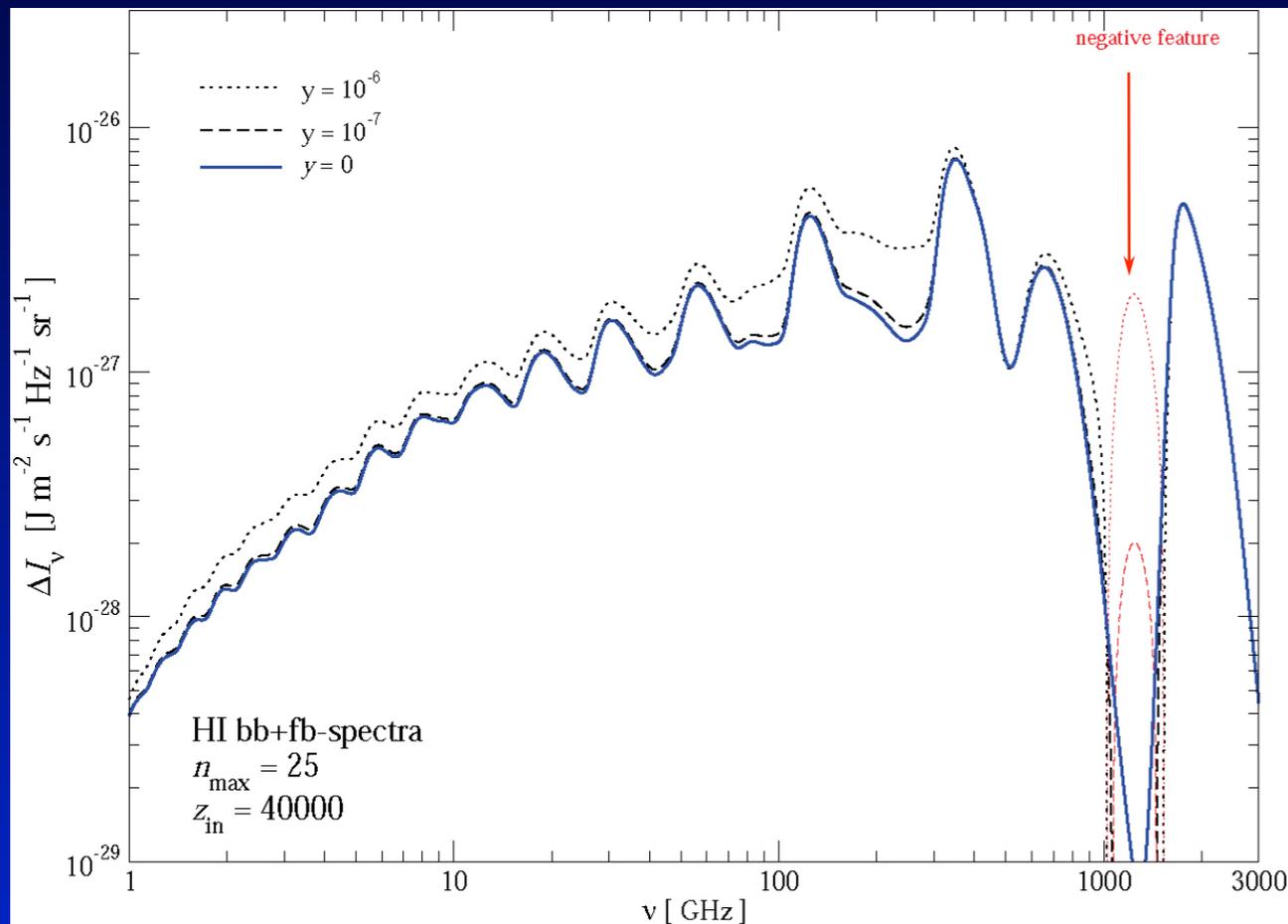
Helium +



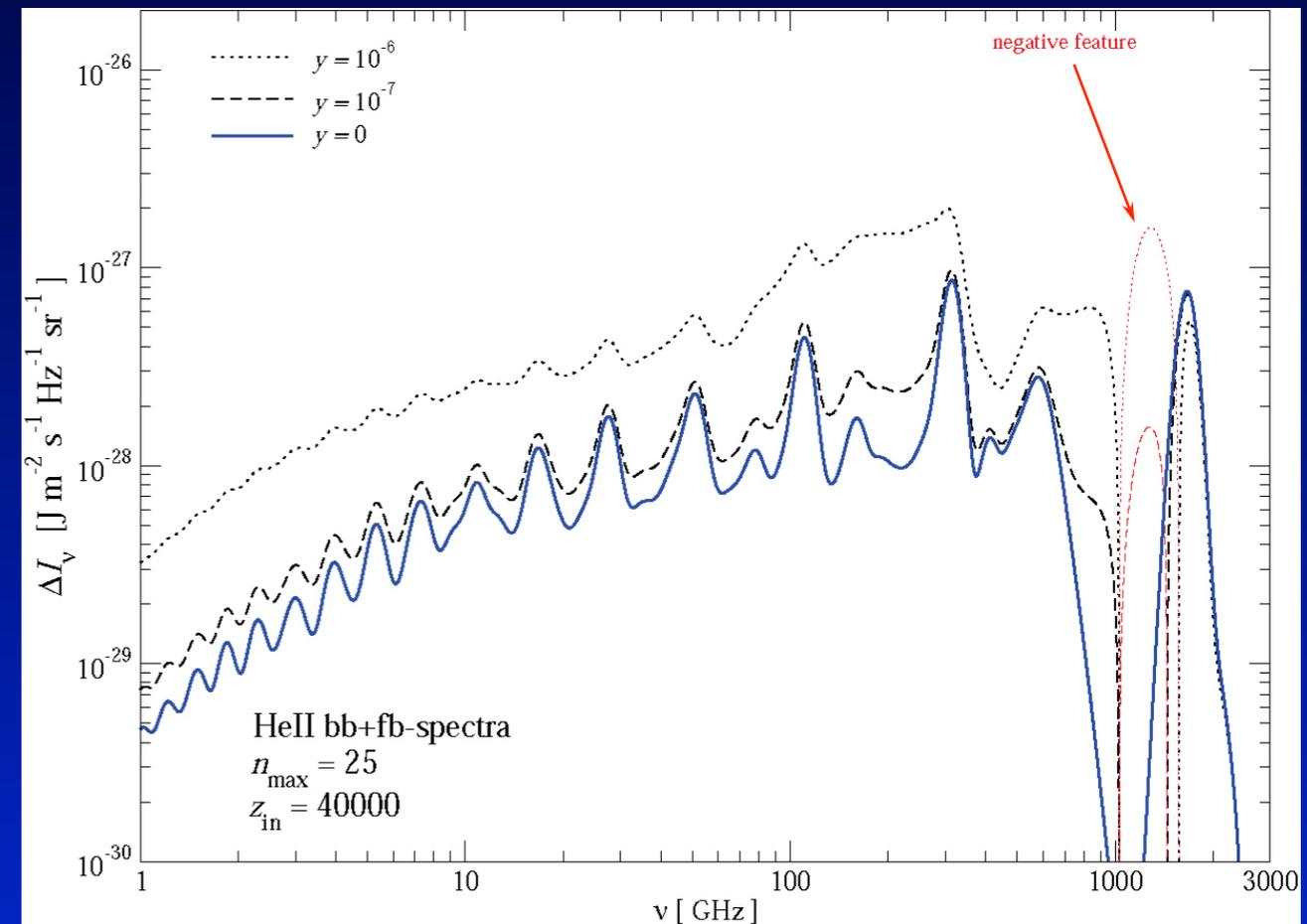
CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on y*

Hydrogen



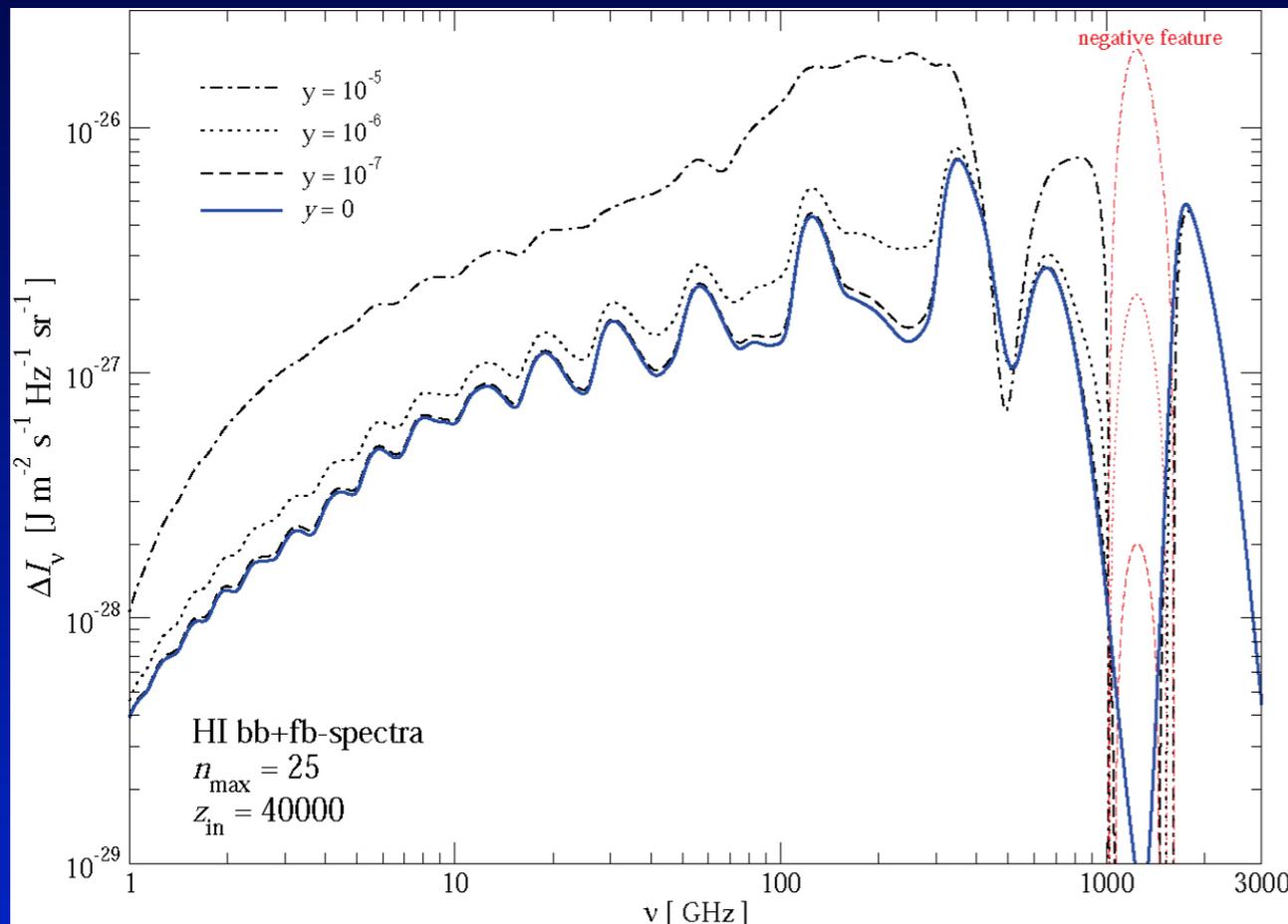
Helium +



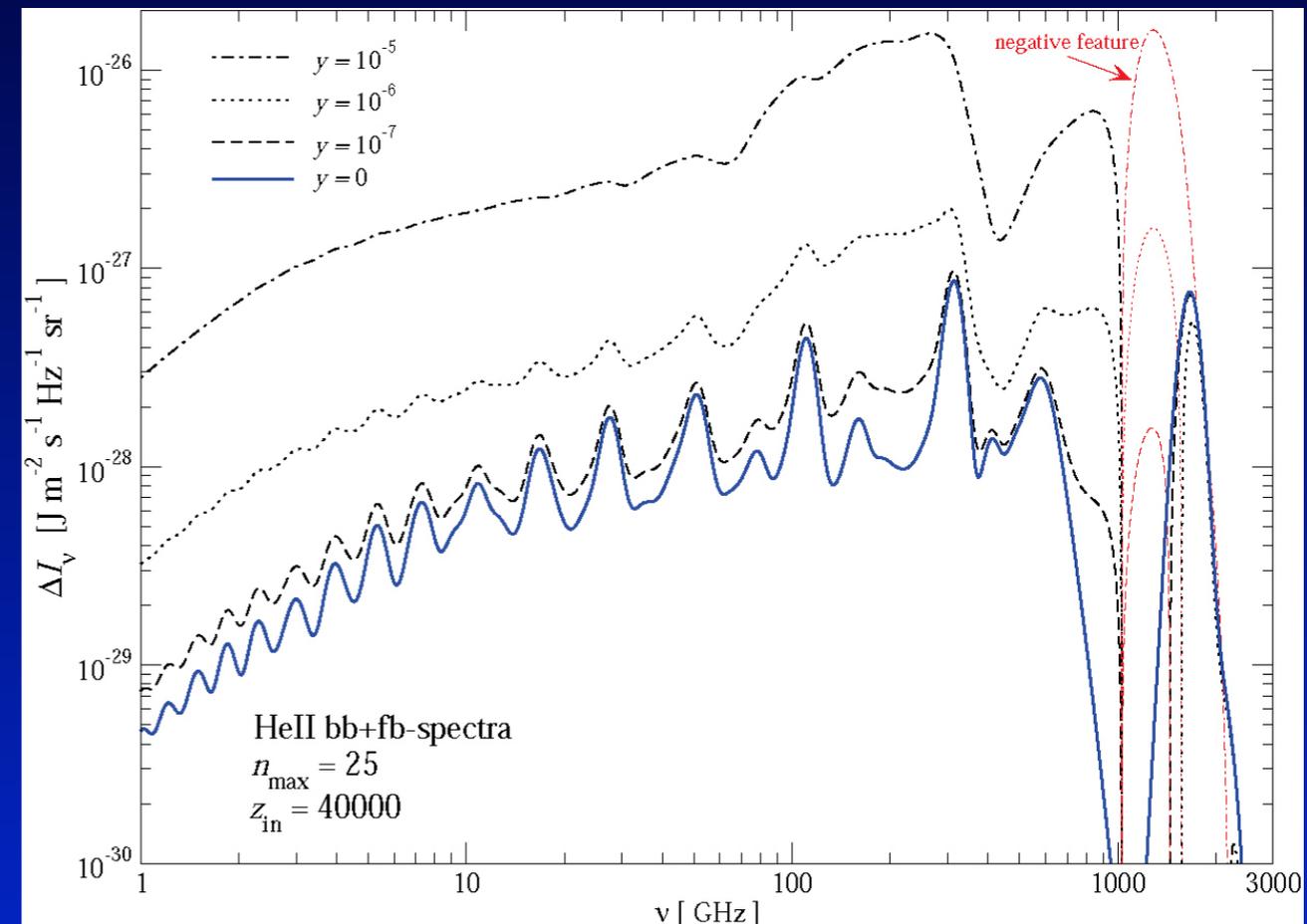
CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on y*

Hydrogen



Helium +



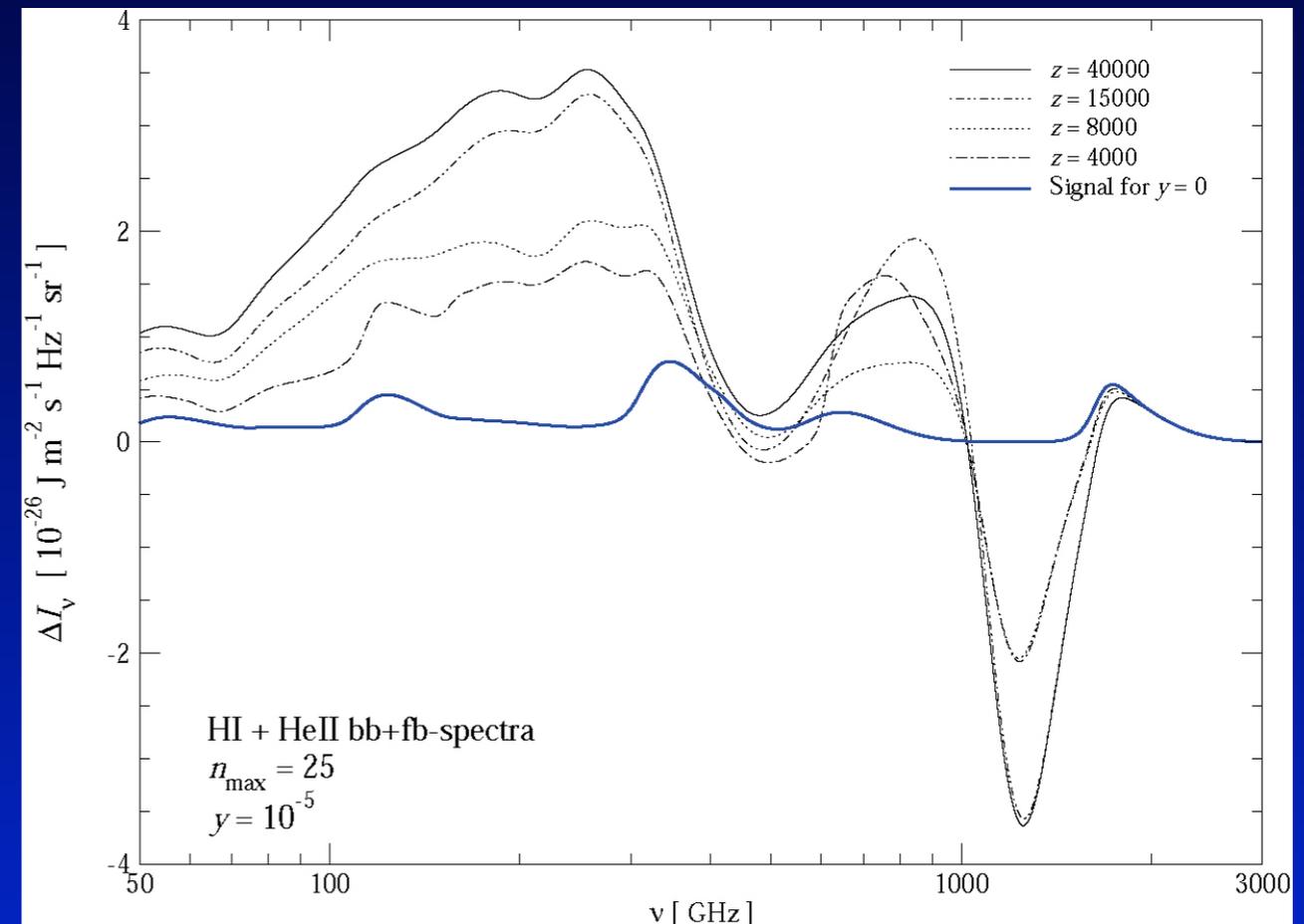
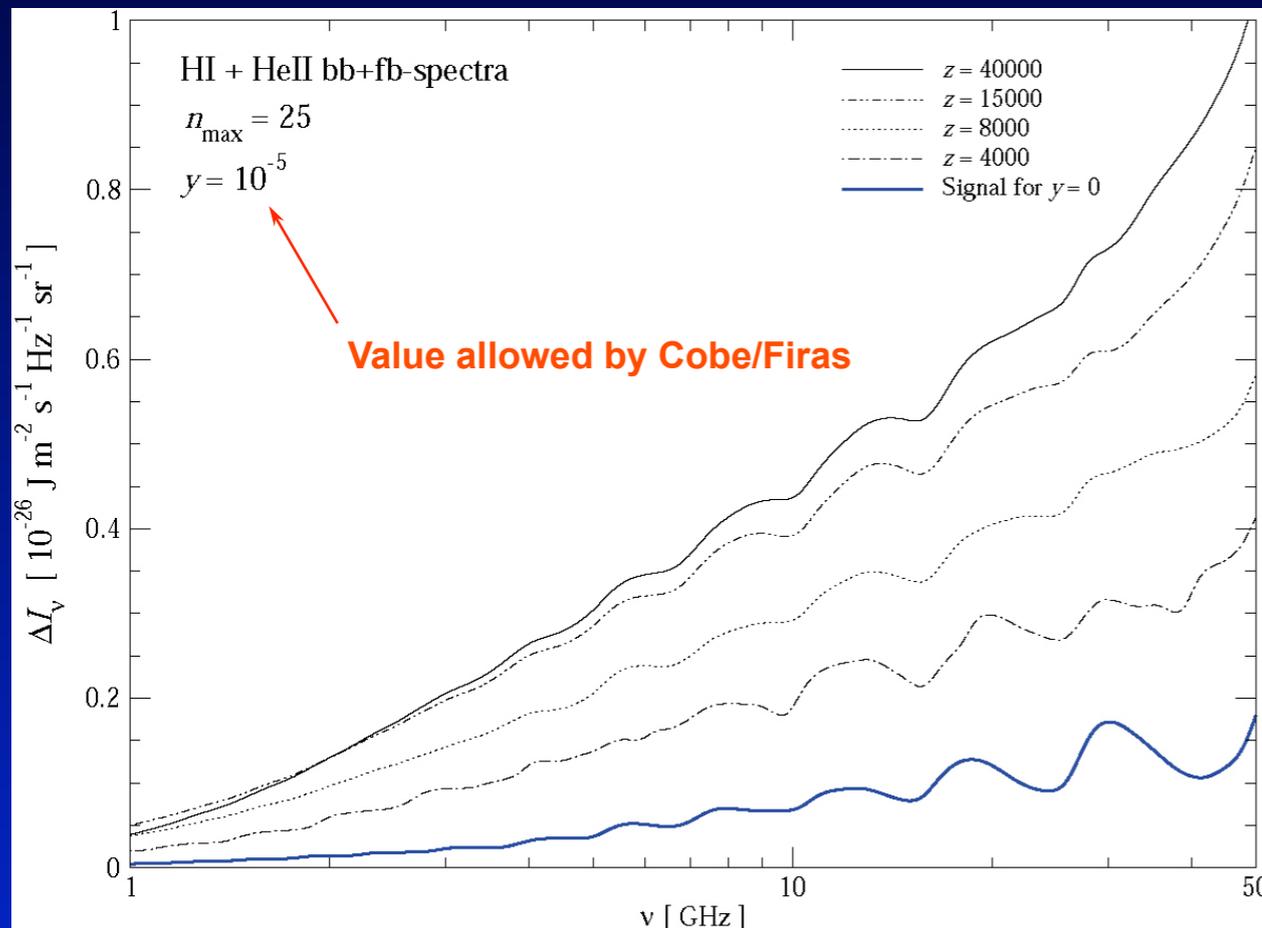
JC & Sunyaev, 2008, astro-ph/0803.3584

- ◆ Large increase in the total amplitude of the distortions with value of y !
- ◆ Strong emission-absorption feature in the Wien-part of CMB (absent for $y=0$!!!)
- ◆ HeII contribution to the pre-recombinational emission as strong as the one from Hydrogen alone !

CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on z*

Hydrogen and Helium +



JC & Sunyaev, 2008, astro-ph/0803.3584

- ◆ Large increase in the total amplitude of the distortions with injection redshift!
- ◆ Number of spectral features depends on injection redshift!
- ◆ Emission-Absorption feature increases ~ 2 for energy injection $z \Rightarrow 11000$

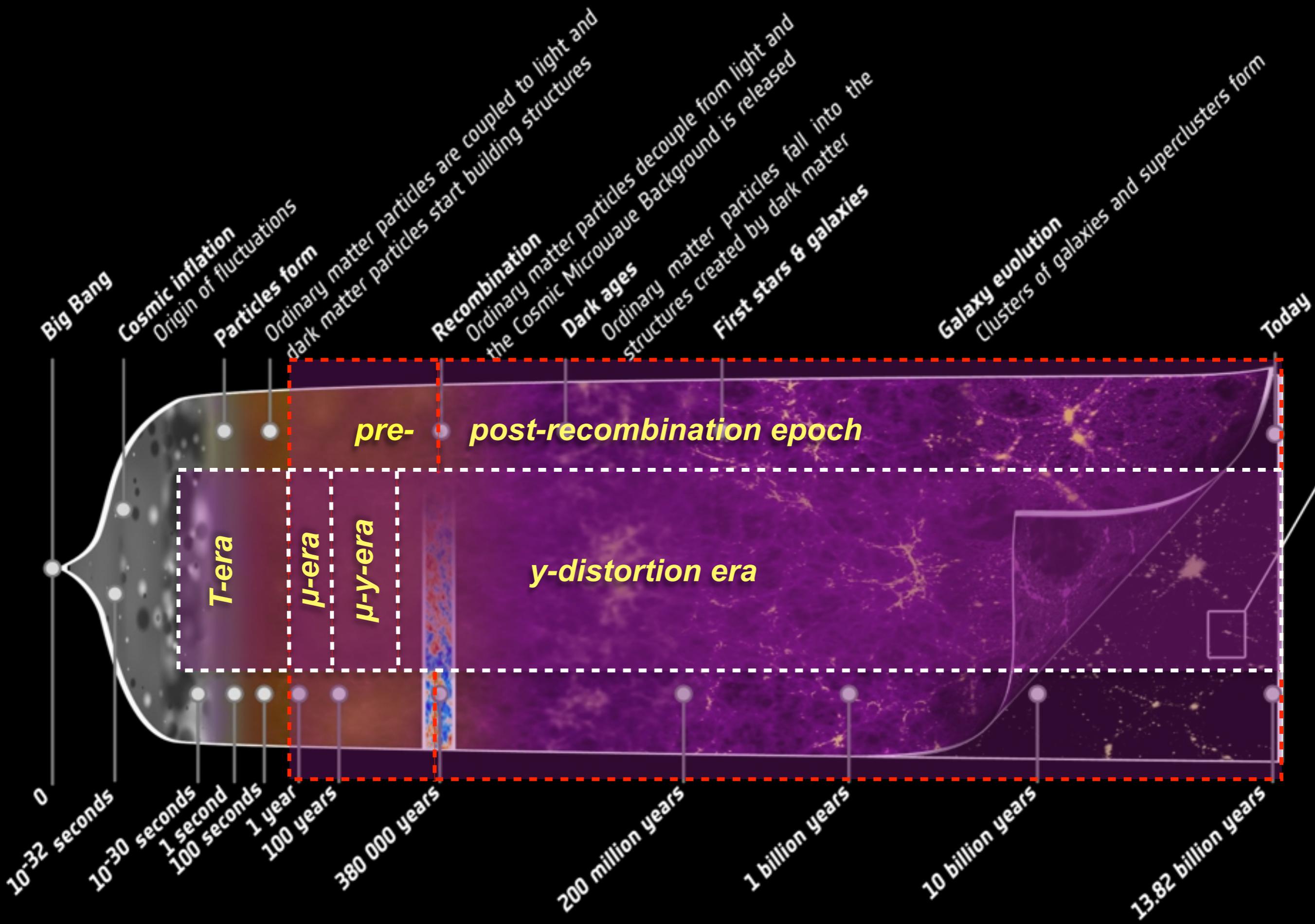
What would we actually learn by doing such hard job?

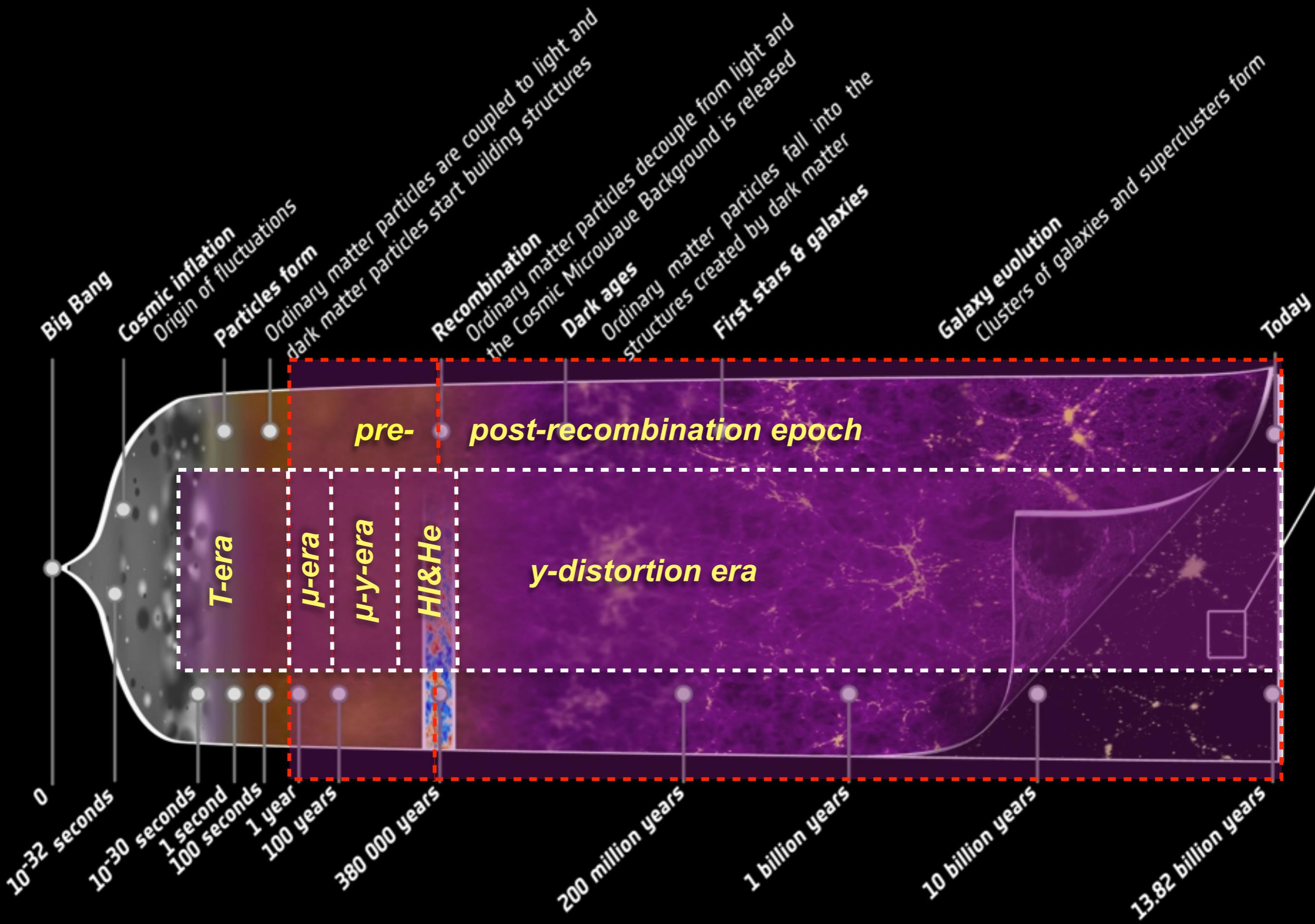
Cosmological Recombination Spectrum opens a way to measure:

- the specific *entropy* of our universe (related to $\Omega_b h^2$)
- the CMB *monopole* temperature T_0
- *the pre-stellar abundance of helium* Y_p
- *If recombination occurs as we think it does, then the lines can be predicted with very high accuracy!*
- *In principle allows us to directly check our understanding of the standard recombination physics*

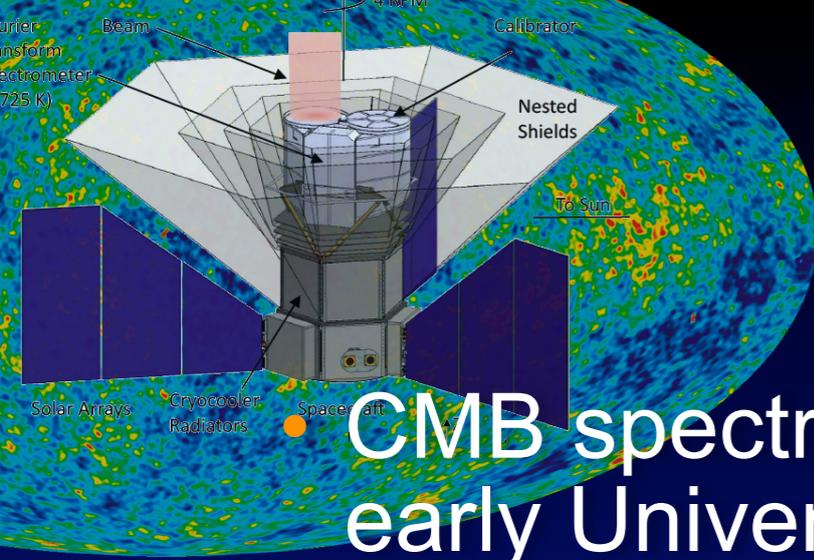
If something unexpected or non-standard happened:

- *non-standard thermal histories should leave some measurable traces*
- *direct way to measure/reconstruct the recombination history!*
- *possibility to distinguish pre- and post-recombination y-type distortions*
- *sensitive to energy release during recombination*
- *variation of fundamental constants*





Summary



CMB spectral distortions open a *new window* to the early Universe and inflationary epoch

- *complementary* and *independent* source of information about our Universe *not* just confirmation
- simplicity of thermalization physics allows making very *precise predictions* for the distortions caused by different heating mechanisms
- in *standard cosmology* several processes lead to *early energy release* at a level that will be detectable in the future
- extremely interesting *future* for CMB based science!

