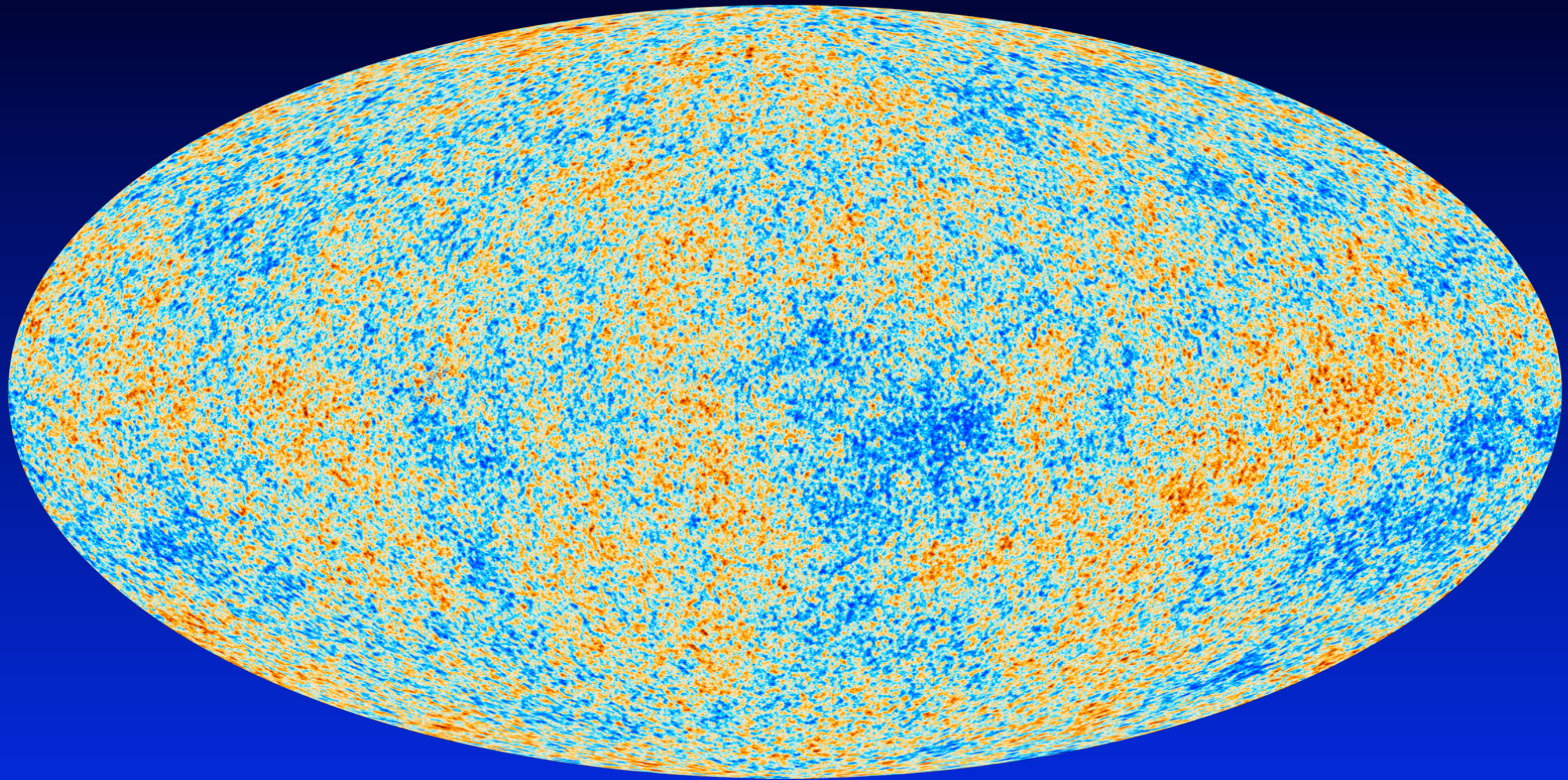


Part II: Distortions for different scenarios and what we may learn by studying them

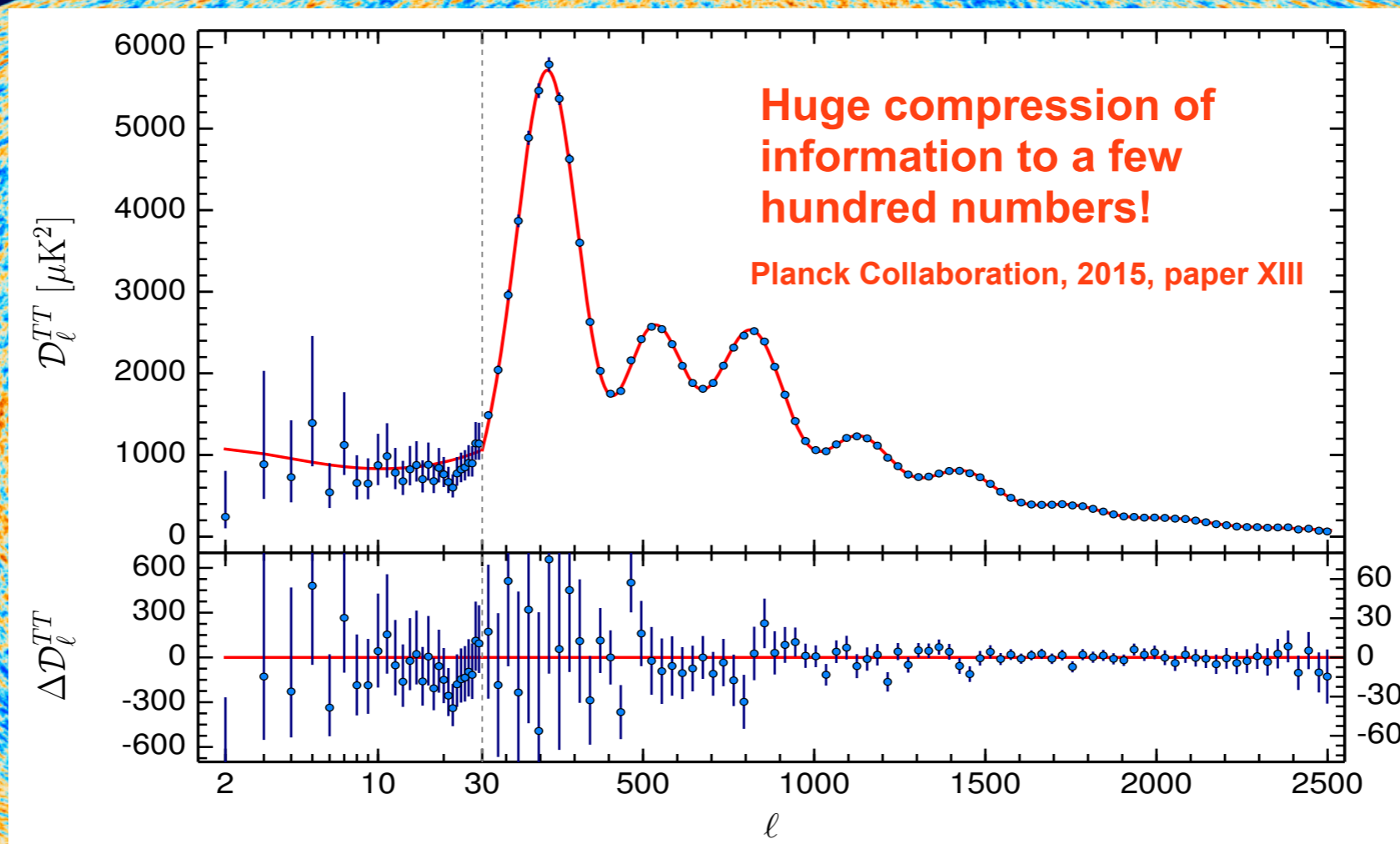
Cosmic Microwave Background Anisotropies



Planck all-sky
temperature map

- CMB has a blackbody spectrum in every direction
- tiny variations of the CMB temperature $\Delta T/T \sim 10^{-5}$

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temperature map

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CMB anisotropies (with SN, LSS, etc...) clearly taught us a lot about the Universe we live in!

- Standard 6 parameter concordance cosmology with parameters known to percent level precision
- Gaussian-distributed adiabatic fluctuations with nearly scale-invariant power spectrum over a wide range of scales
- cold dark matter (“CDM”)
- accelerated expansion today (“ Λ ”)
- Standard BBN scenario $\rightarrow N_{\text{eff}}$ and Y_p
- Standard ionization history $\rightarrow N_e$ as a function of z

Parameter	TT+lowP 68 % limits	TT+lowP+lensing 68 % limits	TT+lowP+lensing+ext 68 % limits	TT,TE,EE+lowP 68 % limits	TT,TE,EE+lowP+lensing 68 % limits	TT,TE,EE+lowP+lensing+ext 68 % limits
$\Omega_b h^2$	0.02222 ± 0.00023	0.02226 ± 0.00023	0.02227 ± 0.00020	0.02225 ± 0.00016	0.02226 ± 0.00016	0.02230 ± 0.00014
$\Omega_c h^2$	0.1197 ± 0.0022	0.1186 ± 0.0020	0.1184 ± 0.0012	0.1198 ± 0.0015	0.1193 ± 0.0014	0.1188 ± 0.0010
$100\theta_{\text{MC}}$	1.04085 ± 0.00047	1.04103 ± 0.00046	1.04106 ± 0.00041	1.04077 ± 0.00032	1.04087 ± 0.00032	1.04093 ± 0.00030
τ	0.078 ± 0.019	0.066 ± 0.016	0.067 ± 0.013	0.079 ± 0.017	0.063 ± 0.014	0.066 ± 0.012
$\ln(10^{10} A_s)$	3.089 ± 0.036	3.062 ± 0.029	3.064 ± 0.024	3.094 ± 0.034	3.059 ± 0.025	3.064 ± 0.023
n_s	0.9655 ± 0.0062	0.9677 ± 0.0060	0.9681 ± 0.0044	0.9645 ± 0.0049	0.9653 ± 0.0048	0.9667 ± 0.0040

What are the *main* next targets for CMB anisotropies?

- CMB temperature power spectrum kind of finished...
- E modes cosmic variance limited to high- l
 - better constraint on τ from large scale E modes
 - refined CMB damping tail science from small-scale E modes
 - CMB lensing and de-lensing of primordial B-modes
- primordial B modes
 - detection of $r \sim 10^{-3}$ (*energy scale of inflation*)
 - upper limit on $n_T < O(0.1)$ as additional 'proof of inflation'
- CMB anomalies
 - stationarity of E and B-modes, lensing potential, etc across the sky
- SZ cluster science
 - large cluster samples and (individual) high-res cluster measurements

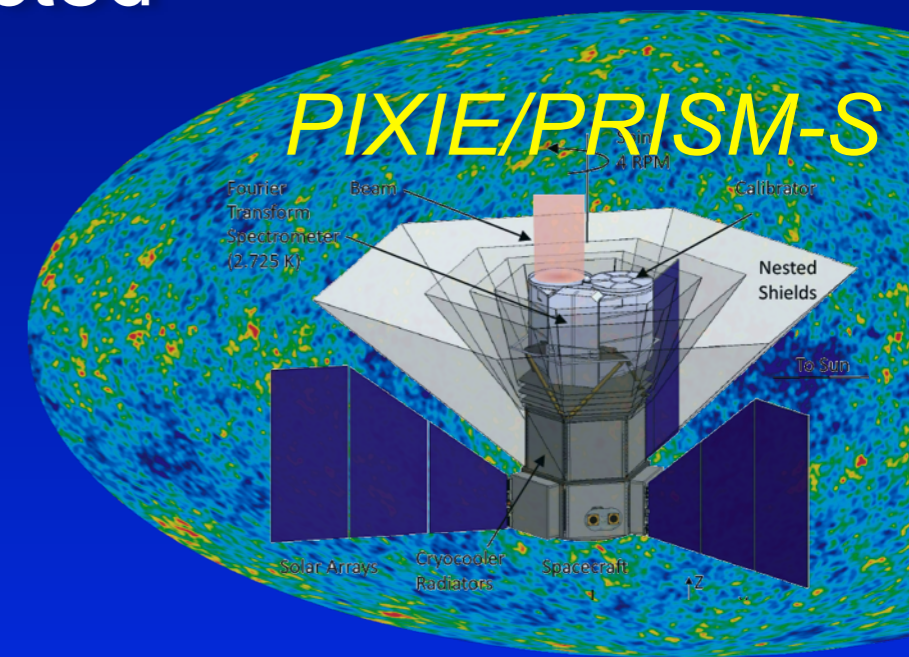
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Lots of competition to reach these goals!

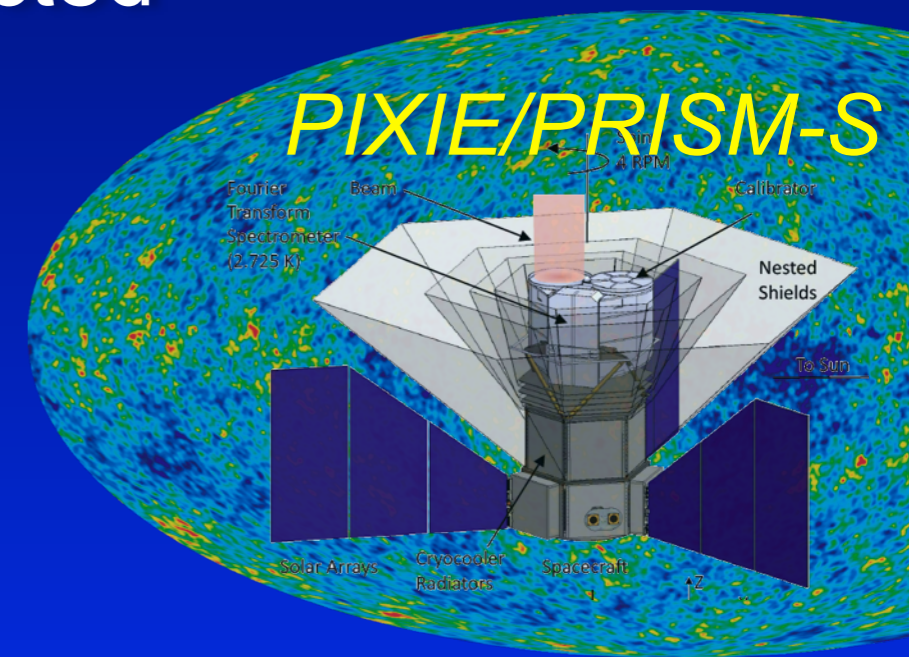
What can CMB spectral distortions add?

- Add a *new dimension* to CMB science
 - probe the thermal history at different stages of the Universe
- *Complementary and independent* information!
 - cosmological parameters from the recombination radiation
 - new/additional test of large-scale anomalies
- Several *guaranteed signals* are expected
 - y -distortion from low redshifts
 - damping signal & recombination radiation
- Test various *inflation* models
 - damping of the small-scale power spectrum
- *Discovery* potential
 - decaying particles and other exotic sources of distortions



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All this largely without any competition from the ground!!!

Physical mechanisms that lead to spectral distortions

- *Cooling by adiabatically expanding ordinary matter*
(JC, 2005; JC & Sunyaev 2011; Khatri, Sunyaev & JC, 2011)
 - Heating by *decaying* or *annihilating* relic particles
(Kawasaki et al., 1987; Hu & Silk, 1993; McDonald et al., 2001; JC, 2005; JC & Sunyaev, 2011; JC, 2013; JC & Jeong, 2013)
 - *Evaporation of primordial black holes & superconducting strings*
(Carr et al. 2010; Ostriker & Thompson, 1987; Tashiro et al. 2012; Pani & Loeb, 2013)
 - *Dissipation of primordial acoustic modes & magnetic fields*
(Sunyaev & Zeldovich, 1970; Daly 1991; Hu et al. 1994; JC & Sunyaev, 2011; JC et al. 2012 - Jedamzik et al. 2000; Kunze & Komatsu, 2013)
 - *Cosmological recombination radiation*
(Zeldovich et al., 1968; Peebles, 1968; Dubrovich, 1977; Rubino-Martin et al., 2006; JC & Sunyaev, 2006; Sunyaev & JC, 2009)
-
- *Signatures due to first supernovae and their remnants*
(Oh, Cooray & Kamionkowski, 2003)
 - *Shock waves arising due to large-scale structure formation*
(Sunyaev & Zeldovich, 1972; Cen & Ostriker, 1999)
 - *SZ-effect from clusters; effects of reionization*
(Refregier et al., 2003; Zhang et al. 2004; Trac et al. 2008)
 - *more exotic processes*
(Lochan et al. 2012; Bull & Kamionkowski, 2013; Brax et al., 2013; Tashiro et al. 2013)

Standard sources
of distortions

pre-recombination epoch

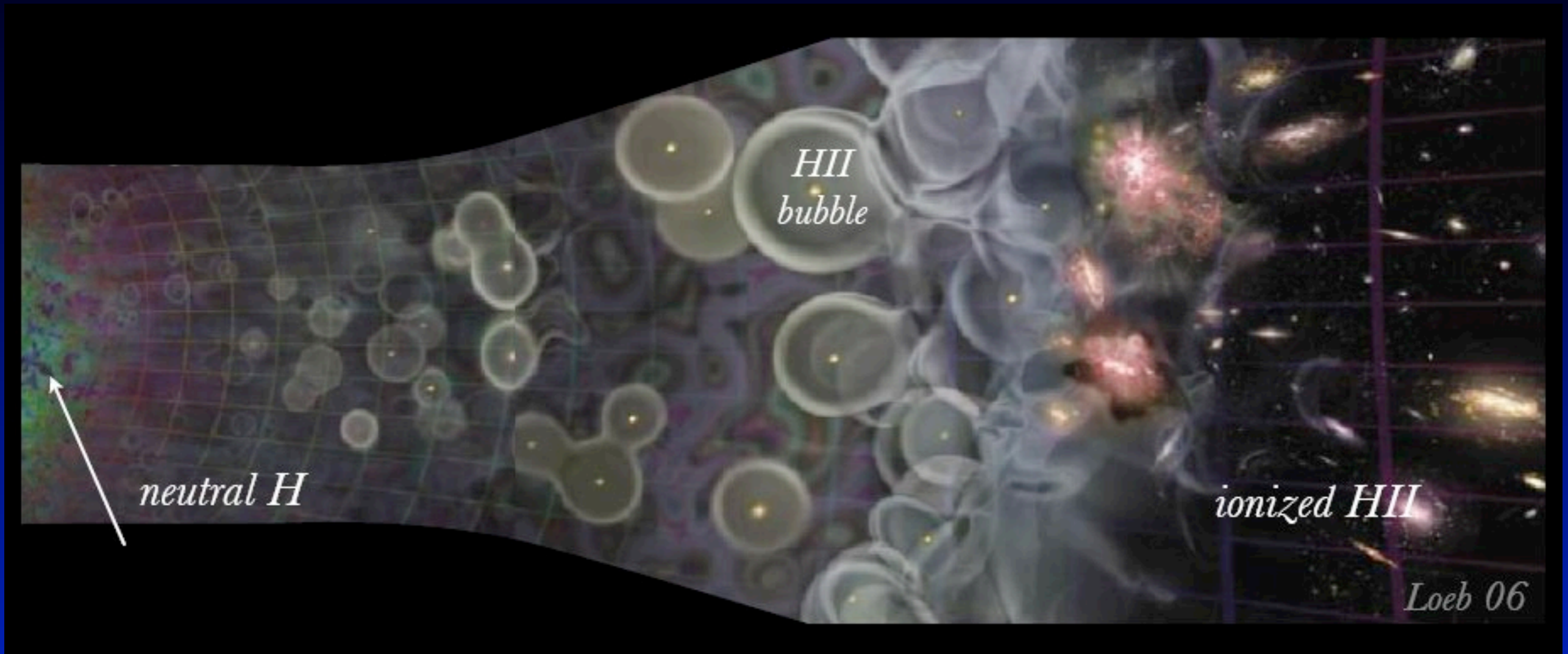
„high“ redshifts

„low“ redshifts

post-recombination

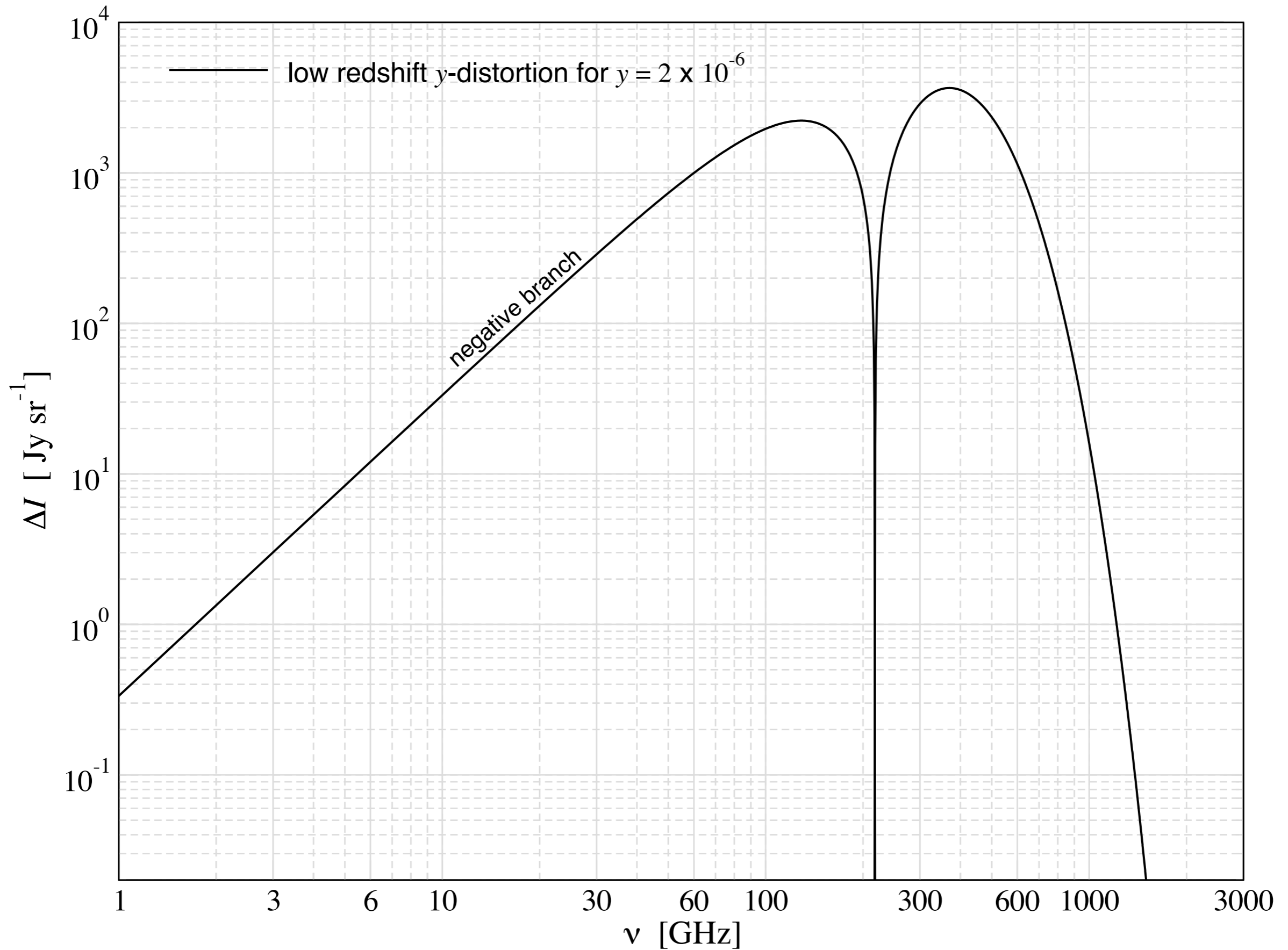
Reionization and structure formation

Simple estimates for the distortion

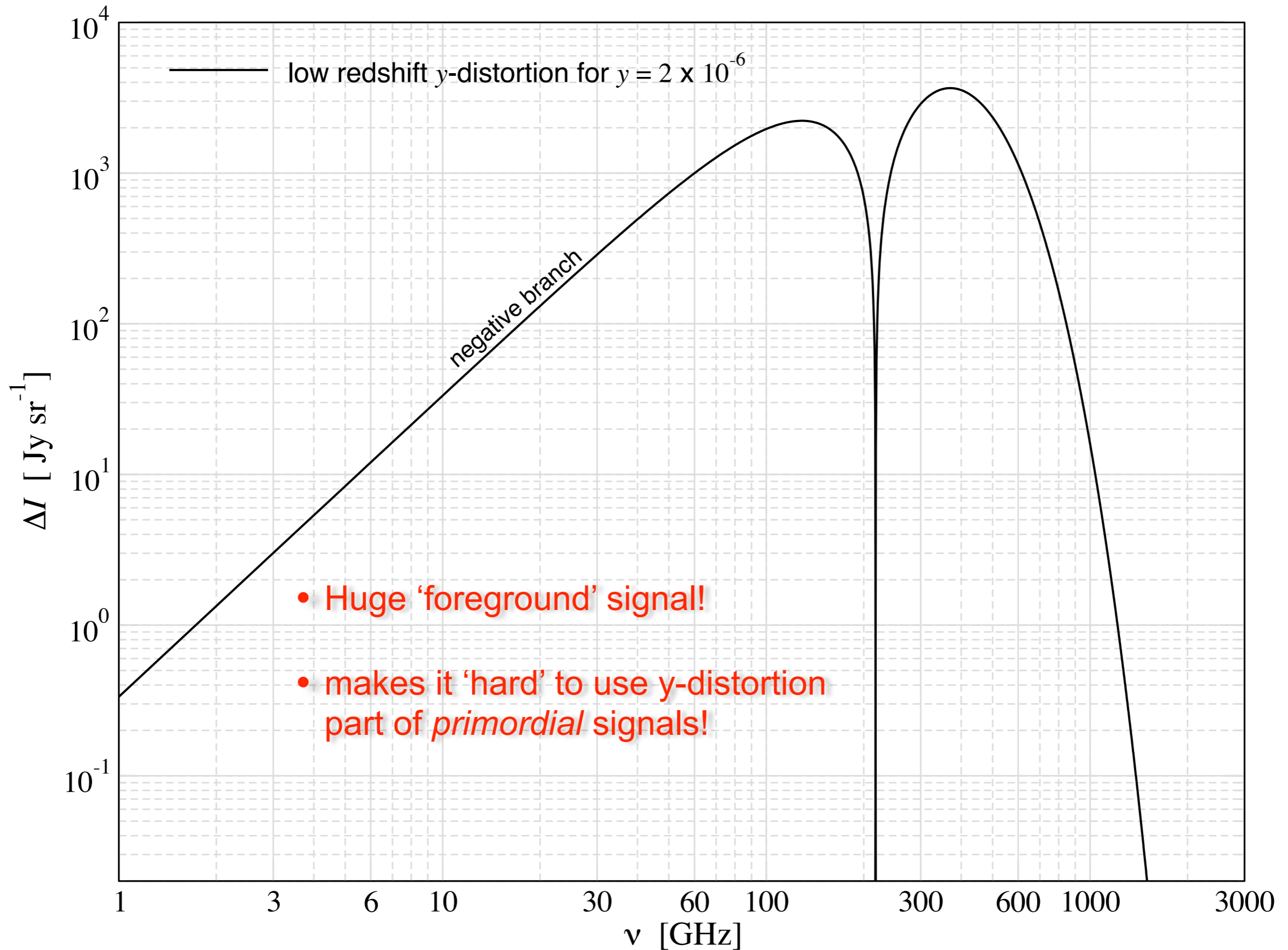


- Gas temperature $T \approx 10^4$ K
 - Thomson optical depth $\tau \approx 0.1$
 - second order Doppler effect $y \approx \text{few} \times 10^{-8}$
 - structure formation / SZ effect (e.g., Refregier et al., 2003) $y \approx \text{few} \times 10^{-7} - 10^{-6}$
- $\implies y \approx \frac{kT_e}{m_e c^2} \tau \approx 2 \times 10^{-7}$

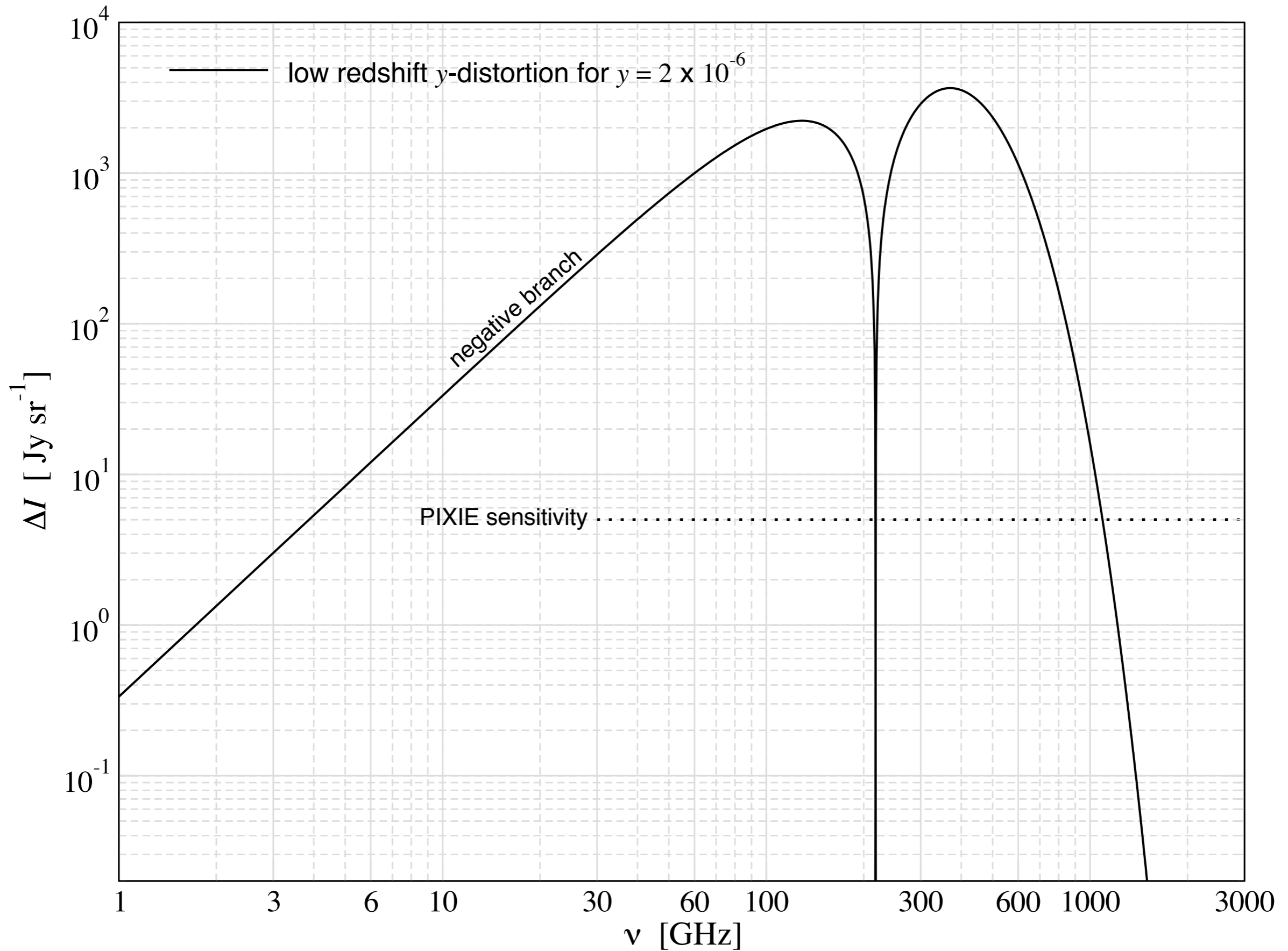
Average CMB spectral distortions



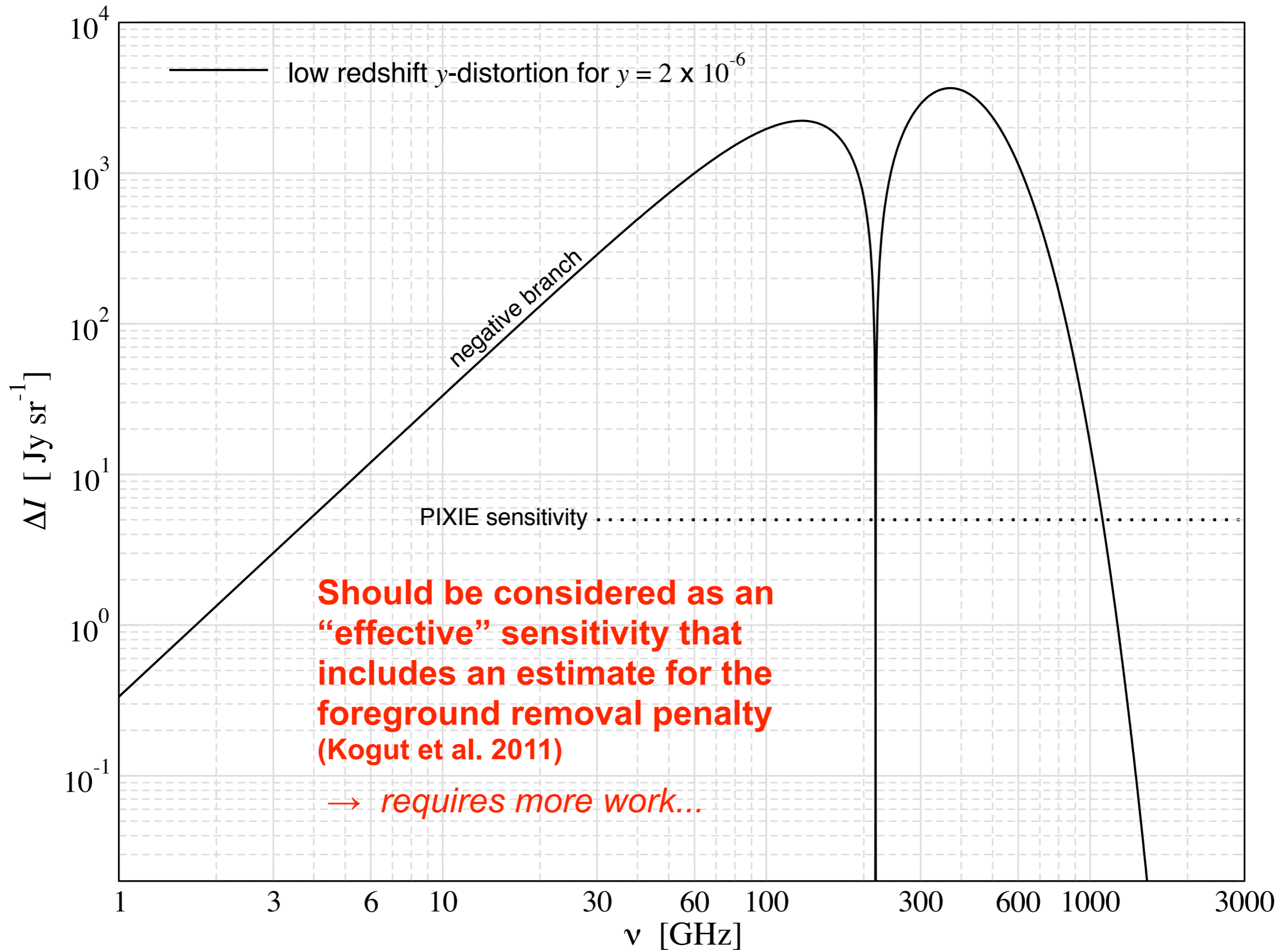
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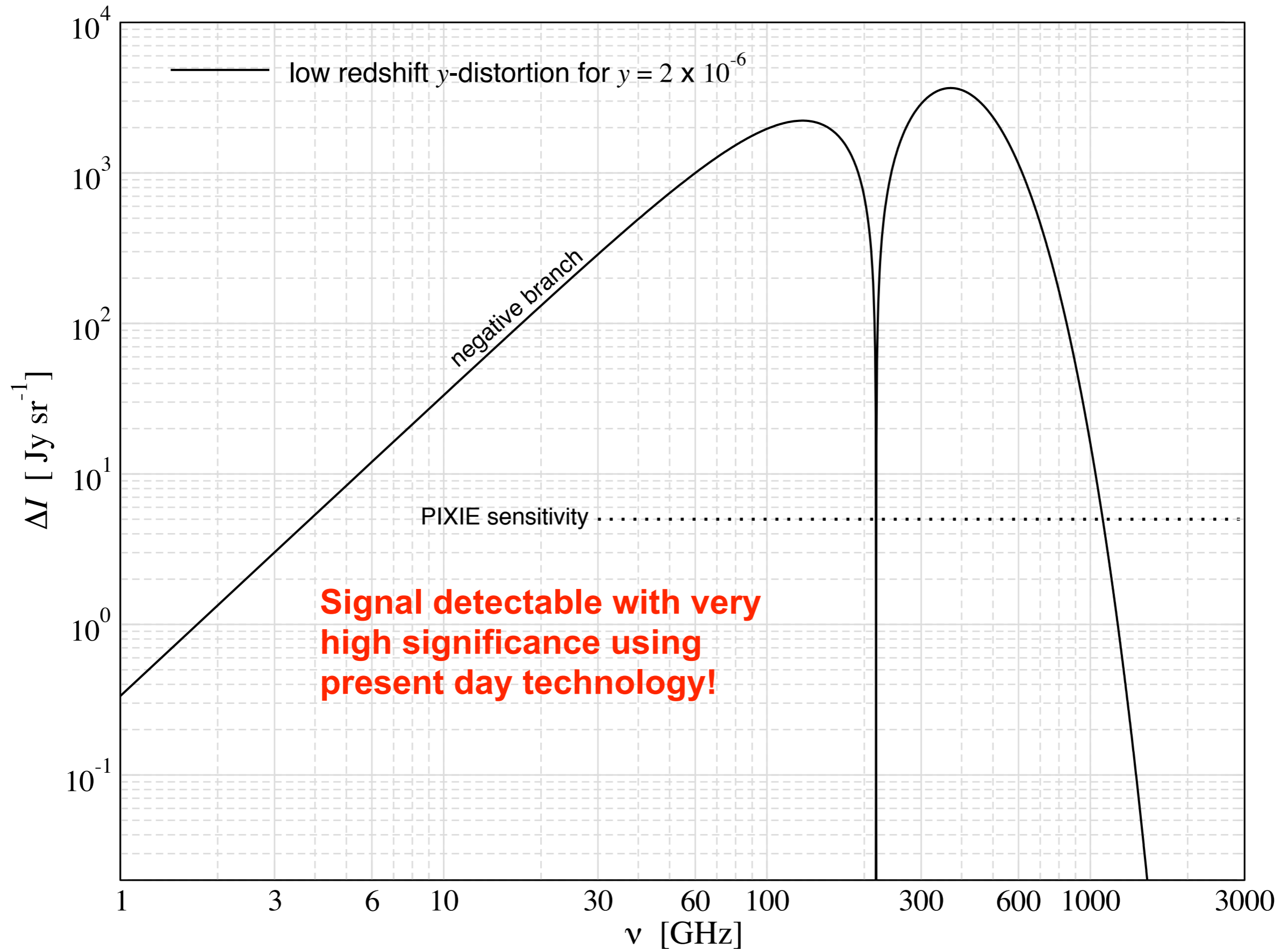
Average CMB spectral distortions



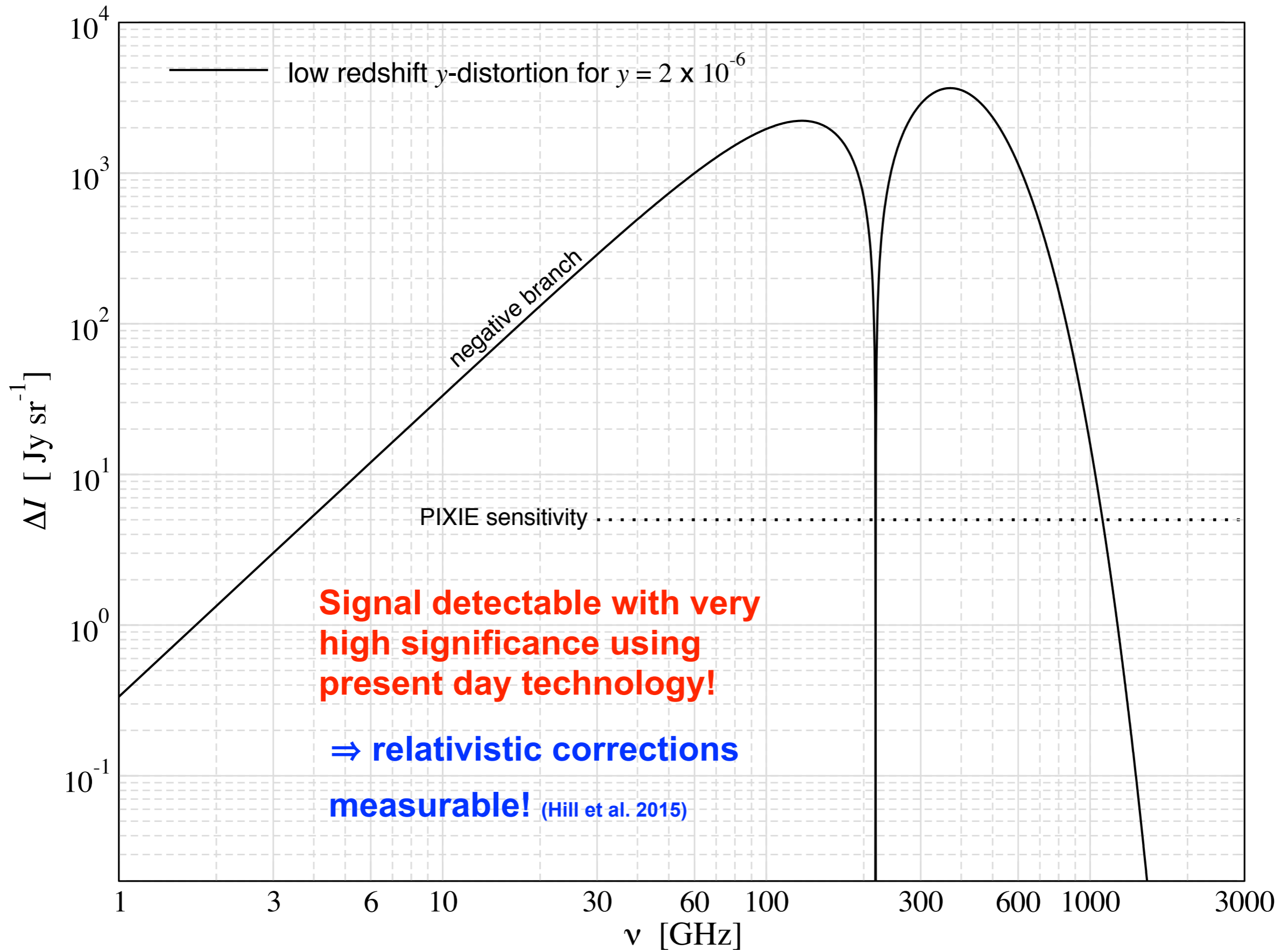
Average CMB spectral distortions



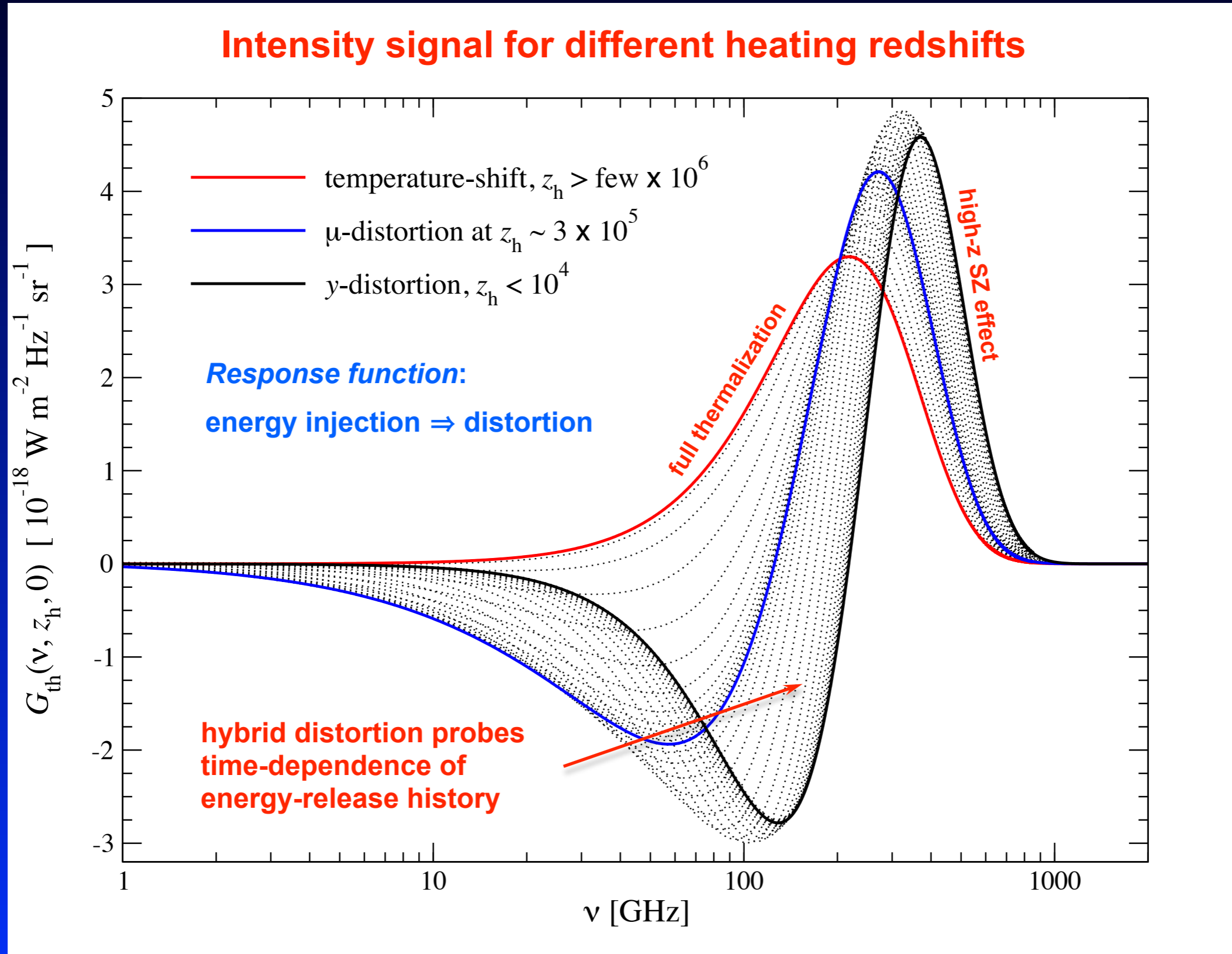
Average CMB spectral distortions



Average CMB spectral distortions

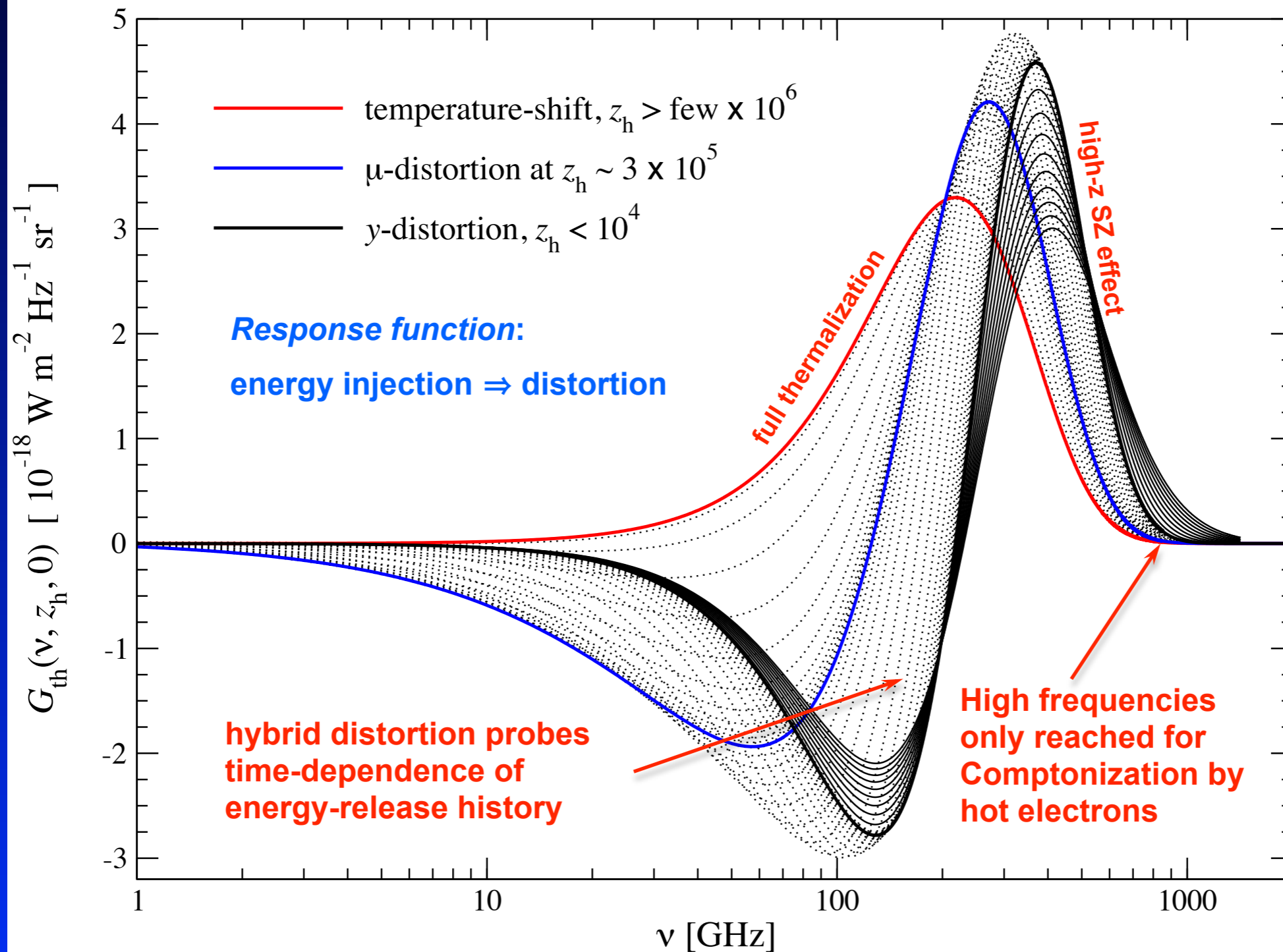


Distortion Green's function for energy release

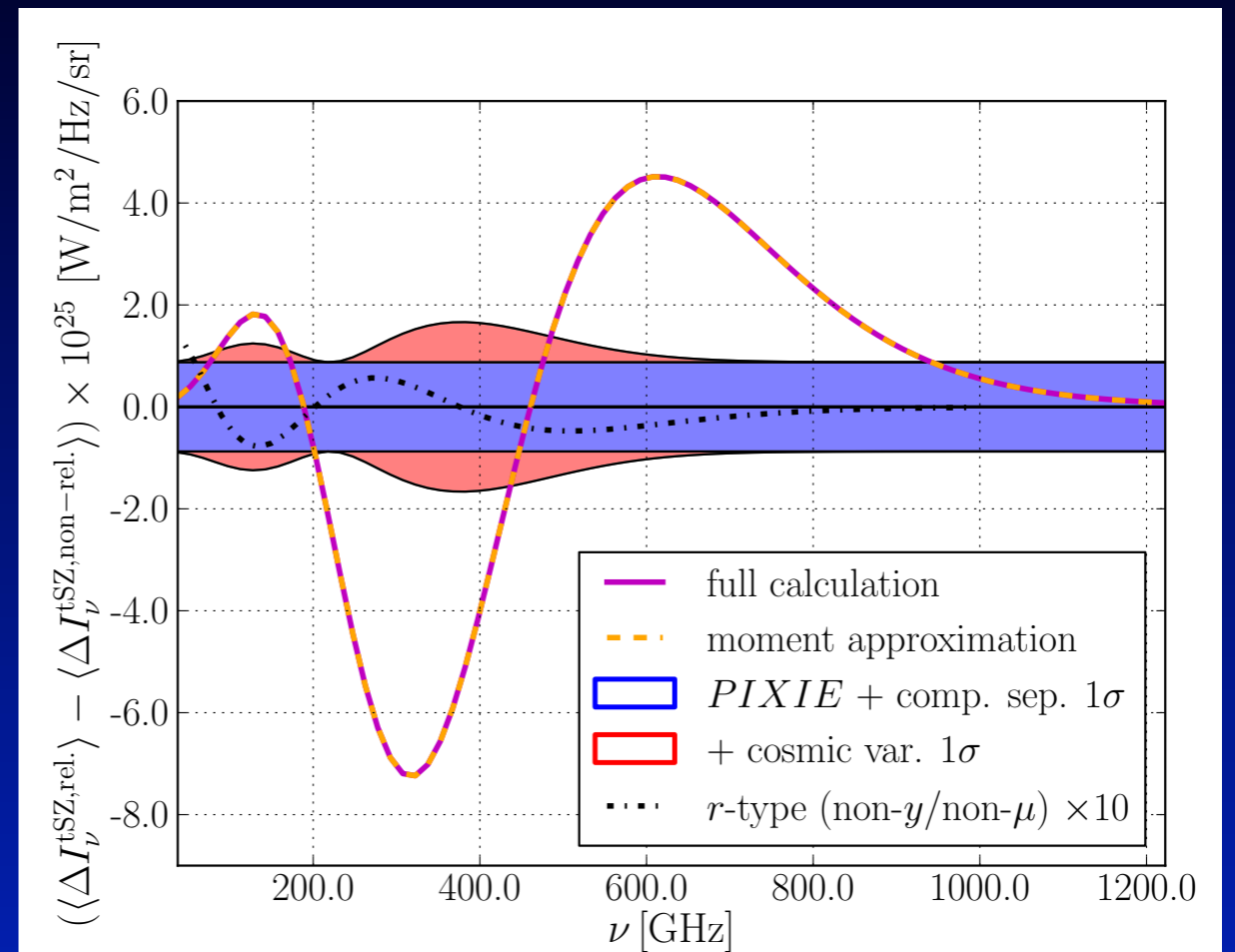
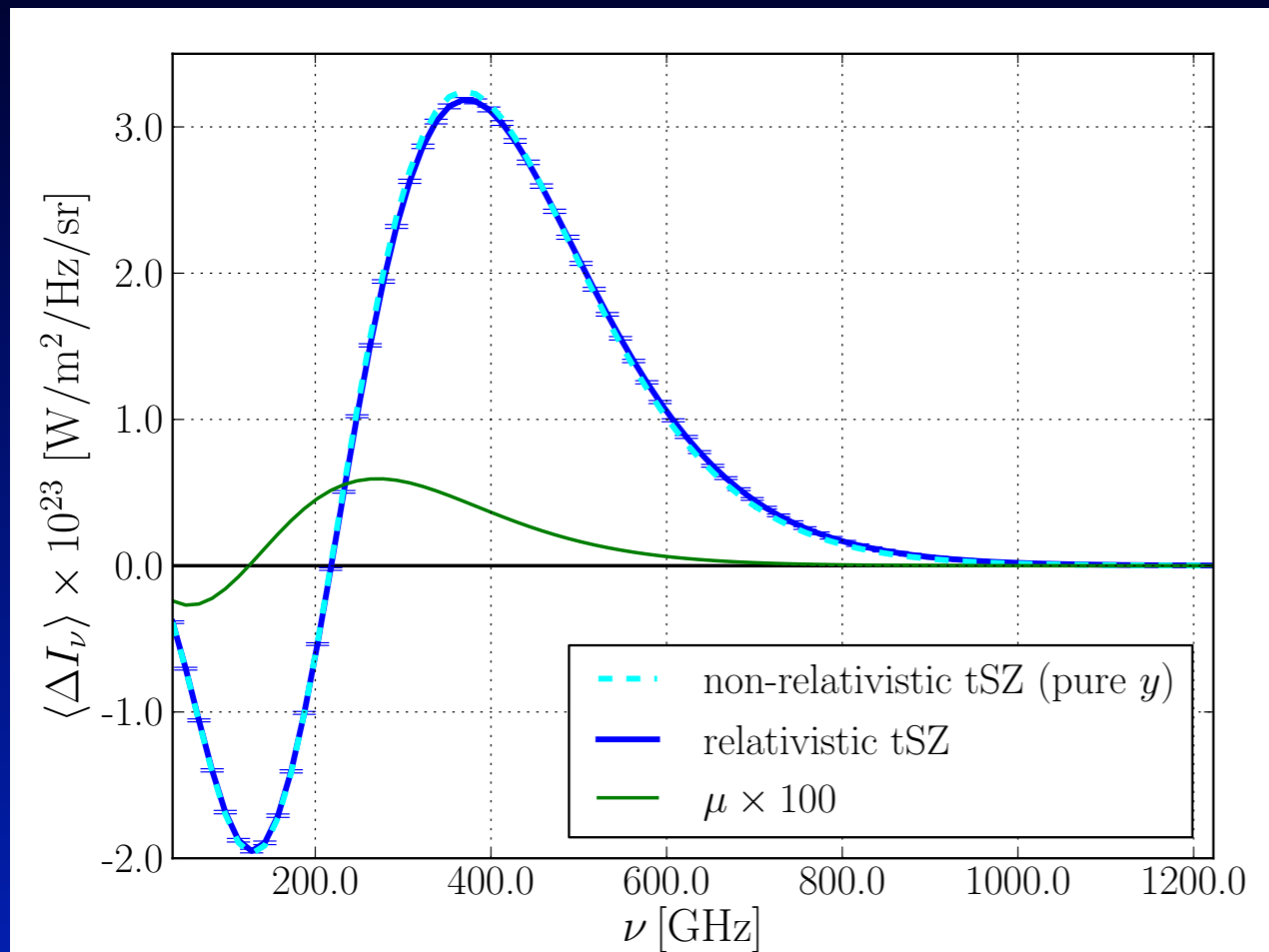


Distortion Green's function for energy release

Intensity signal for different heating redshifts

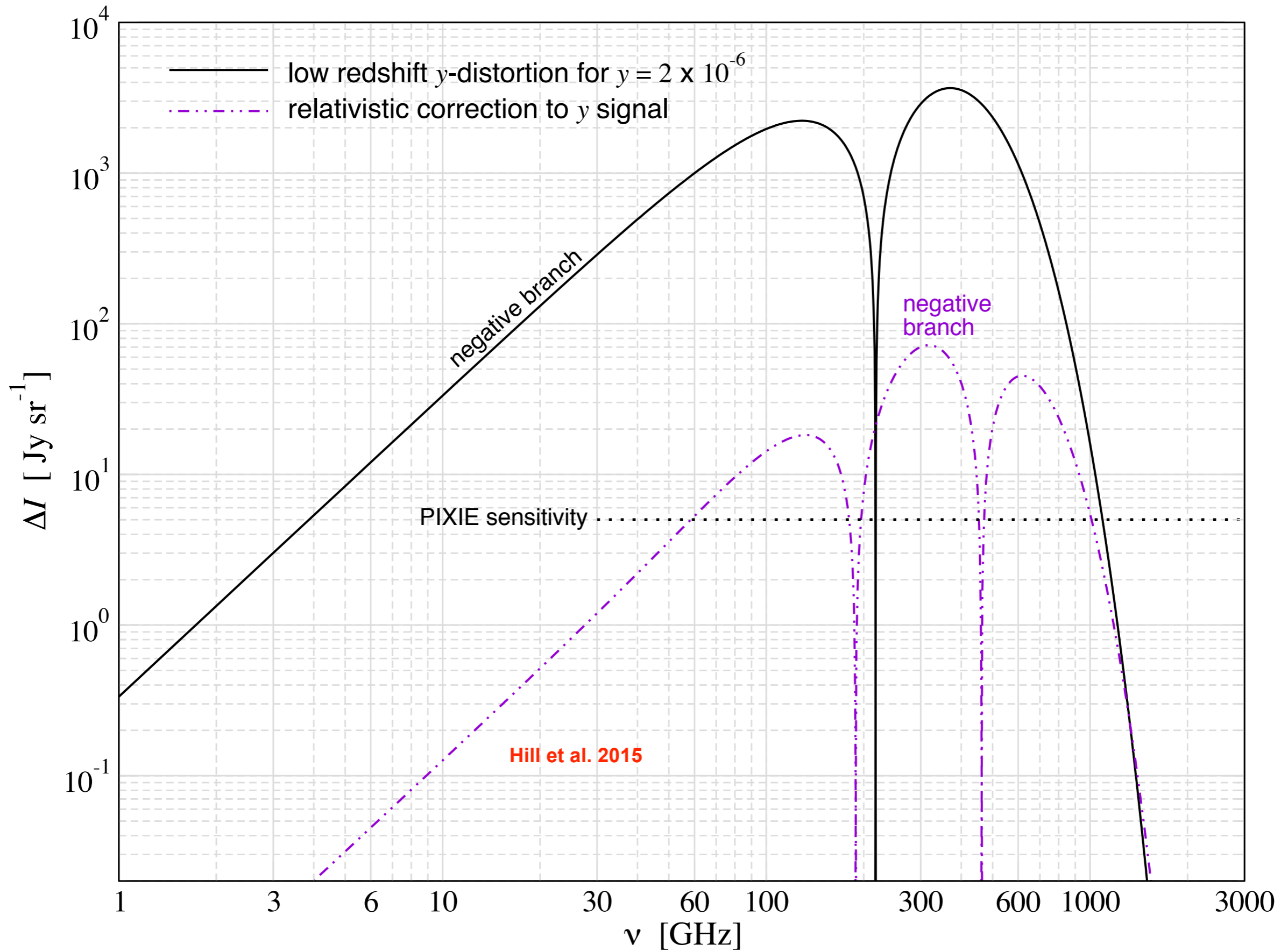


Taking the Universe's temperature

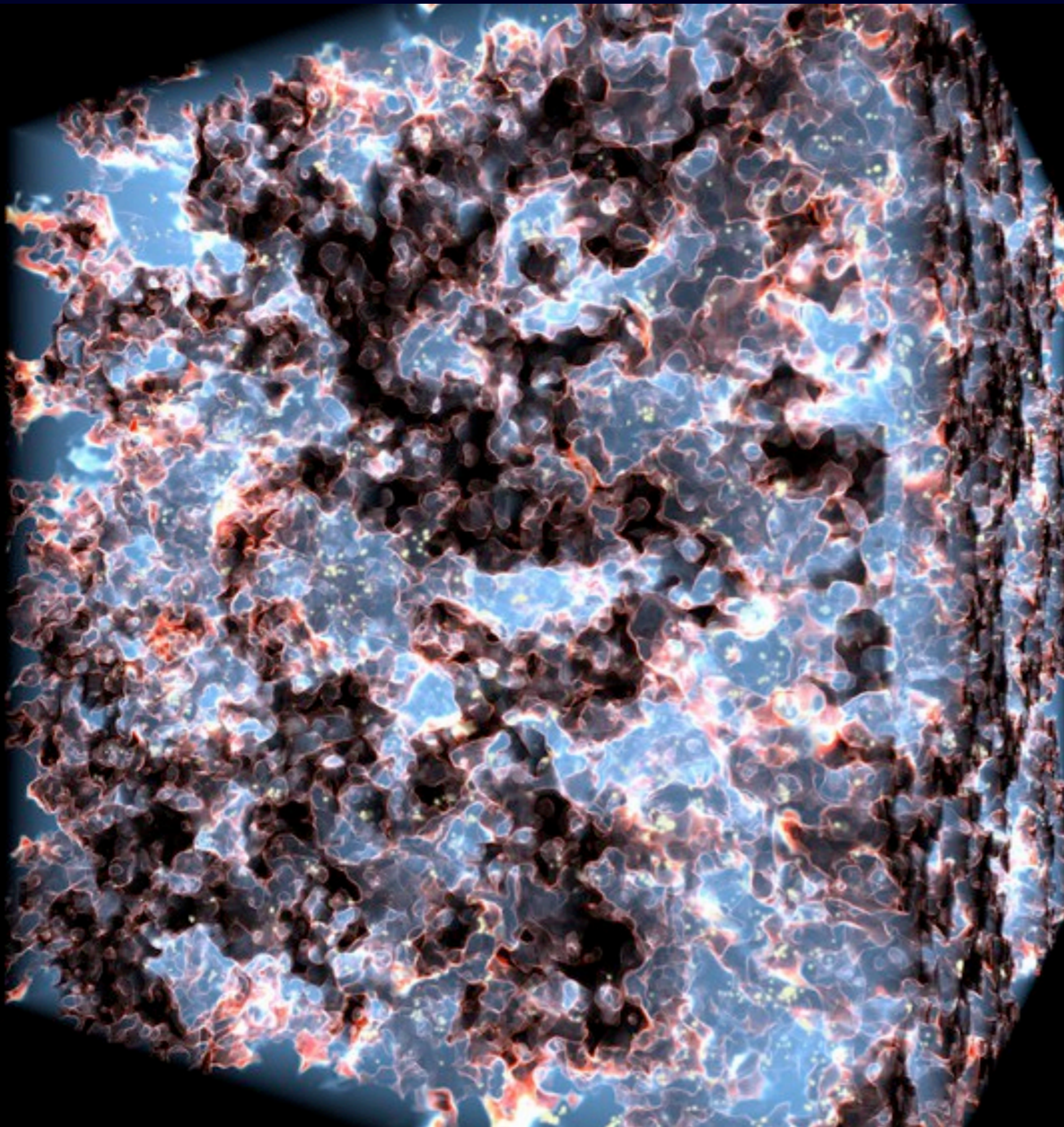


- $\langle y \rangle \simeq 1.8 \times 10^{-6}$ ($\sim 10\%$ from IGM and reionization rest from ICM)
- $> 1000 \sigma$ detection with PIXIE-type experiment
- optical depth-weighted temperature: $\langle kT_e \rangle_\tau \simeq 0.208 \text{ keV} (\equiv 2.4 \times 10^6 \text{ K})$
- $\sim 30 \sigma$ detection with PIXIE-type experiment

Average CMB spectral distortions



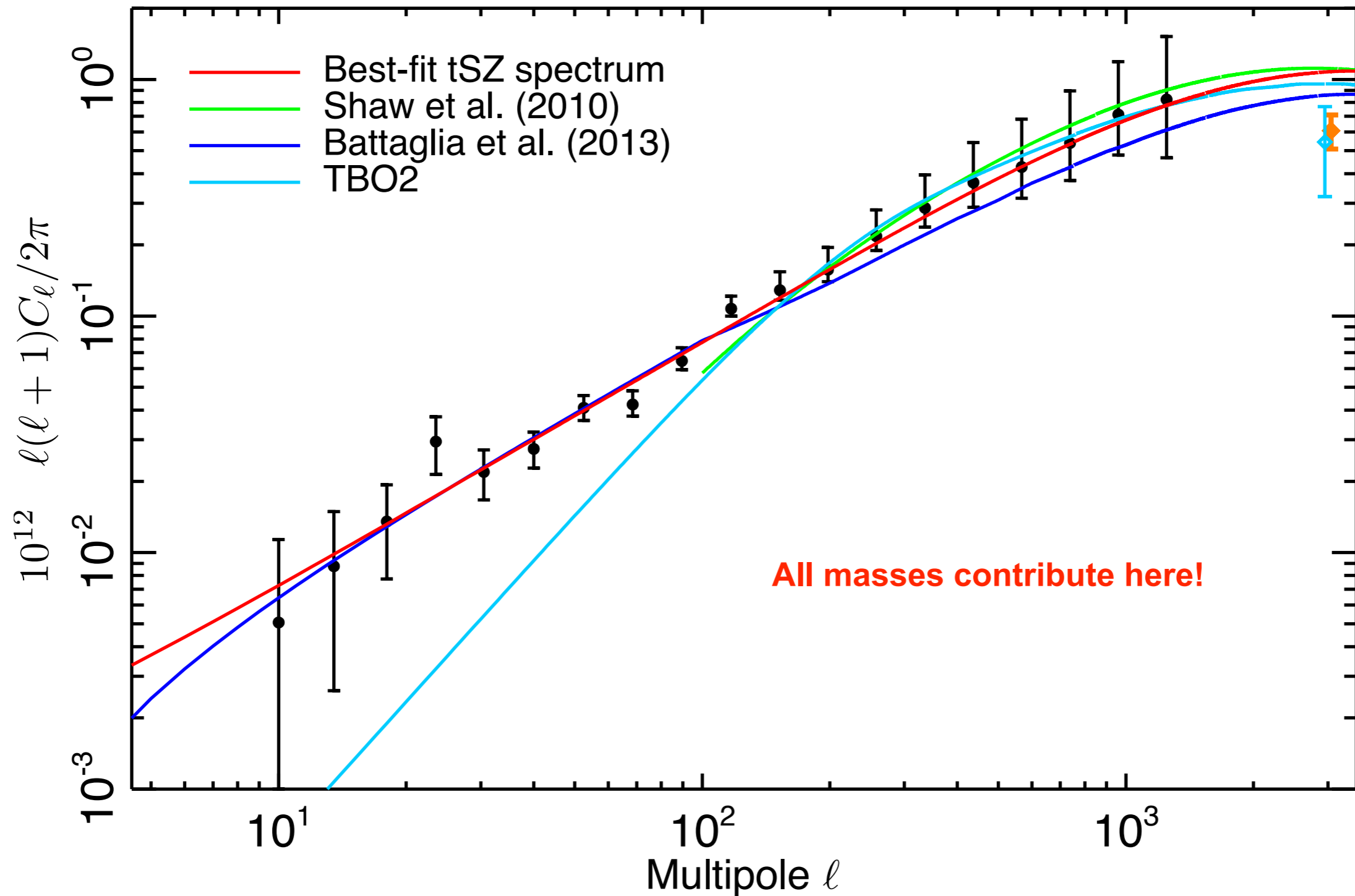
Fluctuations of the γ -parameter at large scales



- spatial variations of the optical depth and temperature cause small-spatial variations of the γ -parameter at different angular scales
- could tell us about the reionization sources and structure formation process
- additional independent piece of information!
- Cross-correlations with other signals

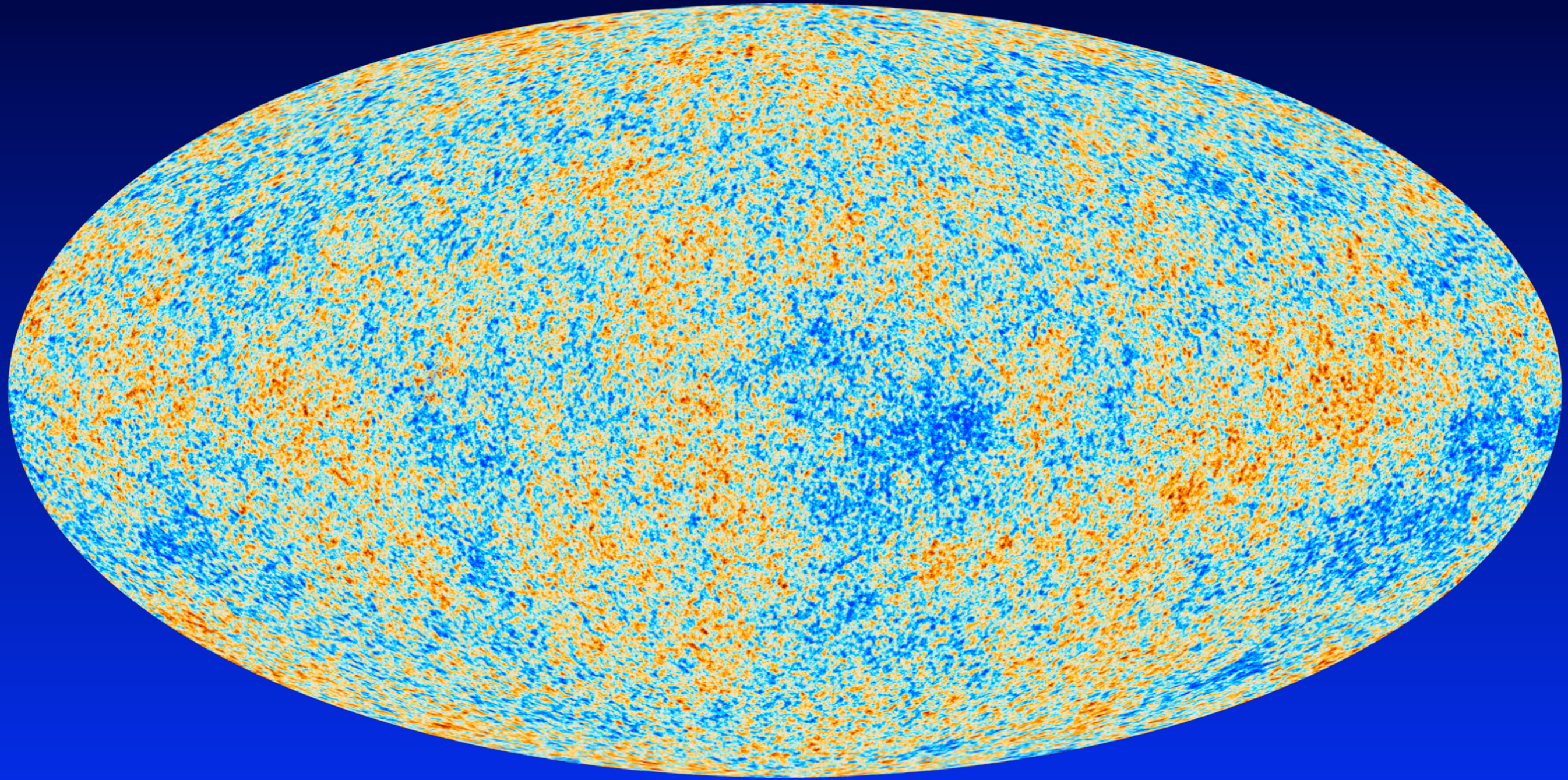
Example:
Simulation of reionization process
(1Gpc/h) by *Alvarez & Abel*

Measured power spectrum for y -parameter

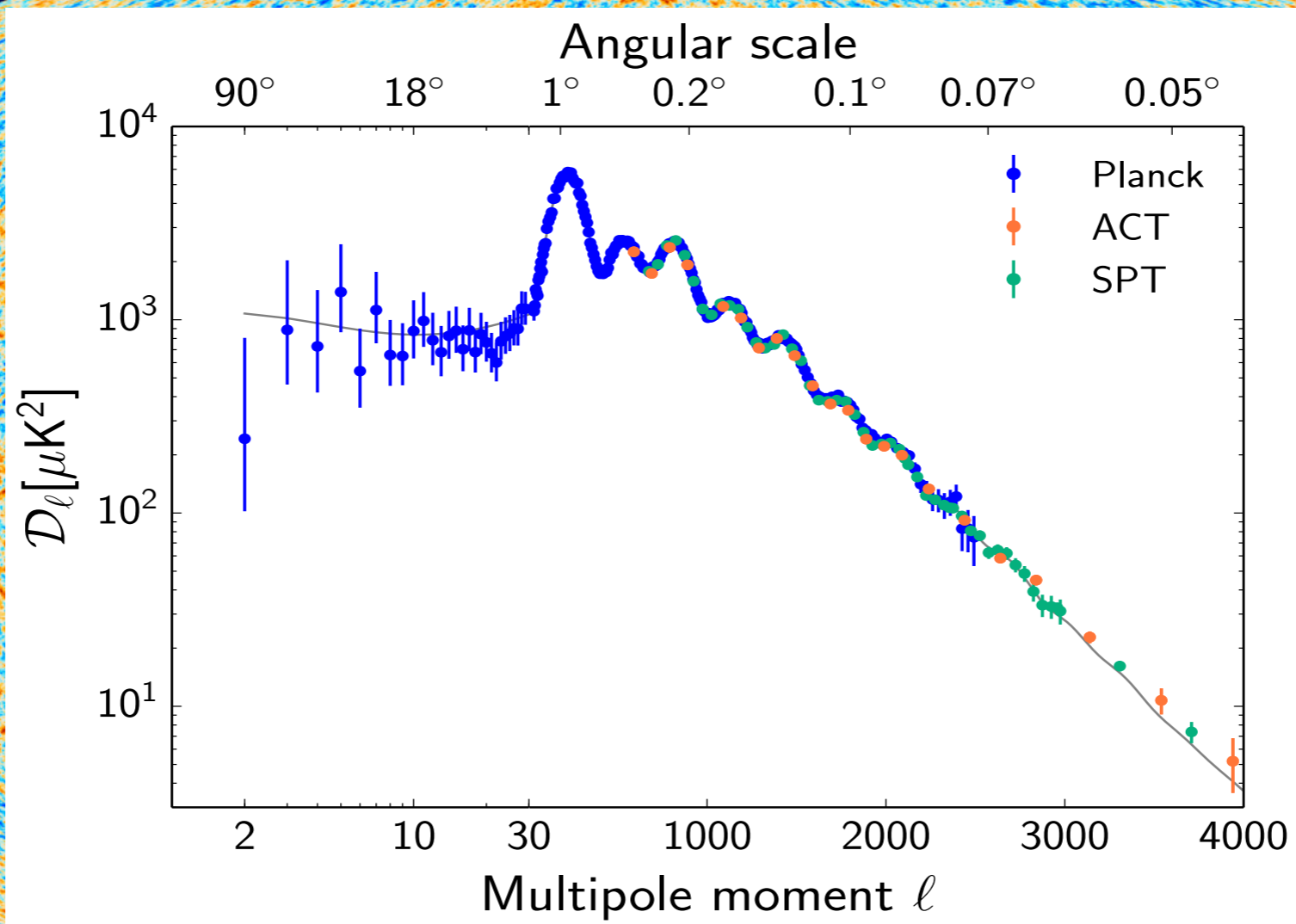


The dissipation of small-scale acoustic modes

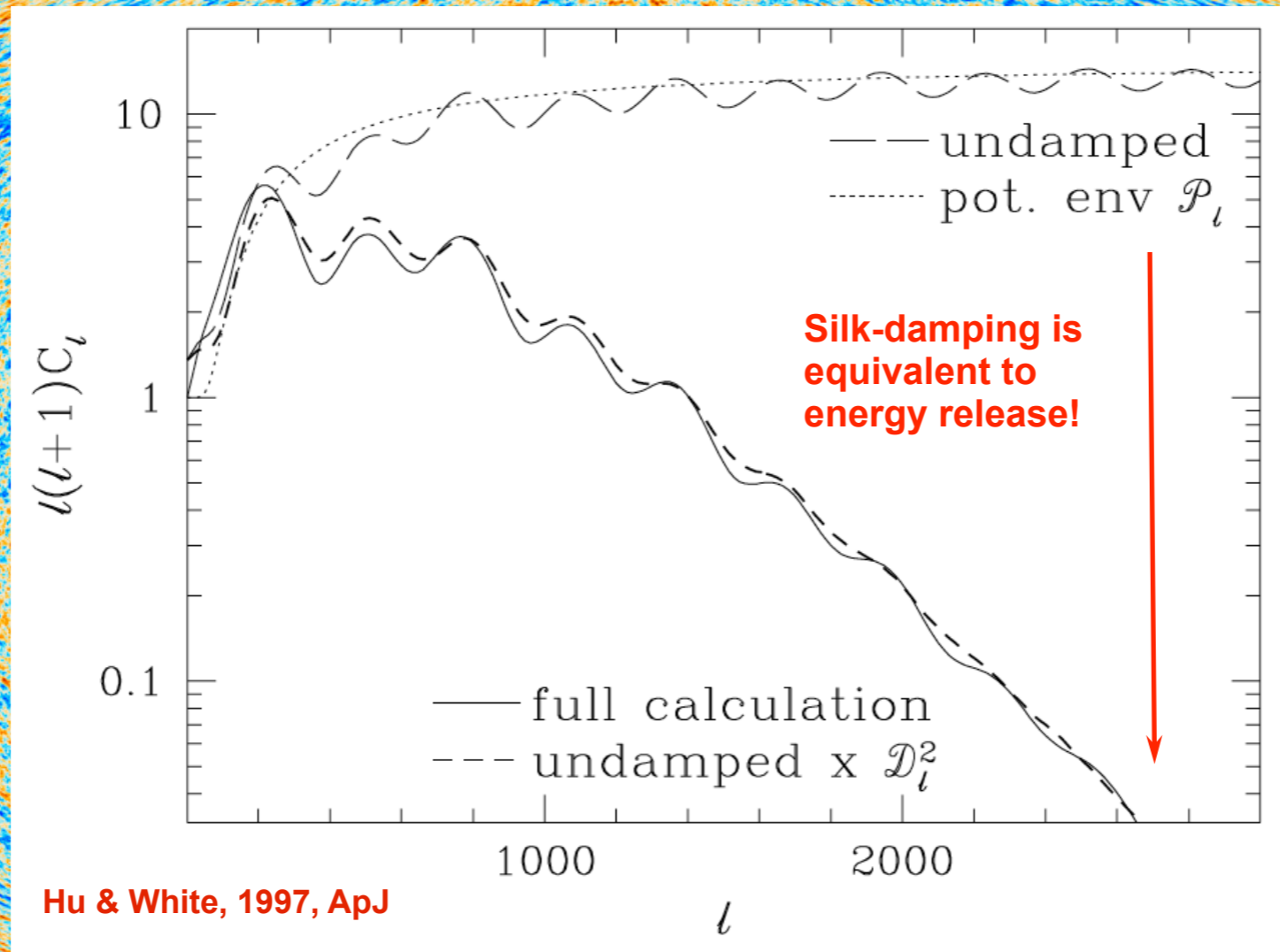
Dissipation of small-scale acoustic modes



Dissipation of small-scale acoustic modes



Dissipation of small-scale acoustic modes



Energy release caused by dissipation process

‘Obvious’ dependencies:

- *Amplitude* of the small-scale power spectrum
- *Shape* of the small-scale power spectrum
- *Dissipation scale* $\rightarrow k_D \sim (H_0 \Omega_{\text{rel}}^{1/2} N_{\text{e},0})^{1/2} (1+z)^{3/2}$ at early times

not so ‘obvious’ dependencies:

- *primordial non-Gaussianity* in the ultra squeezed limit
(Pajer & Zaldarriaga, 2012; Ganc & Komatsu, 2012)
- *Type* of the perturbations (adiabatic \leftrightarrow isocurvature)
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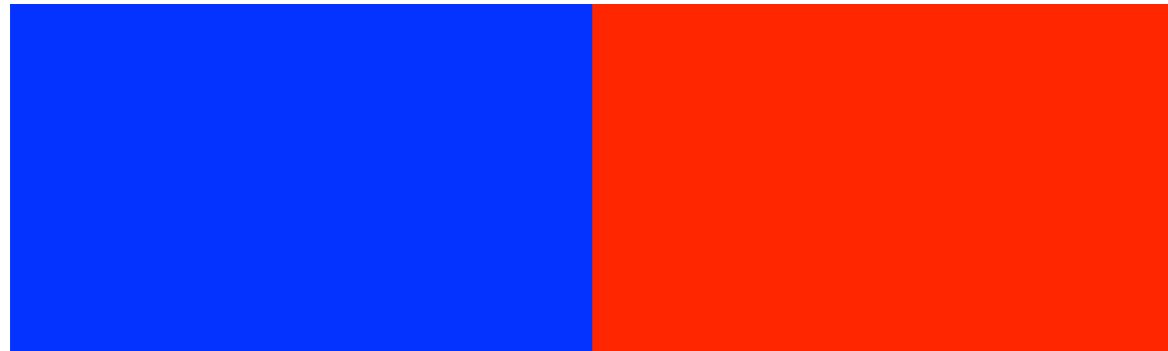
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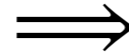
*CMB Spectral distortions could add additional numbers beyond
‘just’ the tensor-to-scalar ratio from B-modes!*

Distortion due to mixing of blackbodies

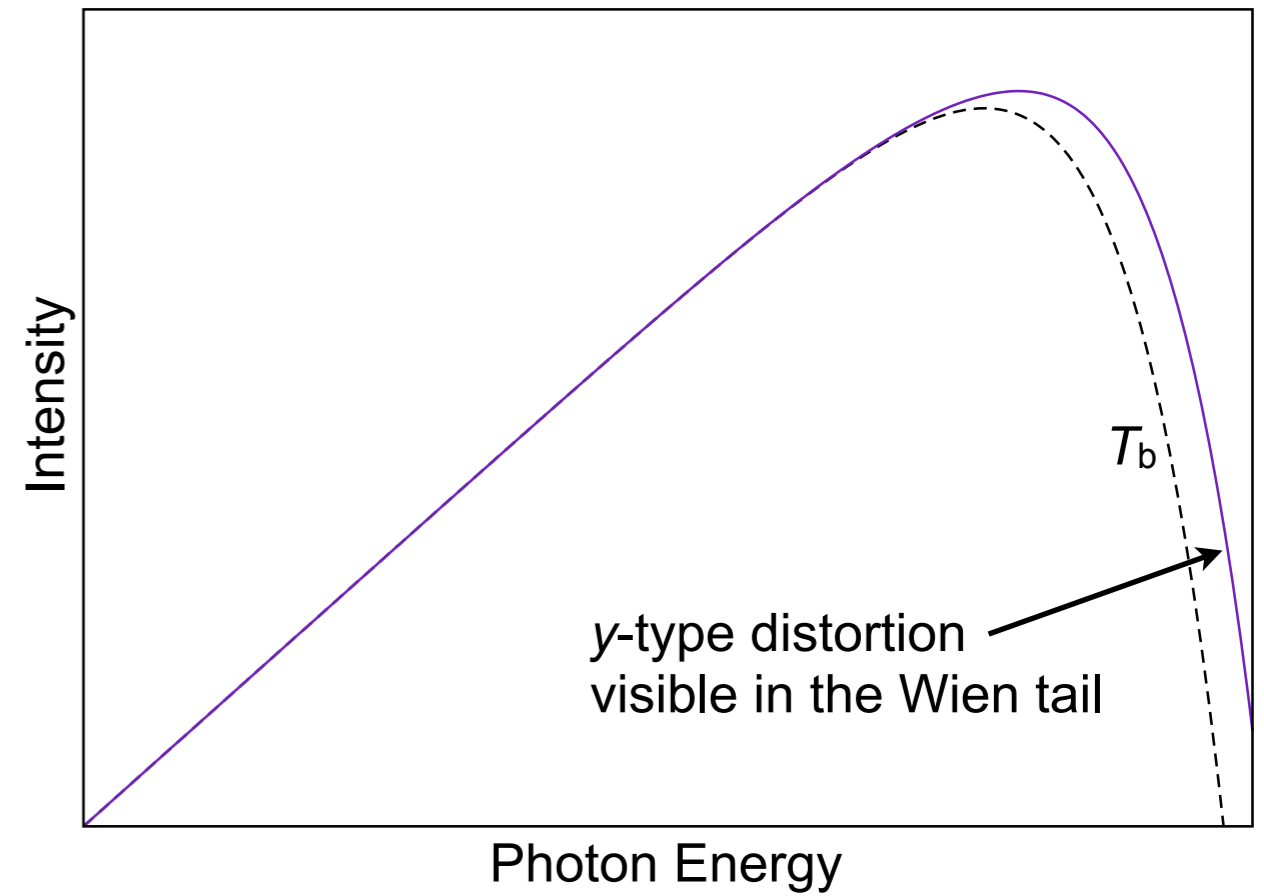
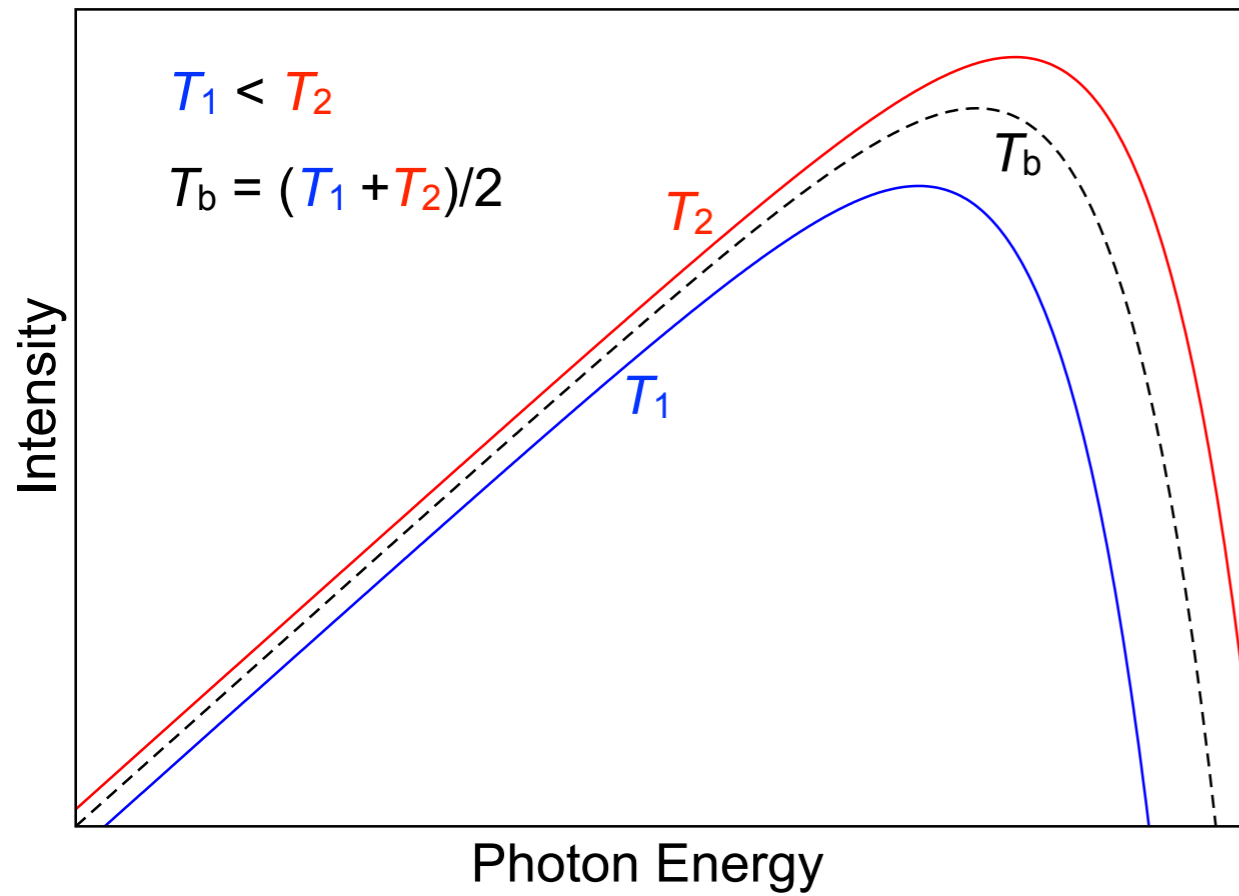
Blackbody spectra



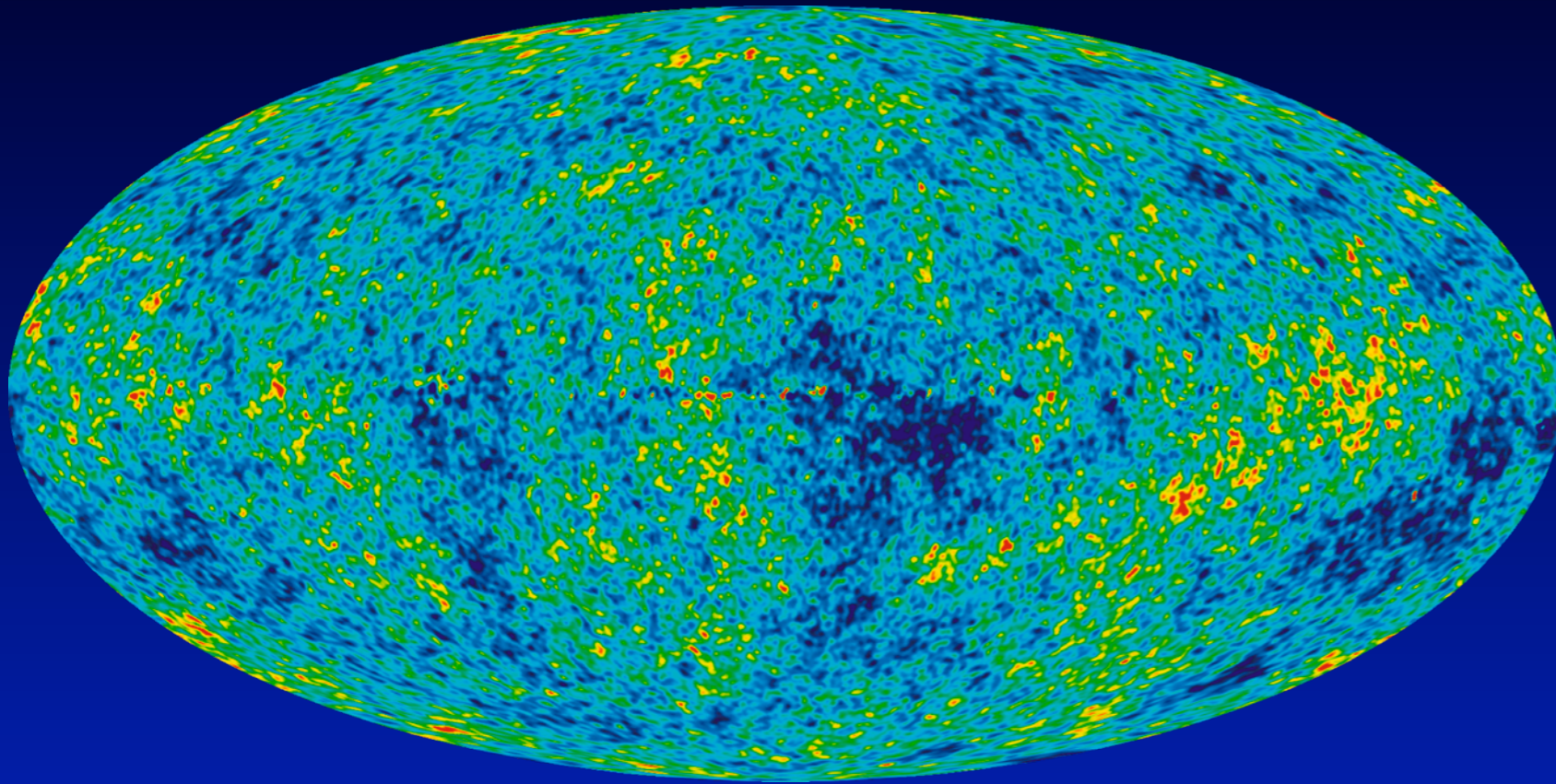
Photon mixing



Blackbody + y -distortion



Distortions caused by superposition of blackbodies



- average spectrum

$$\Rightarrow y \simeq \frac{1}{2} \left\langle \left(\frac{\Delta T}{T} \right)^2 \right\rangle \approx 8 \times 10^{-10}$$

$$\Delta T_{\text{sup}} \simeq T \left\langle \left(\frac{\Delta T}{T} \right)^2 \right\rangle \approx 4.4 \text{ nK}$$

- known with very high precision

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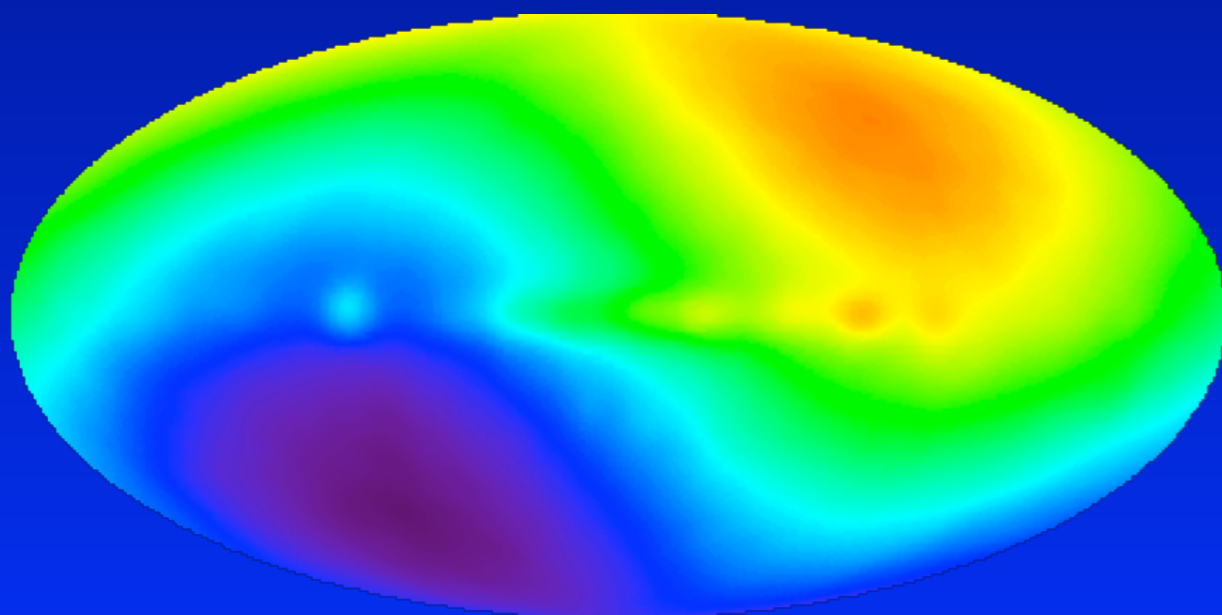
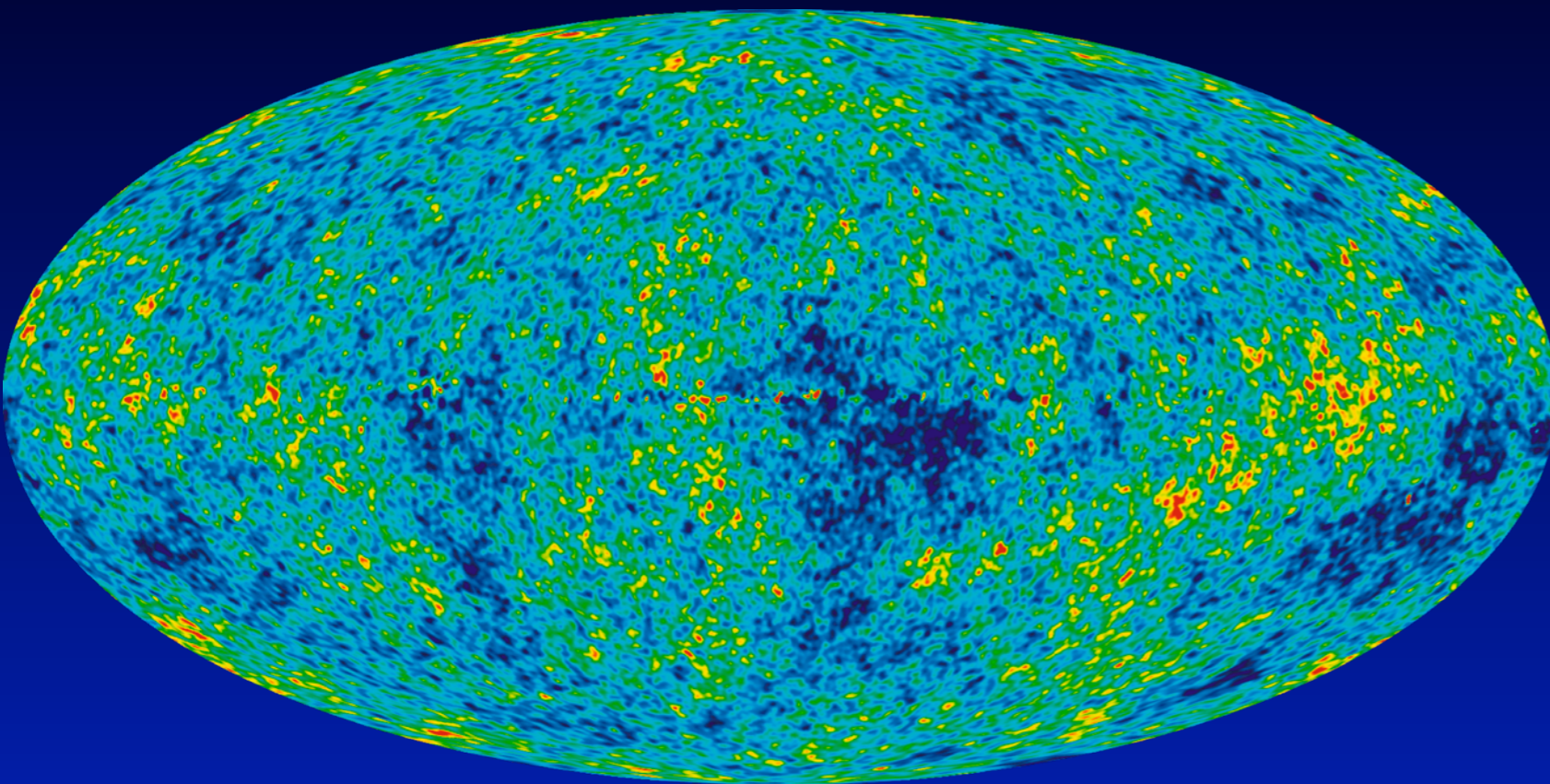
- known with very high precision

- CMB dipole ($\beta \sim 1.23 \times 10^{-3}$)

$$\Rightarrow y = \frac{\beta^2}{6} \approx (2.525 \pm 0.012) \times 10^{-7}$$

$$\Delta T_{\text{sup}} \simeq T \frac{\beta_c^2}{3} \approx 1.4 \mu\text{K}$$

- electrons are up-scattered
- can (and should) be taken out down to the level of $y \sim 10^{-9}$



How do we compute the effective heating rate?

Dissipation of acoustic modes: 'classical treatment'

- energy stored in plane sound waves

$$\text{Landau \& Lifshitz, 'Fluid Mechanics', \S 65} \Rightarrow Q \sim c_s^2 \rho (\delta\rho/\rho)^2$$

- expression for normal ideal gas where ρ is '*mass density*' and c_s denotes '*sounds speed*'

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- photon-baryon fluid with baryon loading $R \ll 1$

$$(c_s/c)^2 = [3(1+R)]^{-1} \sim 1/3$$

$$\rho \rightarrow \rho_Y = a_R T^4$$

$$\delta\rho/\rho \rightarrow 4(\delta T_0/T) \equiv 4\Theta_0 \leftarrow \text{only perturbation in the monopole accounted for}$$

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$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt = -16/3 d\langle \Theta_0^2 \rangle / dt$$

'minus' because *decrease* of Θ at small scales means *increase* for average spectrum

can be calculated using first order perturbation theory

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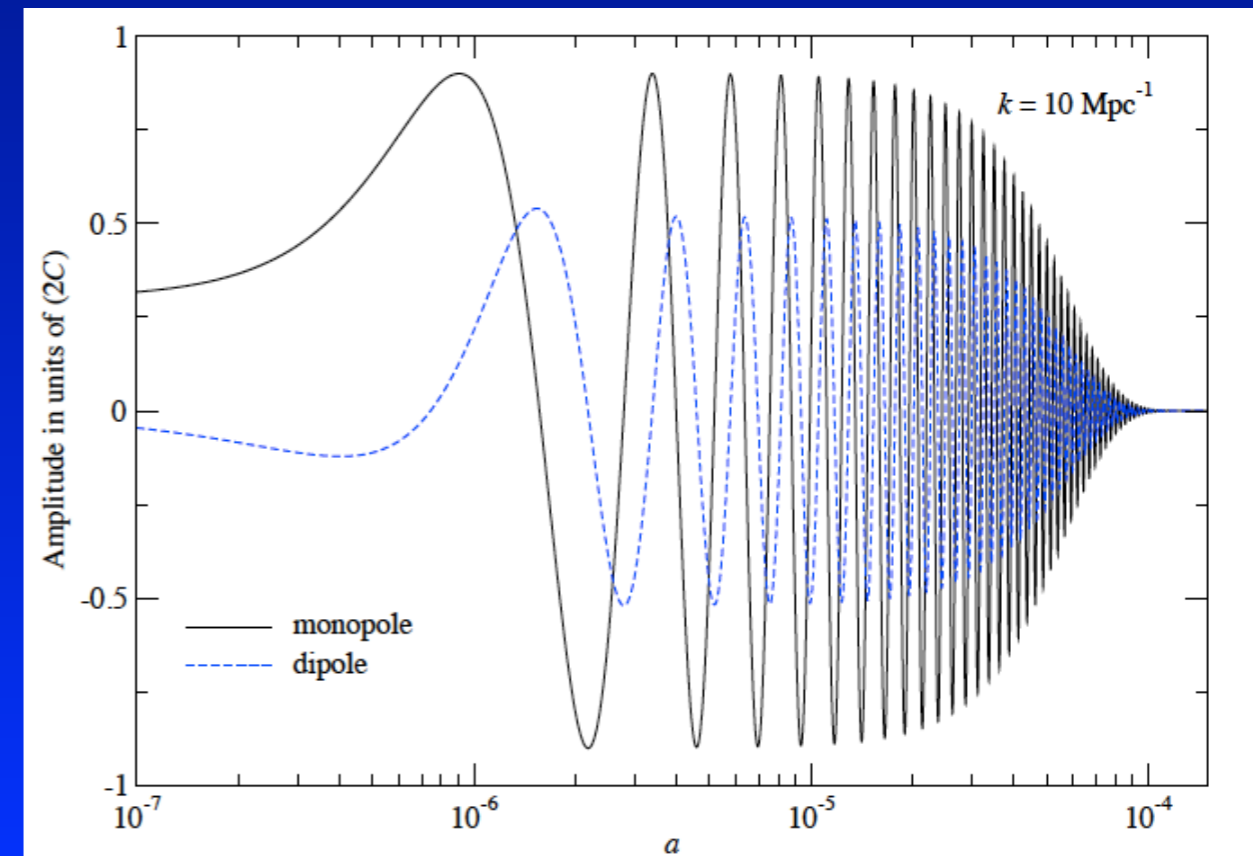
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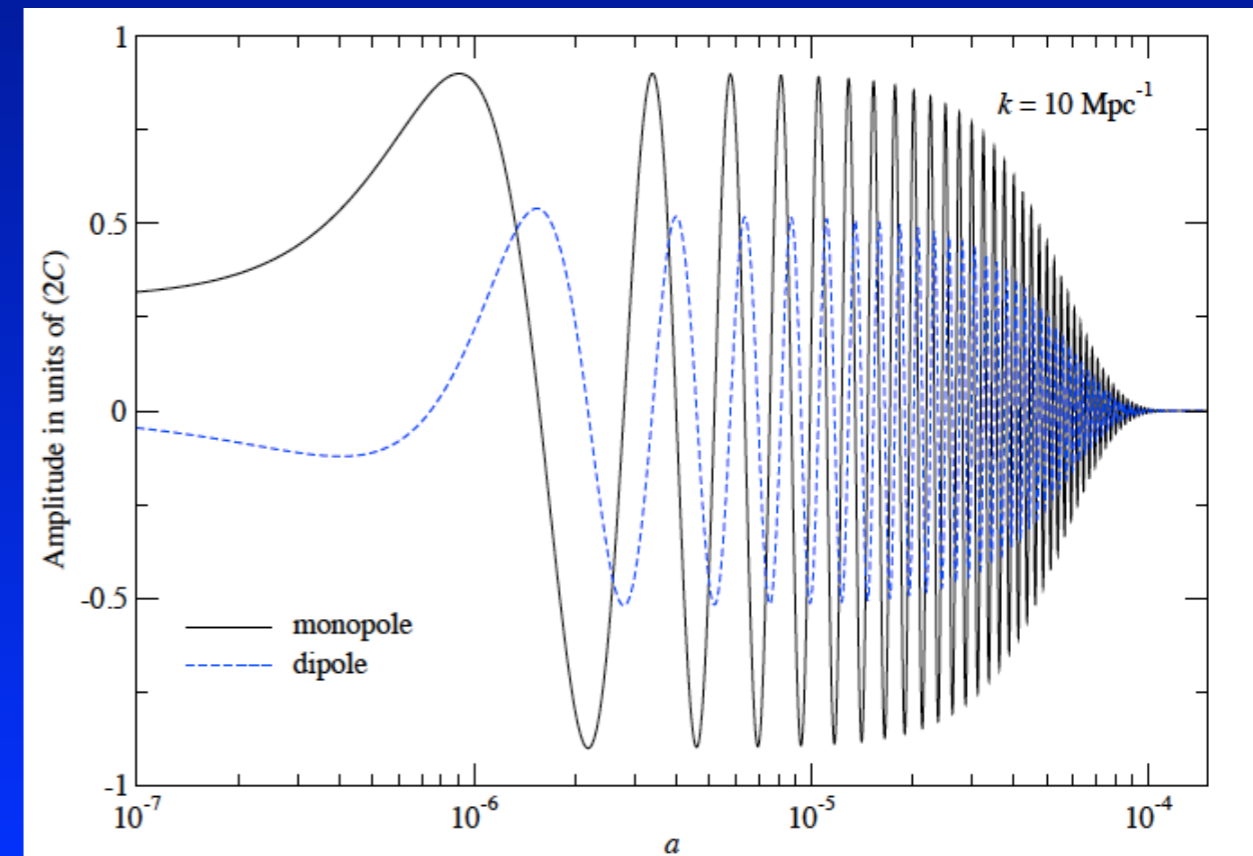
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$$\delta\rho/\rho \rightarrow 4(\delta T_0/T) \equiv 4\Theta_0$$

- Simple estimate does *not* capture all the physics of the problem:

- ▶ *total energy release is 9/4 ~ 2.25 times larger!*
- ▶ *only 1/3 of the released energy goes into distortions (follows from superposition of blackbodies...)*



Early power spectrum constraints from FIRAS

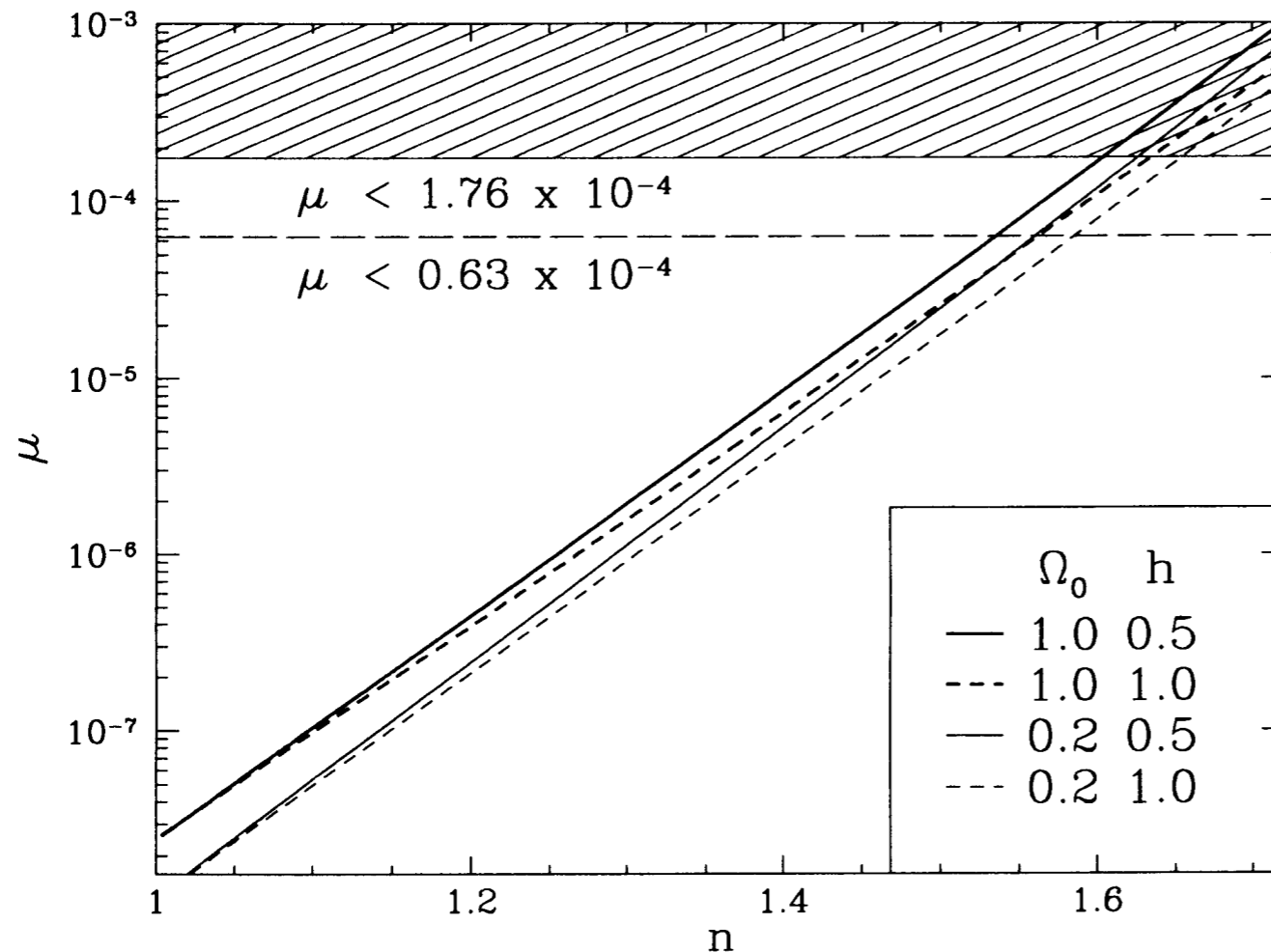


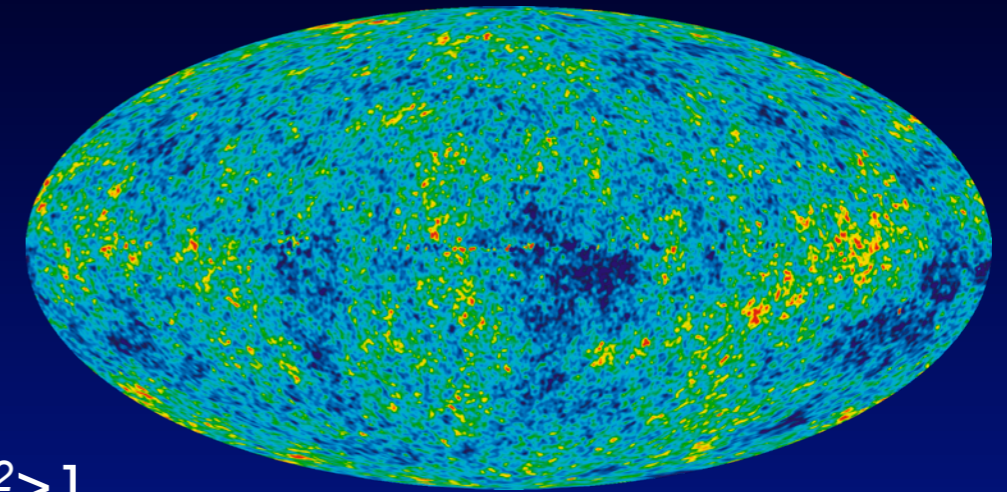
FIG. 1.—Spectral distortion μ , predicted from the full eq. (11), as a function of the power index n for a normalization at the mean of the *COBE* DMR detection $(\Delta T/T)_{10^\circ} = 1.12 \times 10^{-5}$. With the uncertainties on *both* the DMR and FIRAS measurements, the conservative 95% upper limit is effectively $\mu < 1.76 \times 10^{-4}$ (see text). The corresponding constraint on n is relatively weakly dependent on cosmological parameters: $n < 1.60$ ($h = 0.5$) and $n < 1.63$ ($h = 1.0$) for $\Omega_0 = 1$ and quite similar for $0.2 < \Omega_0 = 1 - \Omega_\Lambda < 1$ universes. These limits are nearly independent of Ω_B . We have also plotted the optimistic 95% upper limit on $\mu < 0.63 \times 10^{-4}$ for comparison as discussed in the text.

- based on classical estimate for heating rate
- Tightest / cleanest constraint at that point!
- simple power-law spectrum assumed
- $\mu \sim 10^{-8}$ for scale-invariant power spectrum
- $n_s \lesssim 1.6$

Dissipation of acoustic modes: 'microscopic picture'

- after inflation: photon field has spatially varying temperature T
- average energy stored in photon field at any given moment

$$\langle \rho_\gamma \rangle = a_R \langle T^4 \rangle \approx a_R \langle T \rangle^4 [1 + \underbrace{4\langle \Theta \rangle}_{=0} + 6\langle \Theta^2 \rangle]$$



E.g., our snapshot at $z=0$

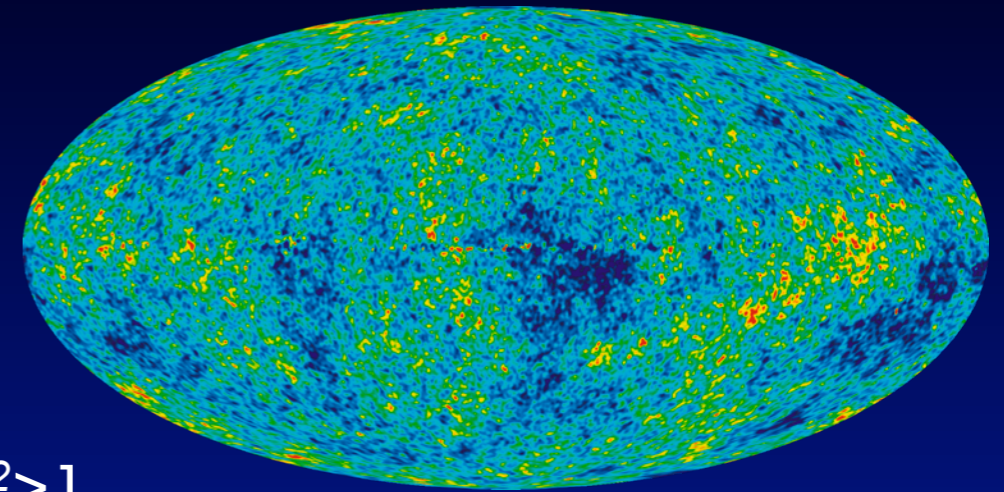
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$$\Rightarrow (a^4 \rho_\gamma)^{-1} da^4 Q_{ac}/dt = -6 d\langle \Theta^2 \rangle/dt$$

- Monopole actually **drops** out of the equation!
- In principle **all** higher multipoles contribute to the energy release



E.g., our snapshot at $z=0$

Dissipation of acoustic modes: 'microscopic picture'

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$$\langle \rho_Y \rangle = a_R \langle T^4 \rangle \approx a_R \langle T \rangle^4 [1 + 4\langle \Theta \rangle + 6\langle \Theta^2 \rangle]_{\Theta=0}$$

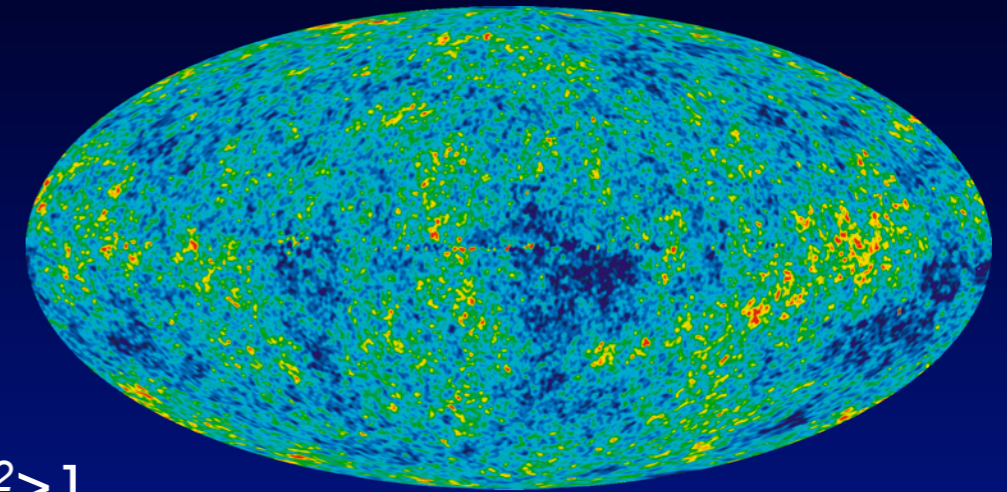
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- At high redshifts ($z \geq 10^4$):

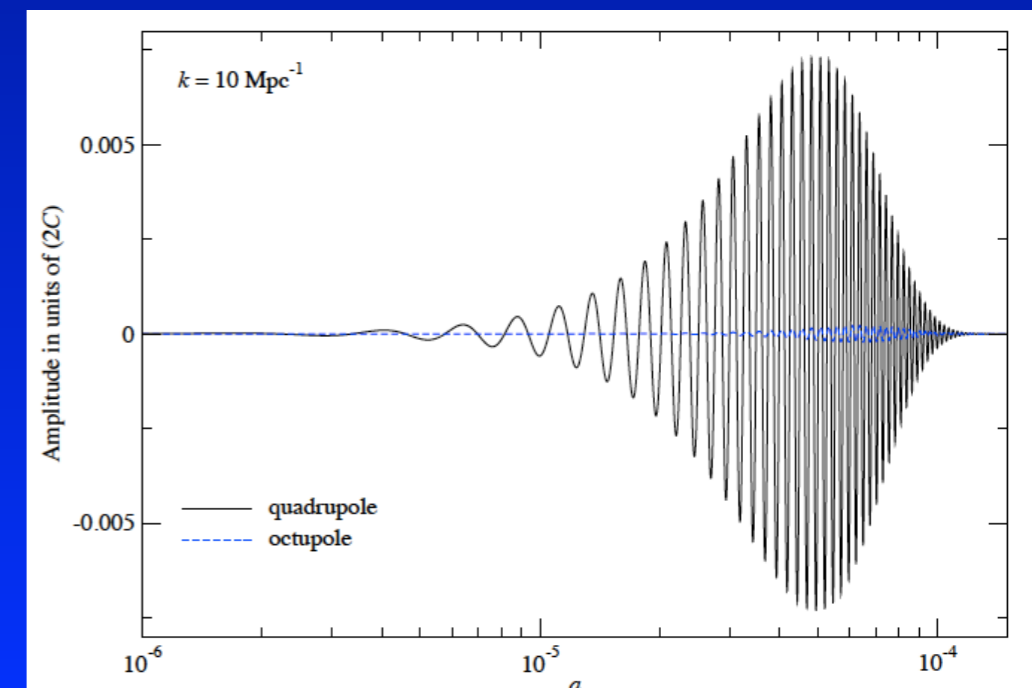
- ▶ *net (gauge-invariant) dipole and contributions from higher multipoles are negligible*
- ▶ *dominant term caused by quadrupole anisotropy*

$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt \approx -12 d\langle \Theta_0^2 \rangle/dt$$

9/4 larger than classical estimate



E.g., our snapshot at $z=0$



Effective energy release caused by damping effect

- Effective heating rate from full 2x2 Boltzmann treatment (JC, Khatri & Sunyaev, 2012)

$$\frac{1}{a^4 \rho_\gamma} \frac{da^4 Q_{ac}}{dt} = 4\sigma_T N_e c \left\langle \frac{(3\Theta_1 - \beta)^2}{3} + \frac{9}{2}\Theta_2^2 - \frac{1}{2}\Theta_2(\Theta_0^P + \Theta_2^P) + \sum_{l \geq 3} (2l + 1)\Theta_l^2 \right\rangle$$

$$\Theta_l = \frac{1}{2} \int \Theta(\mu) P_l(\mu) d\mu$$

gauge-independent dipole

effect of polarization

higher multipoles

$$\langle XY \rangle = \int \frac{k^2 dk}{2\pi^2} P(k) X(k) Y(k)$$

Primordial power spectrum

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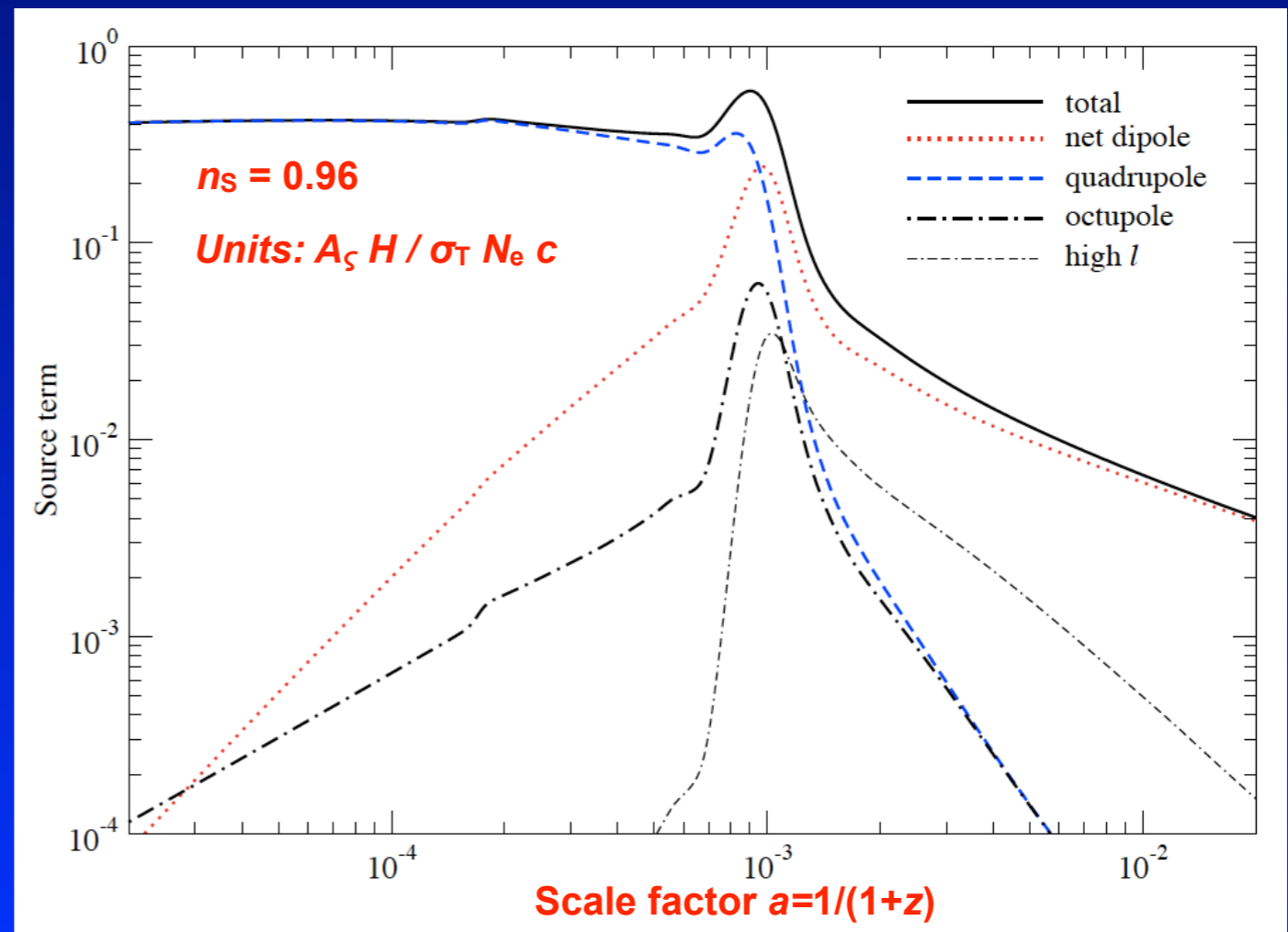
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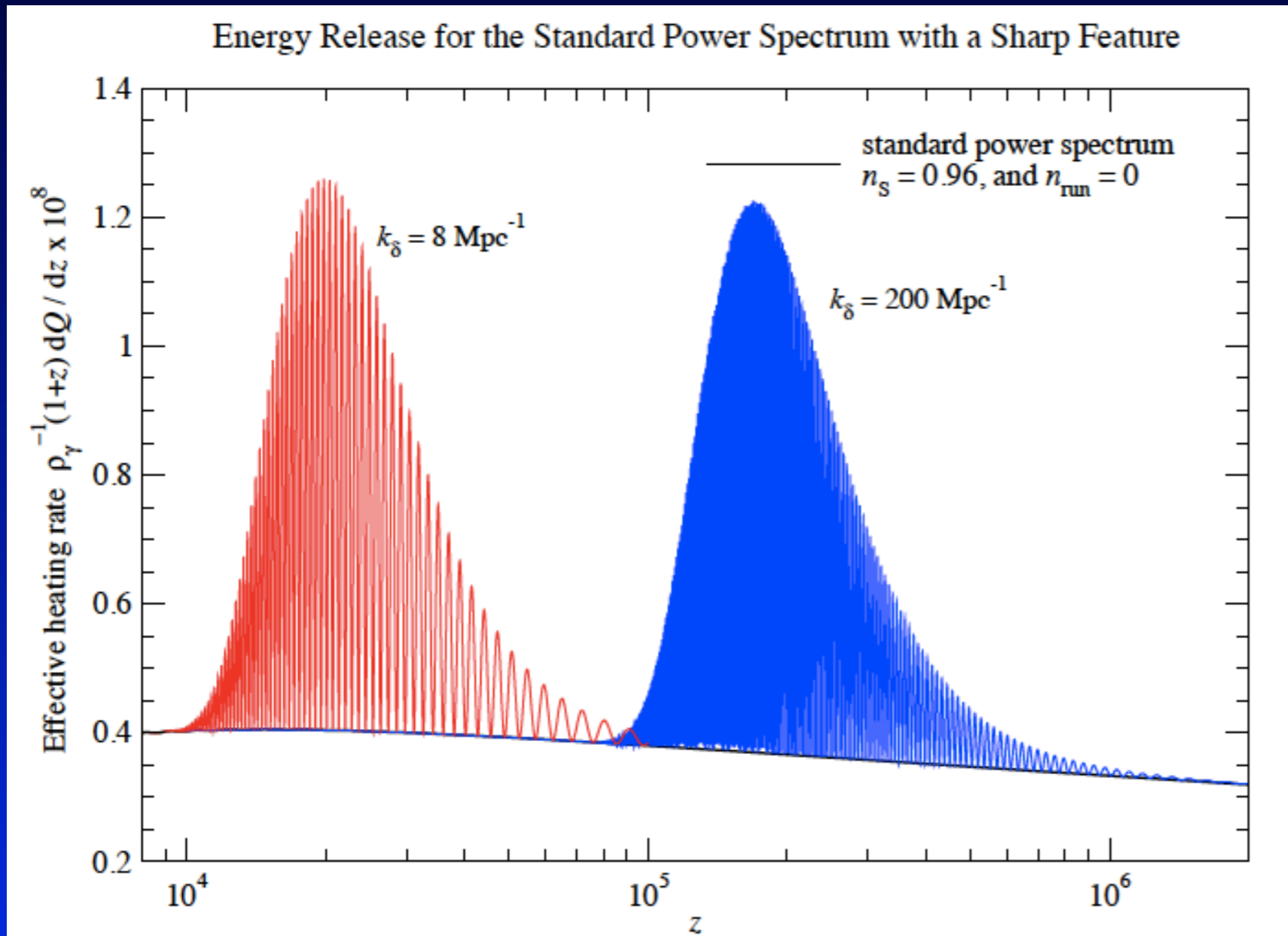
$$\langle XY \rangle = \int \frac{k^2 dk}{2\pi^2} P(k) X(k) Y(k)$$

Primordial power spectrum

- quadrupole dominant at high z
- net dipole important only at low redshifts
- polarization $\sim 5\%$ effect
- contribution from higher multipoles rather small



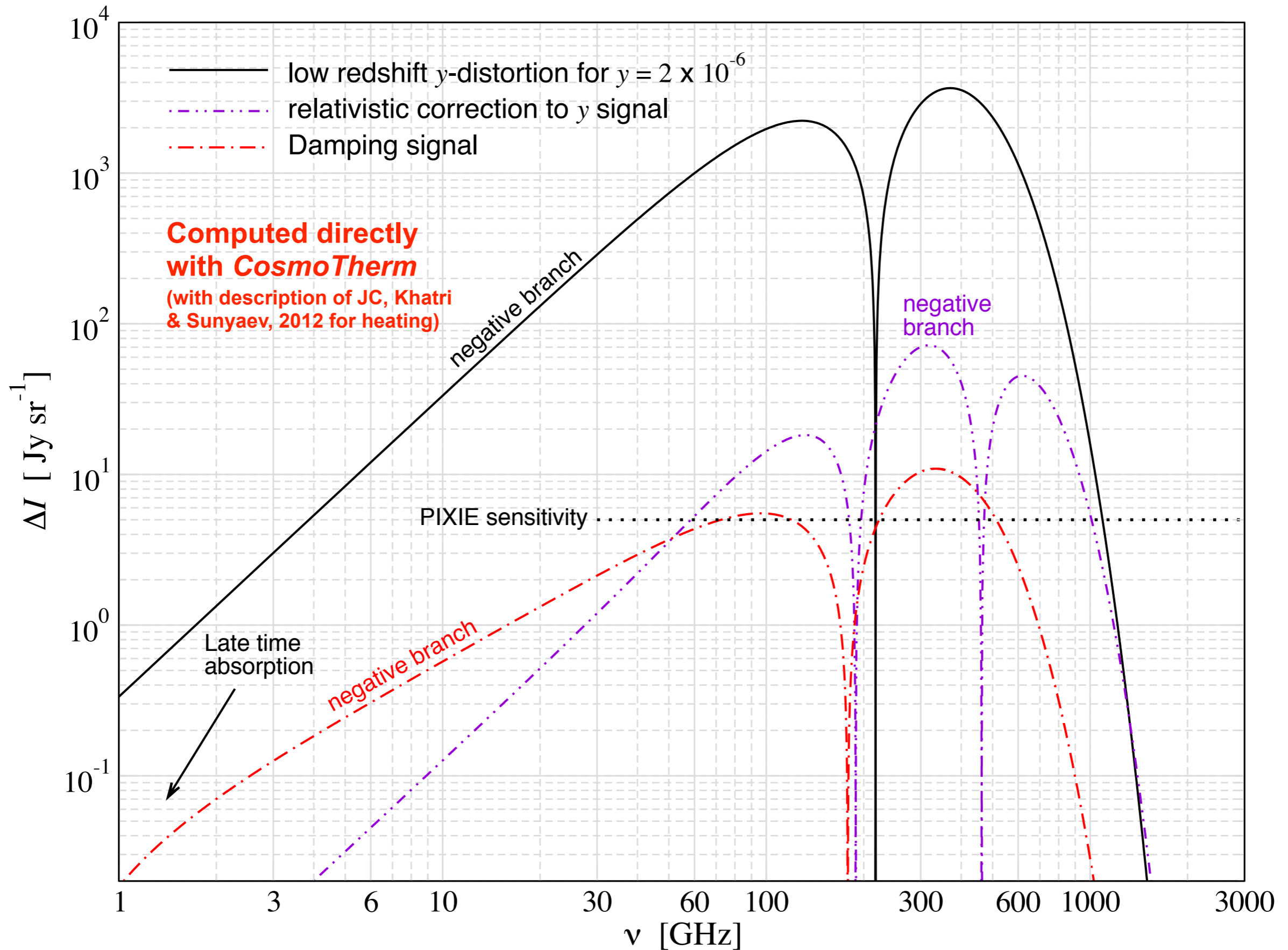
Which modes dissipate in the μ and y -eras?



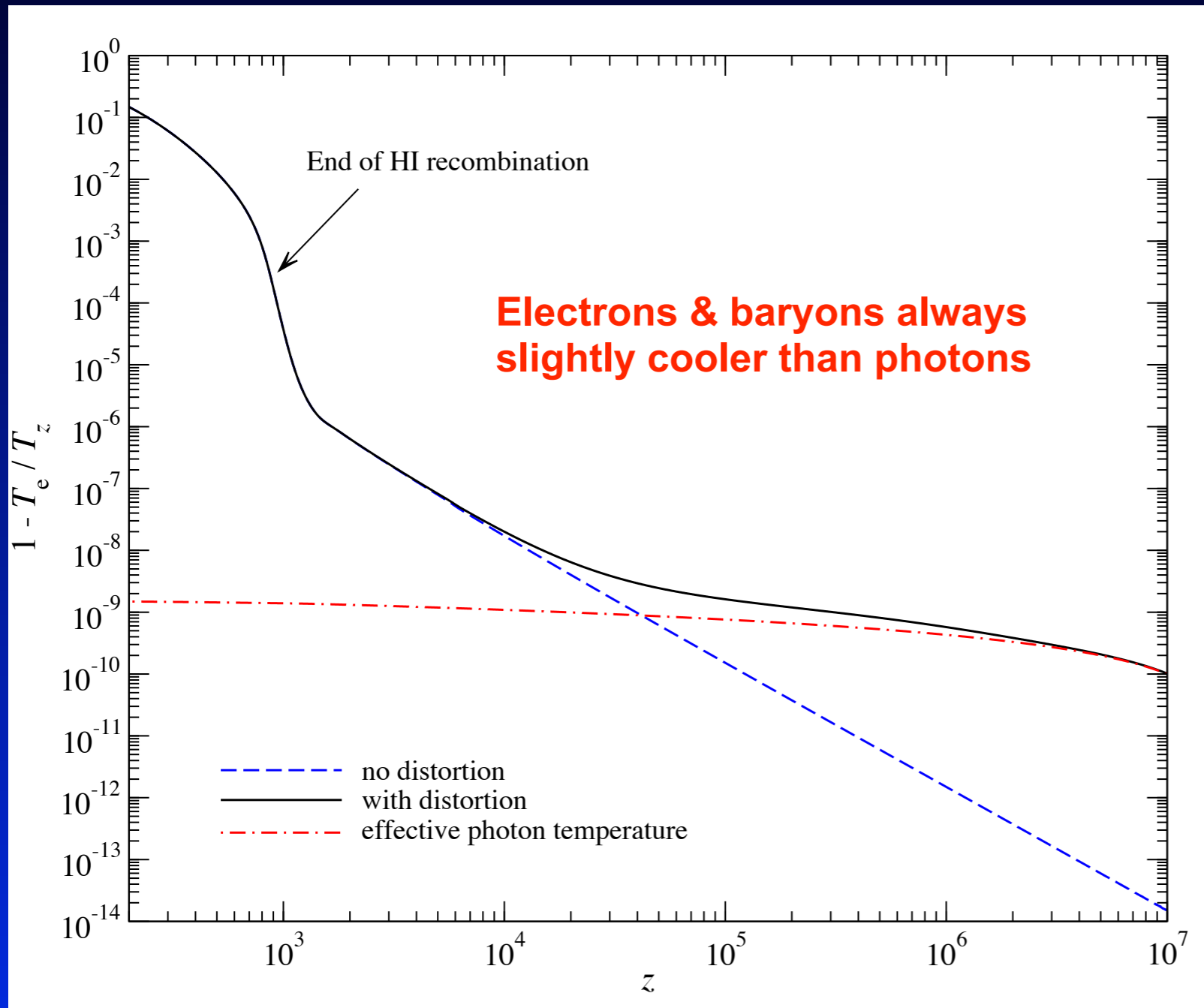
- Single mode with wavenumber k dissipates its energy at $z_d \sim 4.5 \times 10^5 (k \text{ Mpc}/10^3)^{2/3}$
- Modes with wavenumber $50 \text{ Mpc}^{-1} < k < 10^4 \text{ Mpc}^{-1}$ dissipate their energy during the μ -era
- Modes with $k < 50 \text{ Mpc}^{-1}$ cause y -distortion

So what does one expect within Λ CDM?

Average CMB spectral distortions



Spectral distortion caused by the cooling of ordinary matter



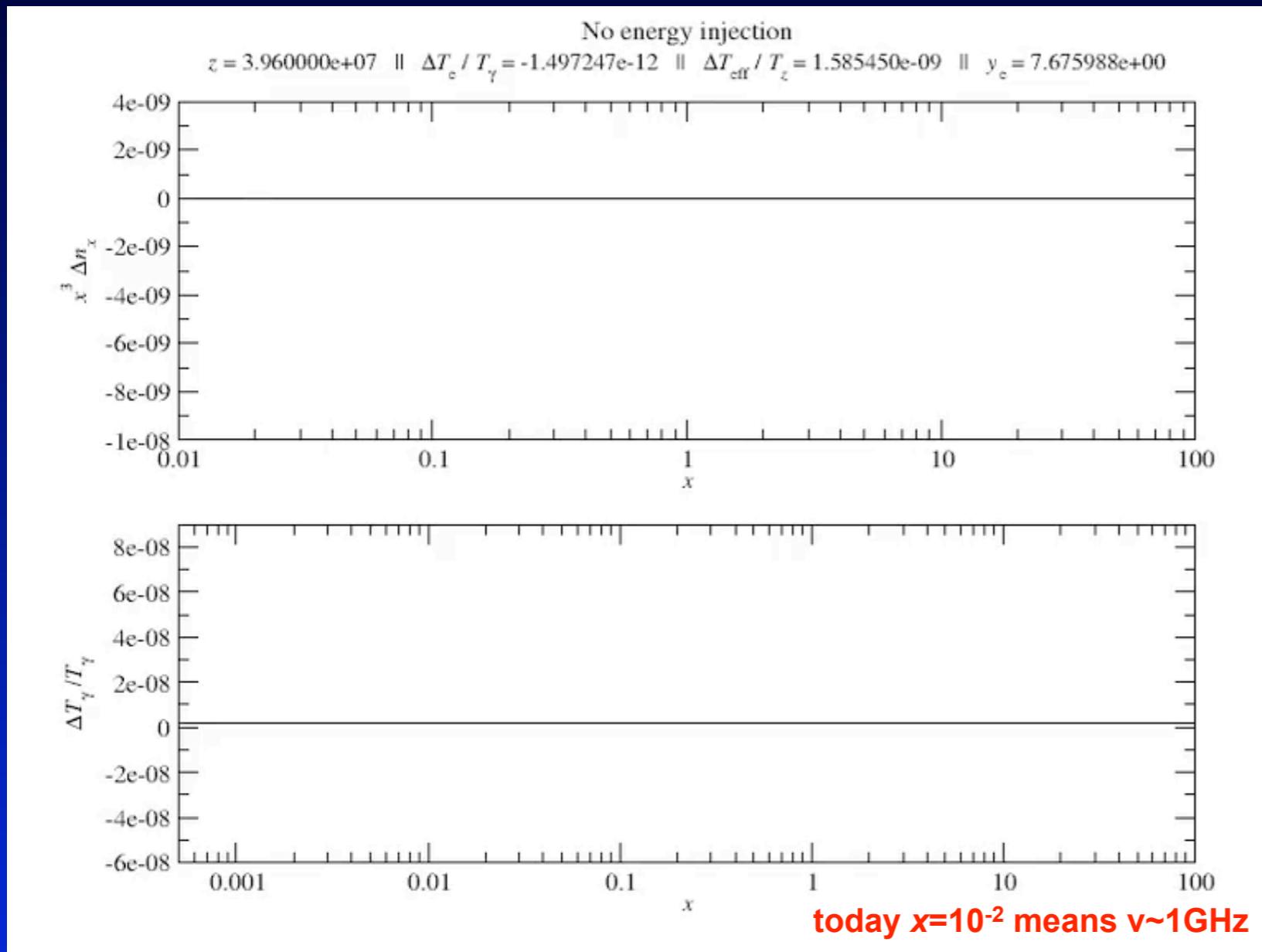
- adiabatic expansion
 $\Rightarrow T_\gamma \sim (1+z) \leftrightarrow T_m \sim (1+z)^2$
- photons continuously *cooled / down-scattered* since day one of the Universe!
- Compton heating balances adiabatic cooling
 $\Rightarrow \frac{da^4 \rho_\gamma}{a^4 dt} \simeq -Hk\alpha_h T_\gamma \propto (1+z)^6$
- at high redshift same scaling as *annihilation* ($\propto N_X^2$) and *acoustic mode damping*
 \Rightarrow partial *cancellation*

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today $x=10^{-2}$ means $\nu \sim 1\text{GHz}$

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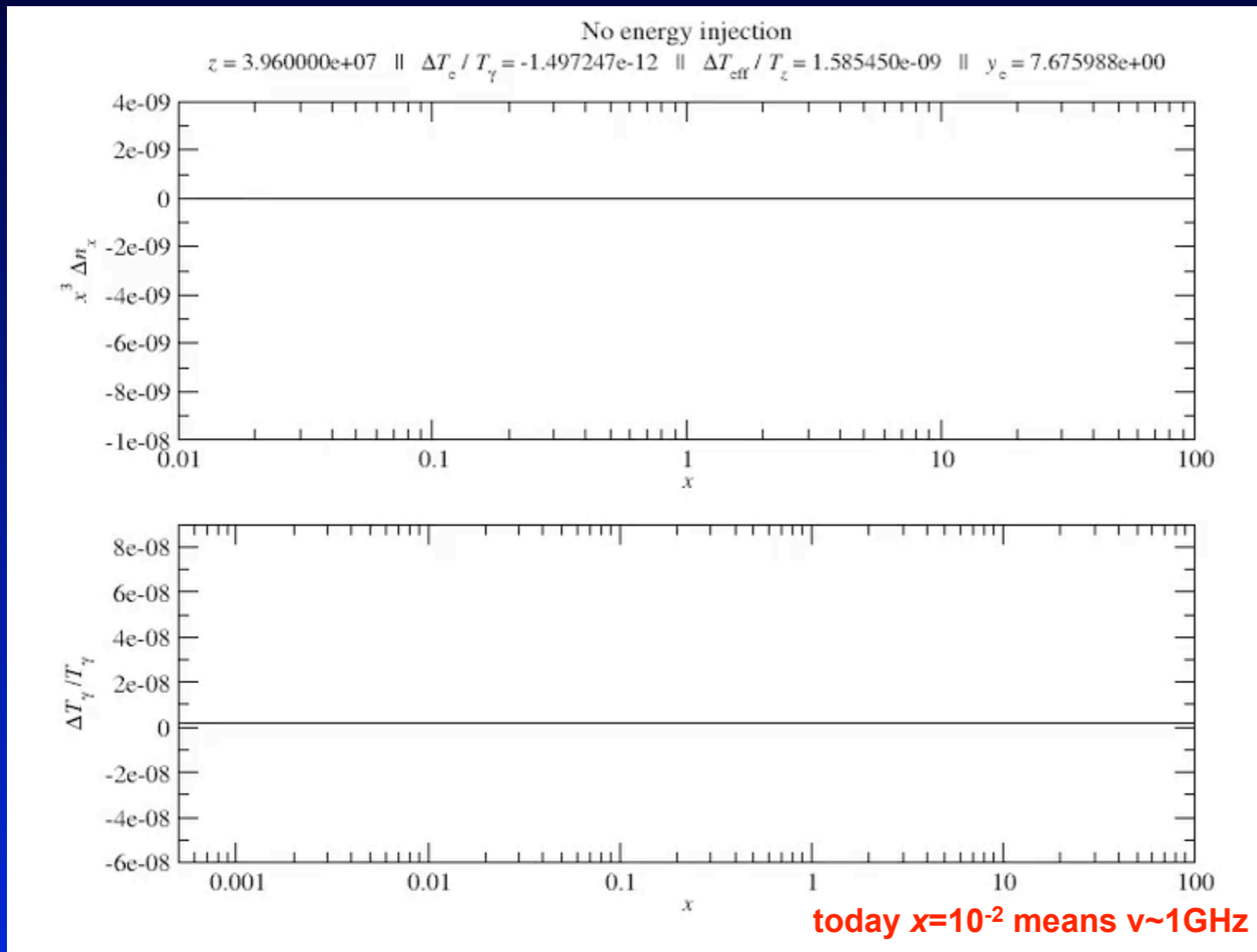
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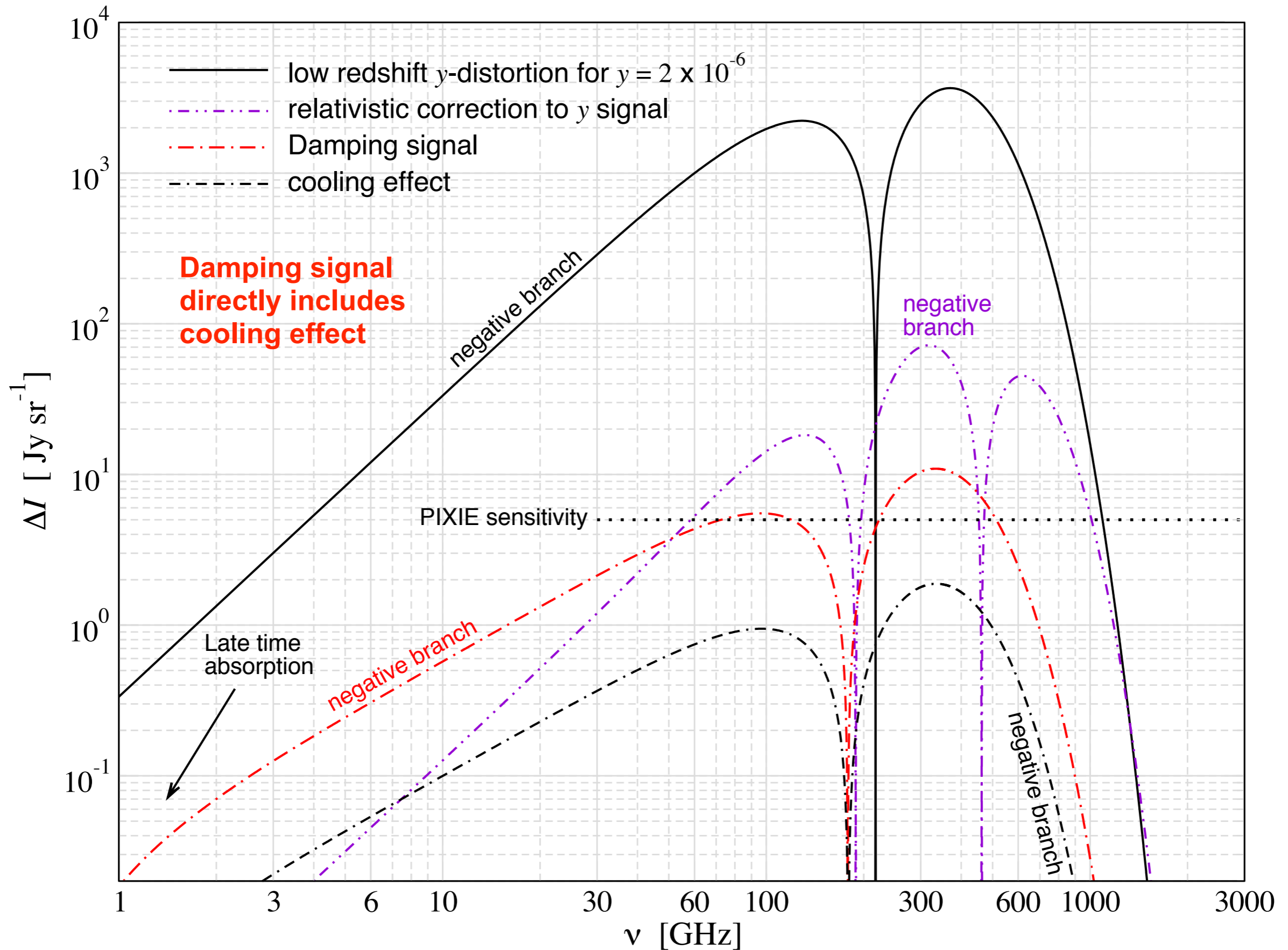
- *negative* μ and y distortion

- late free-free absorption at very low frequencies

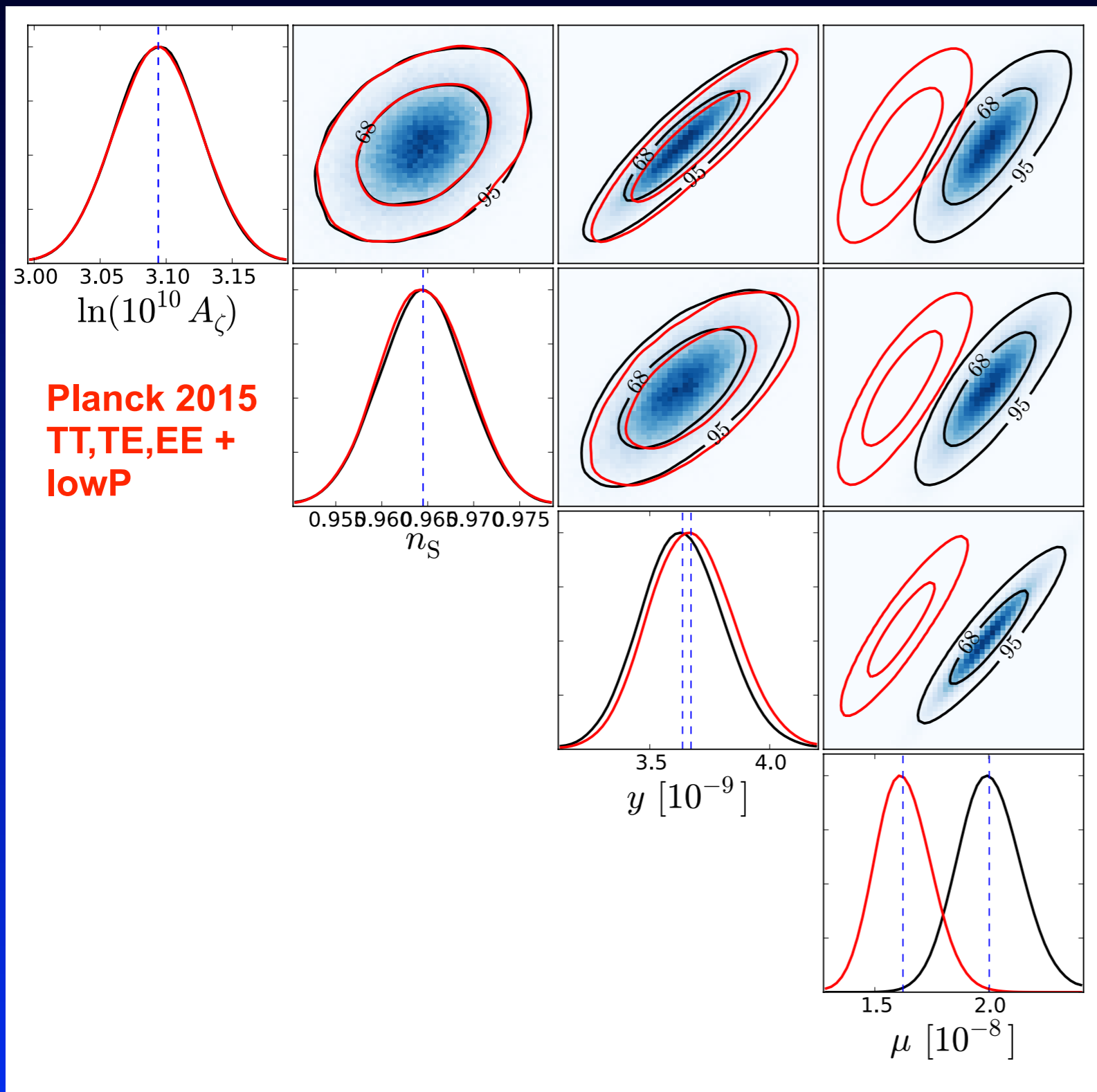
- Distortion a few times below PIXIE's current sensitivity

$$\mu \simeq 1.4 \left. \frac{\Delta \rho_\gamma}{\rho_\gamma} \right|_\mu \approx -3 \times 10^{-9} \quad y \simeq \frac{1}{4} \left. \frac{\Delta \rho_\gamma}{\rho_\gamma} \right|_y \approx -6 \times 10^{-10}$$

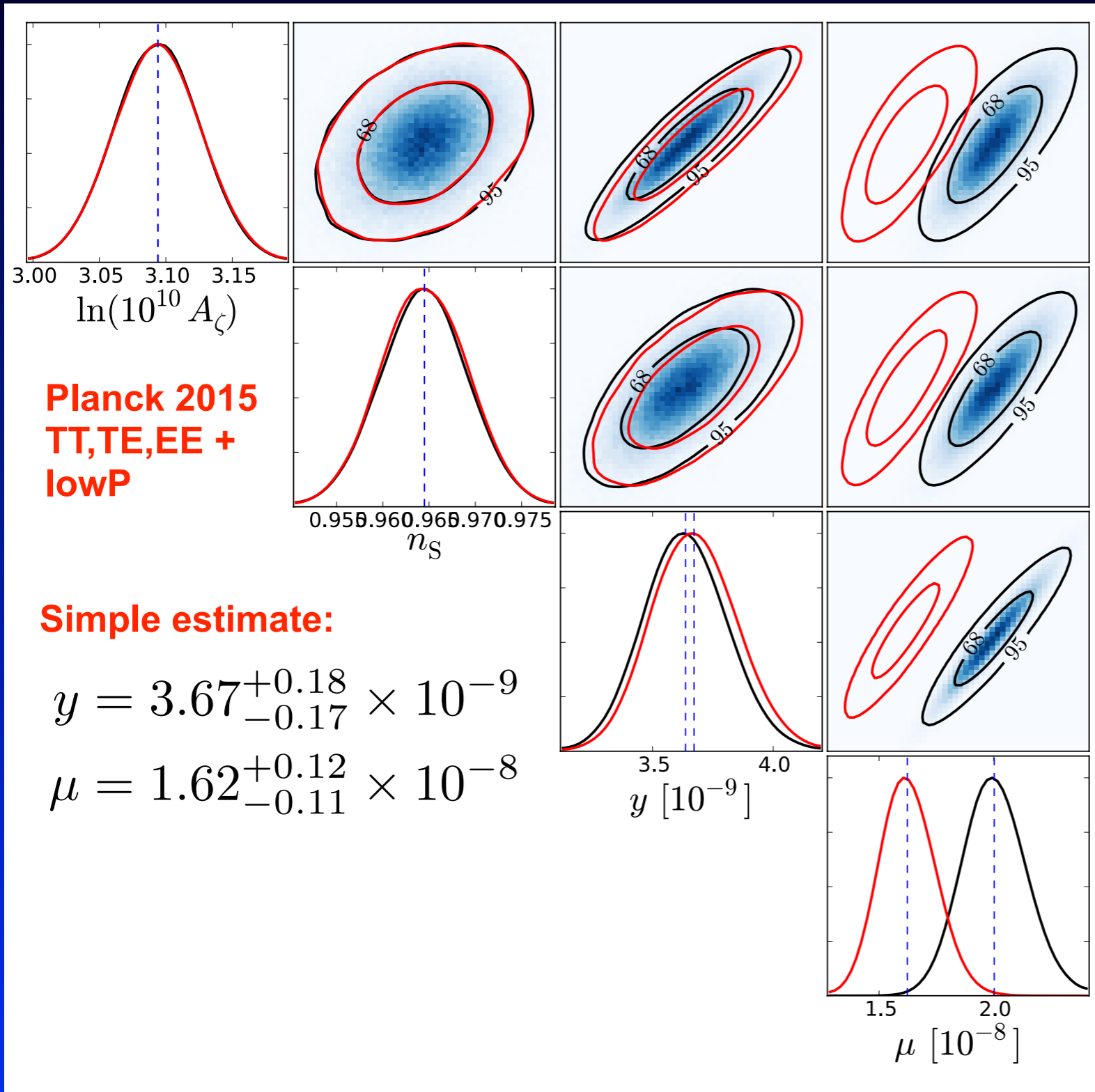
Average CMB spectral distortions



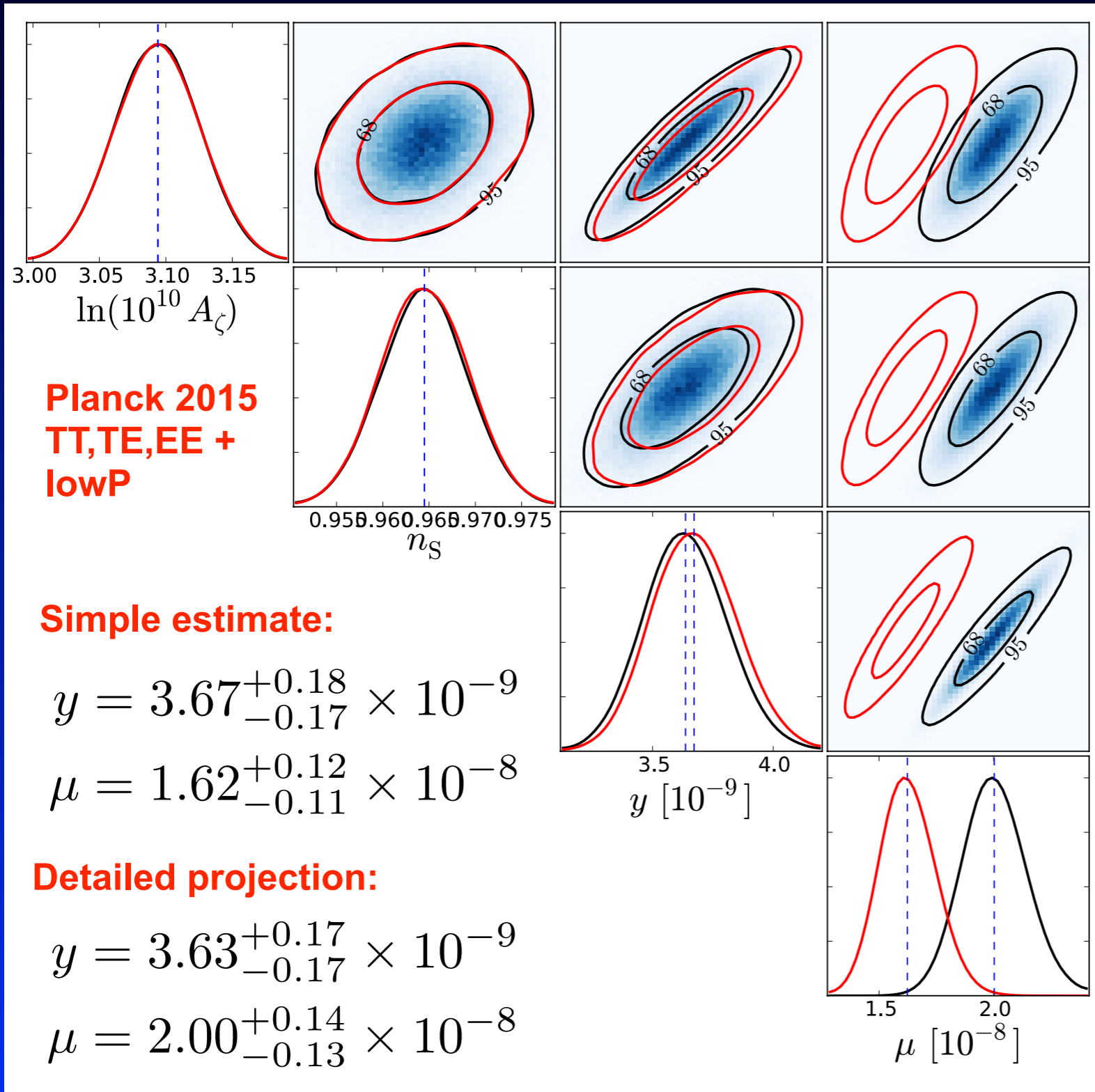
Predicted damping distortion in terms of μ and y



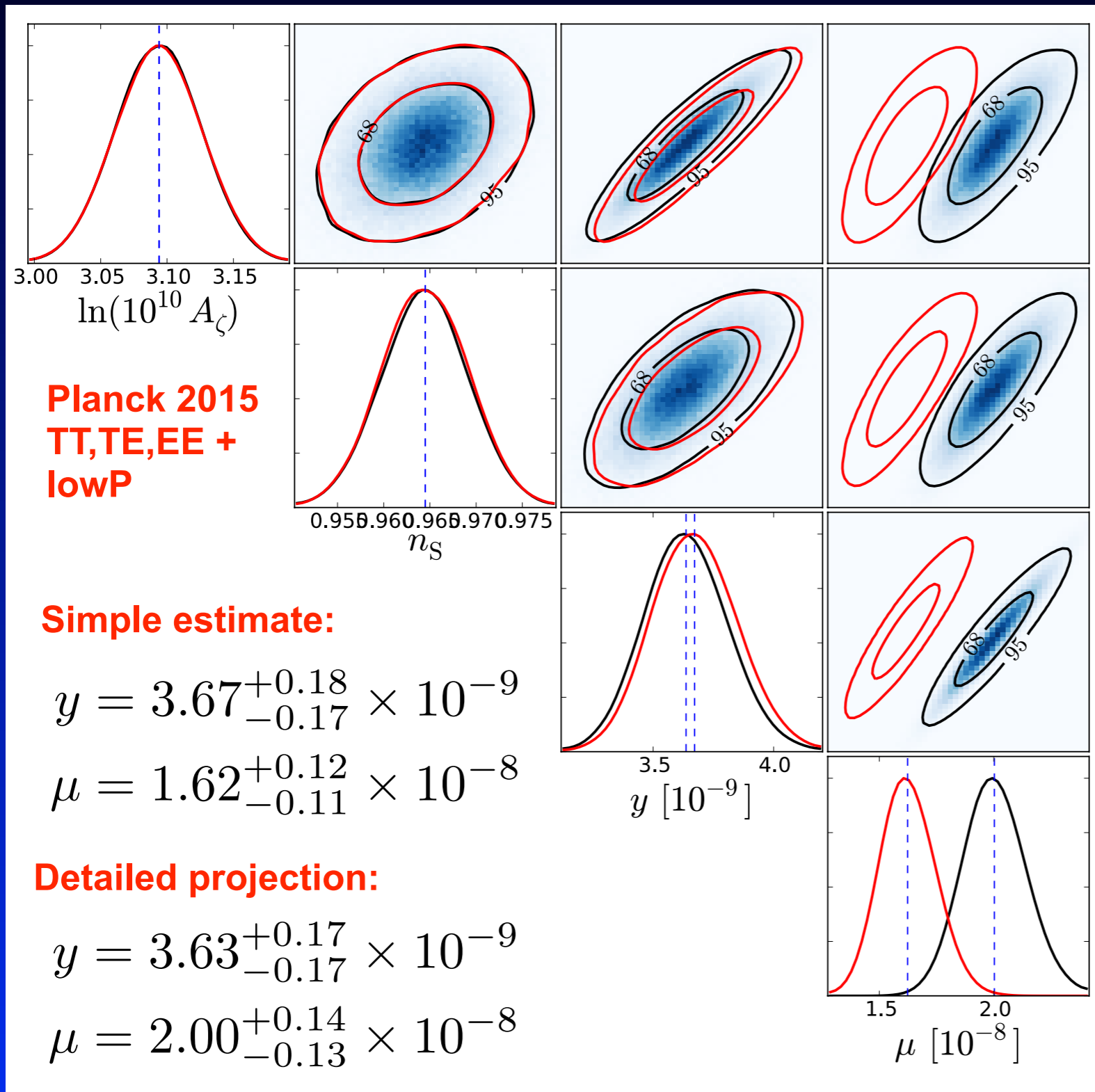
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Predicted damping distortion in terms of μ and y

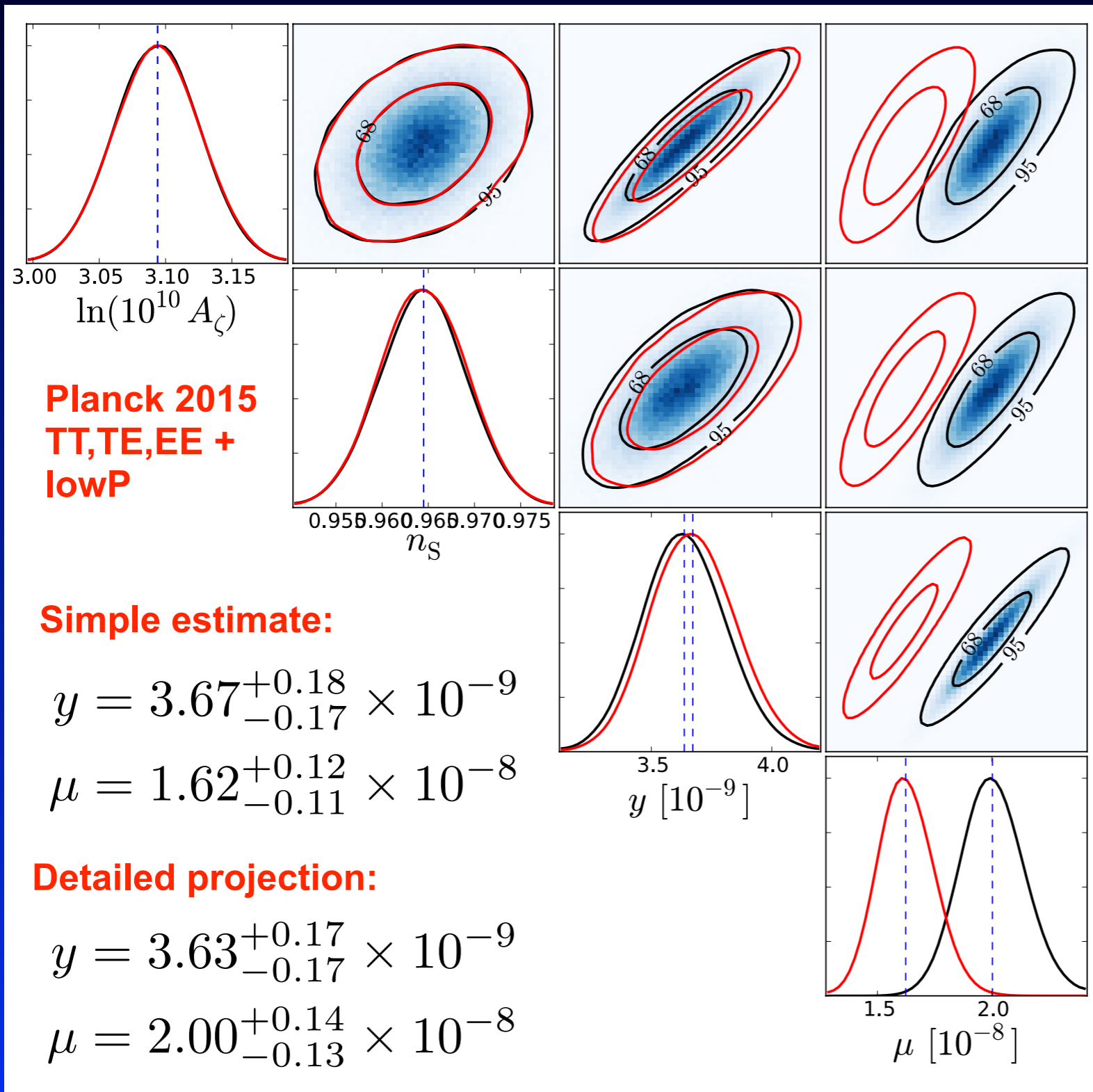


Predicted damping distortion in terms of μ and y



- Errors dominated by power spectrum parameters
- Detailed projections give slightly higher value for μ ($\sim 2.6\sigma$)
- y -part swamped by low redshift distortion
- μ could be detectable at 1.5σ with PIXIE in current setting
(see also JC, Khatri & Sunyaev, 2015)
- a factor of ~ 3.4 short of clear 5σ detection

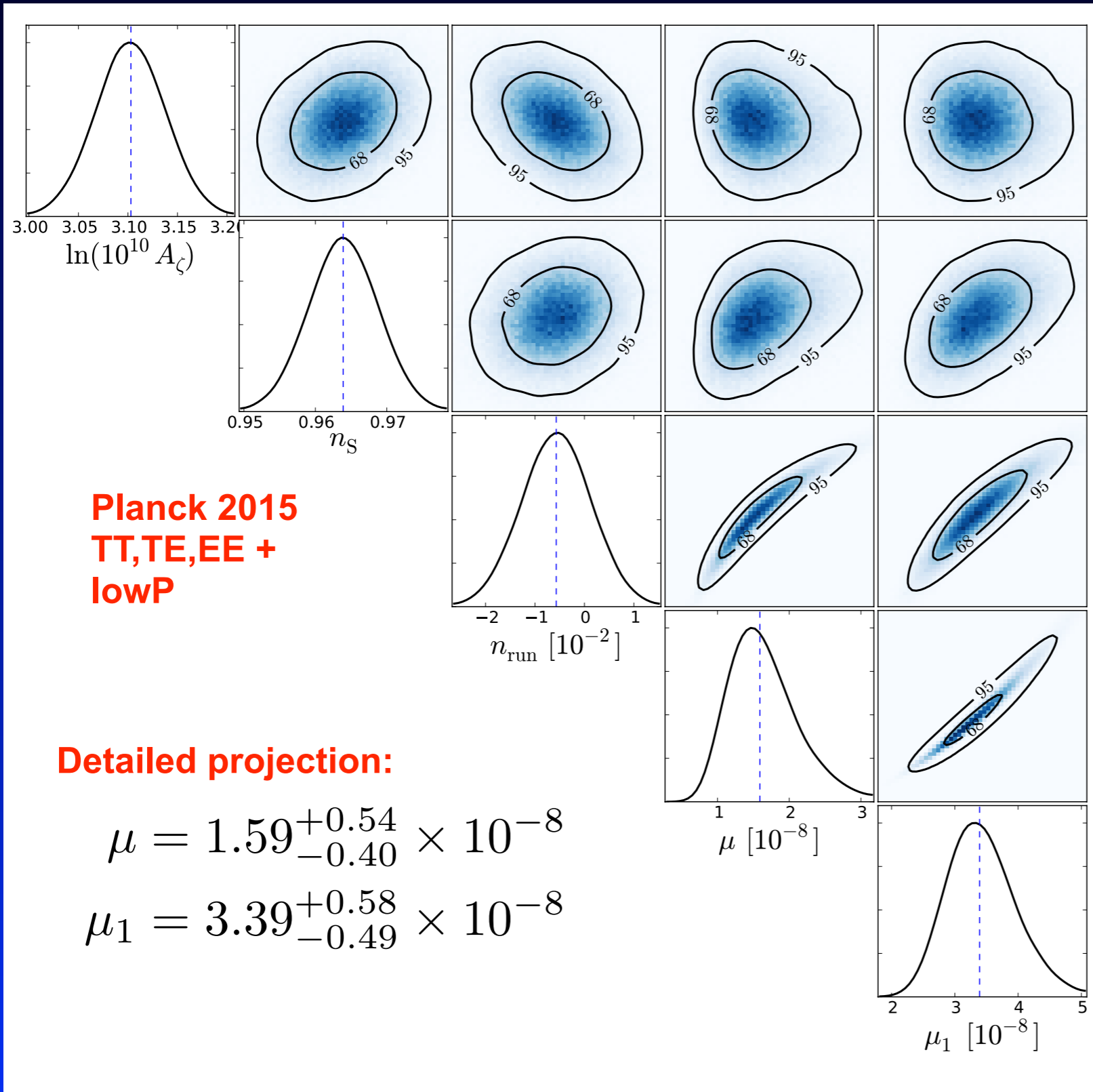
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Improvements of PIXIE are being discussed!

Allowing for running of the spectral index



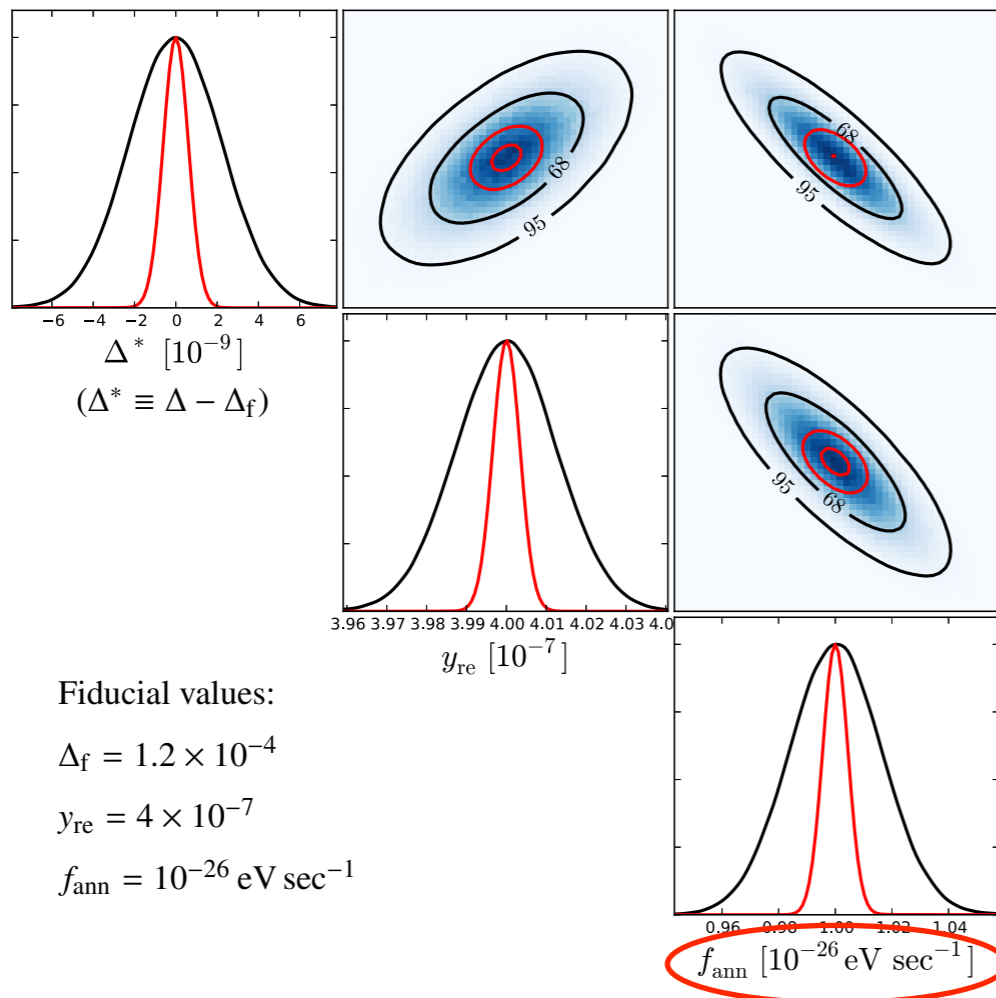
- Posteriors more non-Gaussian
- *extended scenario*
- *small negative running* → lower value of μ
- μ signal $\sim 1\sigma$ above current PIXIE sensitivity
- first residual distortion parameter $\mu_1 \sim 0.3\sigma$ for current PIXIE sensitivity

What are the residual distortion parameters?

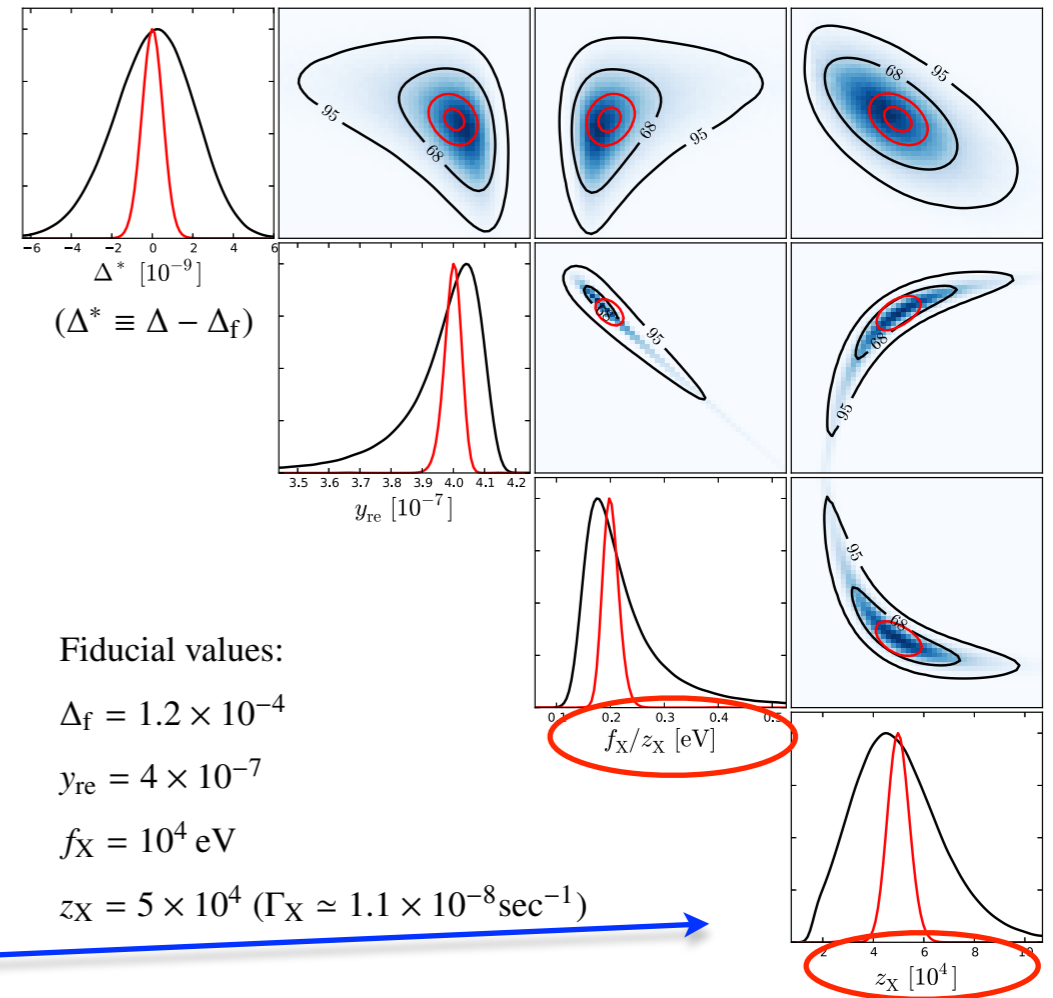
Why model-independent approach to distortion signal

- Model-dependent analysis makes model-selection non-trivial
- Real information in the distortion signal limited by sensitivity and foregrounds
- *Principle Component Analysis* (PCA) can help optimizing this!
- useful for optimizing experimental designs (*frequencies; sensitivities, ...*)!

Annihilation scenario

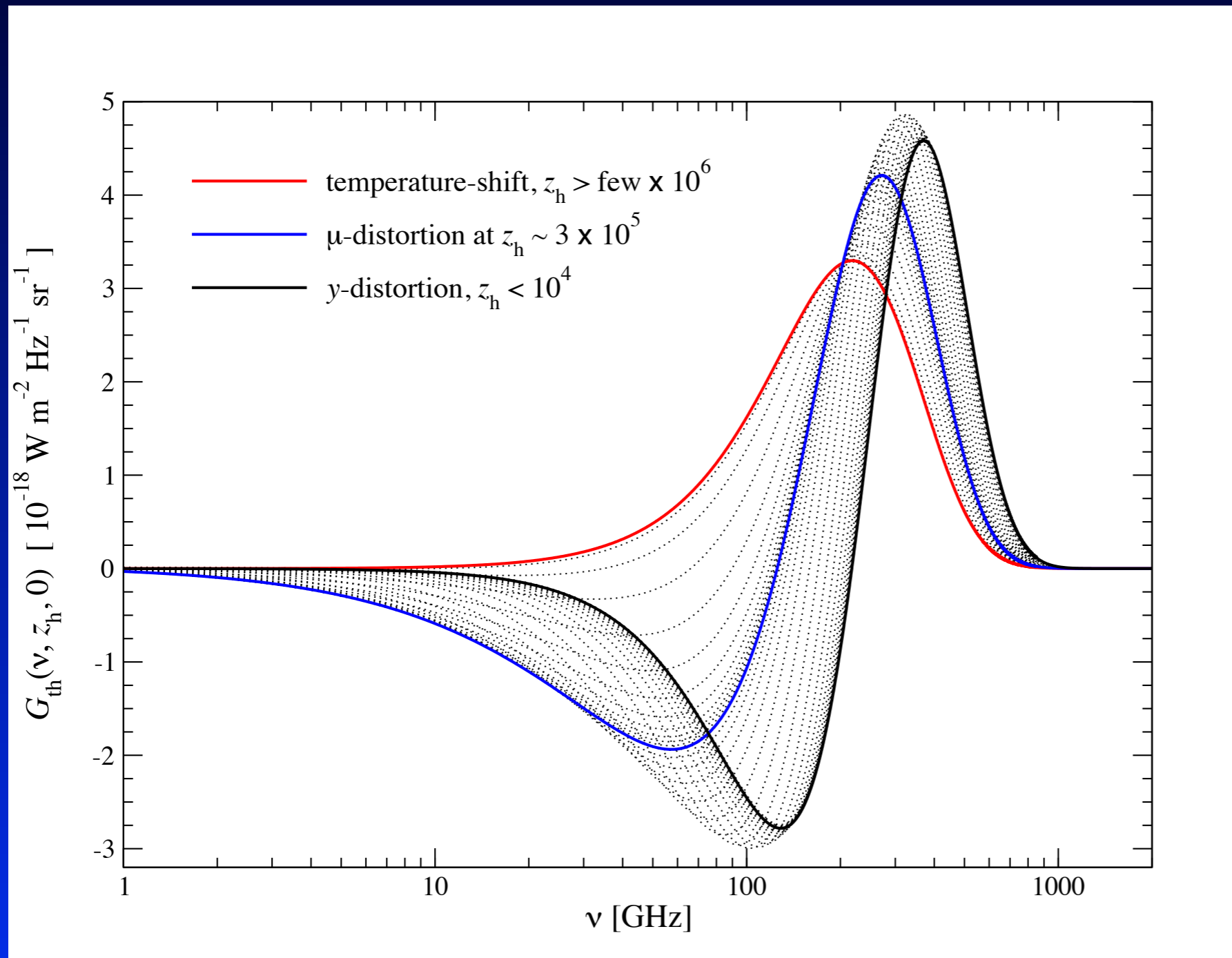


Decaying particle scenario



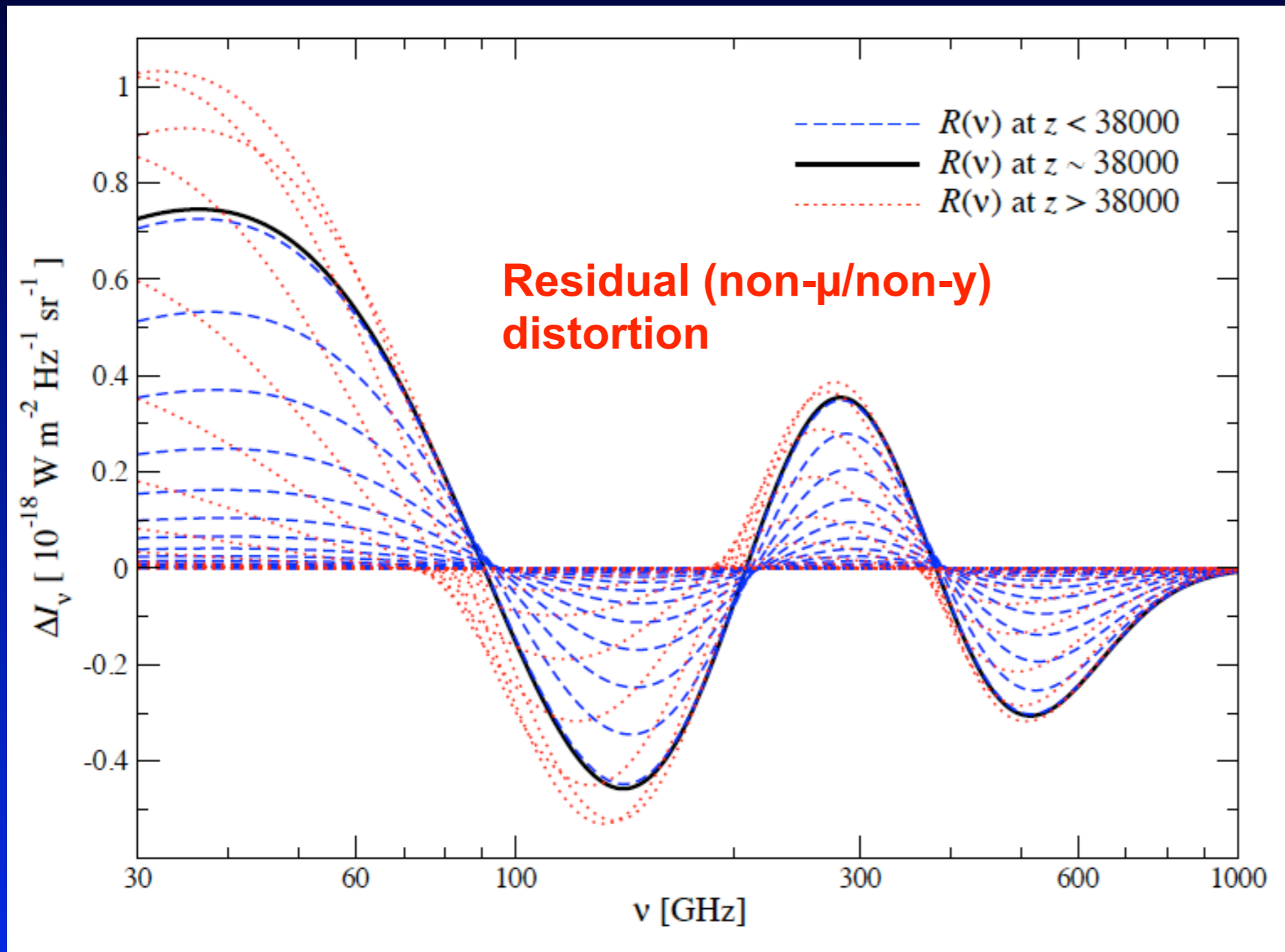
How do we compare these?

Using signal eigenmodes to compress the distortion data



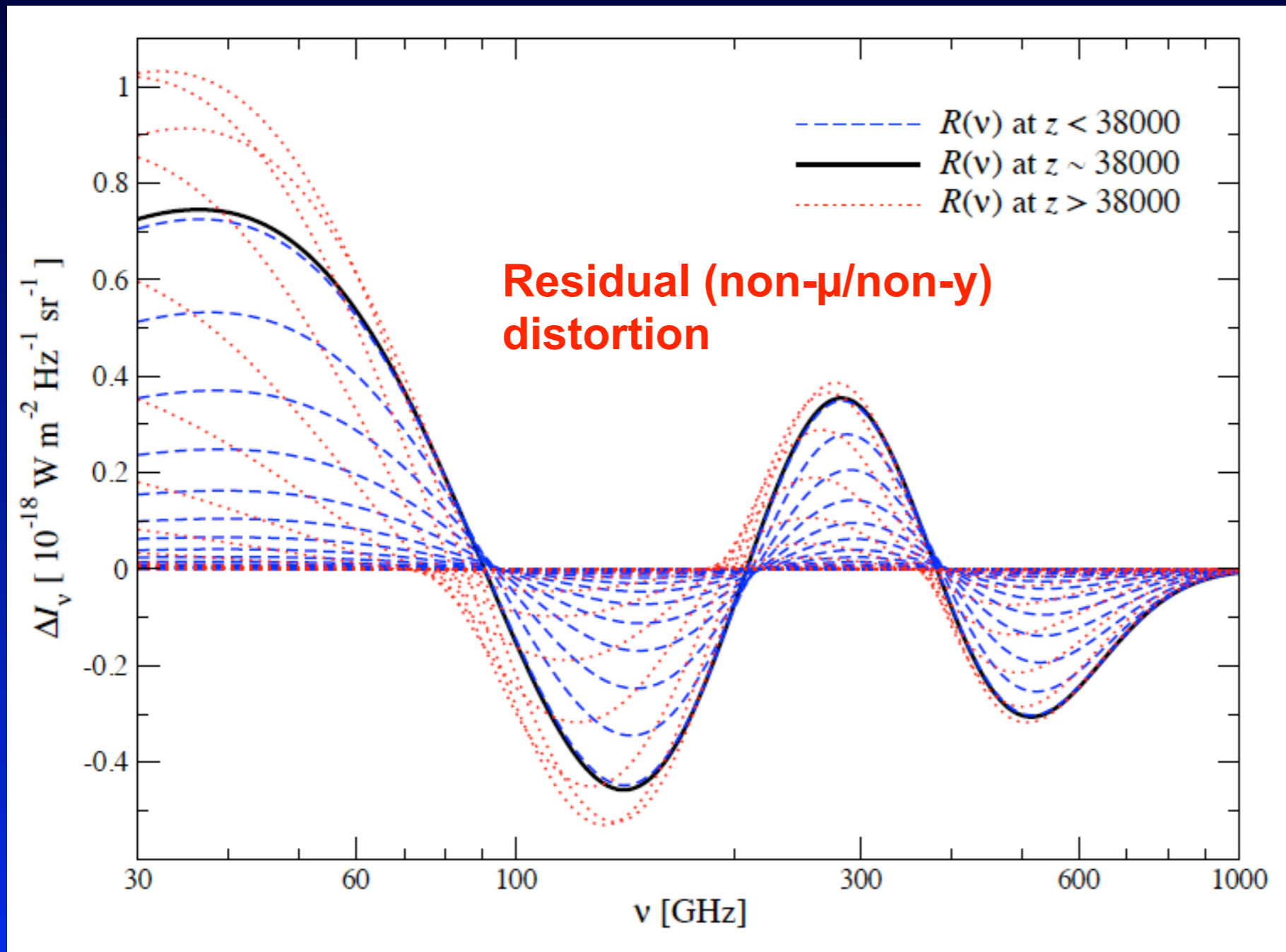
- *Principle component decomposition* of the distortion signal
- compression of the useful information given instrumental settings

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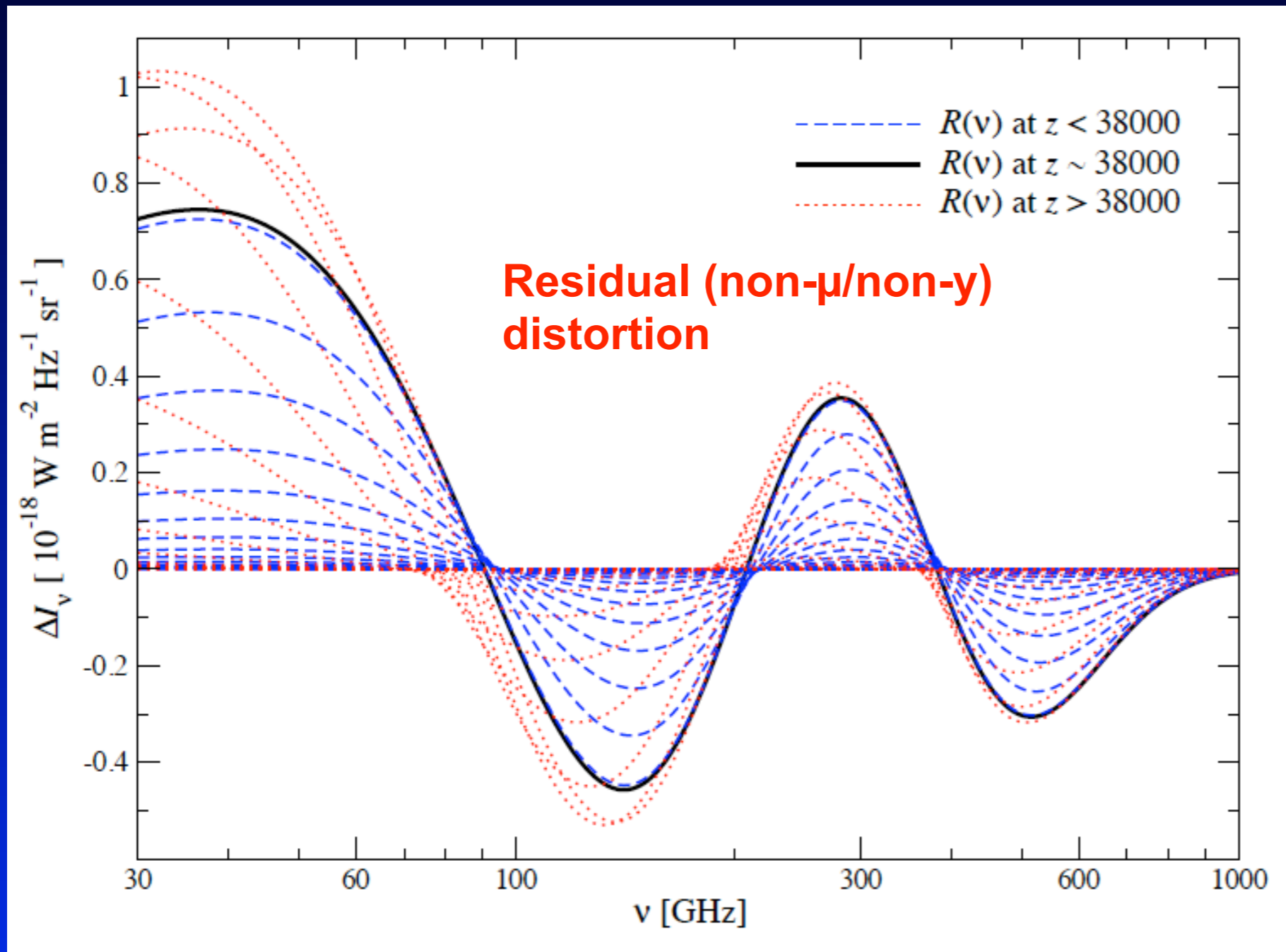
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Using signal eigenmodes to compress the distortion data



- *Principle component decomposition* of the distortion signal
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- new set of observables
 $p = \{y, \mu, \mu_1, \mu_2, \dots\}$
- model-comparison + forecasts of errors very simple!

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JC & Jeong, 2013

Ultimately this may be the only way to learn more!

Eigenmodes for a *PIXIE*-type experiment

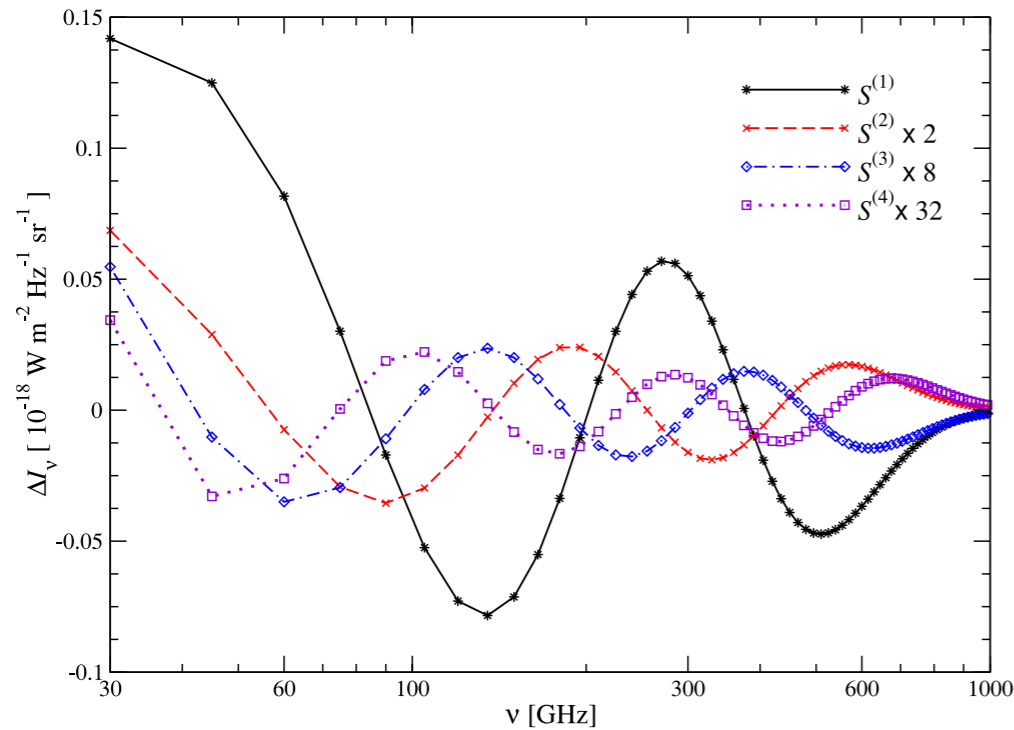
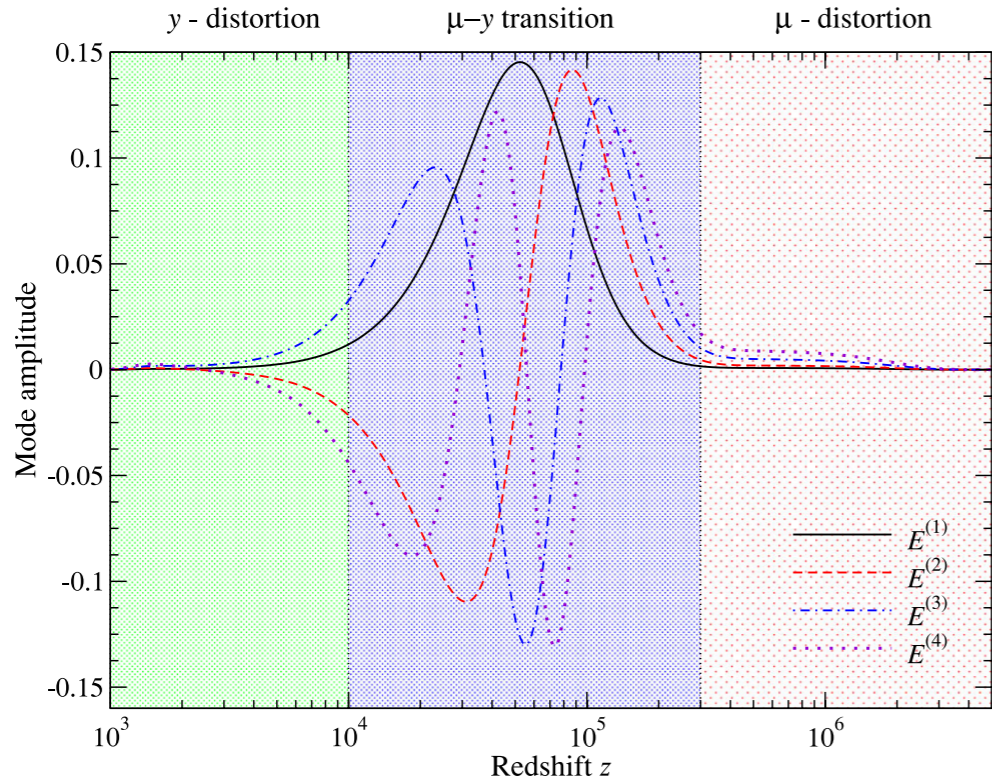


Figure 4. First few eigenmodes $E^{(k)}$ and $S^{(k)}$ for *PIXIE*-type settings ($\nu_{\min} = 30$ GHz, $\nu_{\max} = 1000$ GHz and $\Delta\nu_s = 15$ GHz). In the mode construction, we assumed that energy release only occurred at $10^3 \leq z \leq 5 \times 10^6$.

Estimated error bars

(under idealistic assumptions...)

$$\frac{\Delta T}{T} \simeq 2 \text{ nK} \left(\frac{\Delta I_c}{5 \text{ Jy sr}^{-1}} \right)$$

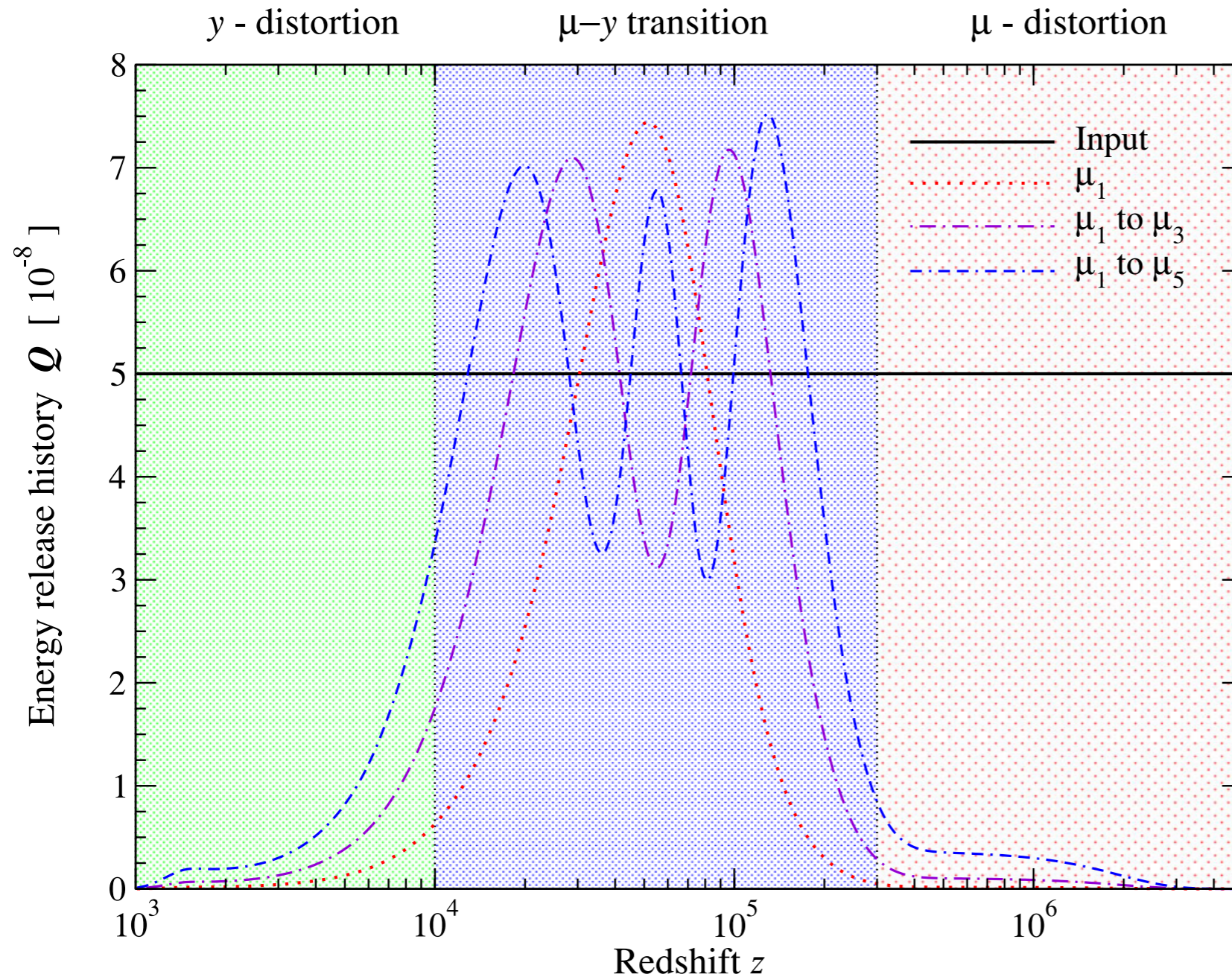
$$\Delta y \simeq 1.2 \times 10^{-9} \left(\frac{\Delta I_c}{5 \text{ Jy sr}^{-1}} \right)$$

$$\Delta \mu \simeq 1.4 \times 10^{-8} \left(\frac{\Delta I_c}{5 \text{ Jy sr}^{-1}} \right)$$

Table 1. Forecasted 1σ errors of the first six eigenmode amplitudes, $E^{(k)}$. We also give $\varepsilon_k = 4 \sum_i S_i^{(k)} / \sum_i G_{i,T}$, and the scalar products $S^{(k)} \cdot S^{(k)}$ (in units of $[10^{-18} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}]^2$). The fraction of energy release to the residual distortion and its uncertainty are given by $\varepsilon \approx \sum_k \varepsilon_k \mu_k$ and $\Delta\varepsilon \approx (\sum_k \varepsilon_k^2 \Delta\mu_k^2)^{1/2}$, respectively. For the mode construction we used *PIXIE*-settings ($\{\nu_{\min}, \nu_{\max}, \Delta\nu_s\} = \{30, 1000, 15\}$ GHz and channel sensitivity $\Delta I_c = 5 \times 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$). The errors roughly scale as $\Delta\mu_k \propto \Delta I_c / \sqrt{\Delta\nu_s}$.

k	$\Delta\mu_k$	$\Delta\mu_k / \Delta\mu_1$	ε_k	$S^{(k)} \cdot S^{(k)}$
1	1.48×10^{-7}	1	-6.98×10^{-3}	1.15×10^{-1}
2	7.61×10^{-7}	5.14	2.12×10^{-3}	4.32×10^{-3}
3	3.61×10^{-6}	24.4	-3.71×10^{-4}	1.92×10^{-4}
4	1.74×10^{-5}	1.18×10^2	8.29×10^{-5}	8.29×10^{-6}
5	8.52×10^{-5}	5.76×10^2	-1.55×10^{-5}	3.45×10^{-7}
6	4.24×10^{-4}	2.86×10^3	2.75×10^{-6}	1.39×10^{-8}

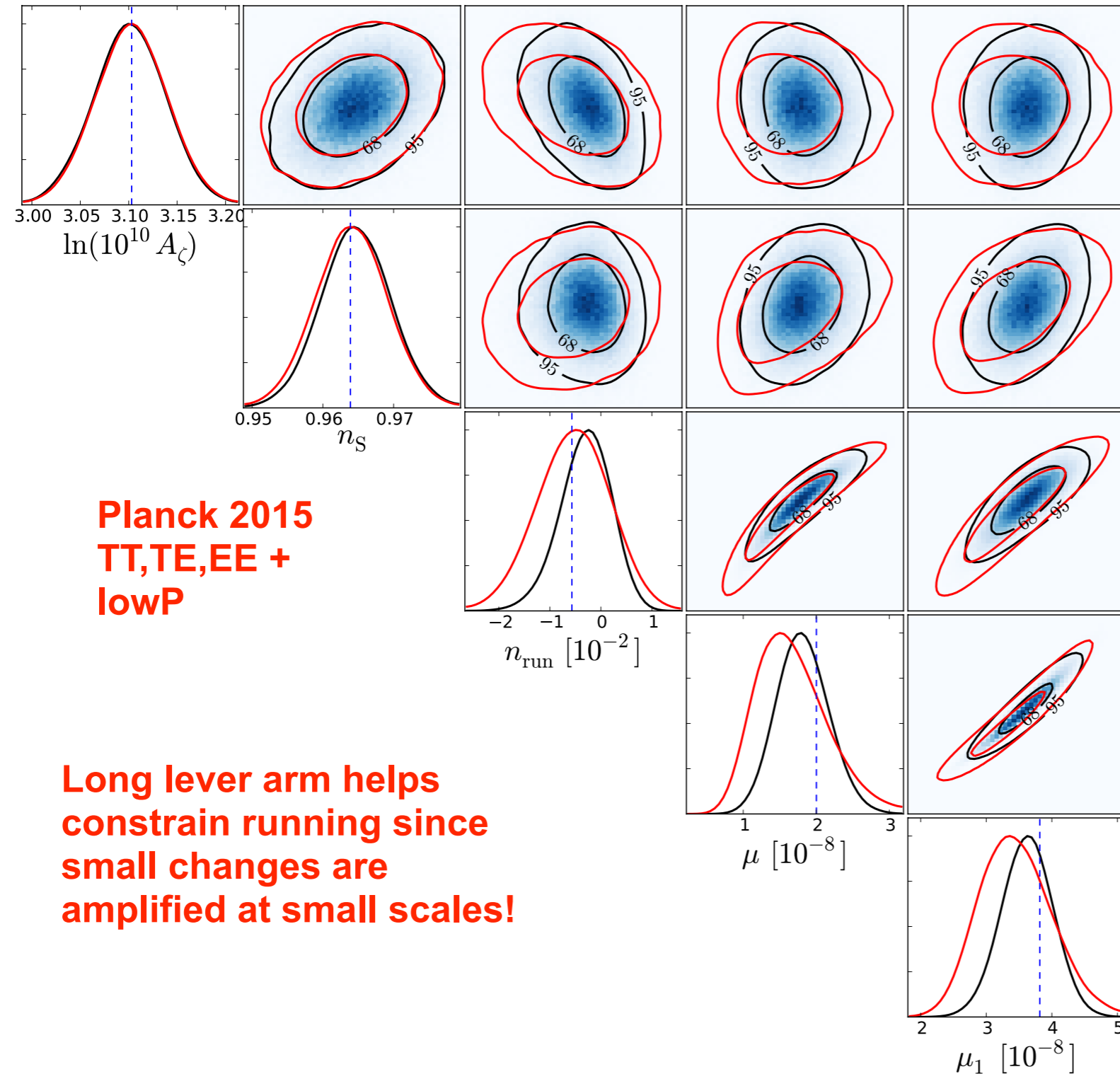
Partial recovery of energy release history



- 'wiggly' recovery of input thermal history possible
- redshift resolution depends on sensitivity and distortion amplitude

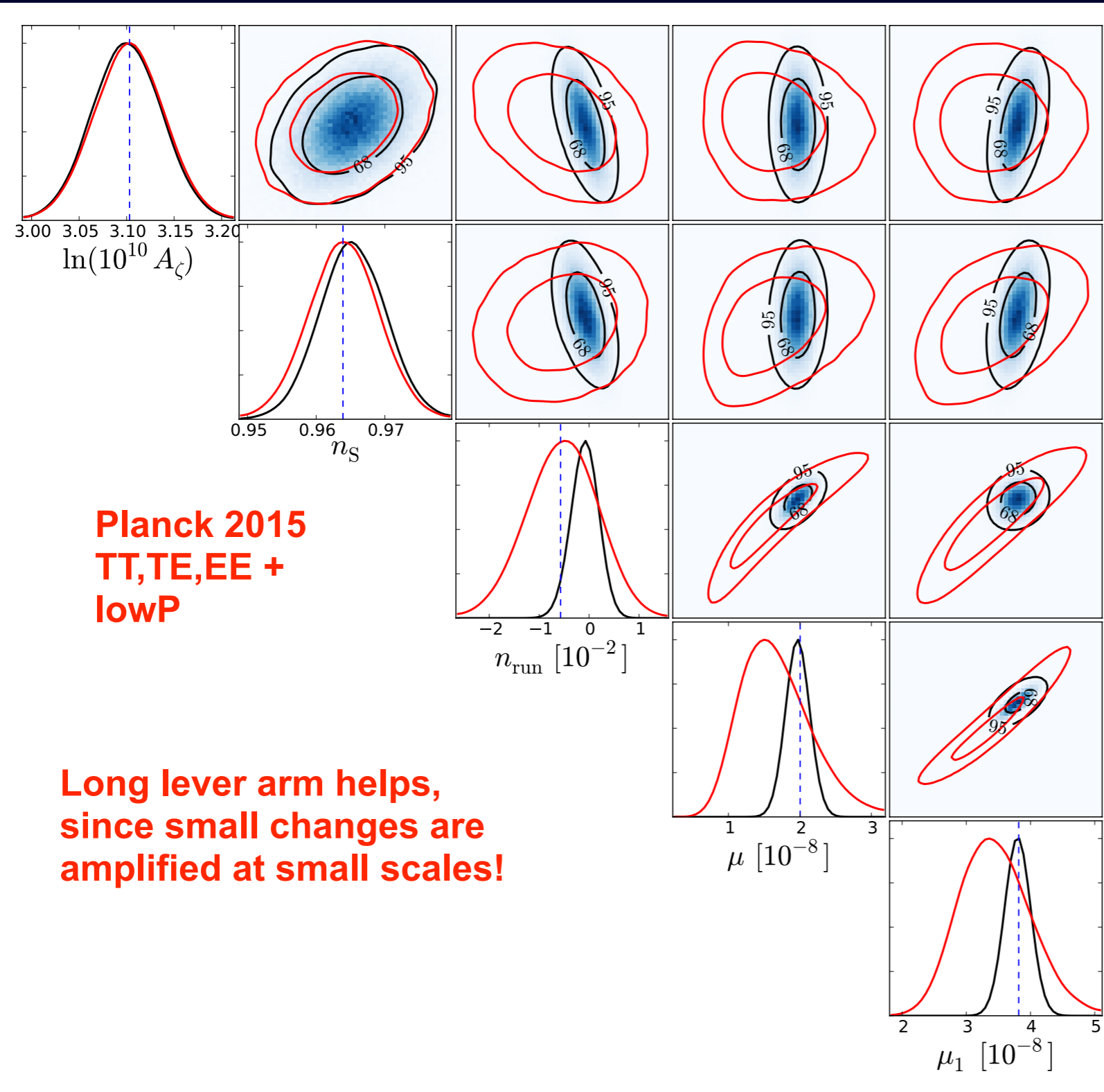
Figure 6. Partial recovery of the input energy-release history, $Q = 5 \times 10^{-8}$.

Testing running with distortions



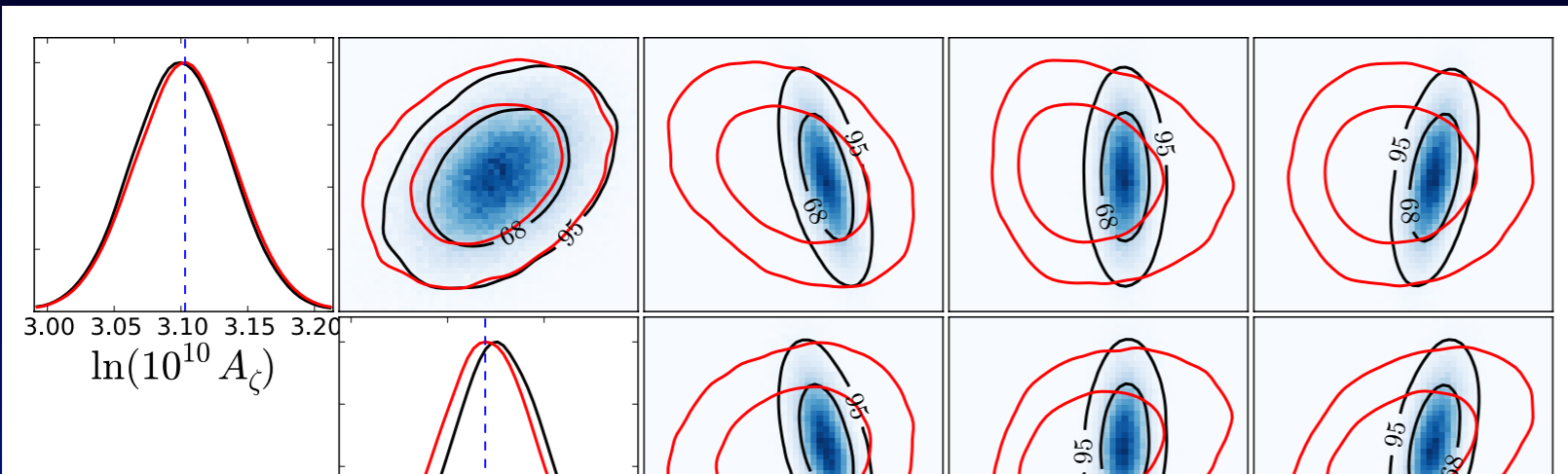
- combined constraint Planck & PIXIE not affected much by distortion information
- at $\sim 3.4 \times$ PIXIE, constraint on running improved ~ 1.5 times
- centroid moves towards fiducial model

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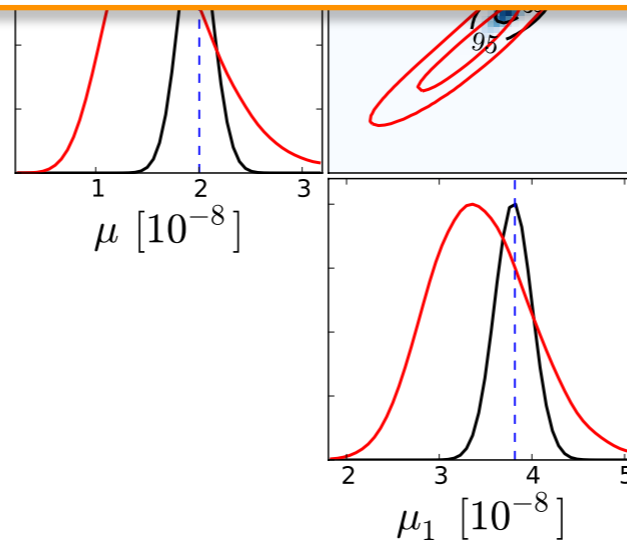
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- at $10 \times$ PIXIE, constraint on running improved 3 times over Planck alone
- μ could be detected at $\sim 15\sigma$ and μ_1 at $\sim 2.6\sigma$
- combining with future imager (e.g., COrE+) *distortions* could still improve constraint on running (e.g., JC & Jeong, 2014)

Testing running with distortions



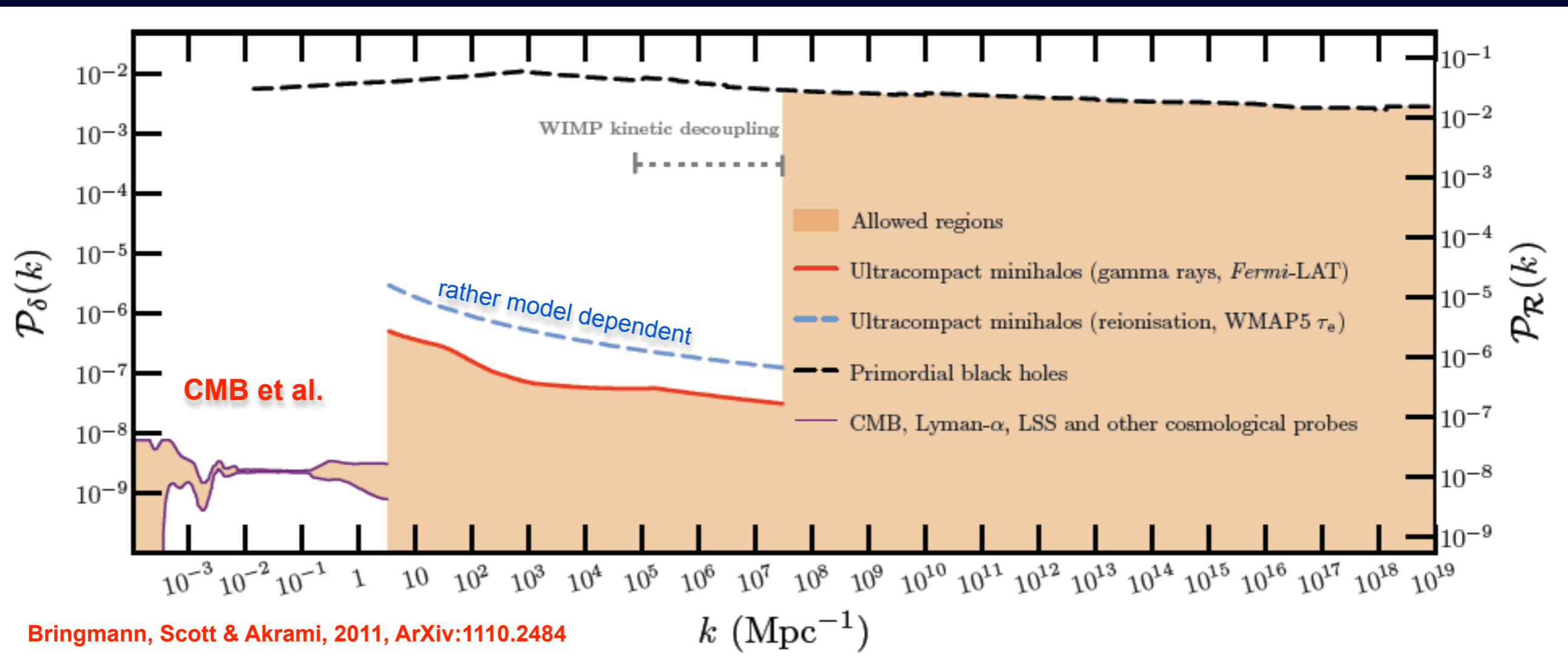
Parameter	Planck alone	+PIXIE	+3.4xPIXIE	+10xPIXIE	Planck Λ CDM values
$\ln(10^{10} A_s)$	$3.103^{+0.036}_{-0.036}$	$3.103^{+0.037}_{-0.037}$	$3.101^{+0.037}_{-0.037}$	$3.100^{+0.036}_{-0.036}$	$3.094^{+0.034}_{-0.034}$
n_s	$0.9639^{+0.0050}_{-0.0050}$	$0.9640^{+0.0050}_{-0.0050}$	$0.9647^{+0.0049}_{-0.0048}$	$0.9653^{+0.0048}_{-0.0047}$	$0.9645^{+0.0049}_{-0.0049}$
$10^3 n_{run}$	$-5.7^{+7.1}_{-7.1}$	$-5.2^{+6.9}_{-7.2}$	$-2.8^{+4.6}_{-5.1}$	$-0.81^{+2.4}_{-2.5}$	0
$\mu/10^{-8}$	$1.59^{+0.54}_{-0.40}$	$1.62^{+0.55}_{-0.42} (1.2\sigma)$	$1.81^{+0.36}_{-0.33} (4.5\sigma)$	$1.993^{+0.053}_{-0.053} (15\sigma)$	$2.00^{+0.14}_{-0.13}$
$\mu_1/10^{-8}$	$3.39^{+0.58}_{-0.49}$	$3.43^{+0.58}_{-0.52} (0.23\sigma)$	$3.63^{+0.38}_{-0.38} (0.83\sigma)$	$3.819^{+0.044}_{-0.044} (2.6\sigma)$	$3.81^{+0.22}_{-0.20}$
$\mu_2/10^{-9}$	$-2.79^{+2.05}_{-1.53}$	$-2.69^{+2.08}_{-1.61} (0\sigma)$	$-2.02^{+1.42}_{-1.31} (0\sigma)$	$-1.28^{+0.43}_{-0.43} (0\sigma)$	$-1.19^{+0.22}_{-0.20}$

Long lever arm helps, since small changes are amplified at small scales!



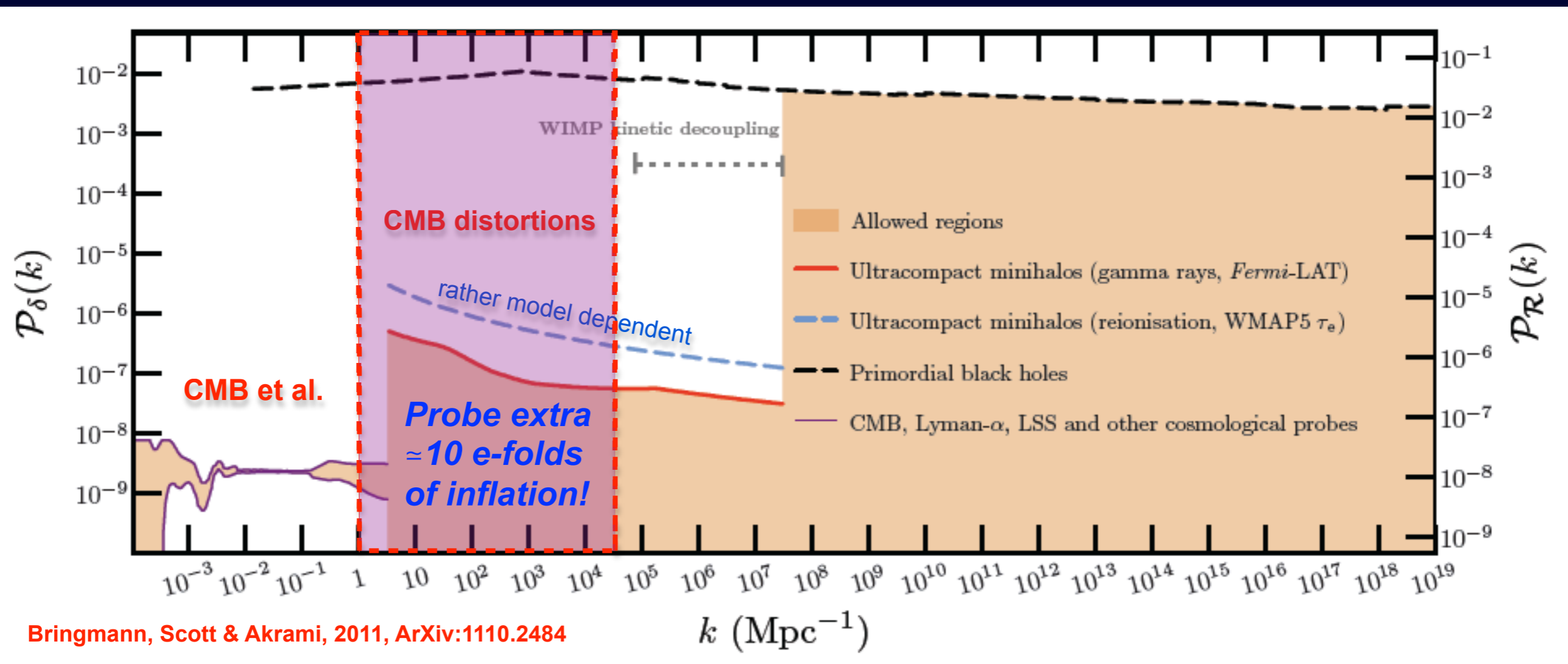
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Distortions provide general power spectrum constraints!

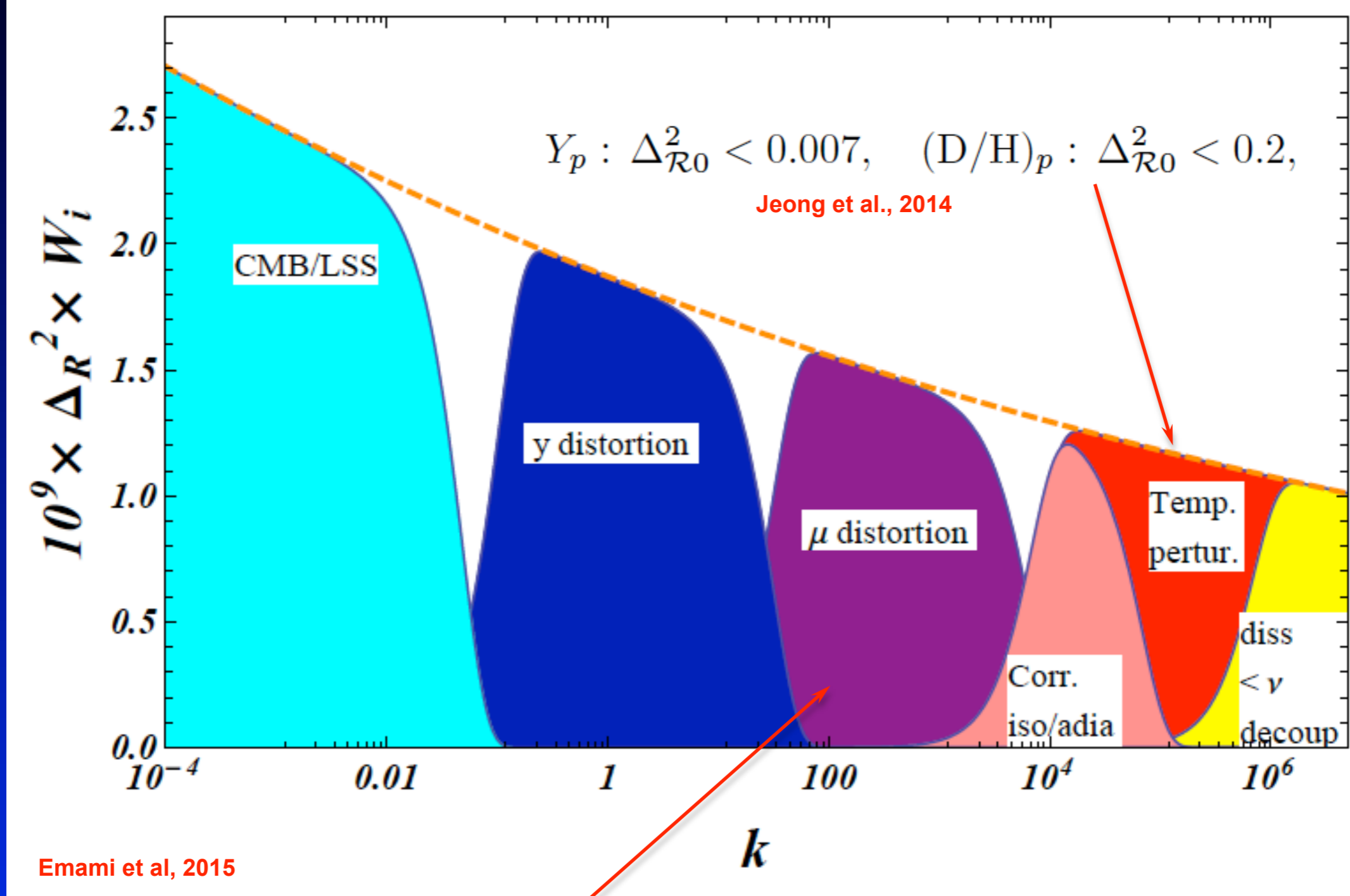


- Amplitude of power spectrum rather uncertain at $k > 3 \text{ Mpc}^{-1}$
- improved limits at smaller scales can *rule out* many *inflationary models*

Distortions provide general power spectrum constraints!

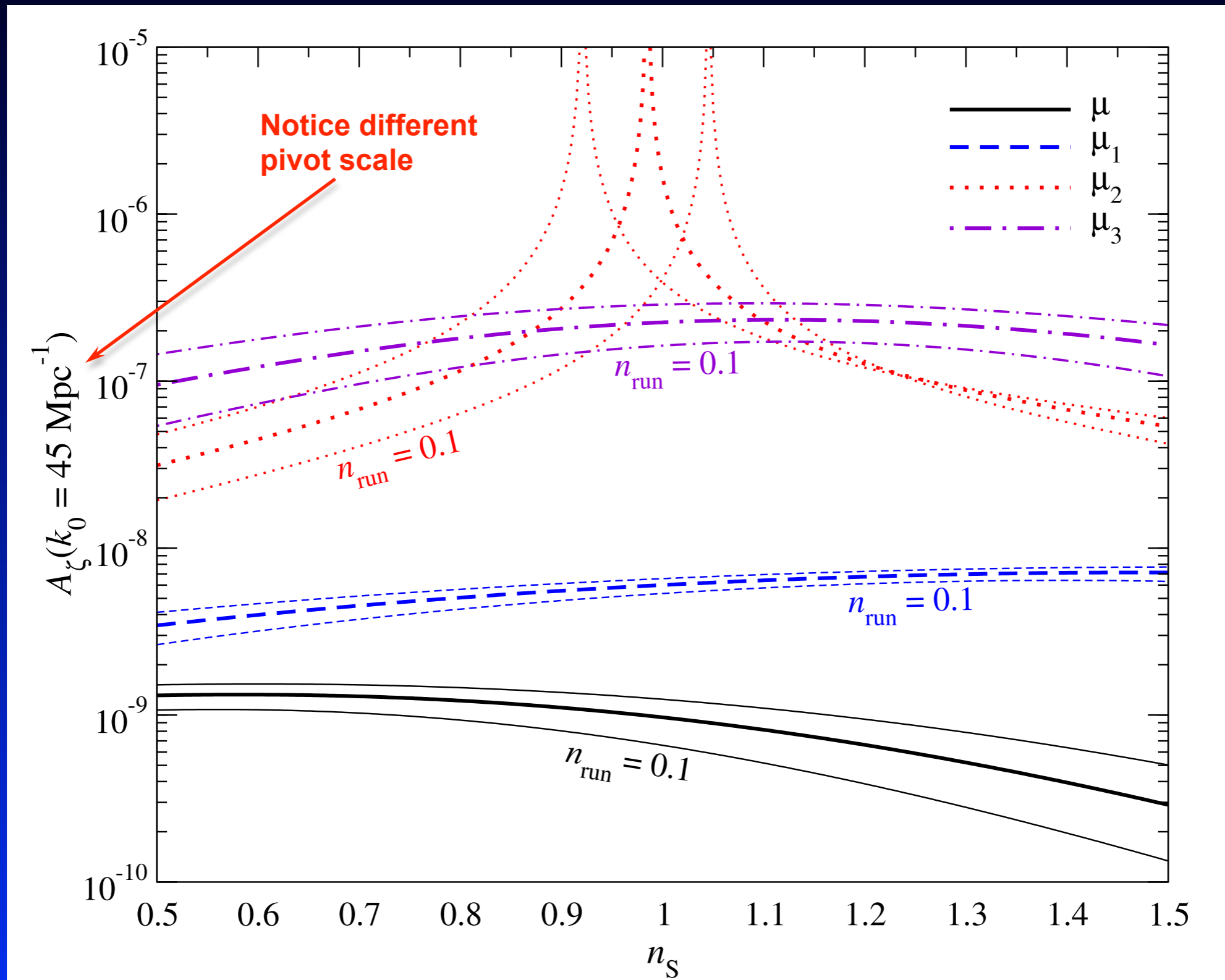


- Amplitude of power spectrum rather uncertain at $k > 3 \text{ Mpc}^{-1}$
- improved limits at smaller scales can *rule out* many *inflationary models*
- CMB spectral distortions would *extend* our *lever arm* to $k \sim 10^4 \text{ Mpc}^{-1}$
- very *complementary* piece of information about early-universe physics

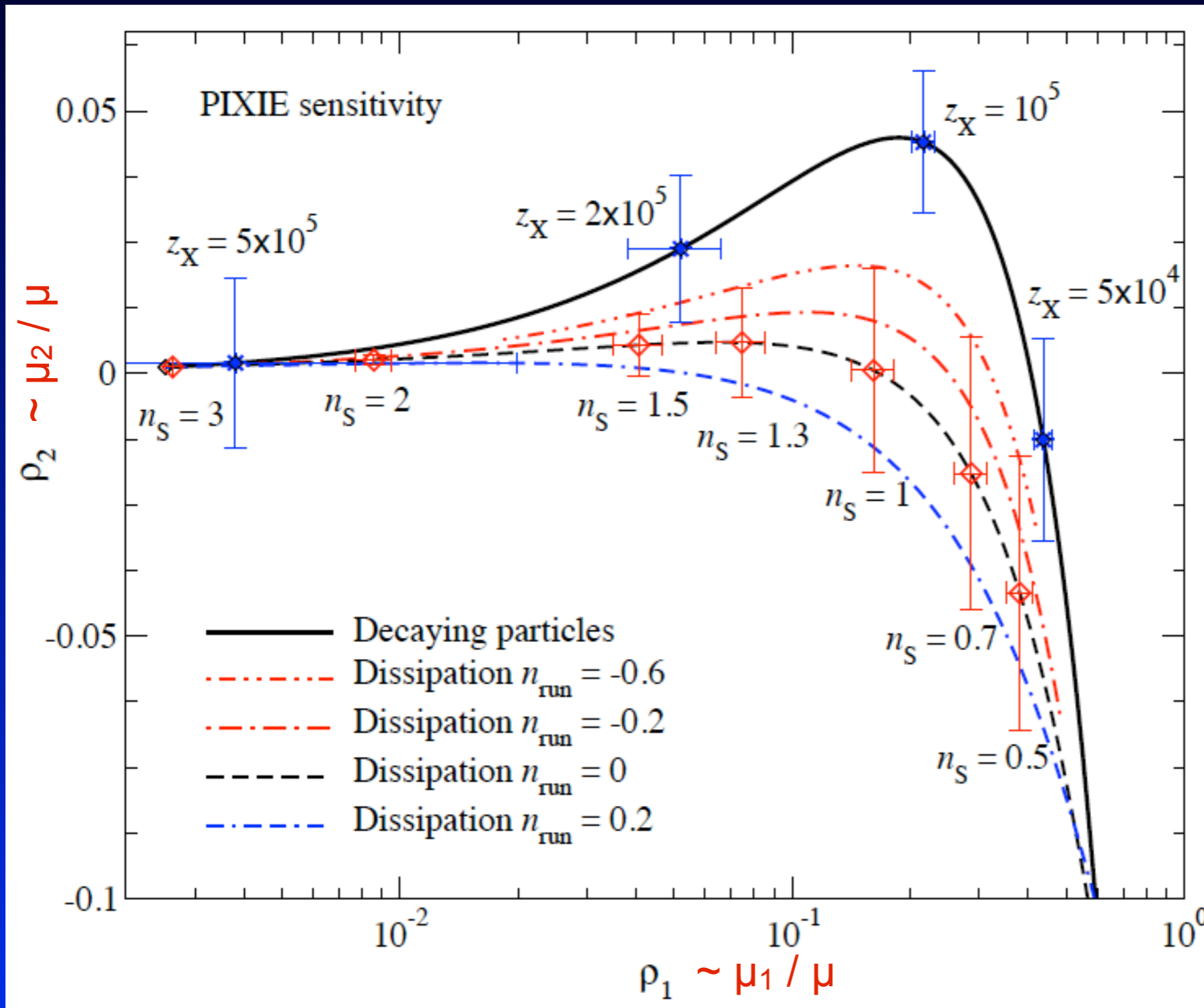


- *Ultra-squeezed limit non-Gaussianity* (Pajer & Zaldarriaga, 2012; Ganc & Komatsu, 2012)

Dissipation scenario: 1σ -detection limits for PIXIE



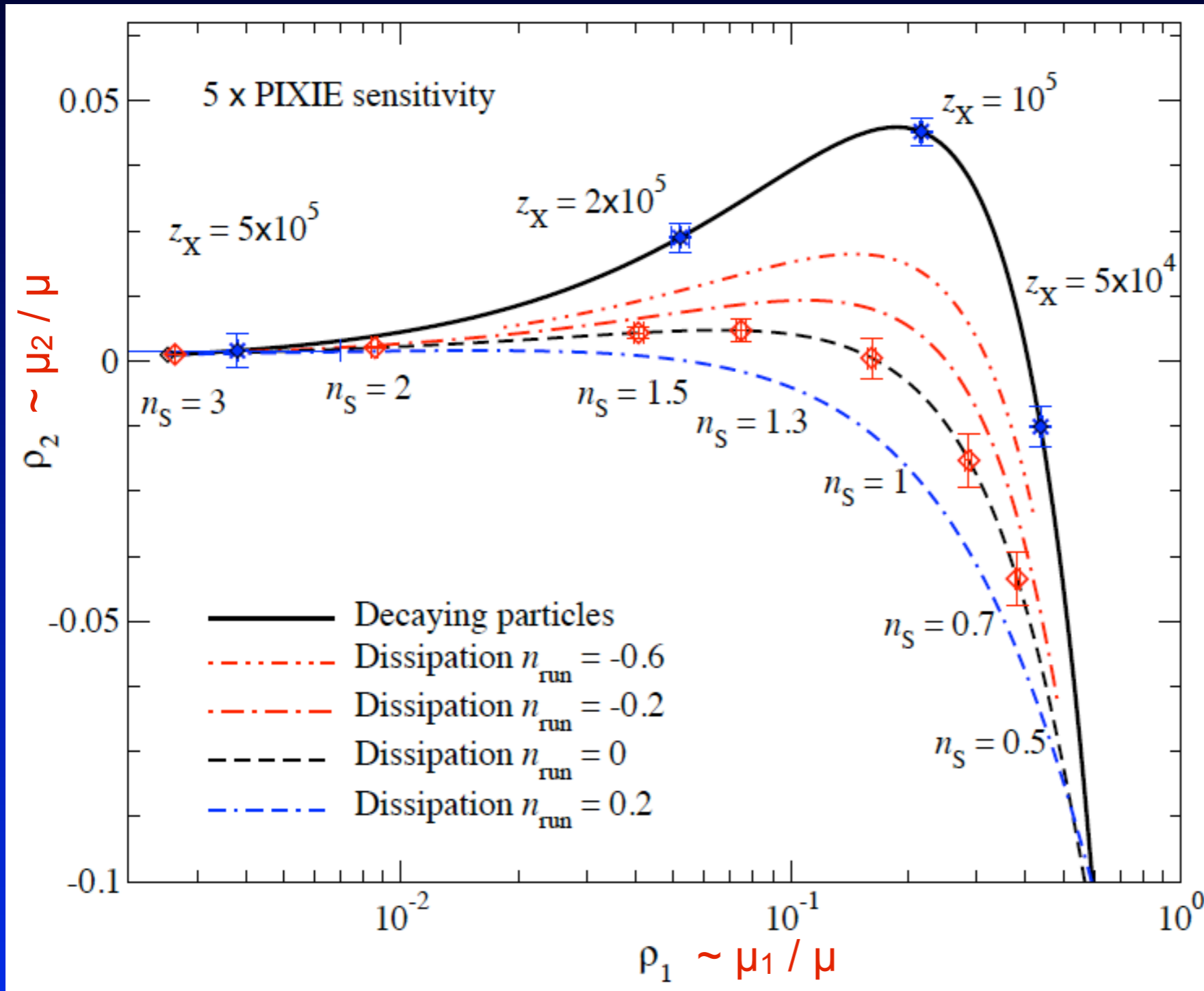
Distinguishing dissipation and decaying particle scenarios



- measurement of μ , μ_1 & μ_2
- trajectories of decaying particle and dissipation scenarios differ!
- scenarios can in principle be distinguished

$$A_\zeta = 5 \times 10^{-8}$$

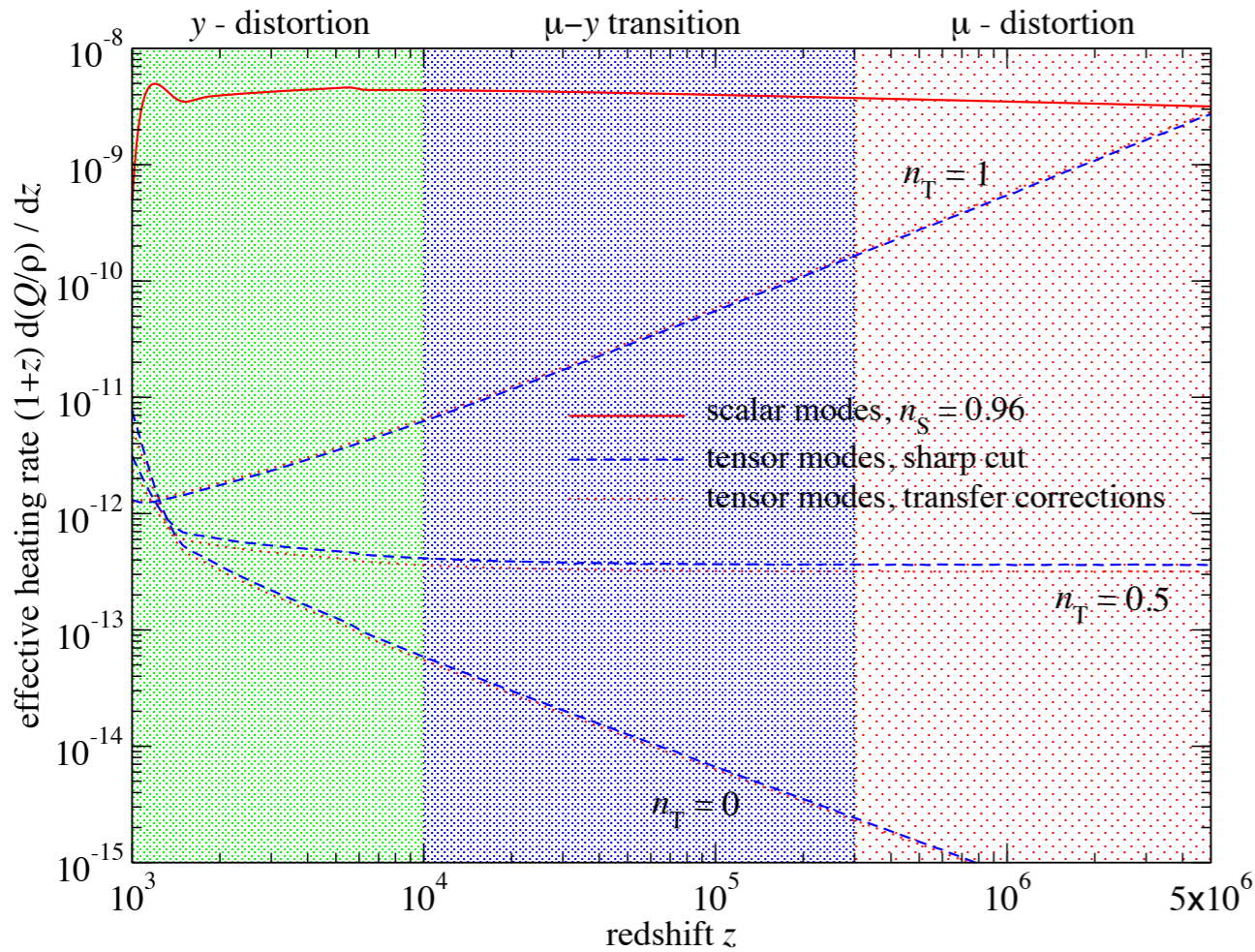
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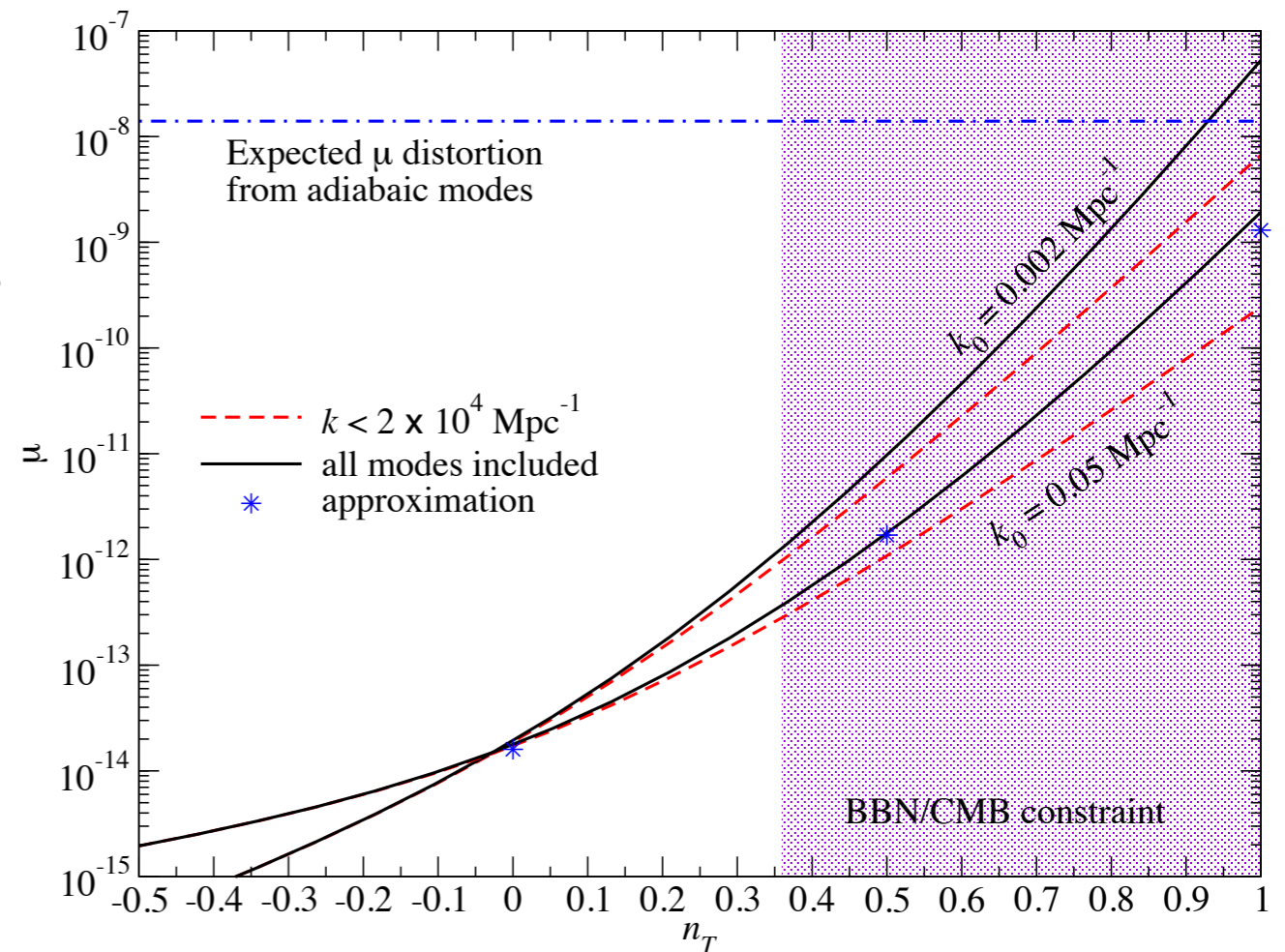
$$A_\zeta = 5 \times 10^{-8}$$

Dissipation of tensor perturbations

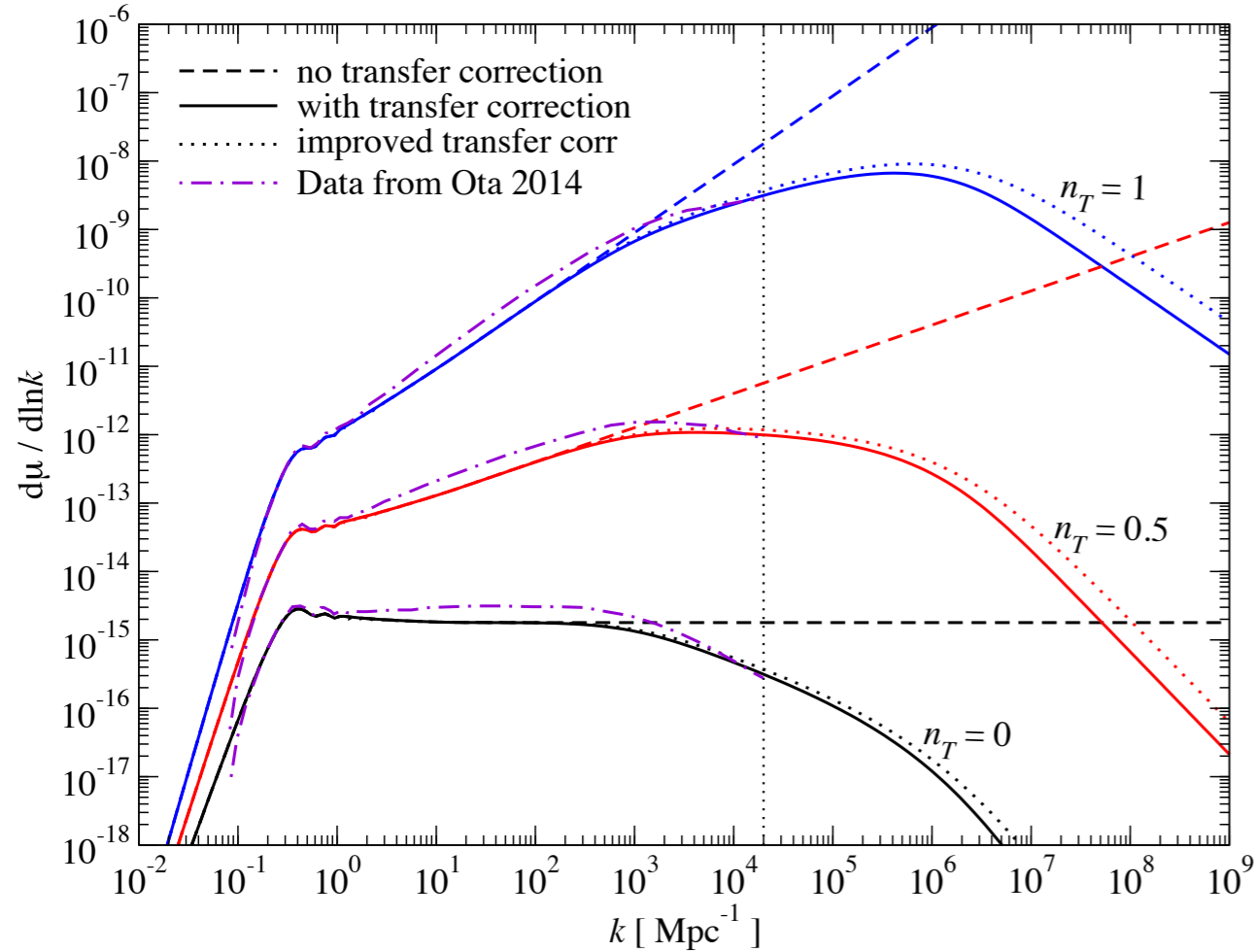


- heating rate can be computed similar to adiabatic modes
- heating rate much smaller than for scalar perturbations
- roughly constant per $d\ln z$ for $n_T \sim 0.5$

- distortion signal very small compared to adiabatic modes
- no severe *contamination* in simplest cases
- models with 'large' distortion already constrained by BBN/CMB



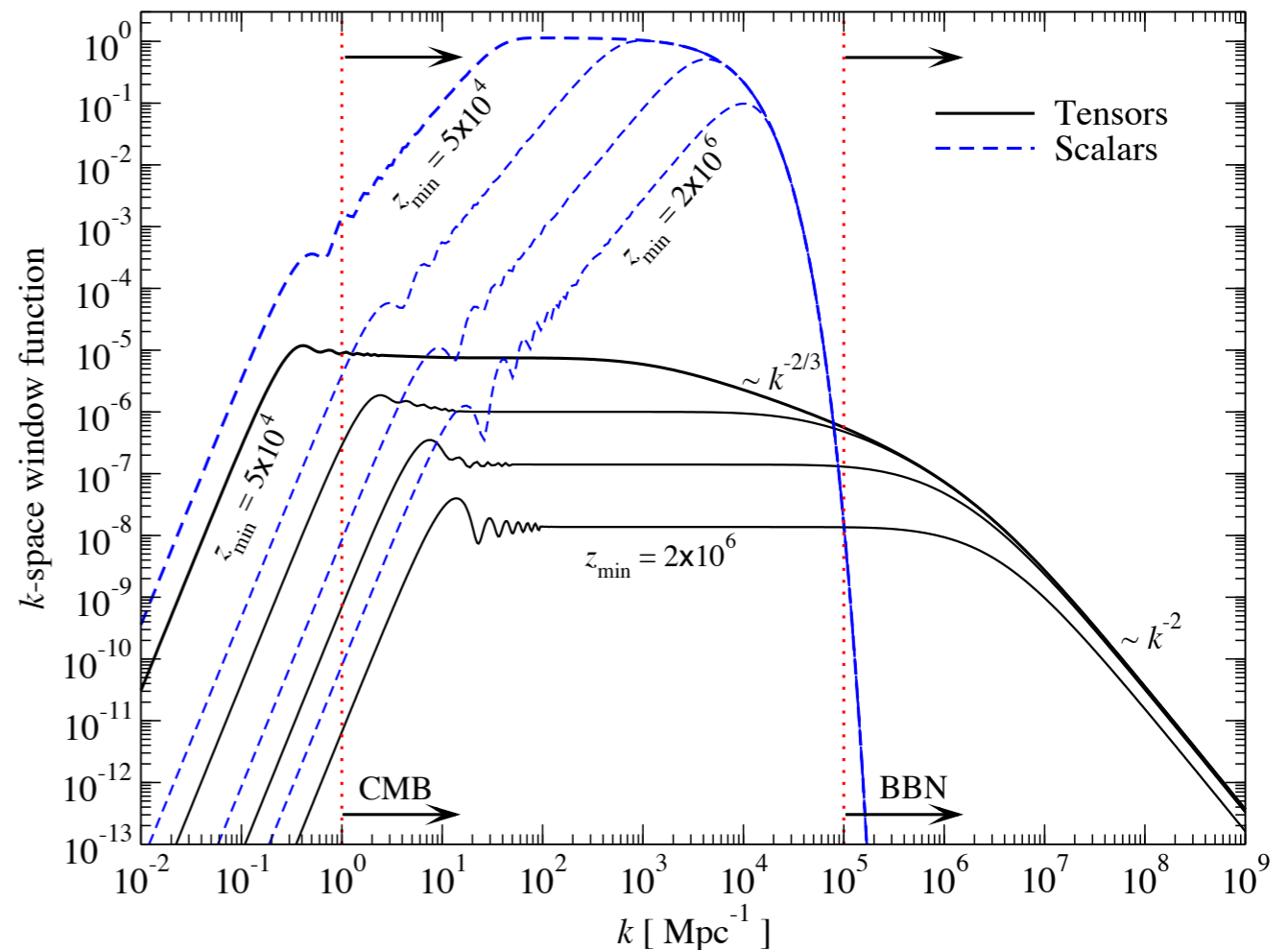
Comparison of the distortion window functions



- small-scale modes important for blue tensor power spectra
- Ota et al. underestimated distortion in this case ~ 7 times

$$\mu_i \approx \int_0^\infty \frac{k^2 dk}{2\pi^2} P_i(k) W_i(k)$$

- adiabatic modes sensitive to a smaller range of scales
- tensors even have contributions from close to the horizon scale
- power-law decay at small scales



The cosmological recombination radiation

Simple estimates for hydrogen recombination

Hydrogen recombination:

- per recombined hydrogen atom an energy of ~ 13.6 eV in form of photons is released
 - at $z \sim 1100 \rightarrow \Delta\varepsilon/\varepsilon \sim 13.6 \text{ eV } N_b / (N_\gamma 2.7kT_r) \sim 10^{-9} - 10^{-8}$
- recombination occurs at redshifts $z < 10^4$
- At that time the *thermalization* process doesn't work anymore!
- There should be some *small* spectral distortion due to additional Ly- α and 2s-1s photons!
- (Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278; Peebles, 1968, ApJ, 153, 1)
- In 1975 **Viktor Dubrovich** emphasized the possibility to observe the recombinational lines from $n > 3$ and $\Delta n \ll n$!

First recombination computations completed in 1968!



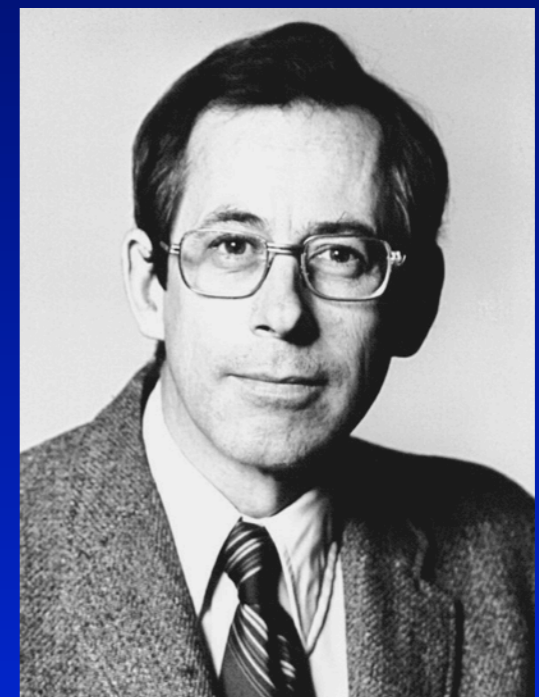
Yakov Zeldovich

Moscow

Princeton



Rashid Sunyaev

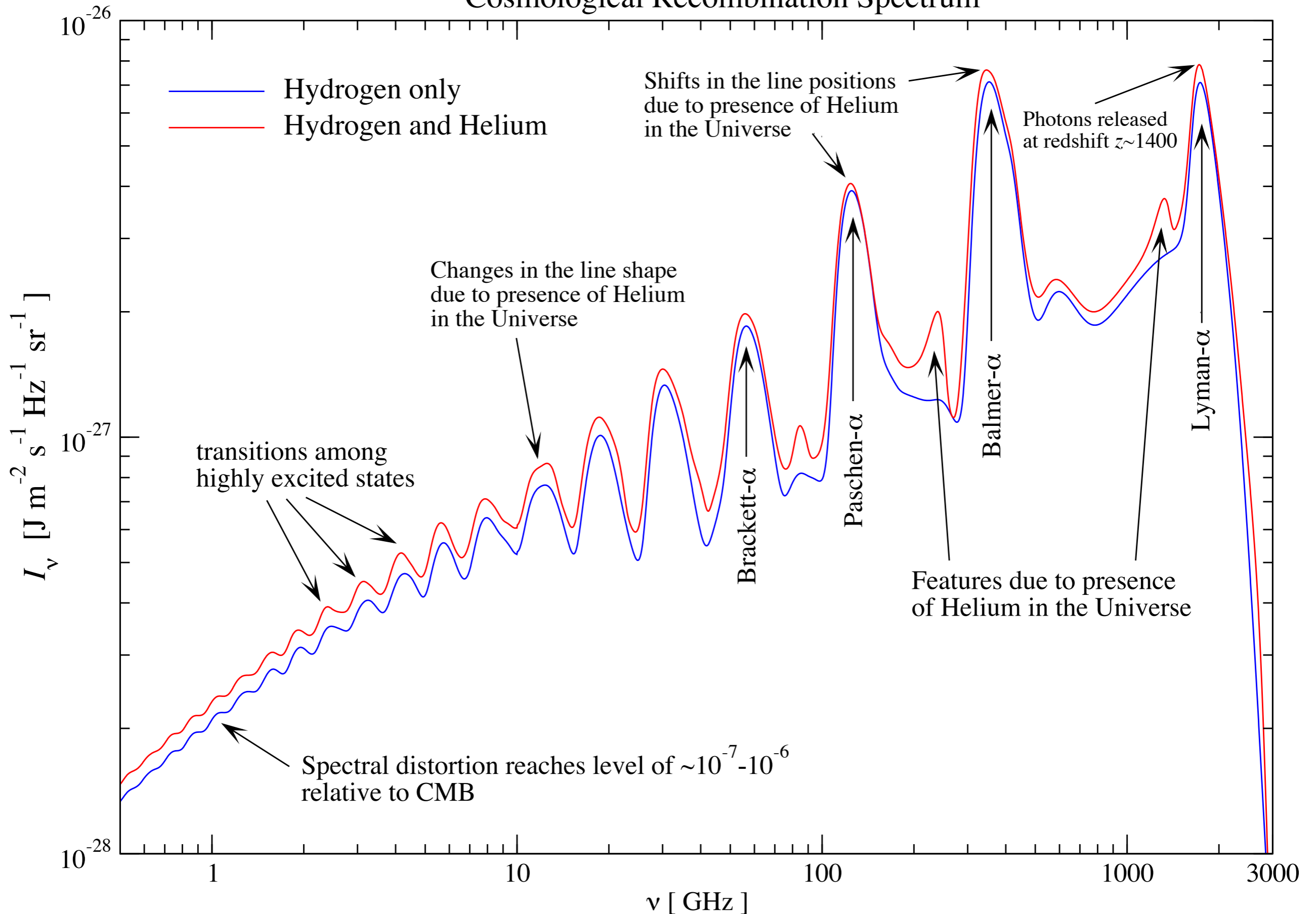


Jim Peebles

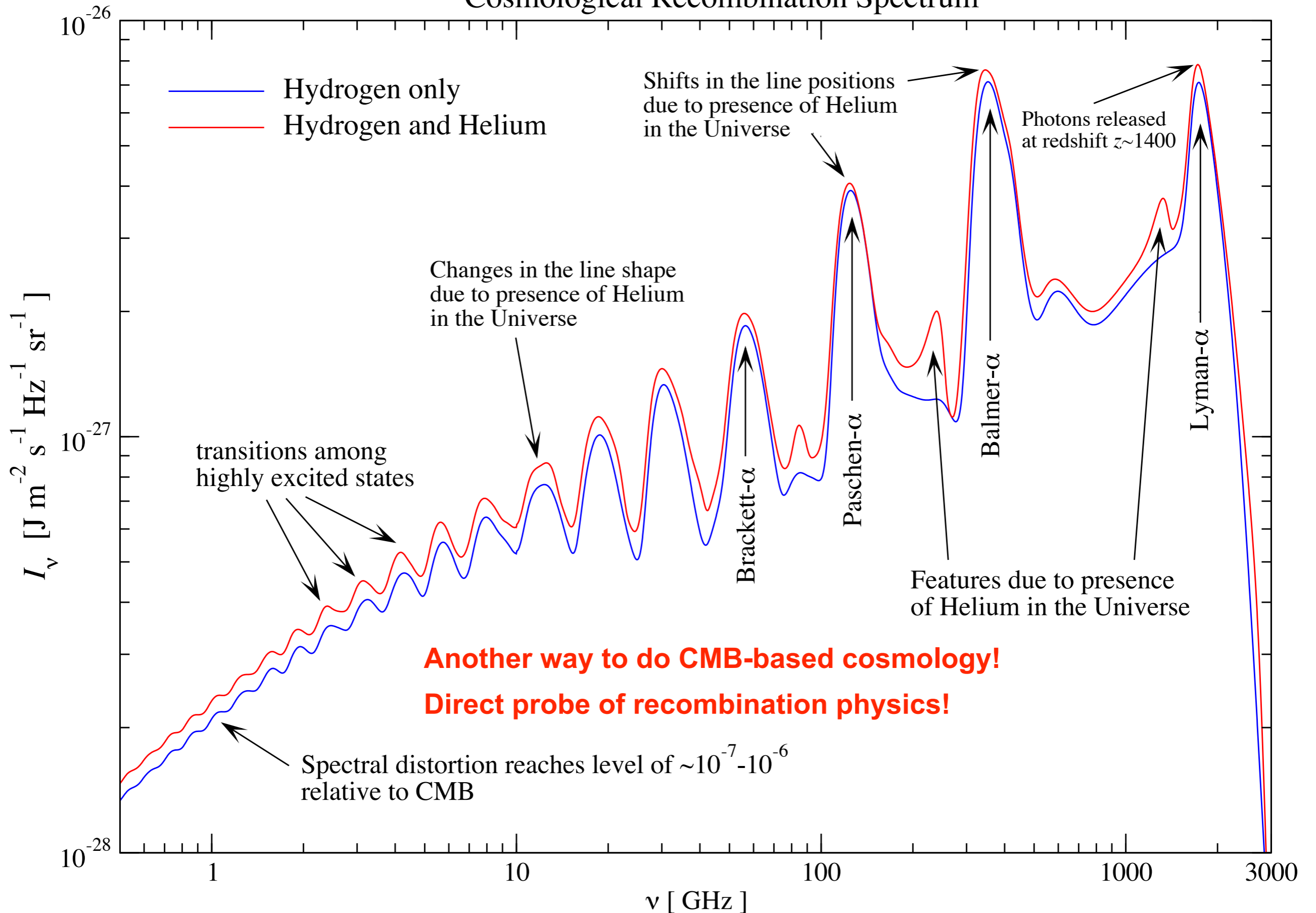


Vladimir Kurt
(UV astronomer)

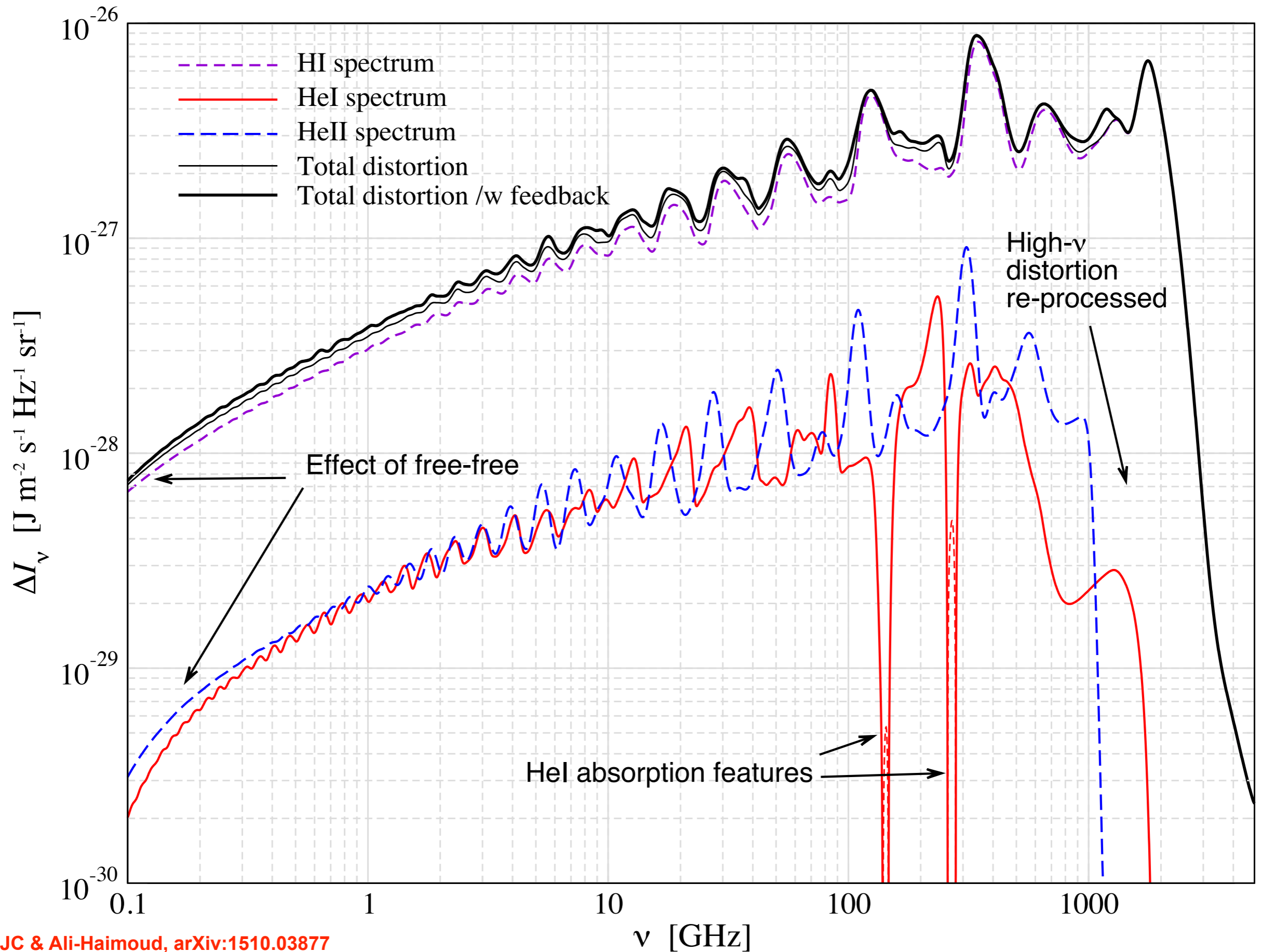
Cosmological Recombination Spectrum



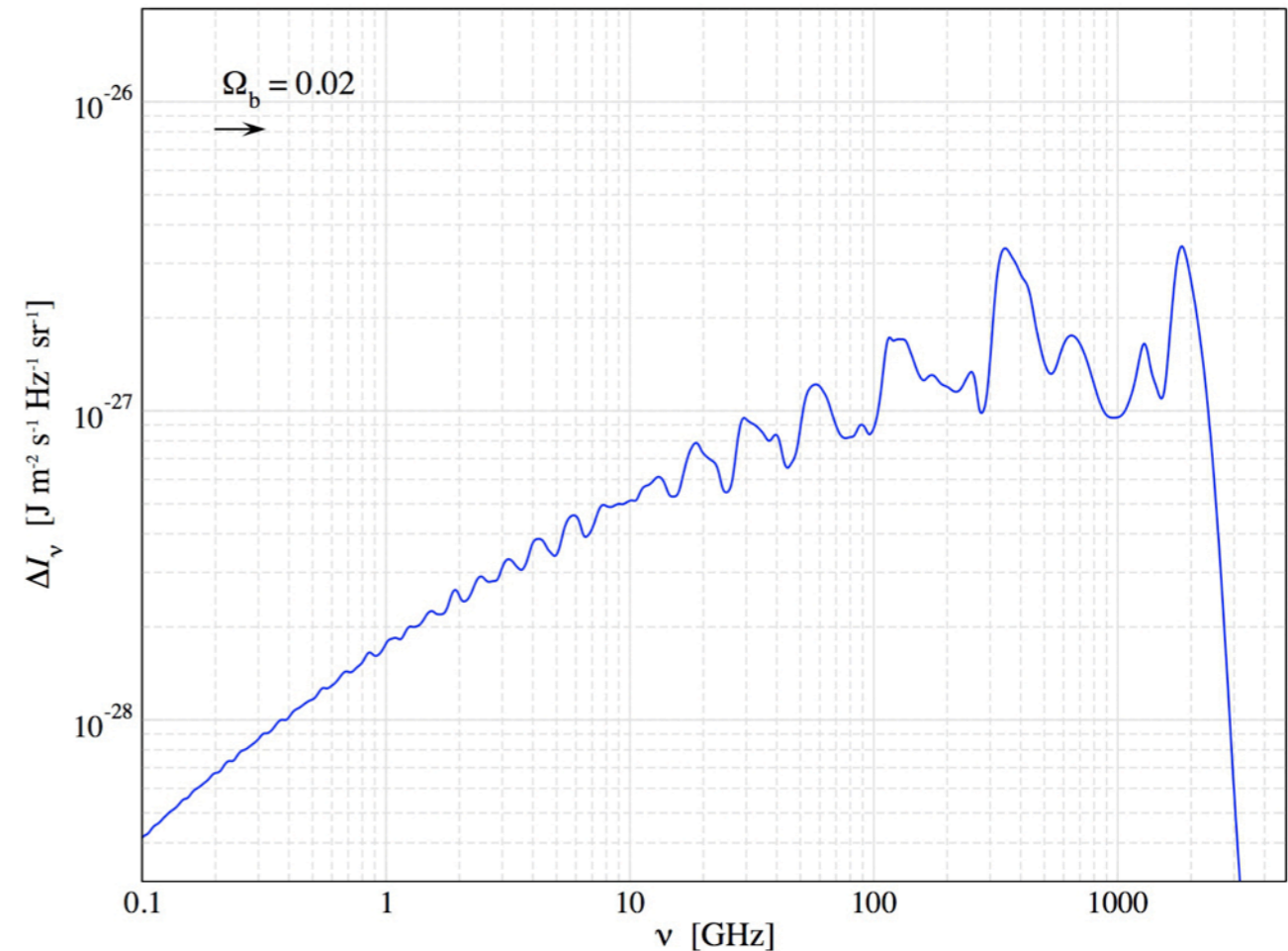
Cosmological Recombination Spectrum



New detailed and fast computation!



CosmoSpec: fast and accurate computation of the CRR

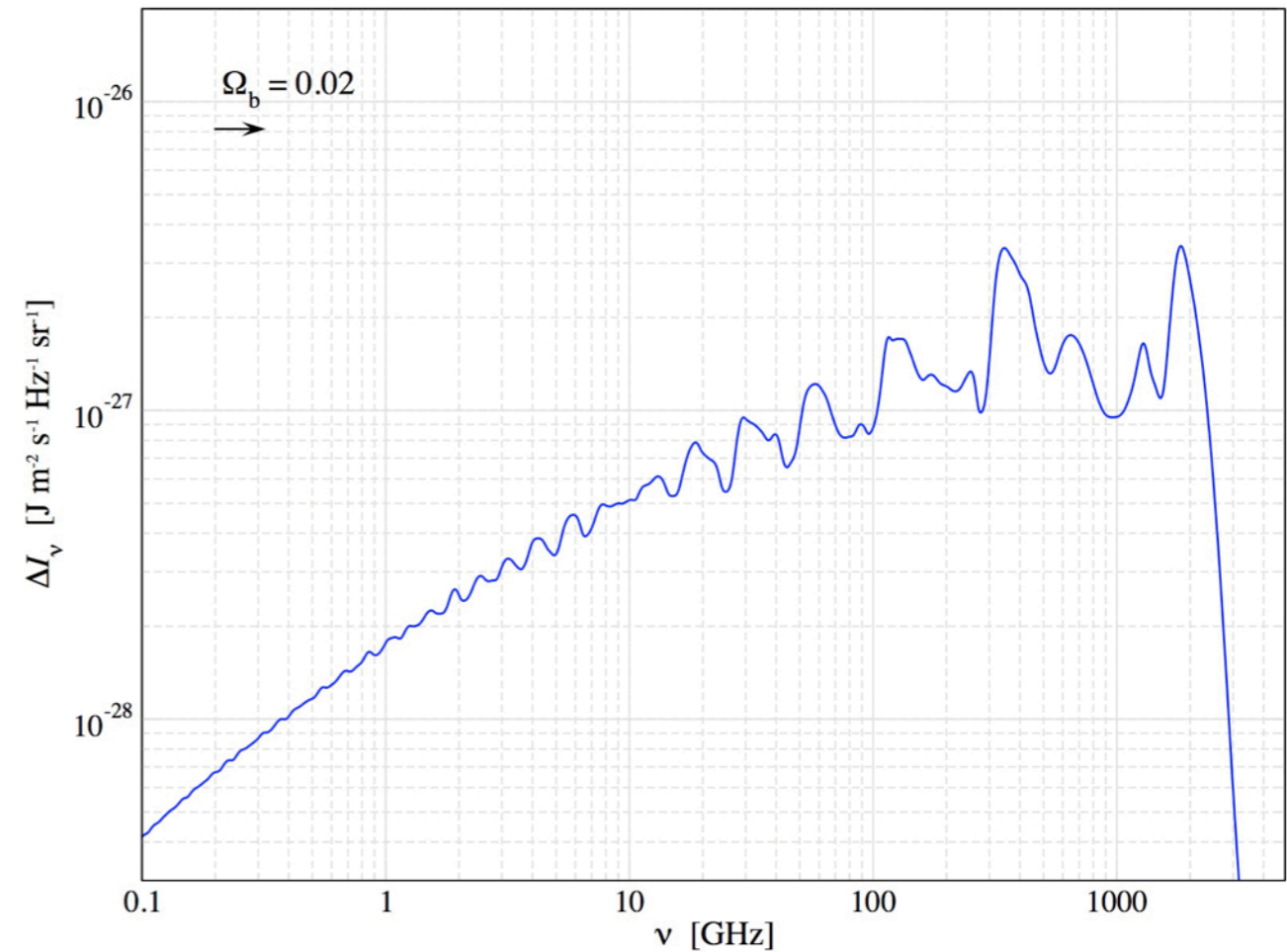
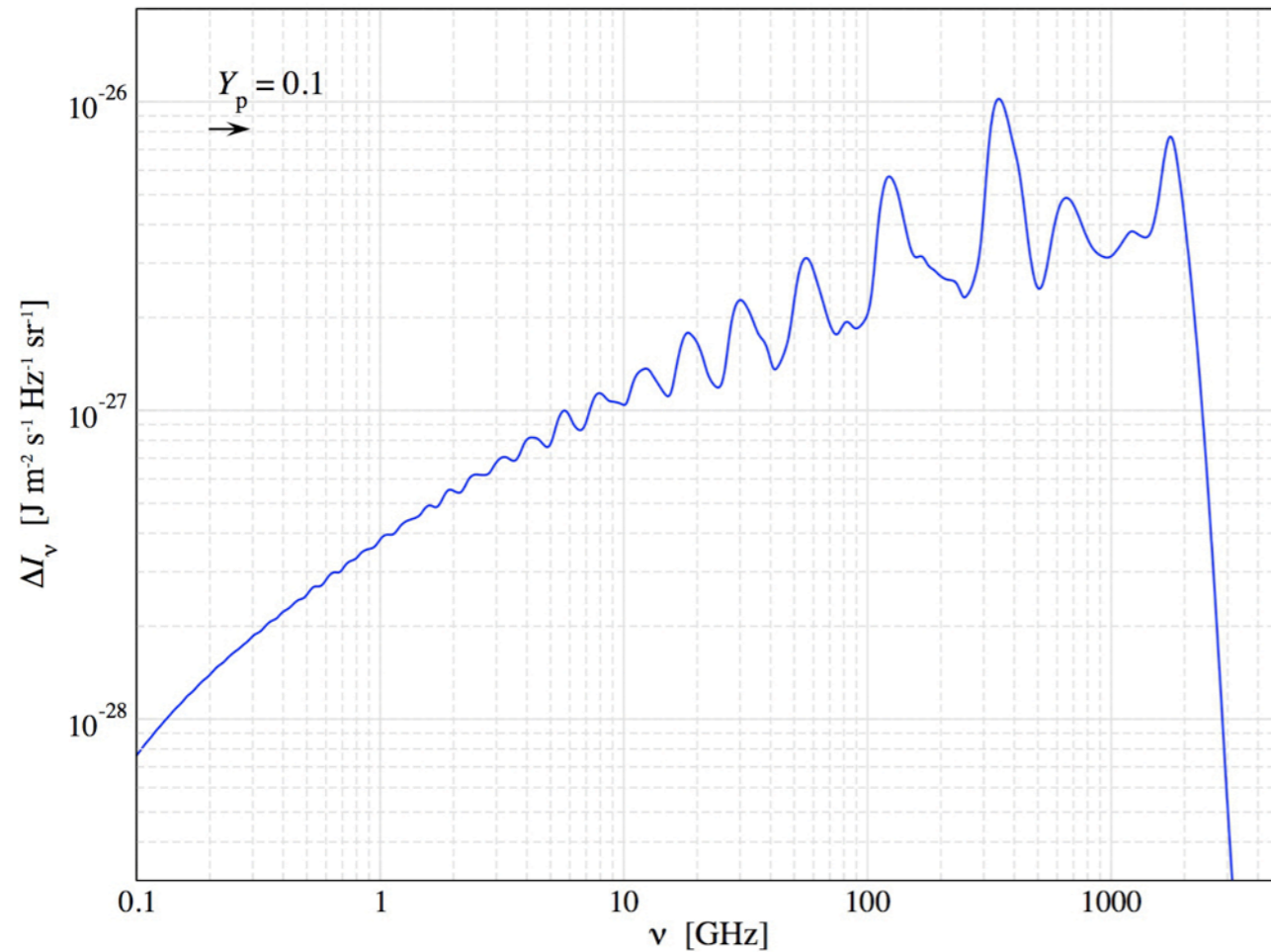


- Like in old days of CMB anisotropies!
- detailed forecasts and feasibility studies
- non-standard physics (variation of α , energy injection etc.)

CosmoSpec will be available here:

www.Chluba.de/CosmoSpec

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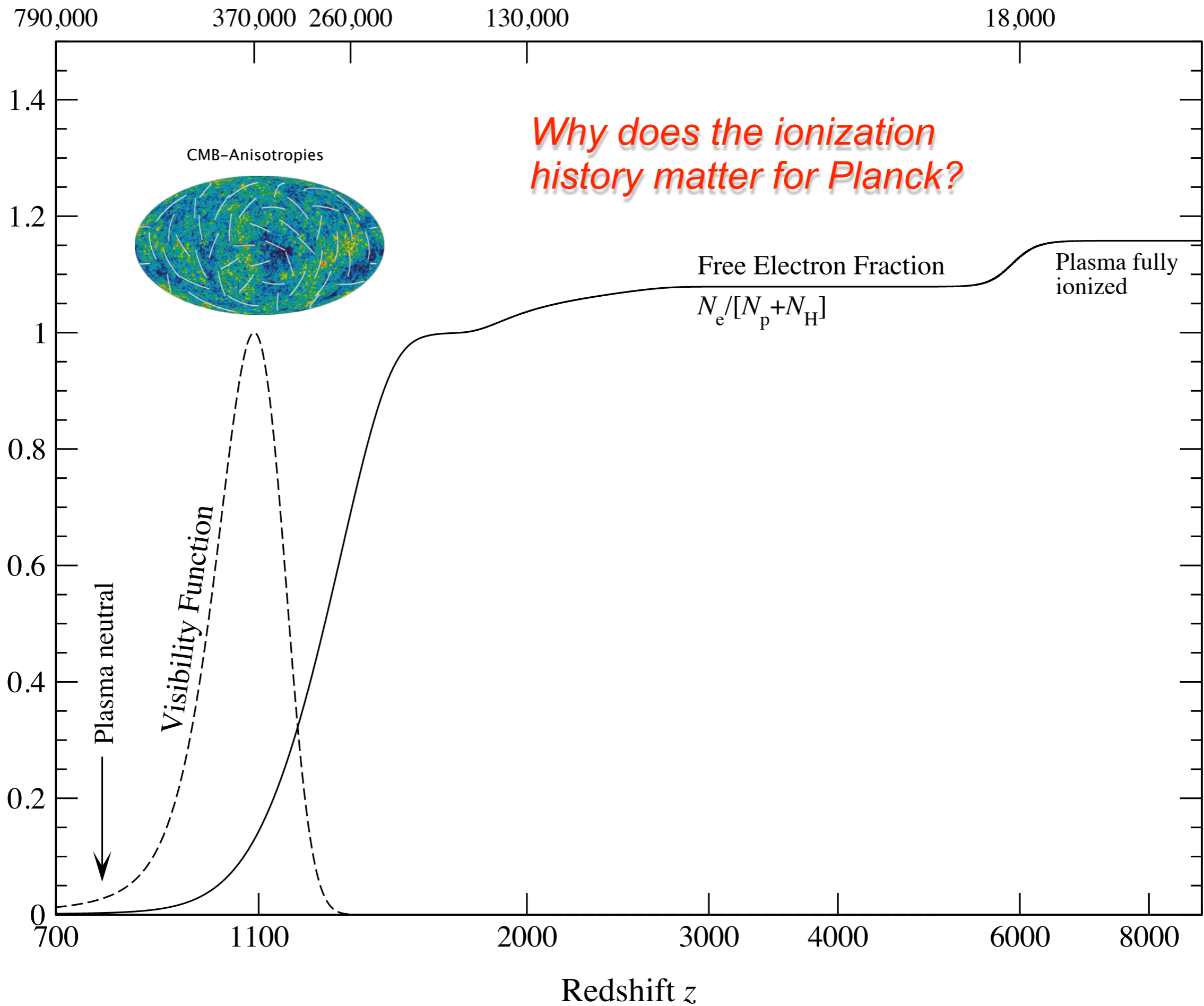


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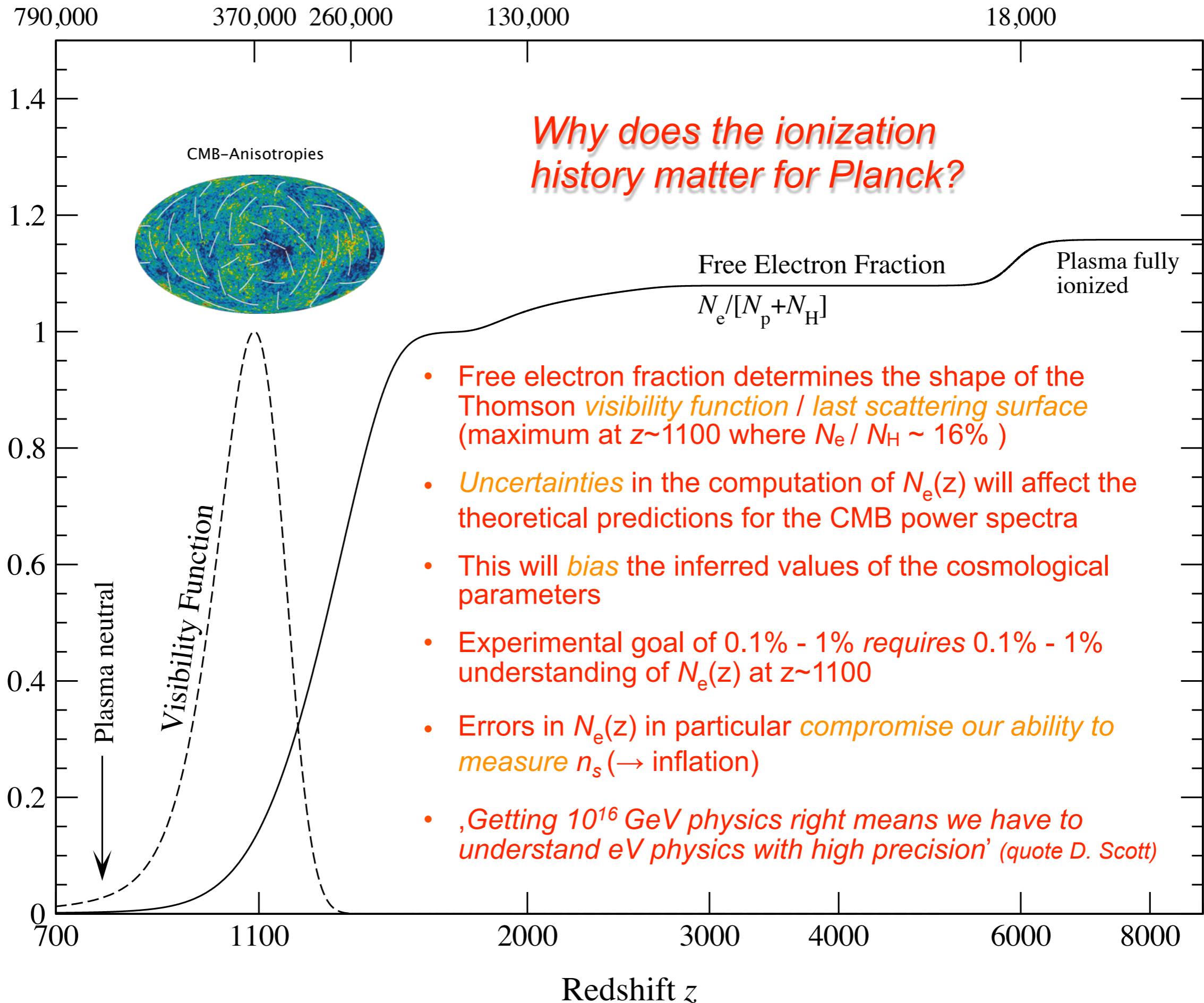
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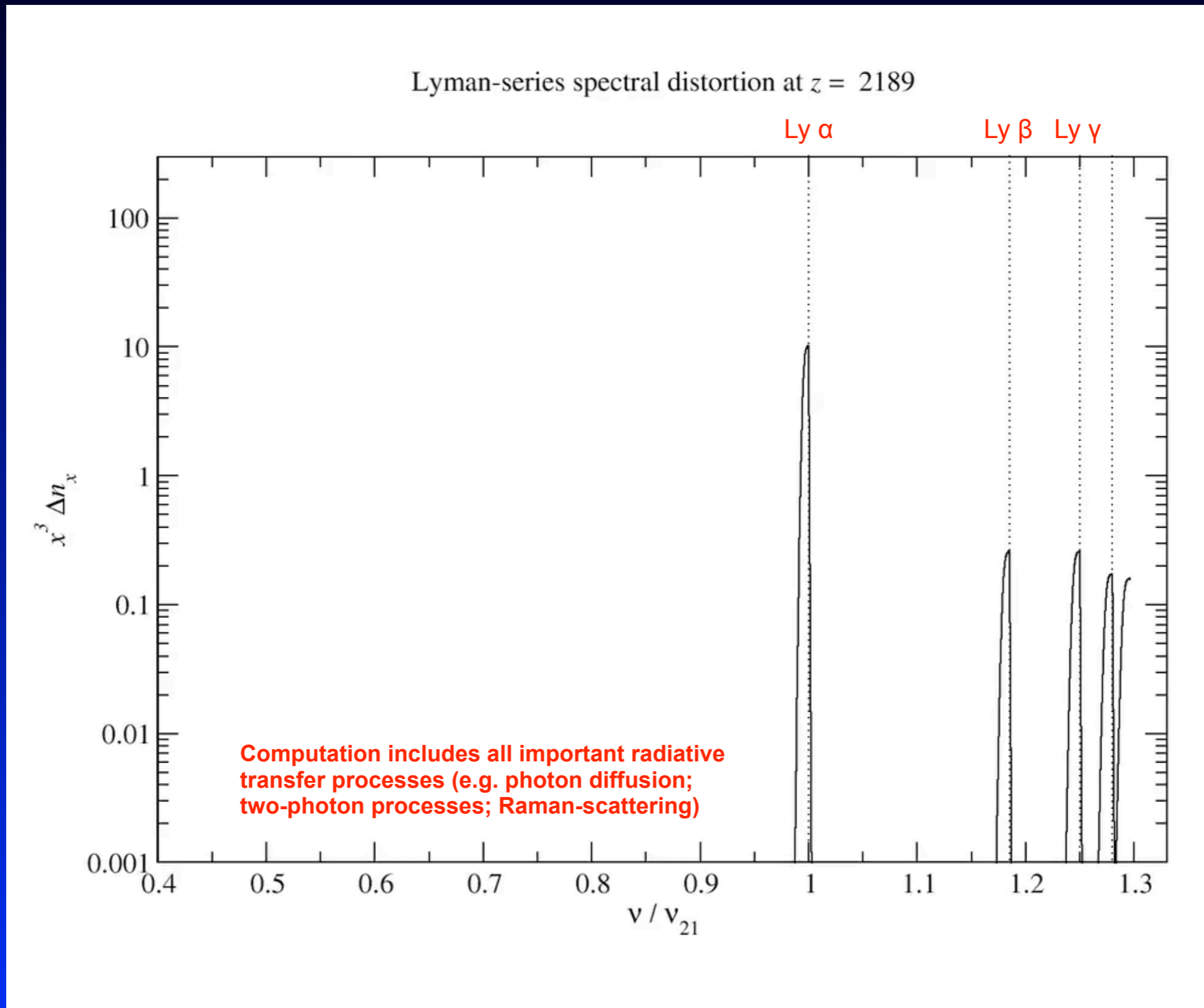
Cosmological Time in Years



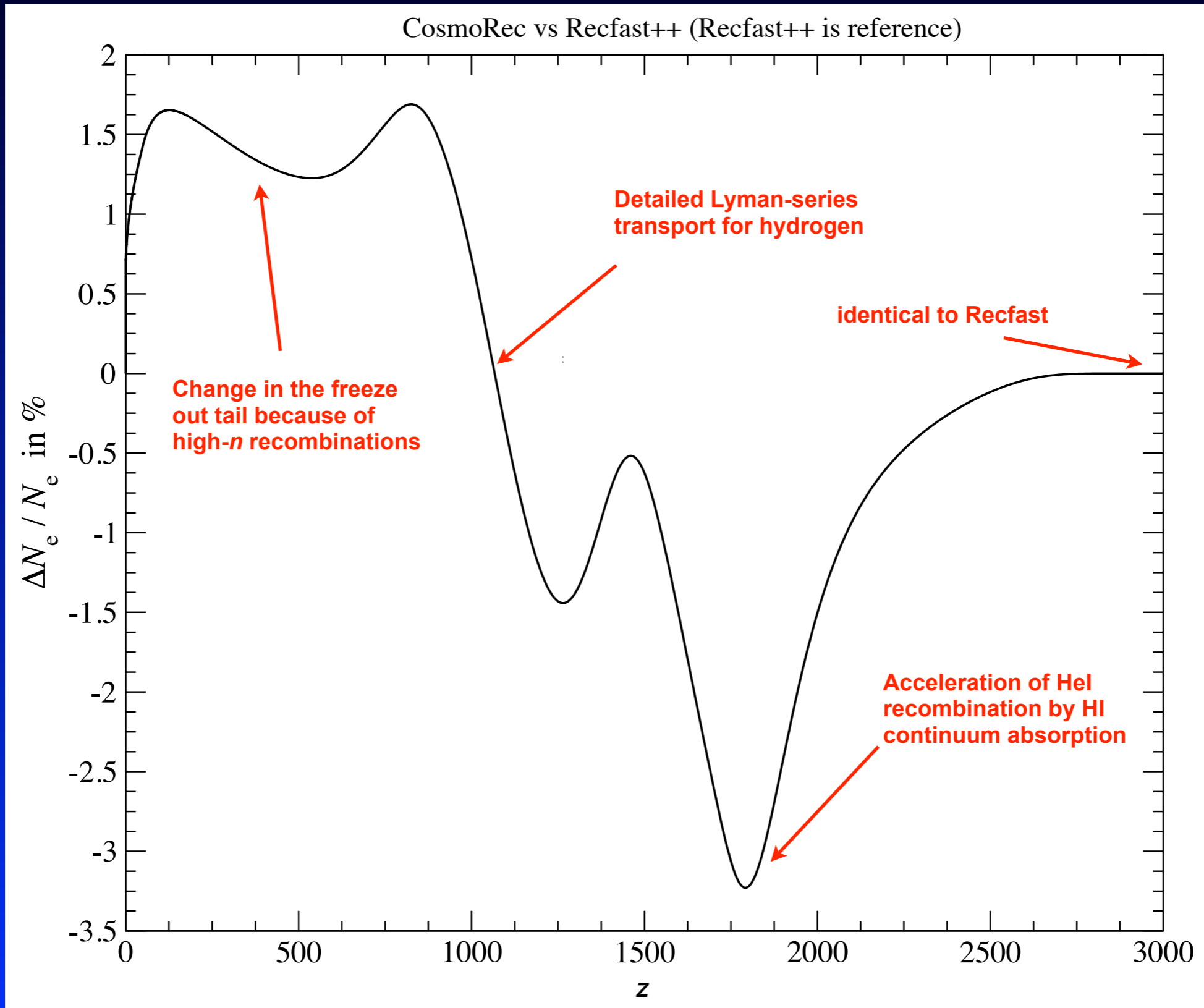
Cosmological Time in Years



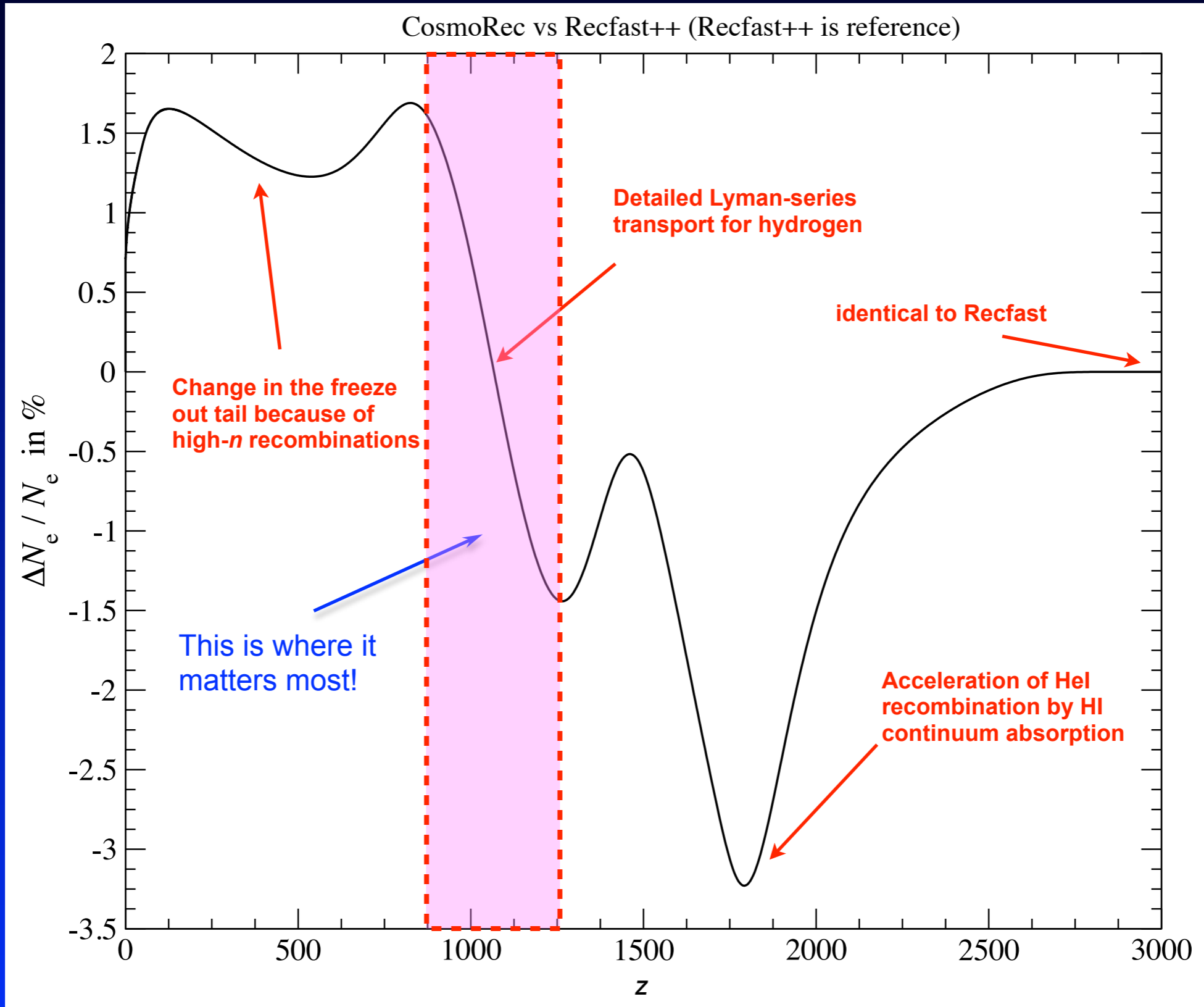
Evolution of the HI Lyman-series distortion



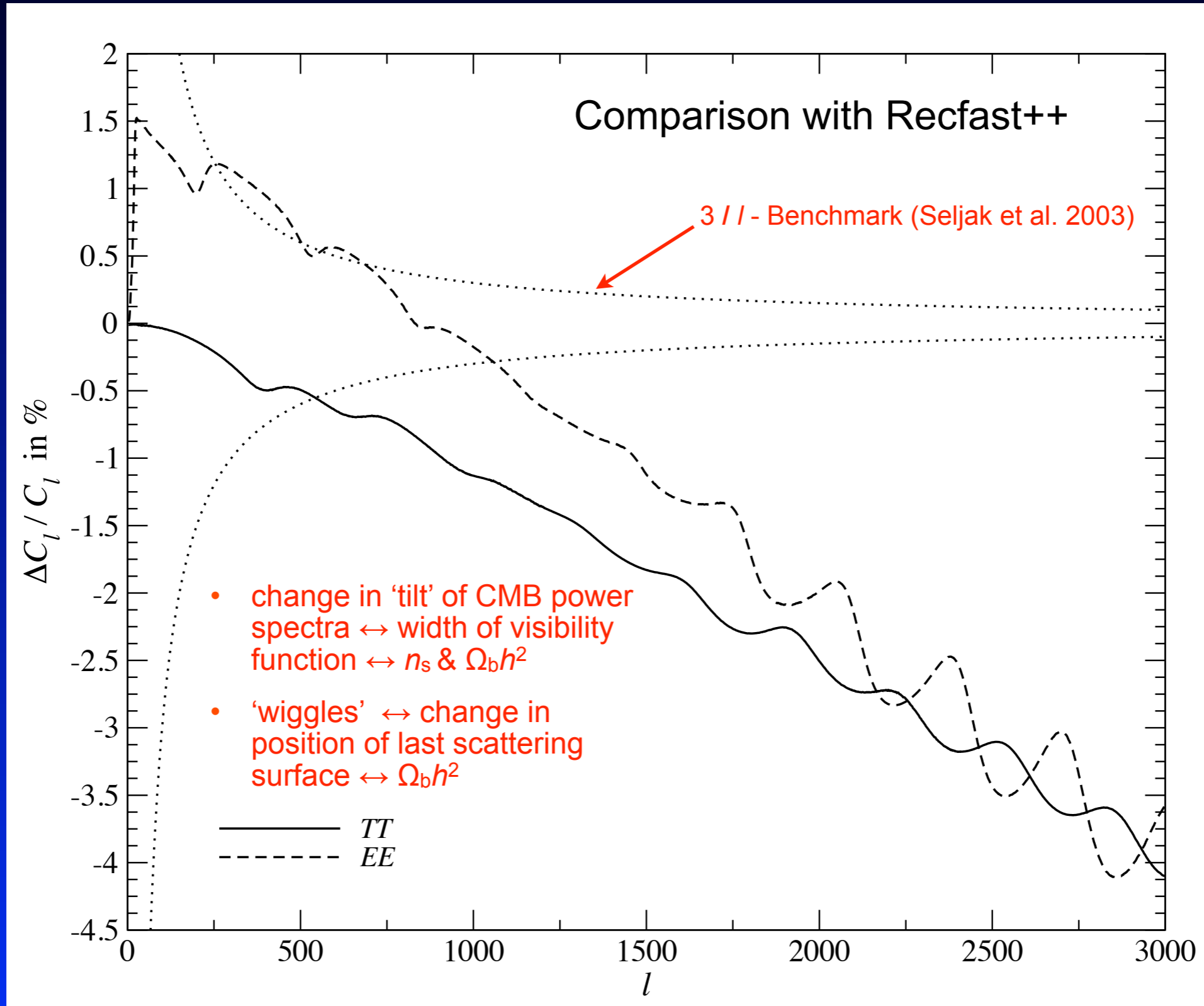
Cumulative Changes to the Ionization History



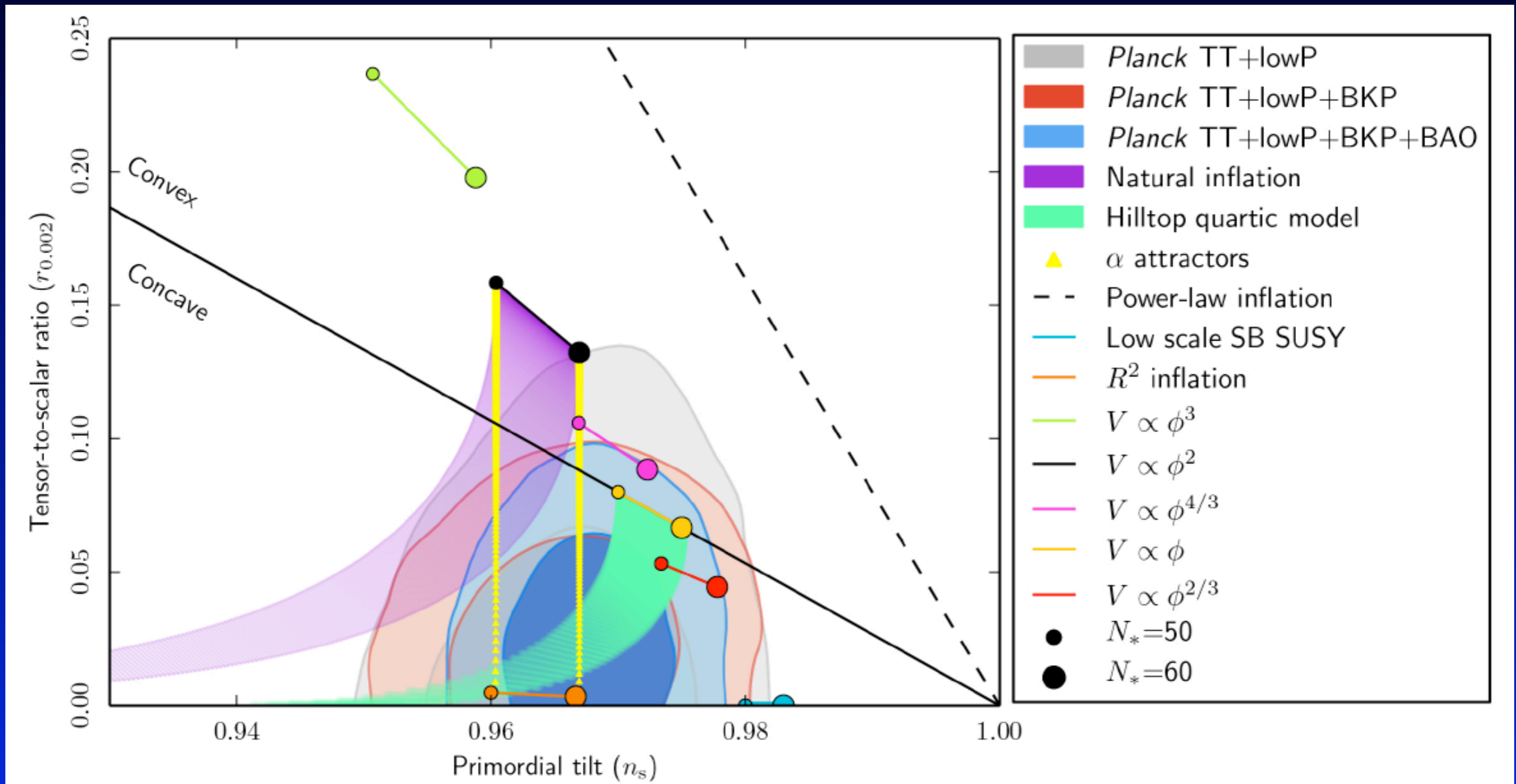
Cumulative Changes to the Ionization History



Cumulative Change in the CMB Power Spectra



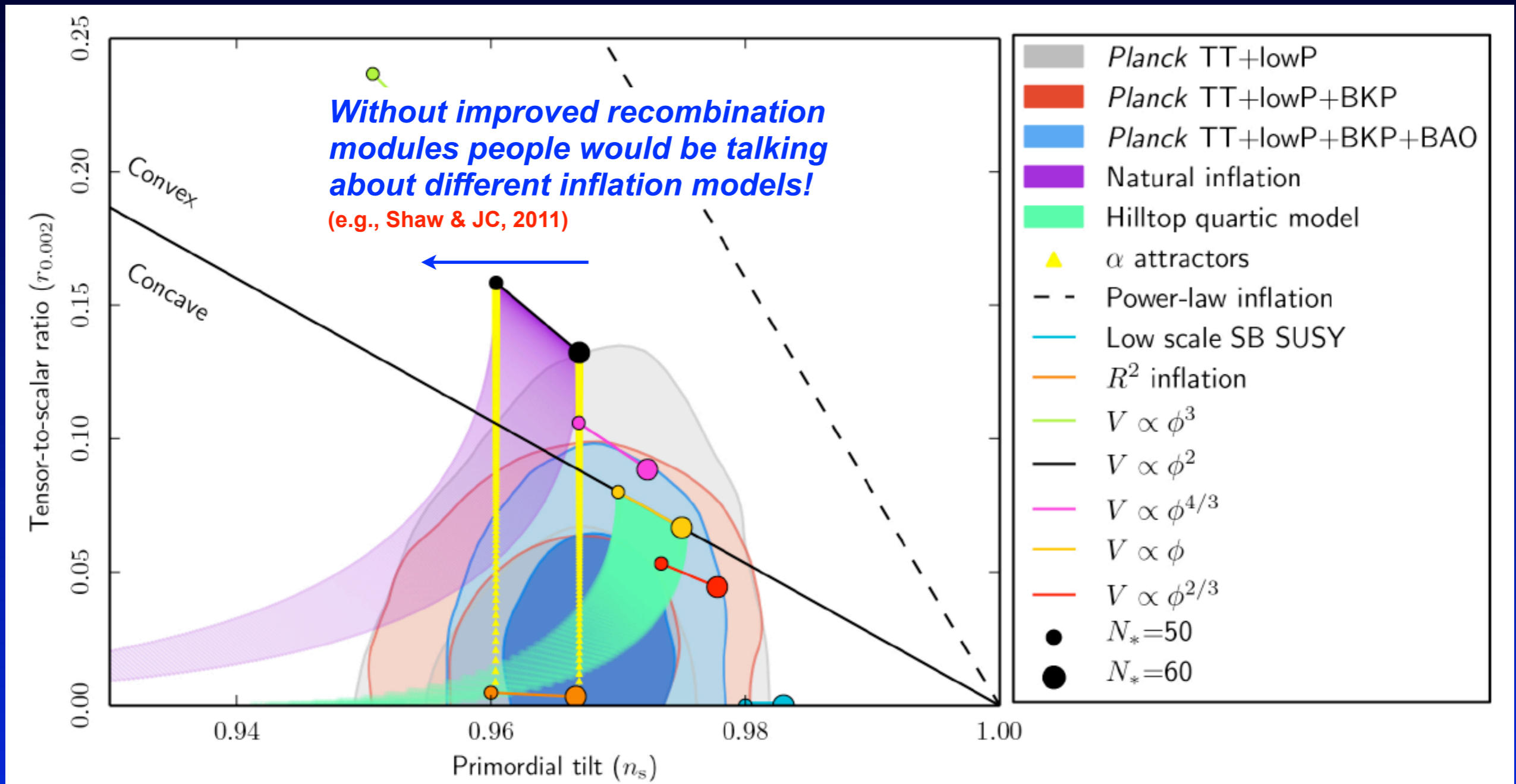
Importance of recombination for inflation constraints



Planck Collaboration, 2015, paper XX

- Analysis uses refined recombination model (CosmoRec/HyRec)

Importance of recombination for inflation constraints

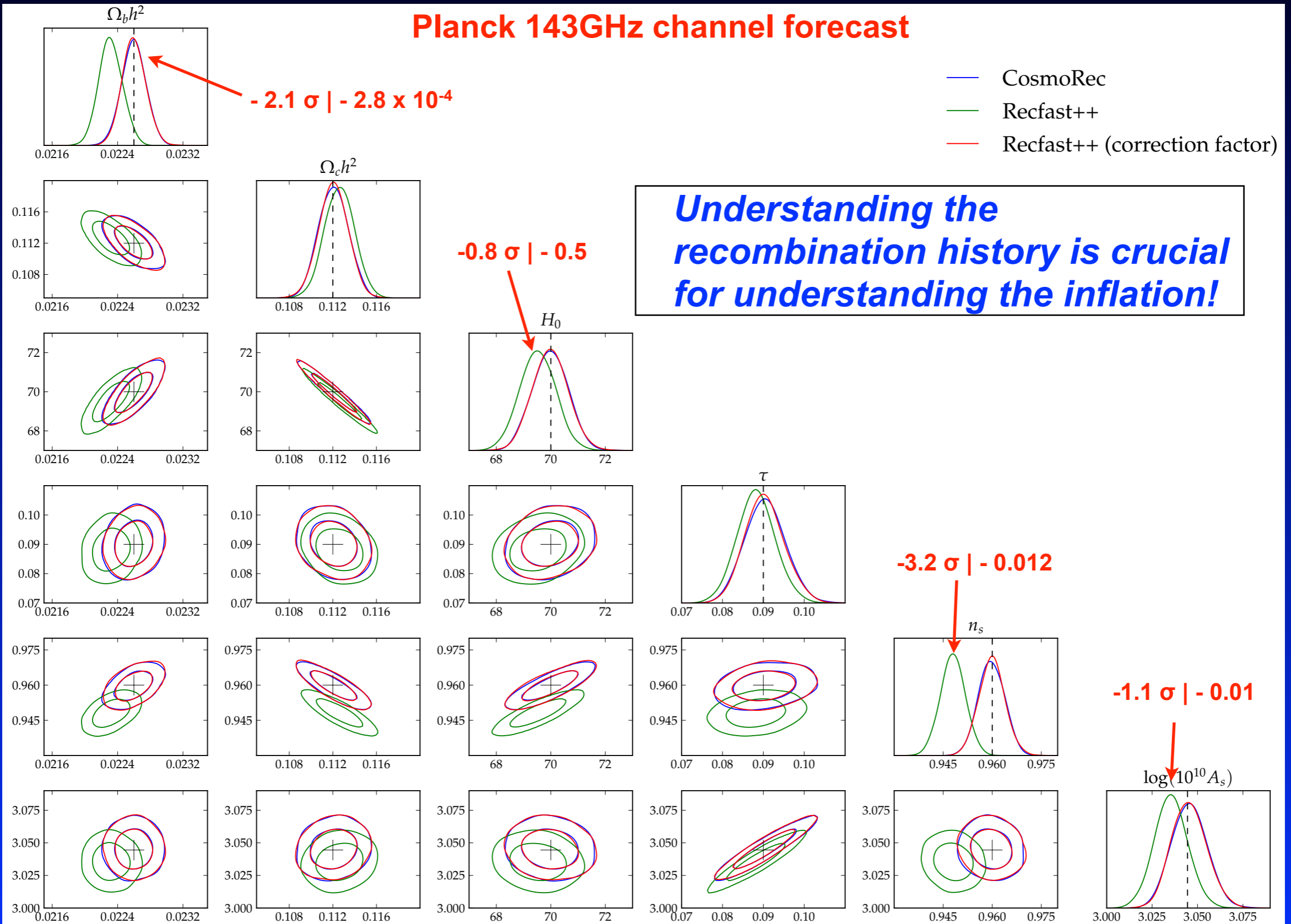


Planck Collaboration, 2015, paper XX

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Importance of recombination

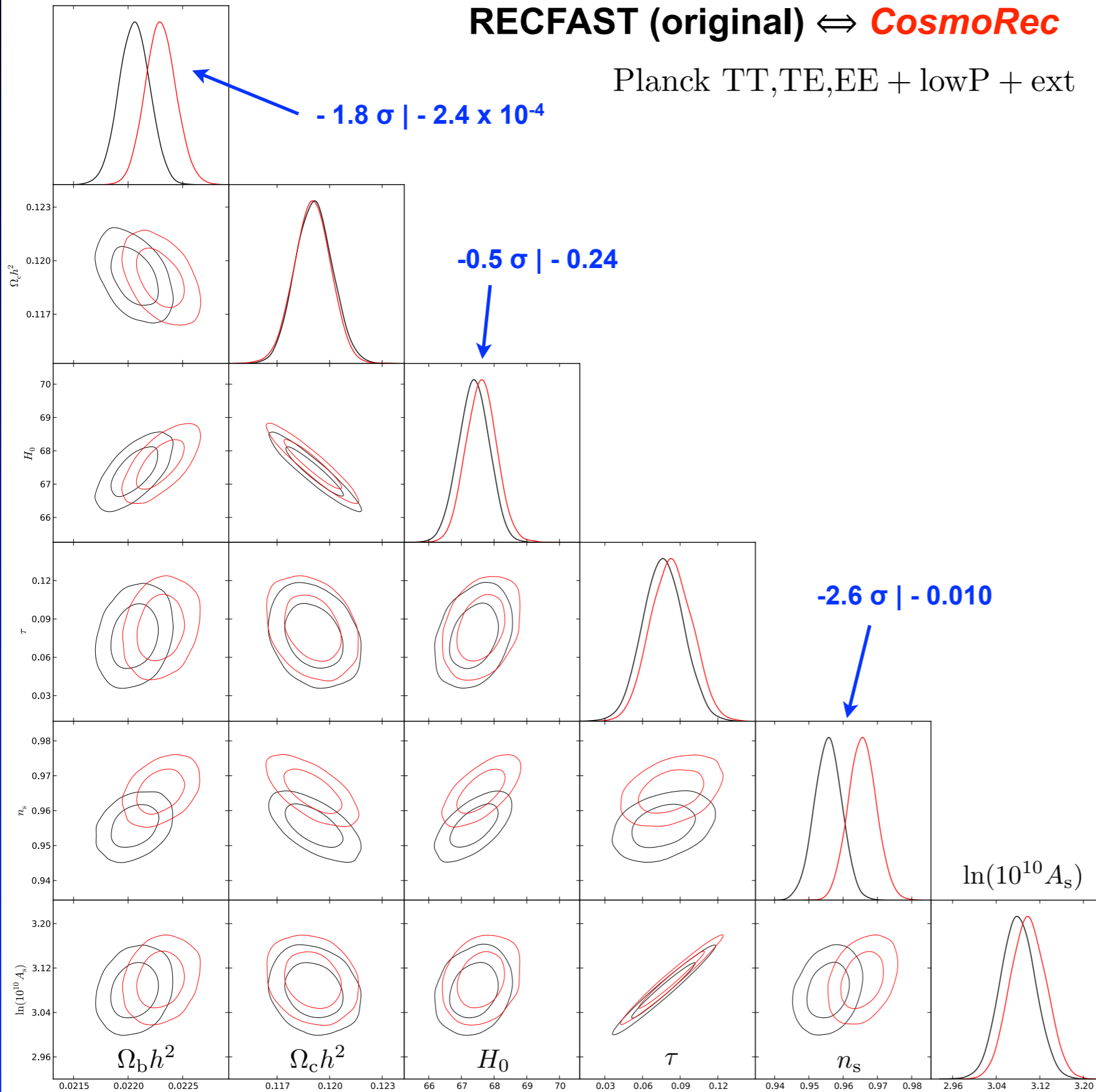
Planck 143GHz channel forecast



Biases as they *would* have been for *Planck*

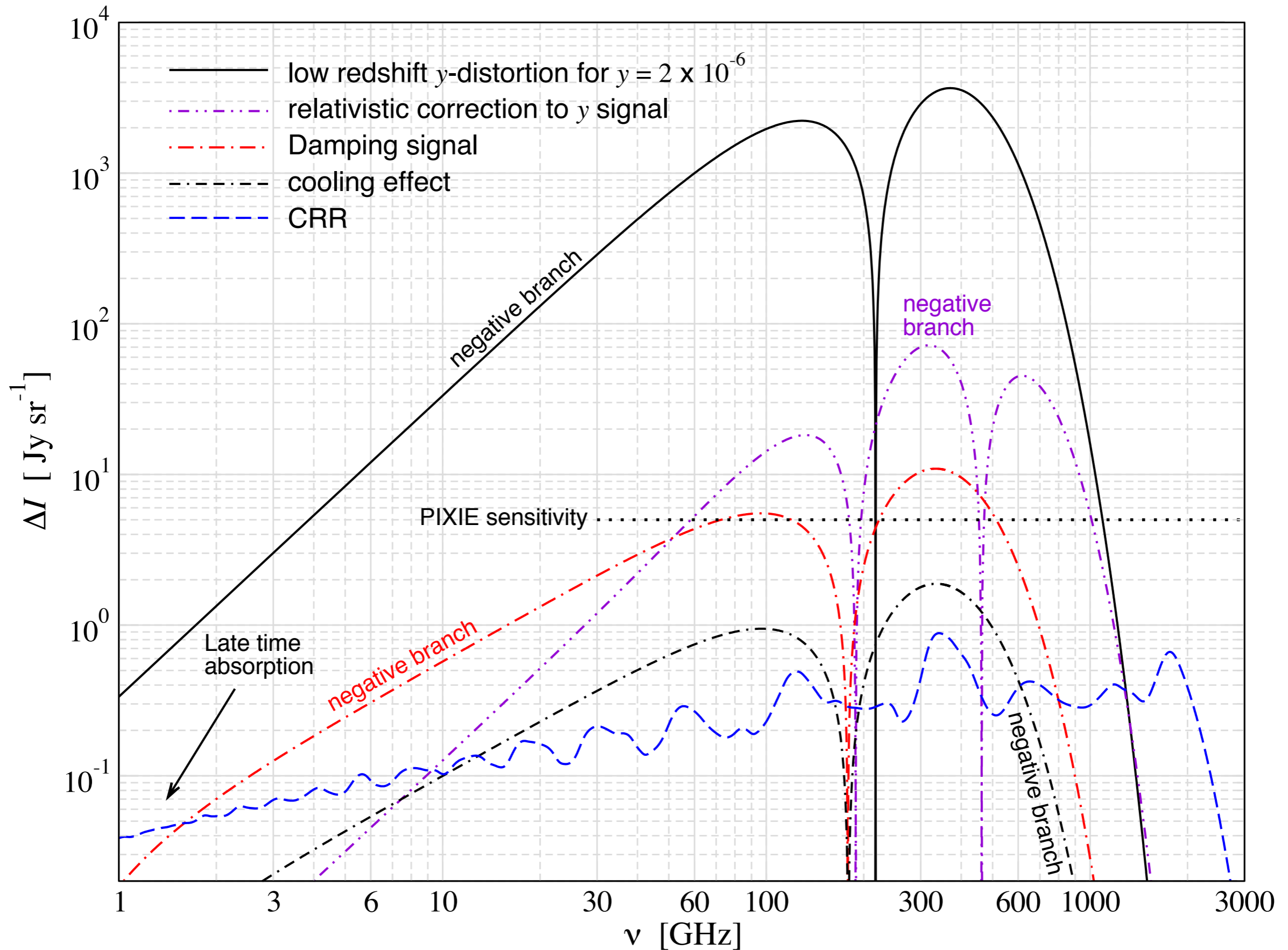
RECFAST (original) \Leftrightarrow **CosmoRec**

Planck TT,TE,EE + lowP + ext

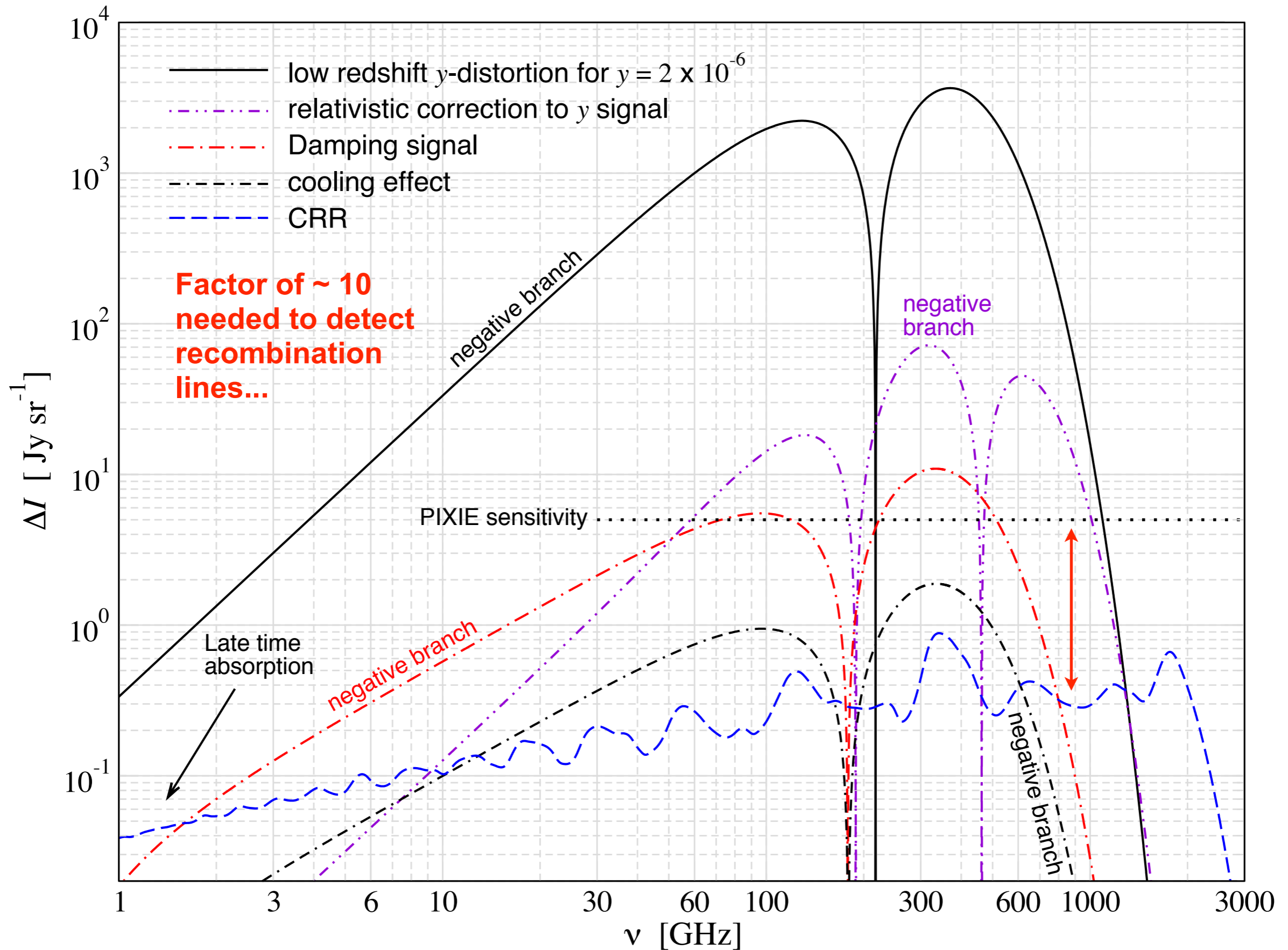


- Biases a little less significant with real *Planck* data
- absolute biases very similar
- In particular n_s would be biased significantly

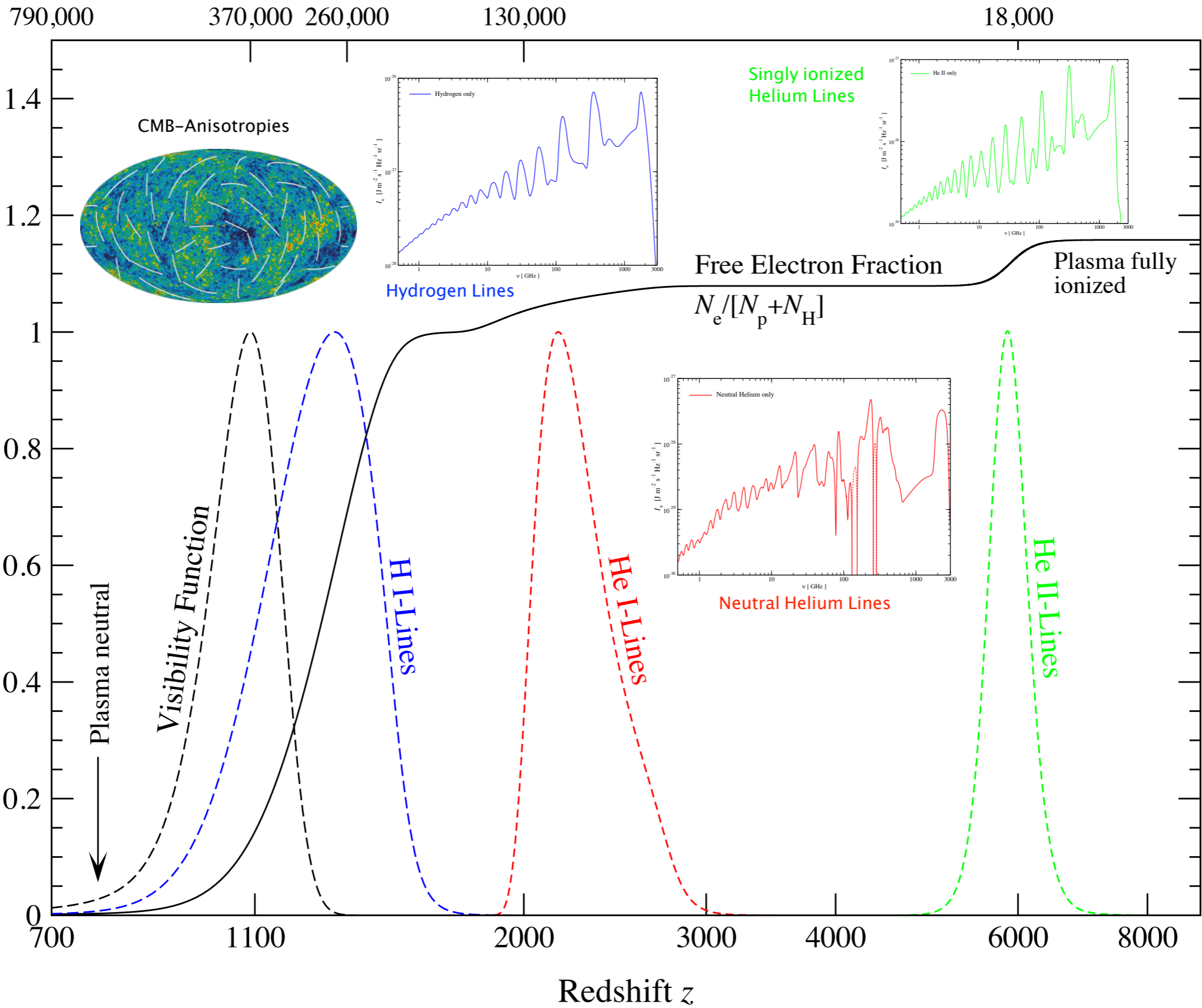
Average CMB spectral distortions



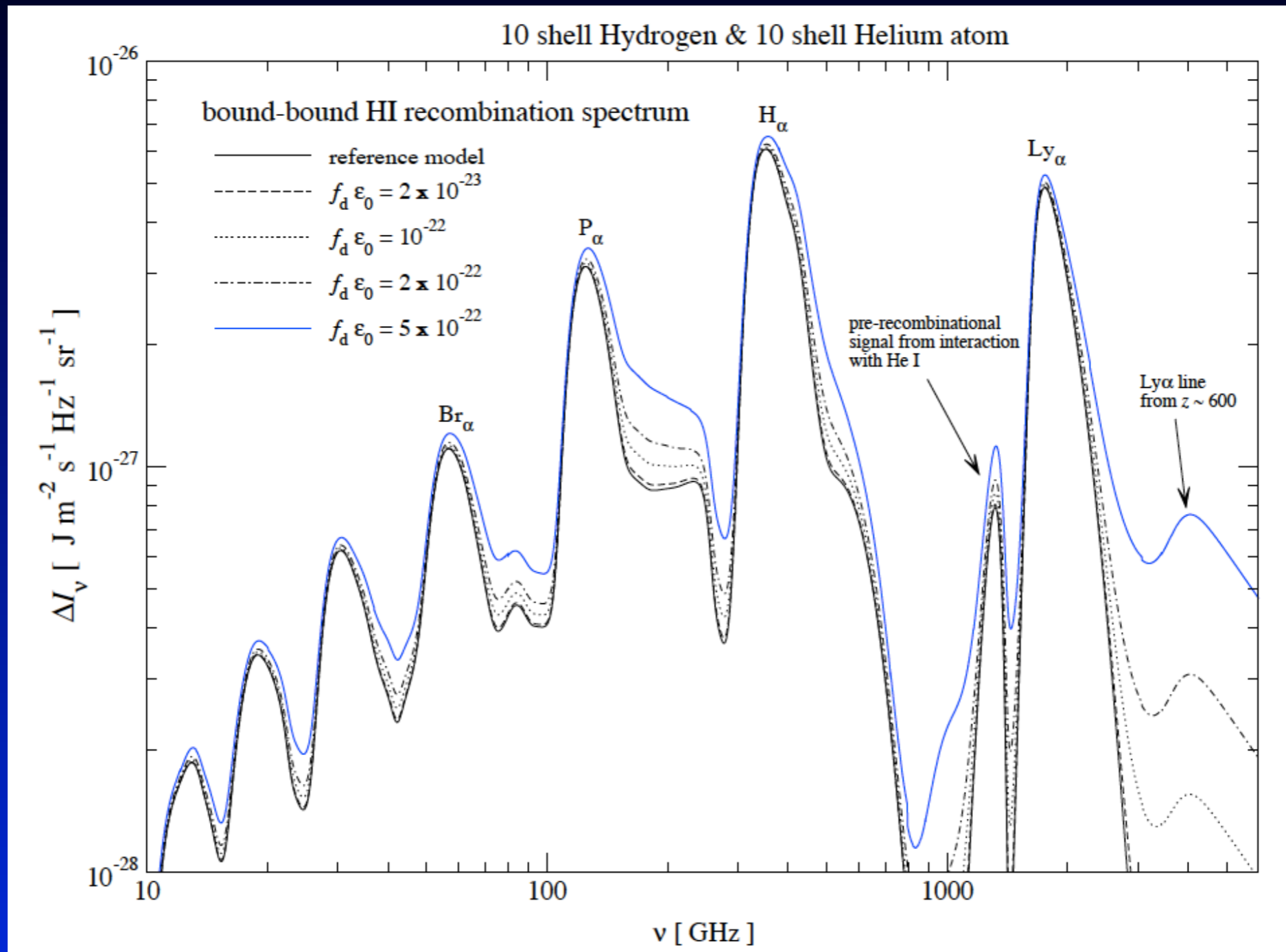
Average CMB spectral distortions



Cosmological Time in Years



Dark matter annihilations / decays



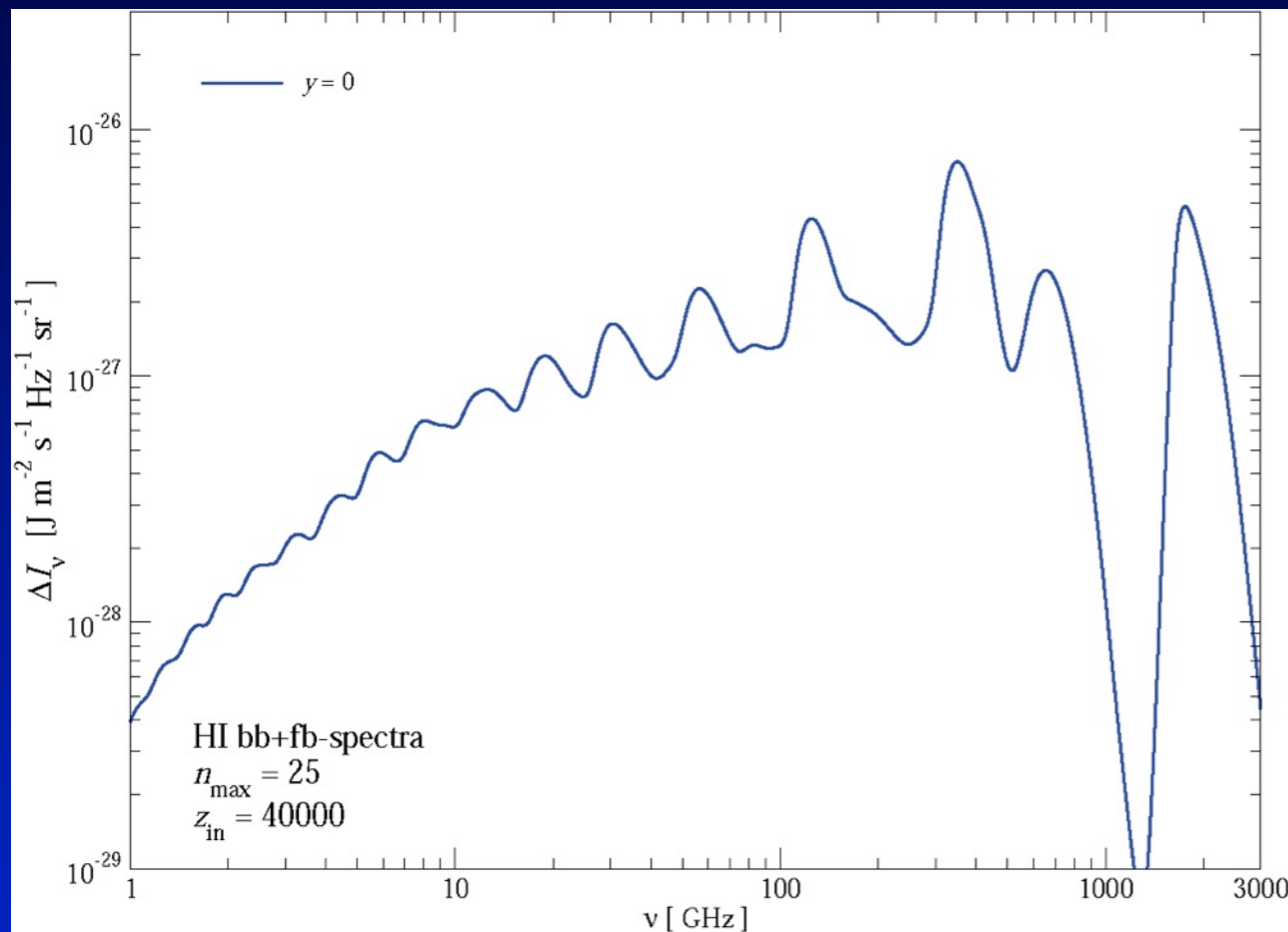
JC, 2009, arXiv:0910.3663

- Additional photons at all frequencies
- Broadening of spectral features
- Shifts in the positions

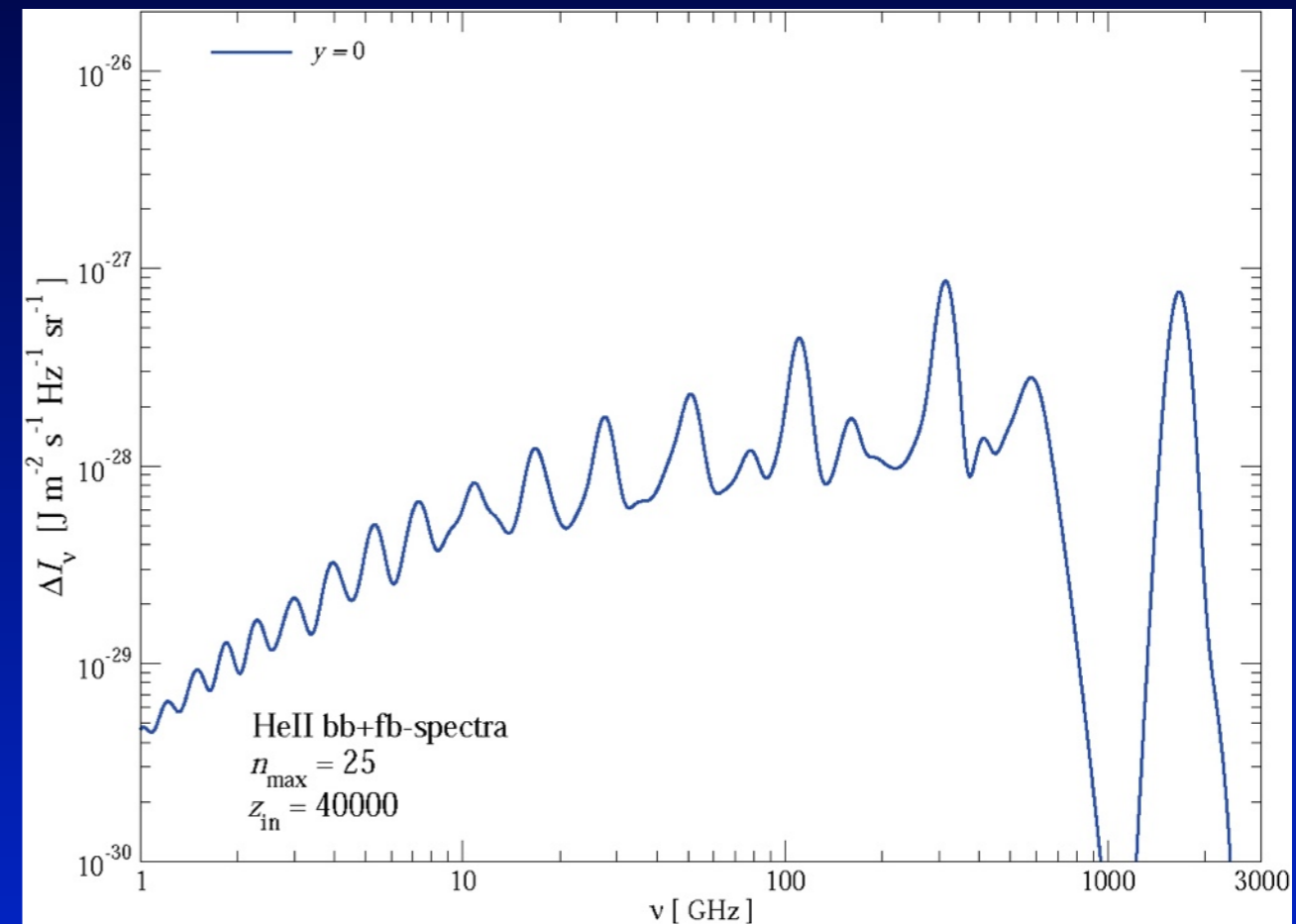
CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on y*

Hydrogen



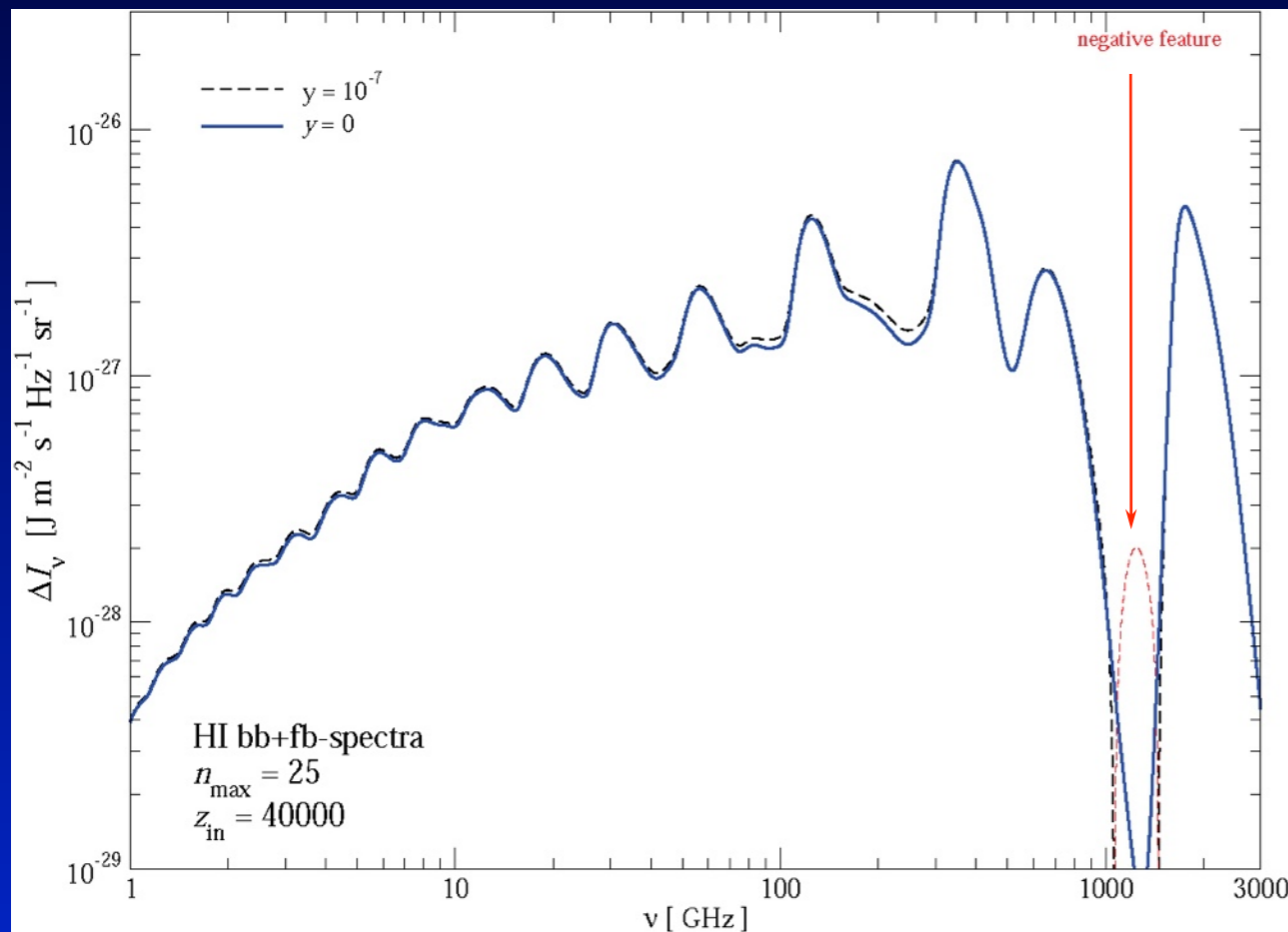
Helium +



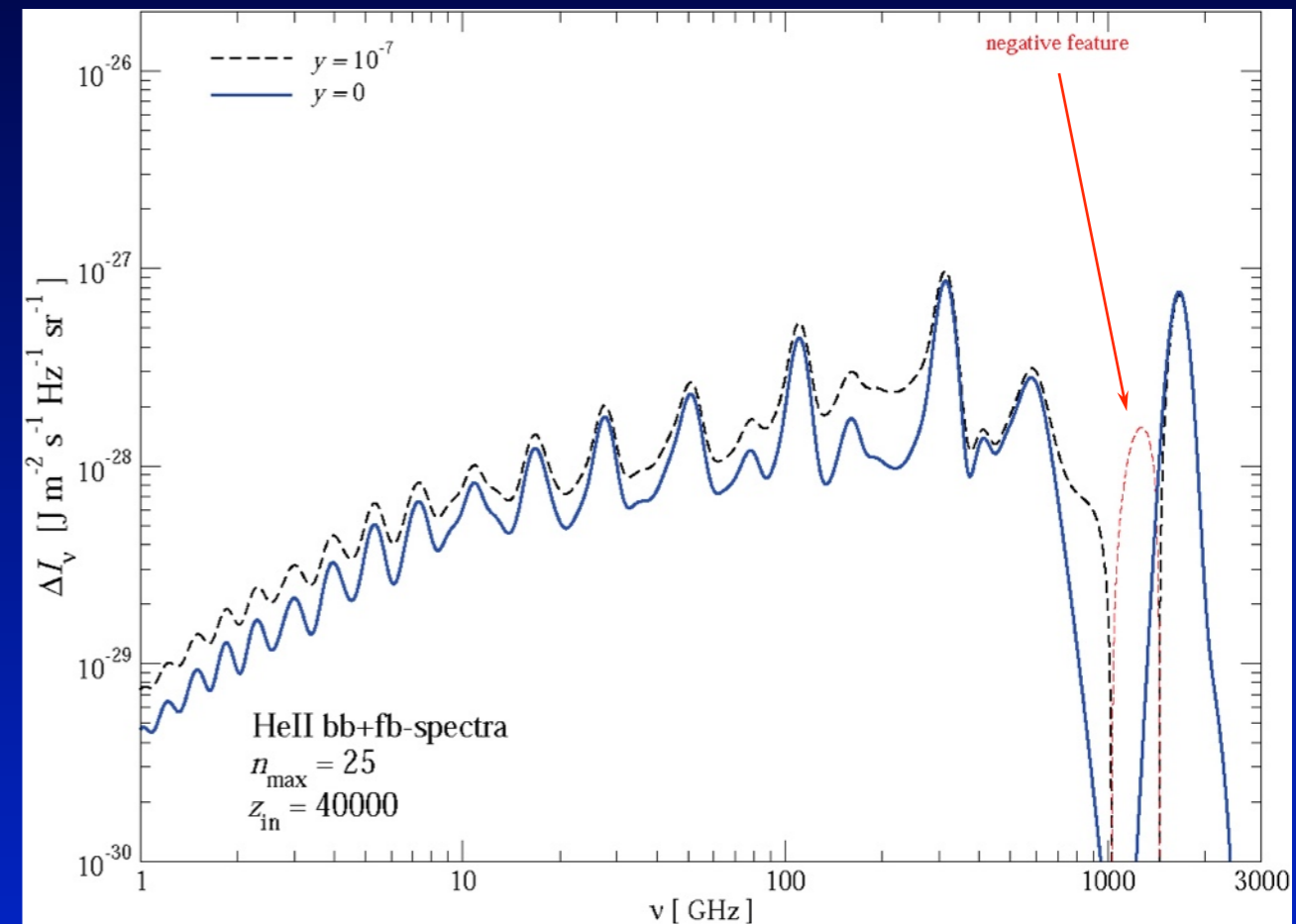
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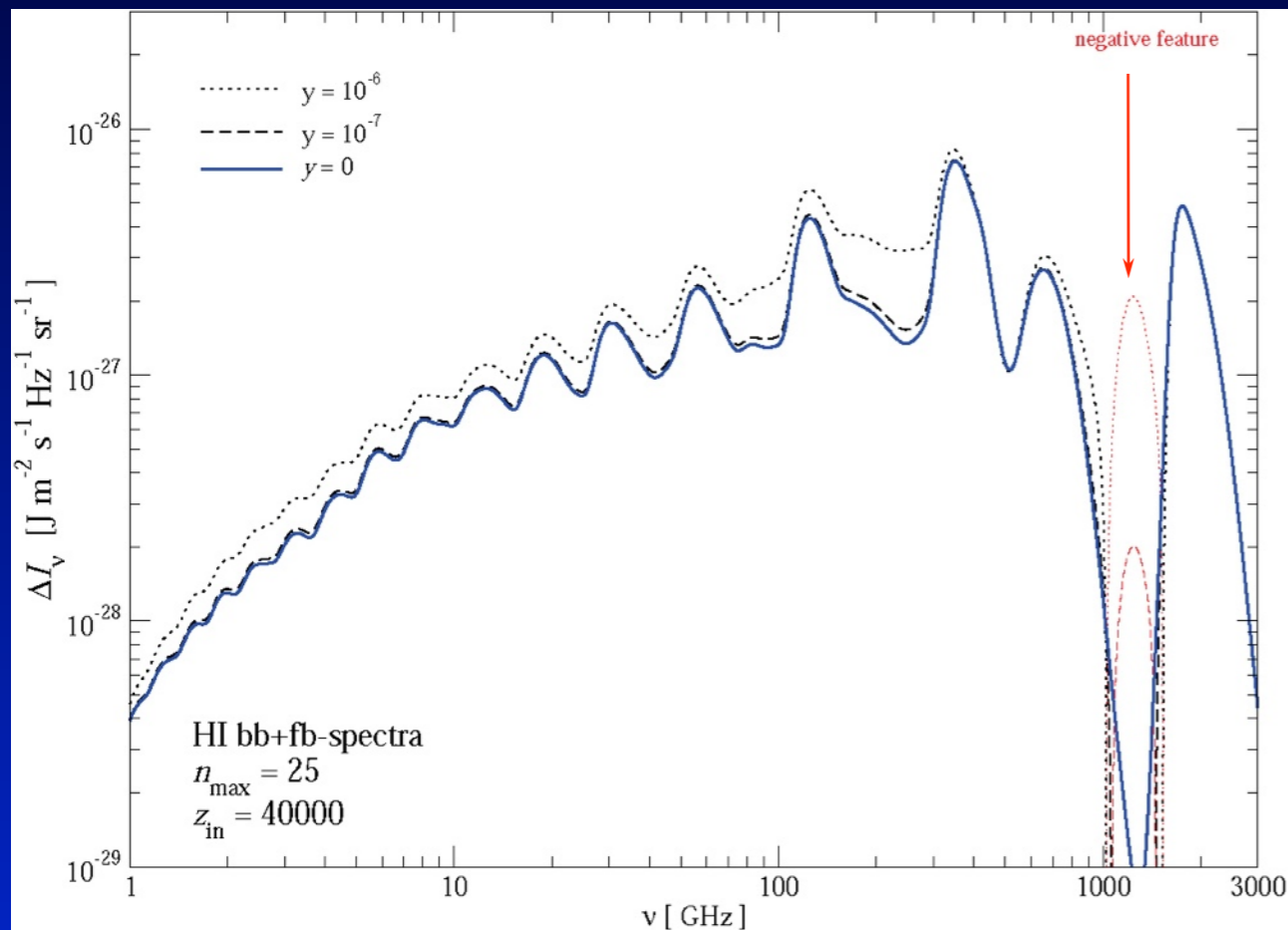
Helium +



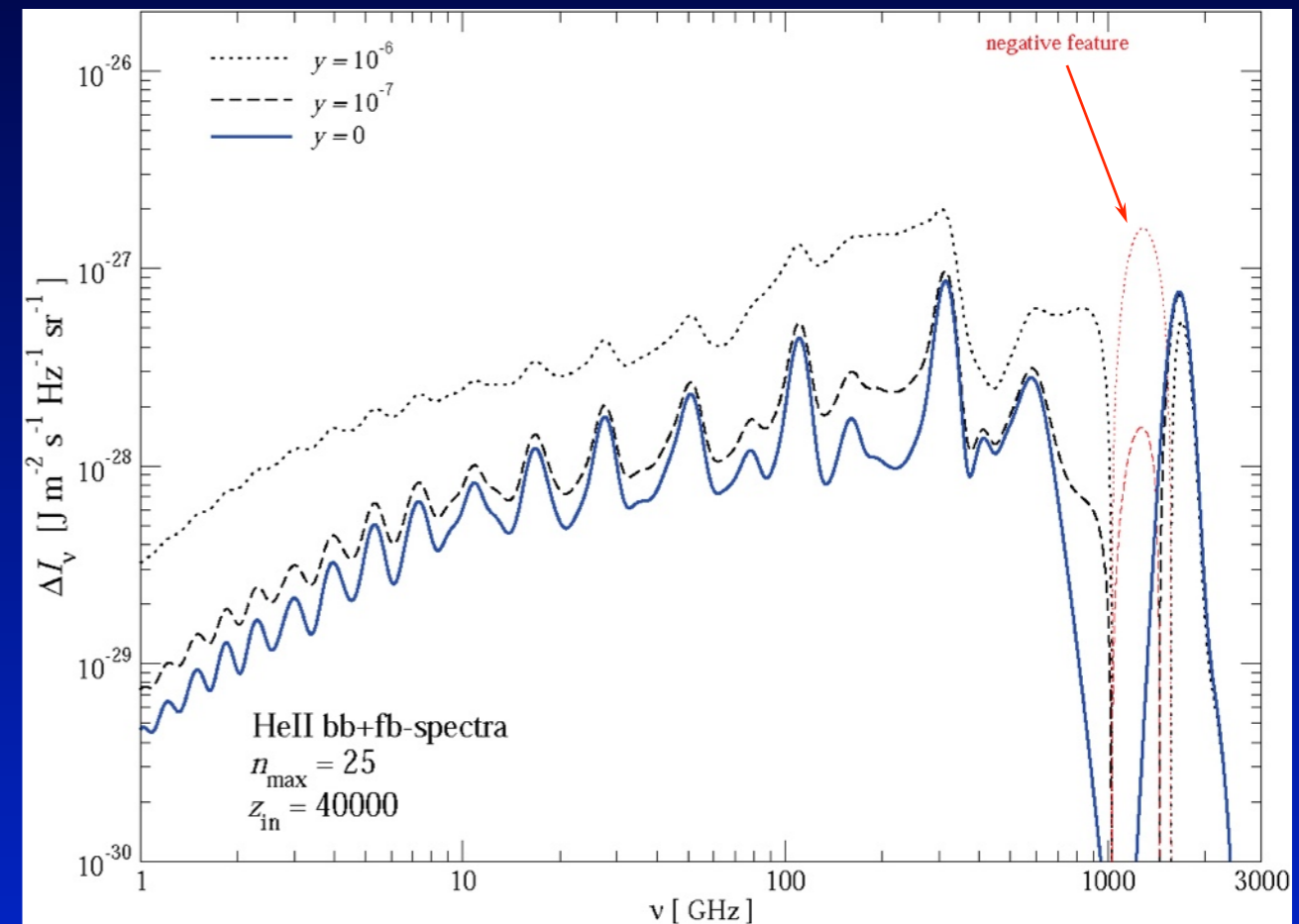
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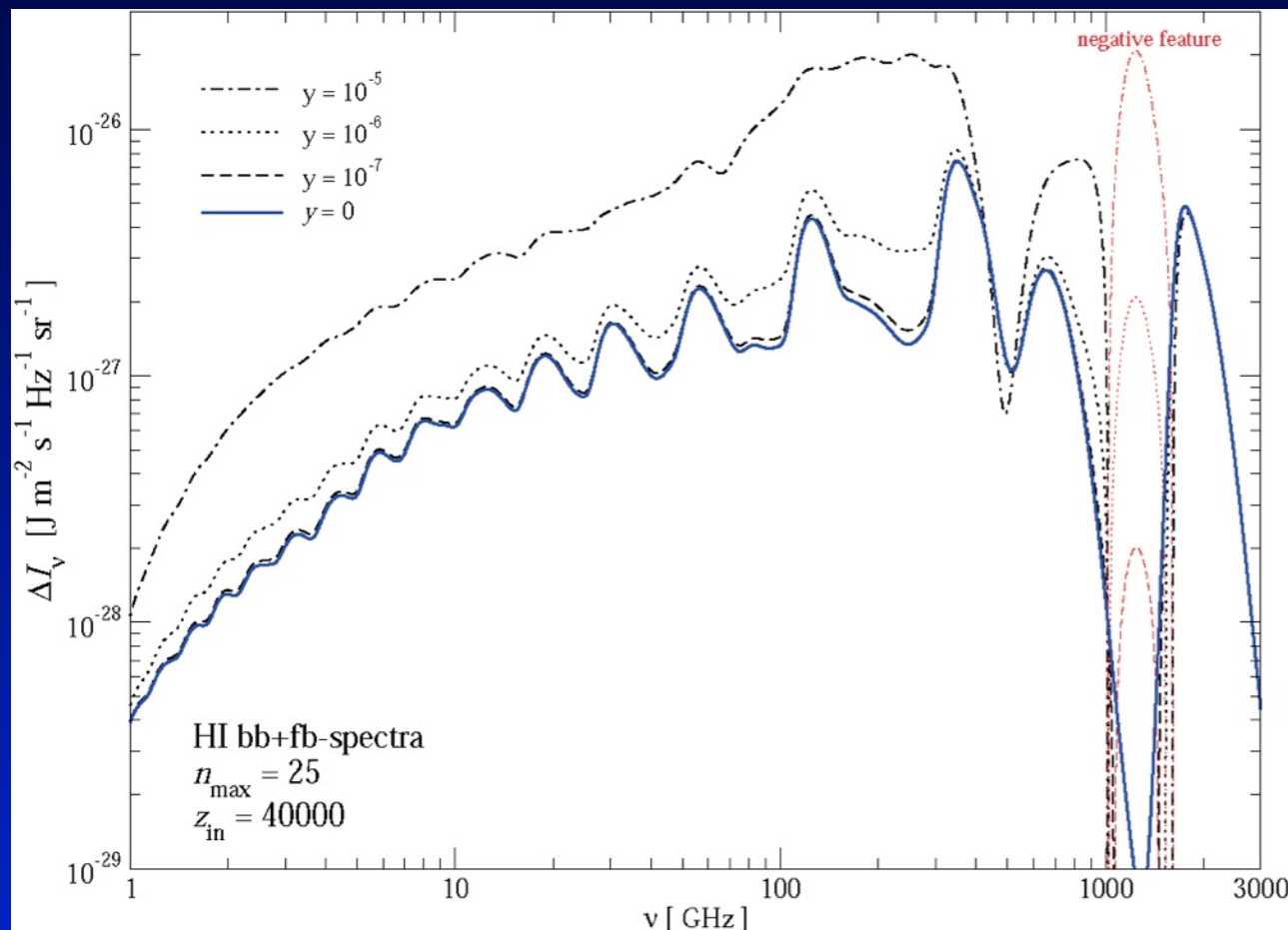
Helium +



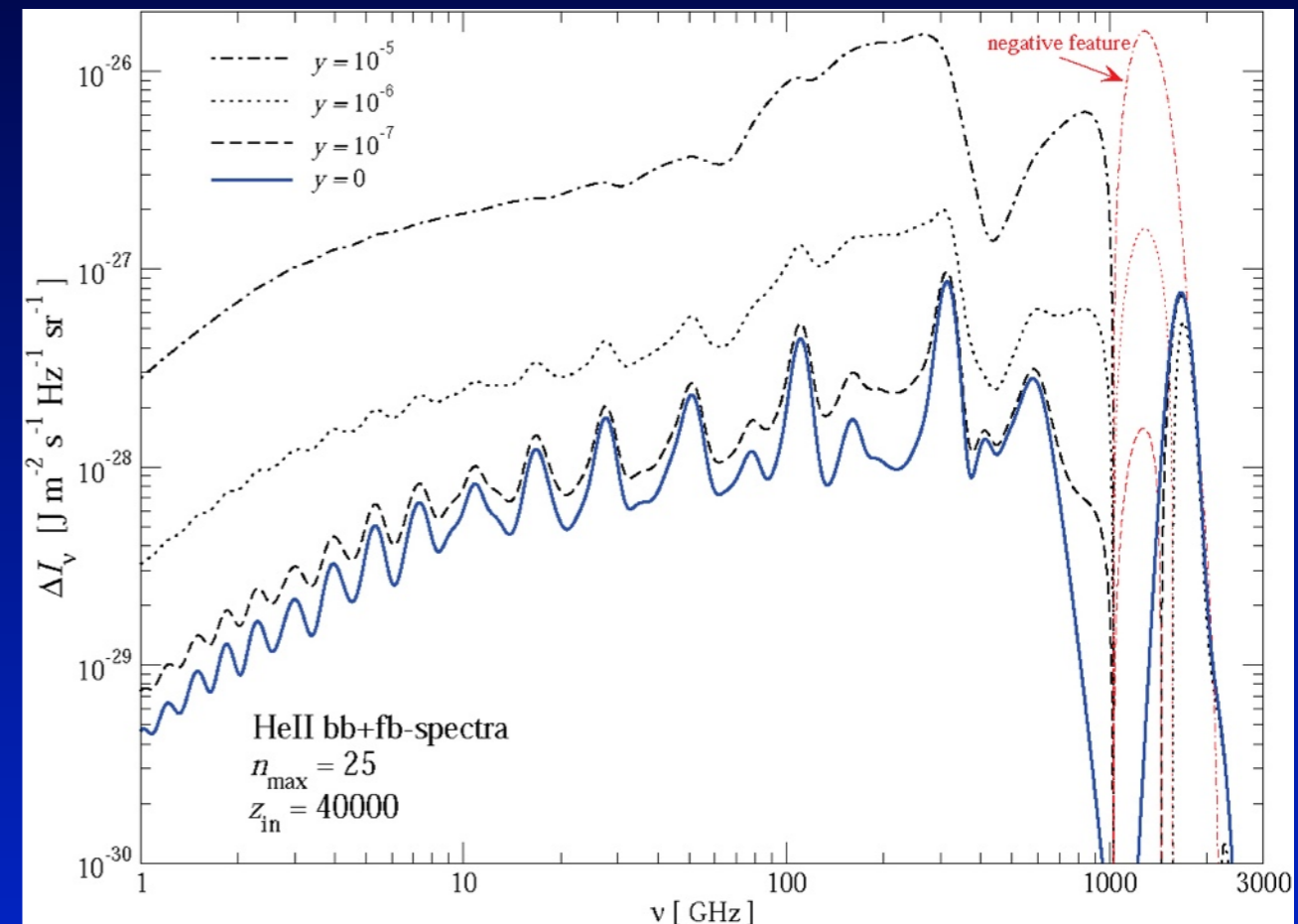
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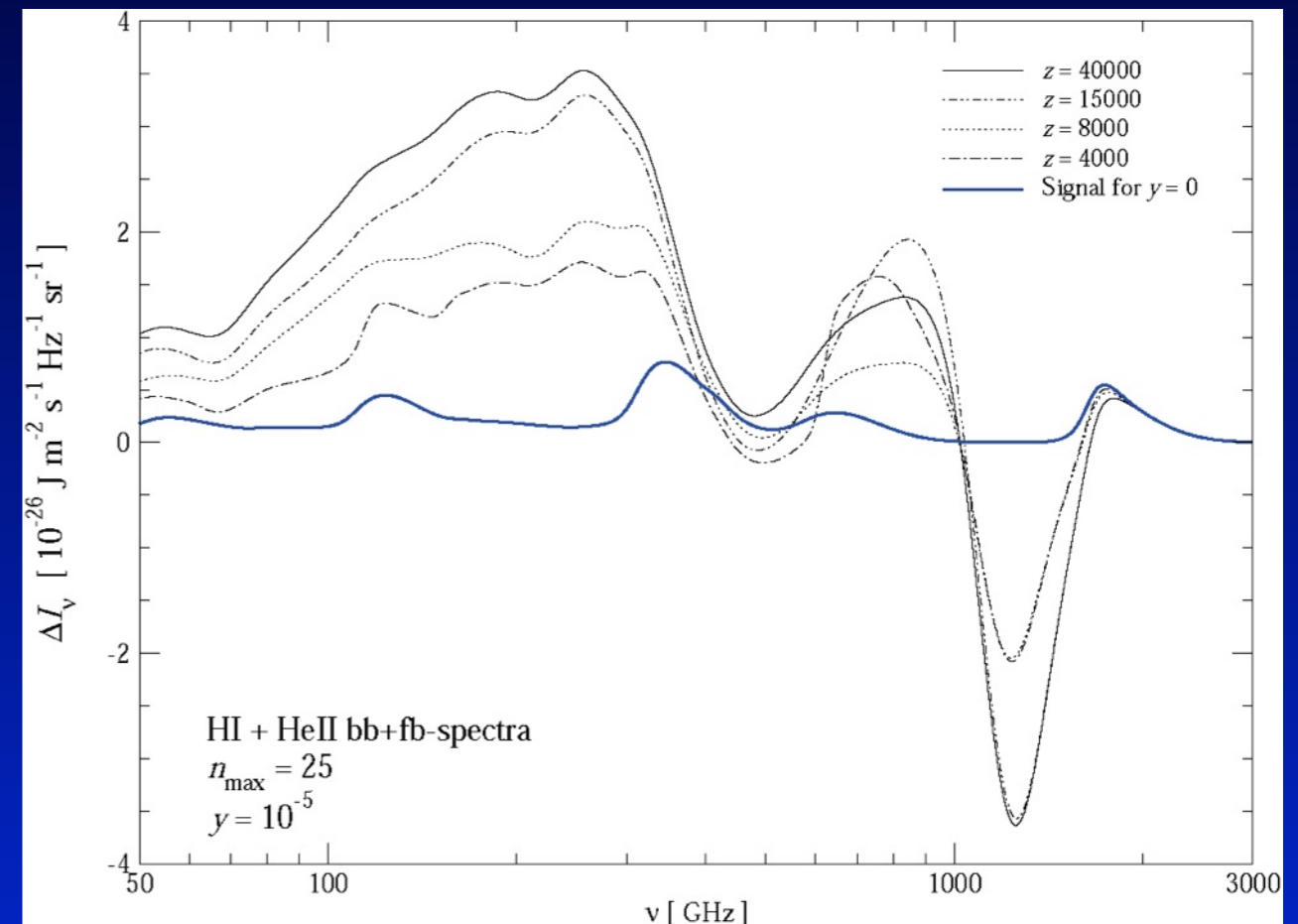
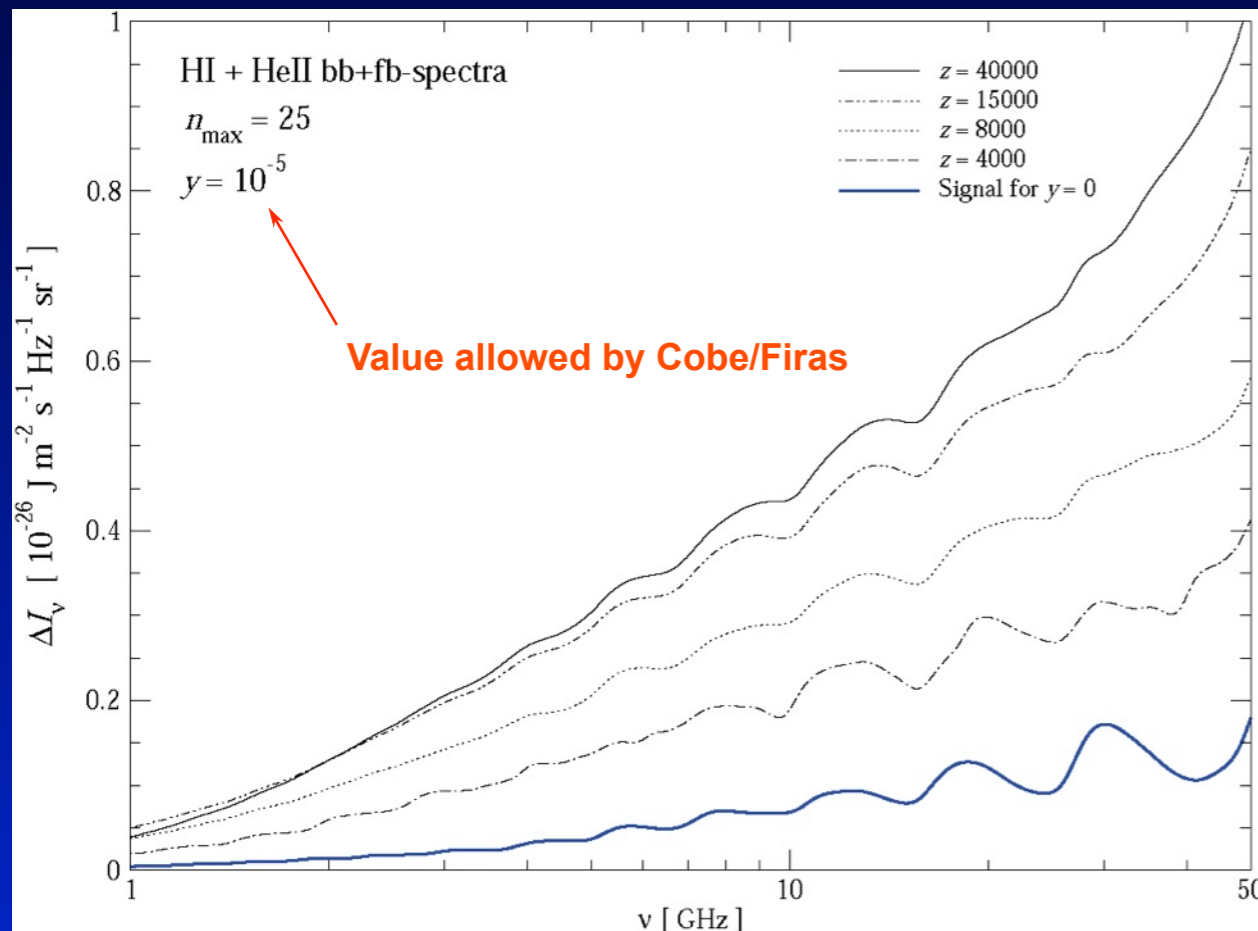
JC & Sunyaev, 2008, astro-ph/0803.3584

- ◆ Large increase in the total amplitude of the distortions with value of y !
- ◆ Strong emission-absorption feature in the Wien-part of CMB (absent for $y=0$!!!)
- ◆ HeII contribution to the pre-recombinational emission as strong as the one from Hydrogen alone !

CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on z*

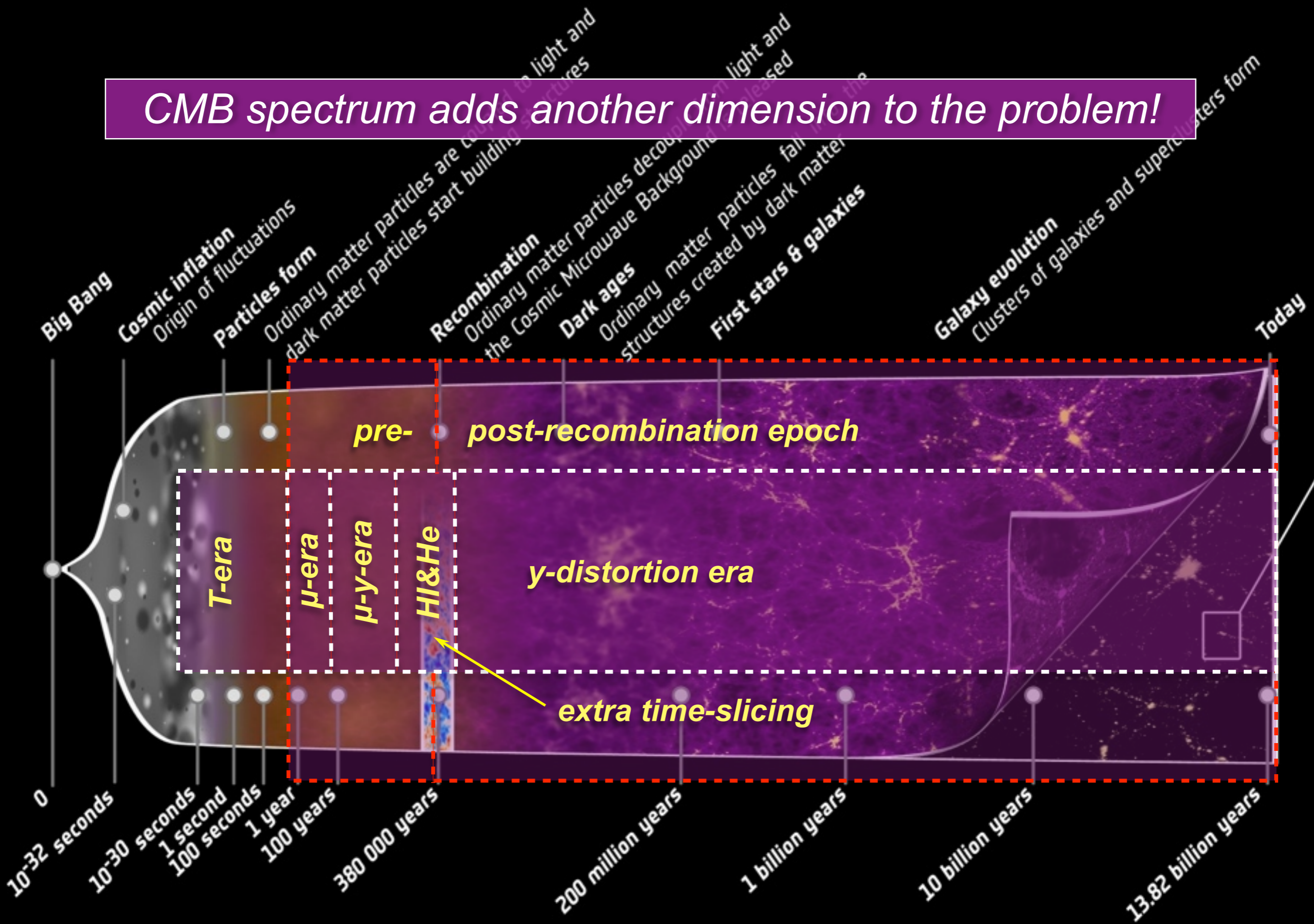
Hydrogen and Helium +



JC & Sunyaev, 2008, astro-ph/0803.3584

- ◆ Large increase in the total amplitude of the distortions with injection redshift!
- ◆ Number of spectral features depends on injection redshift!
- ◆ Emission-Absorption feature increases ~ 2 for energy injection $z \Rightarrow 11000$

CMB spectrum adds another dimension to the problem!



Annihilating/decaying (dark matter) particles

Why is this interesting?

- A priori no specific particle in mind
- *But:* we do not know what dark matter is and where it really came from!
- Was dark matter thermally produced or as a decay product of some heavy particle?
- is dark matter structureless or does it have internal (excited) states?
- sterile neutrinos? moduli? Some other relic particle?
- From the theoretical point of view really no shortage of particles to play with...

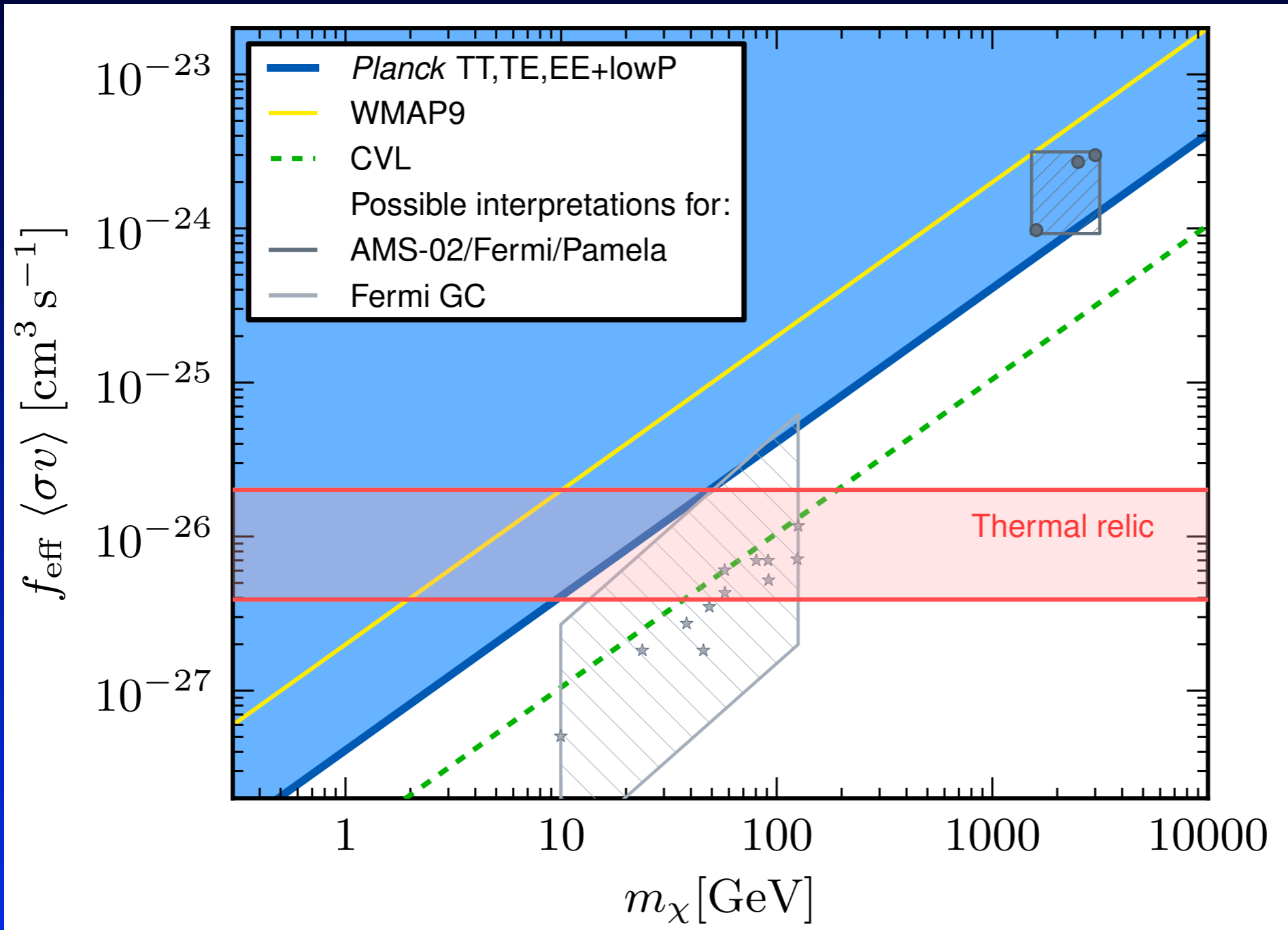
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CMB spectral distortions offer a new independent way to constrain these kind of models

Latest Planck limits on annihilation cross section

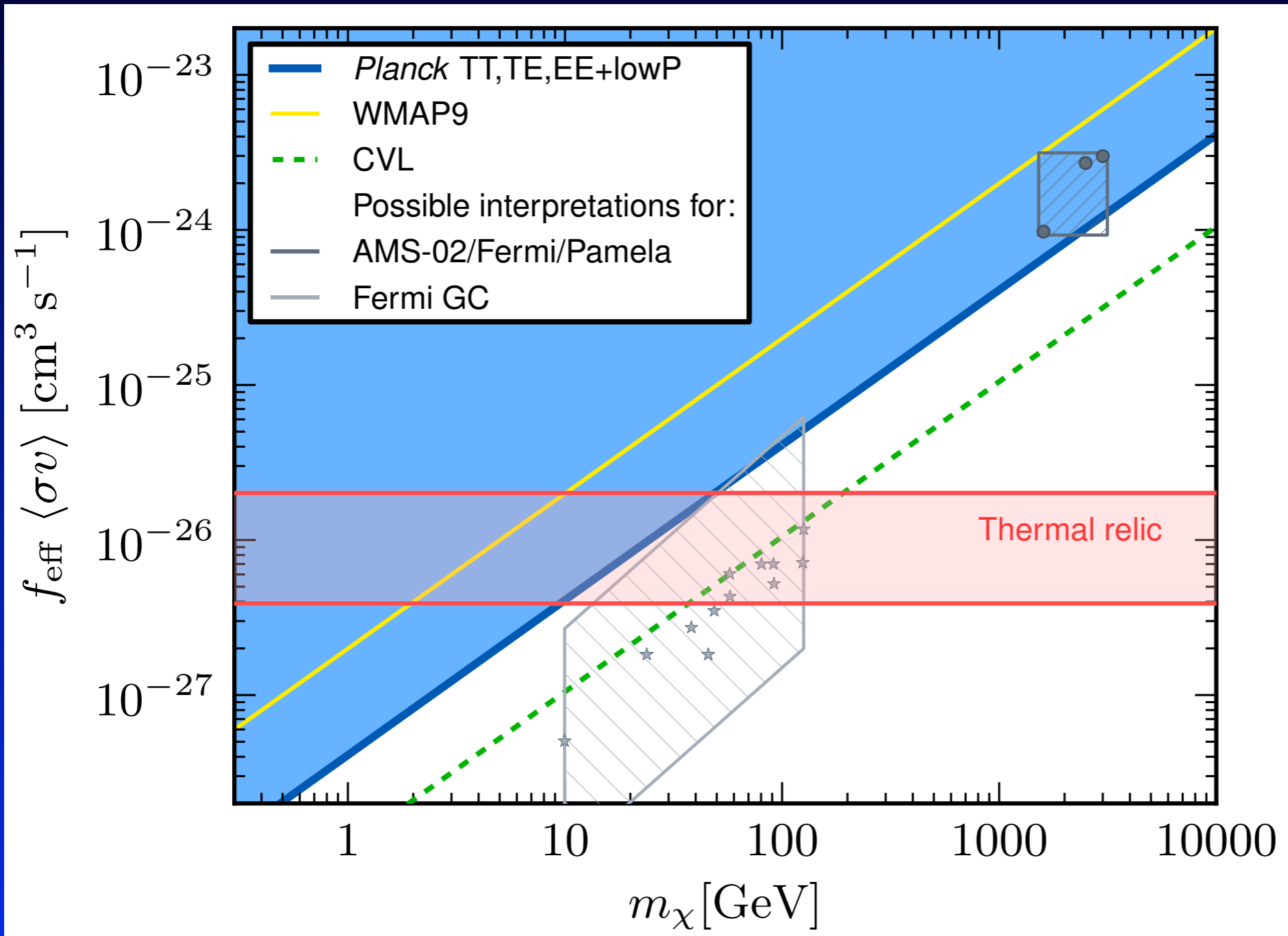
95% c.l.



- AMS/Pamela models in tension
- but interpretation model-dependent
- Sommerfeld enhancement?
- clumping factors?
- annihilation channels?

Latest Planck limits on annihilation cross section

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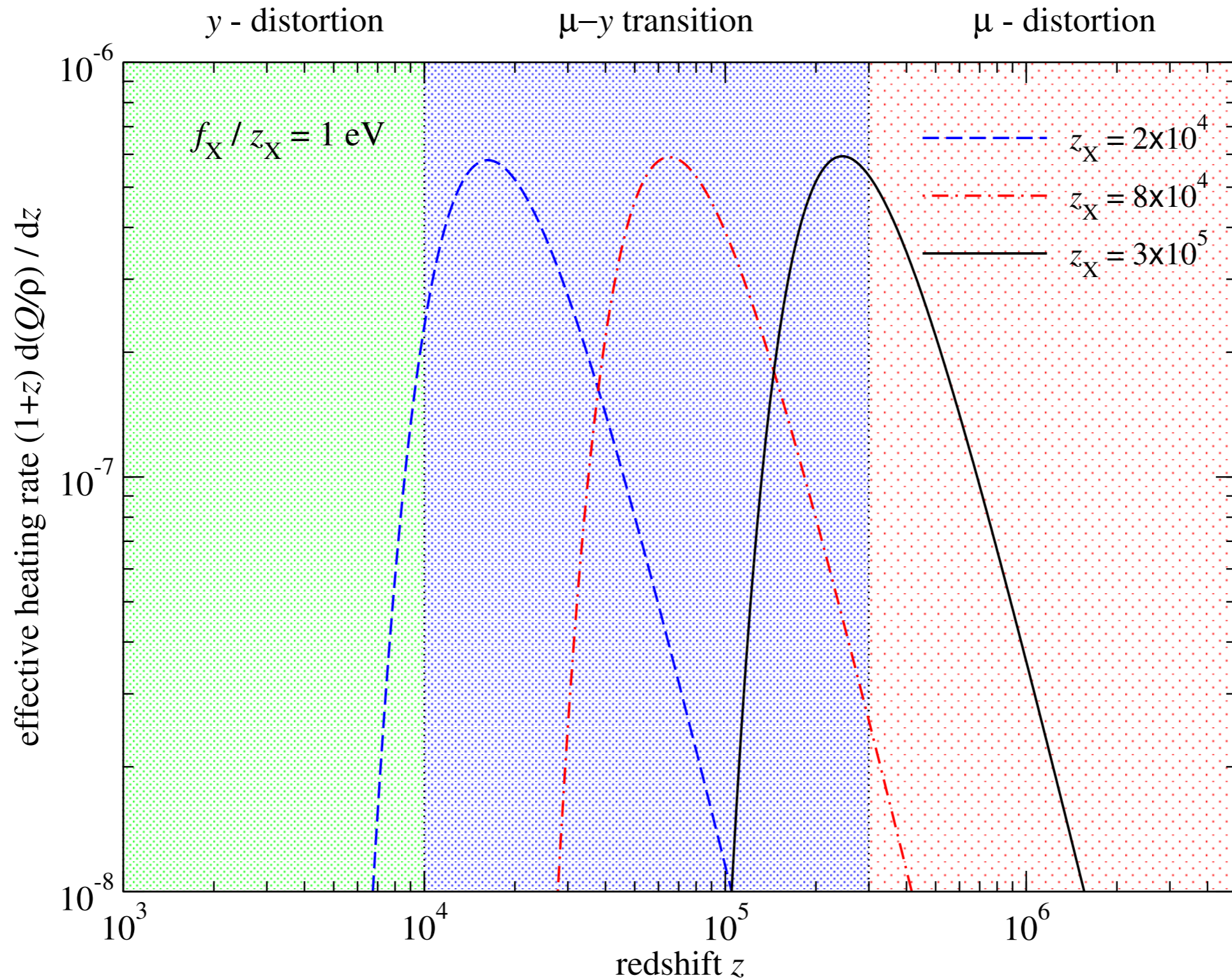


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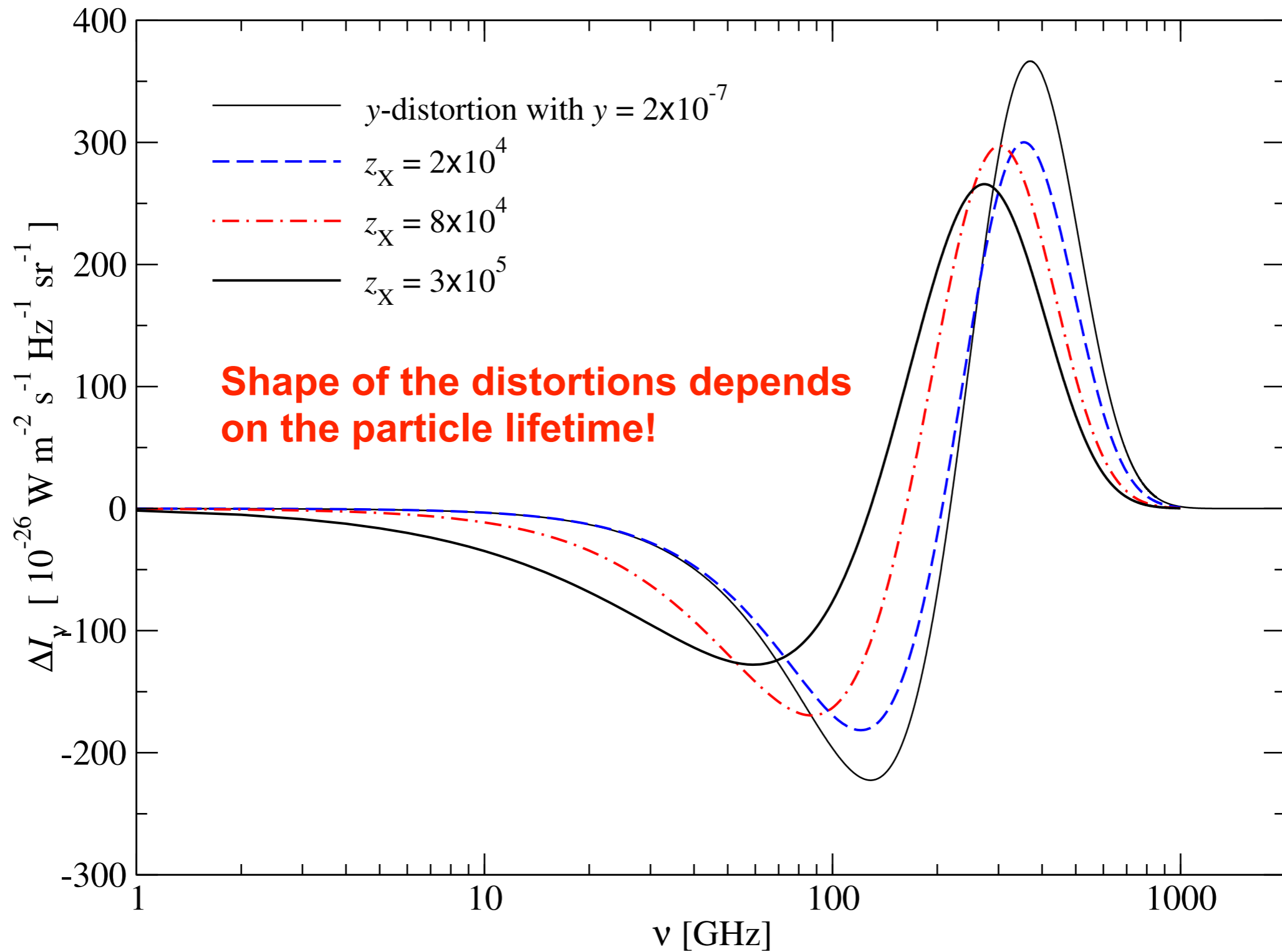
Planck Collaboration, paper XIII, 2015

For current constraint only (weak) upper limits from distortion...

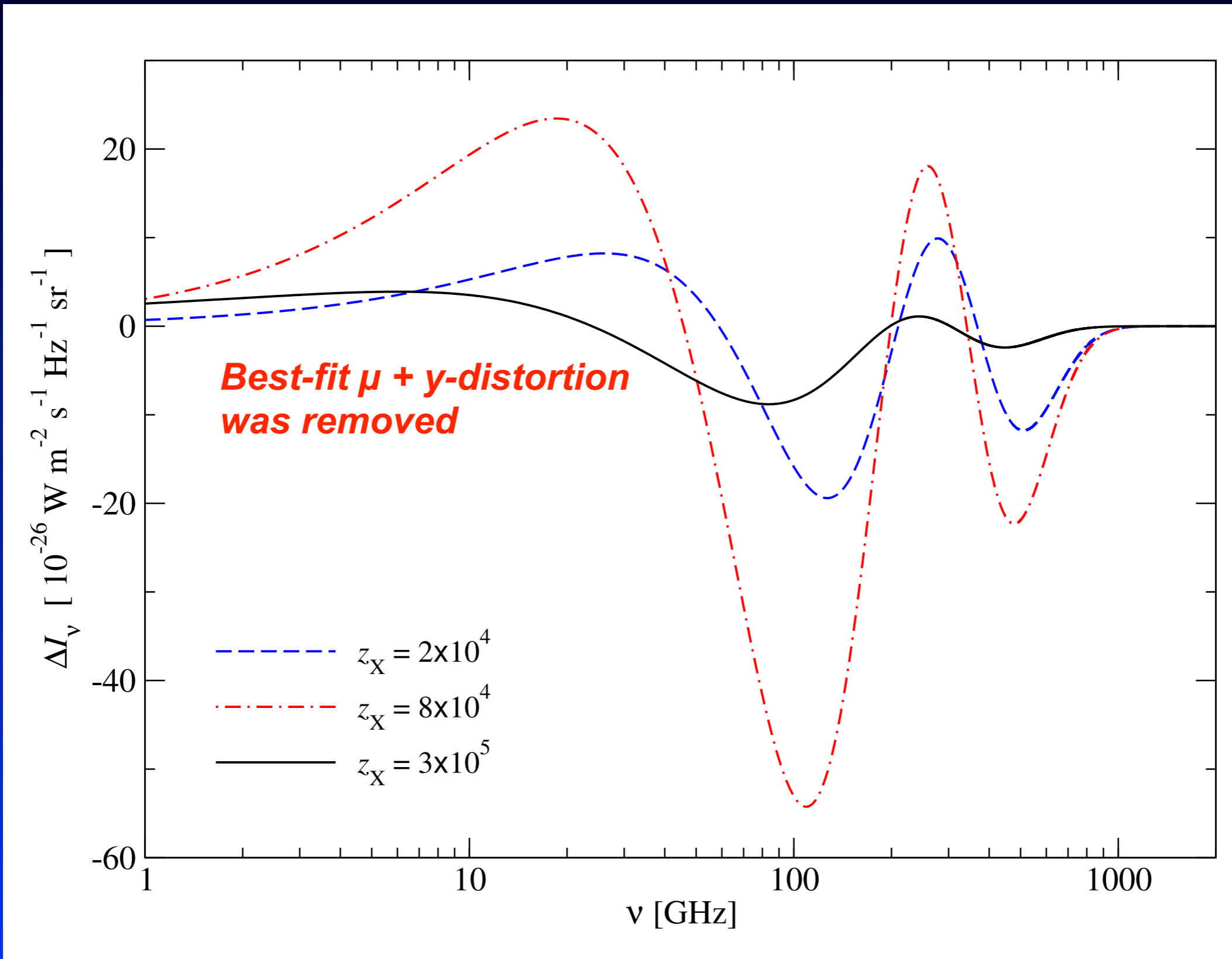
Decaying particle scenarios



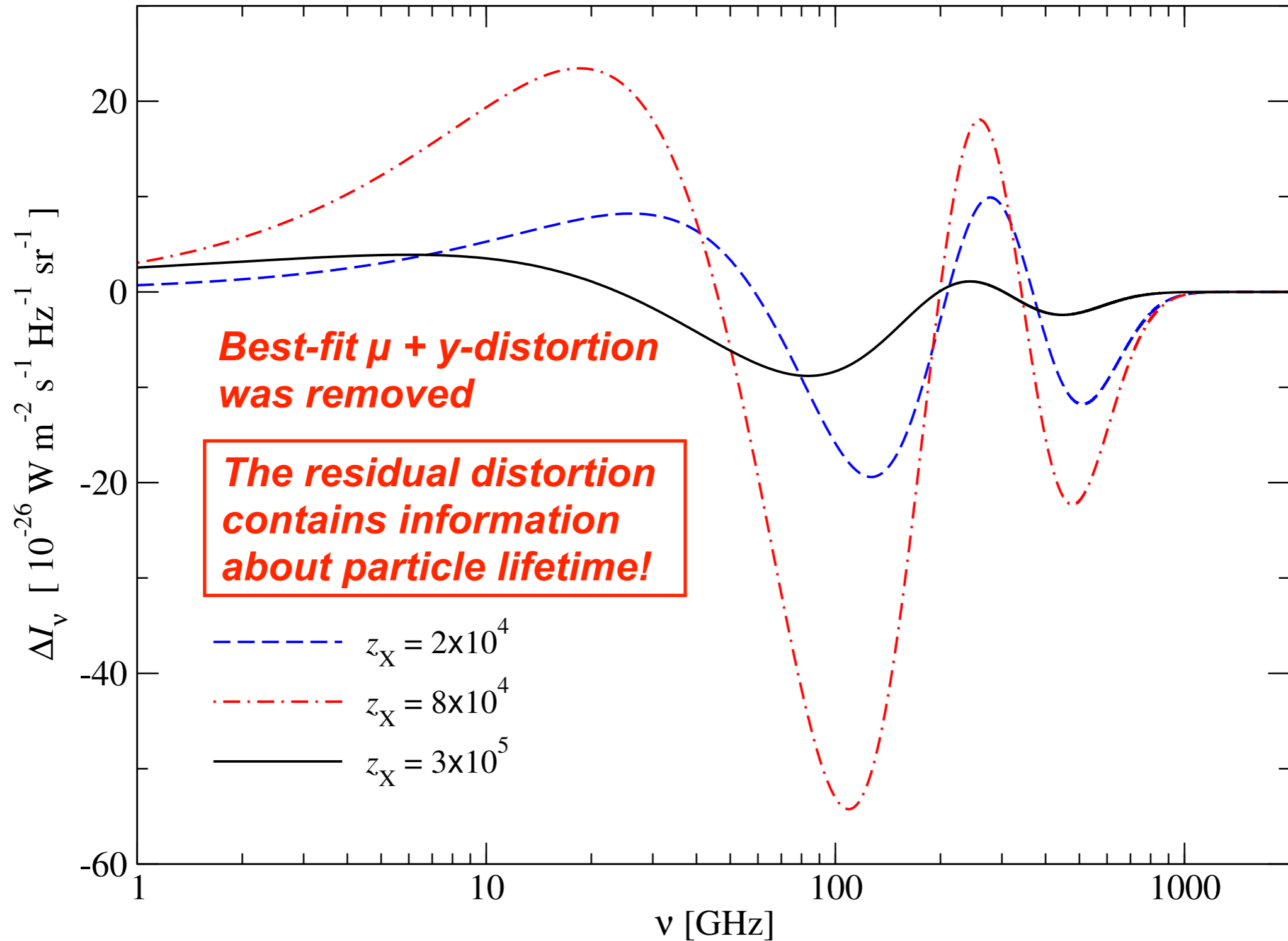
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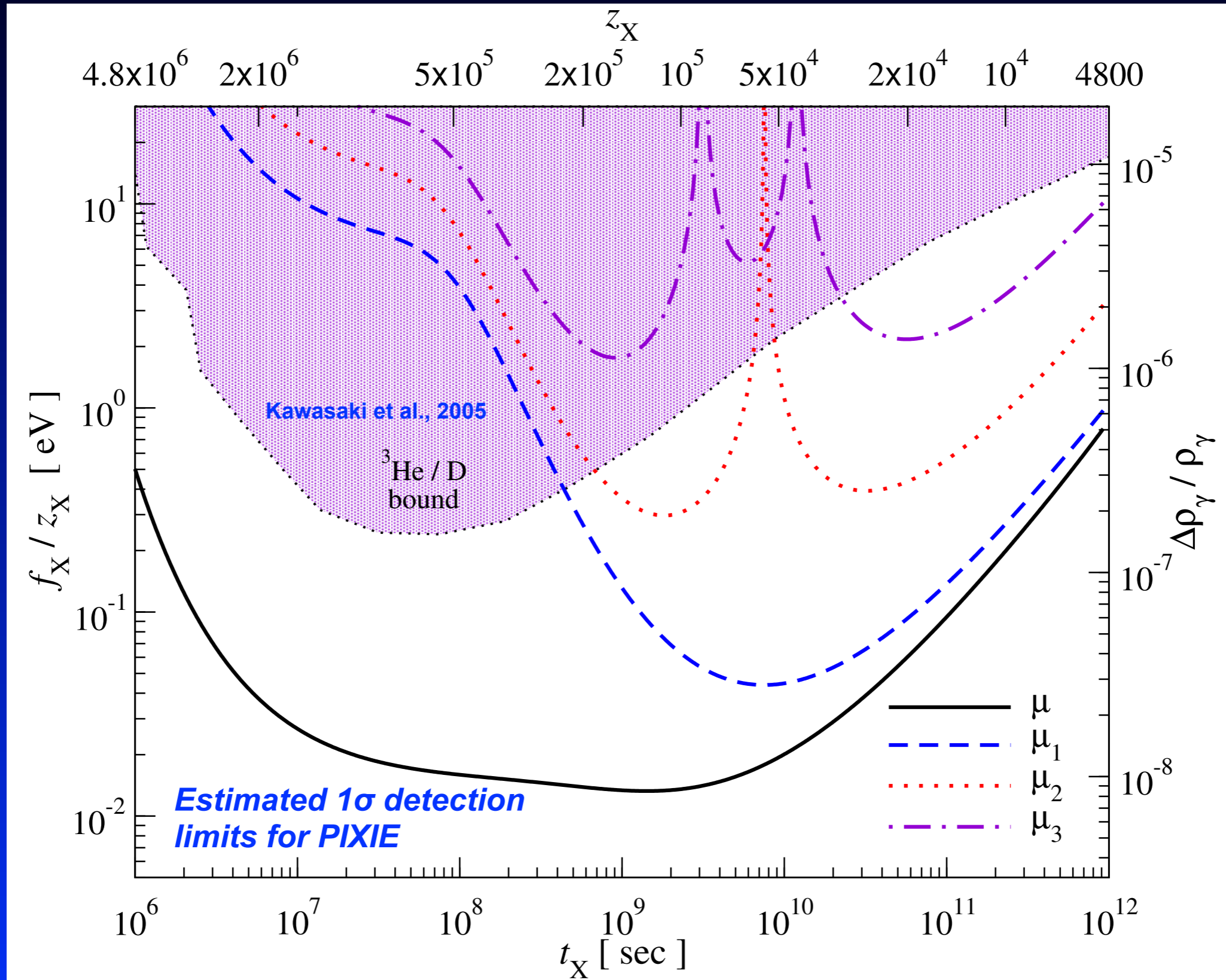
Decaying particle scenarios (information in residual)



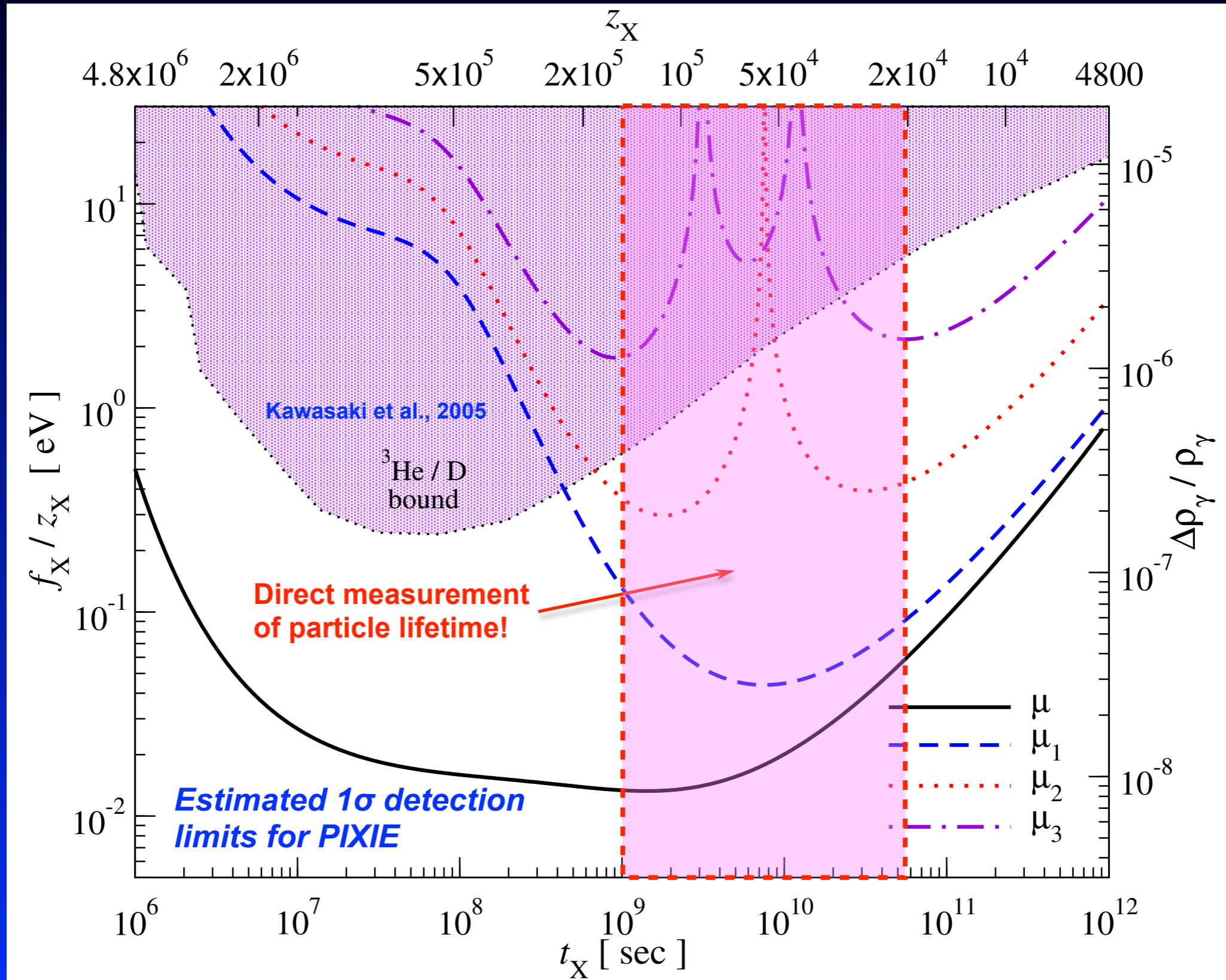
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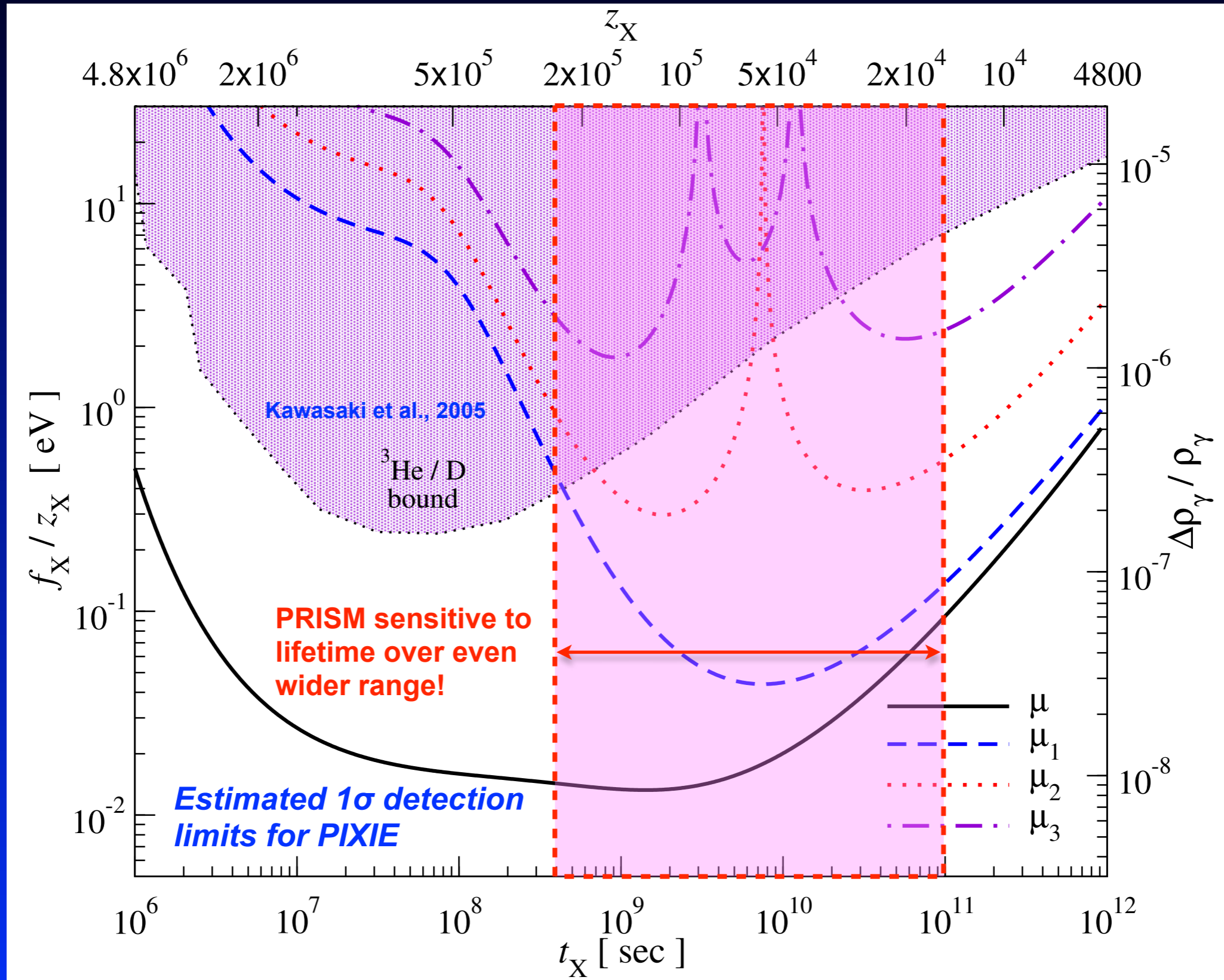
Distortions could shed light on decaying (DM) particles!



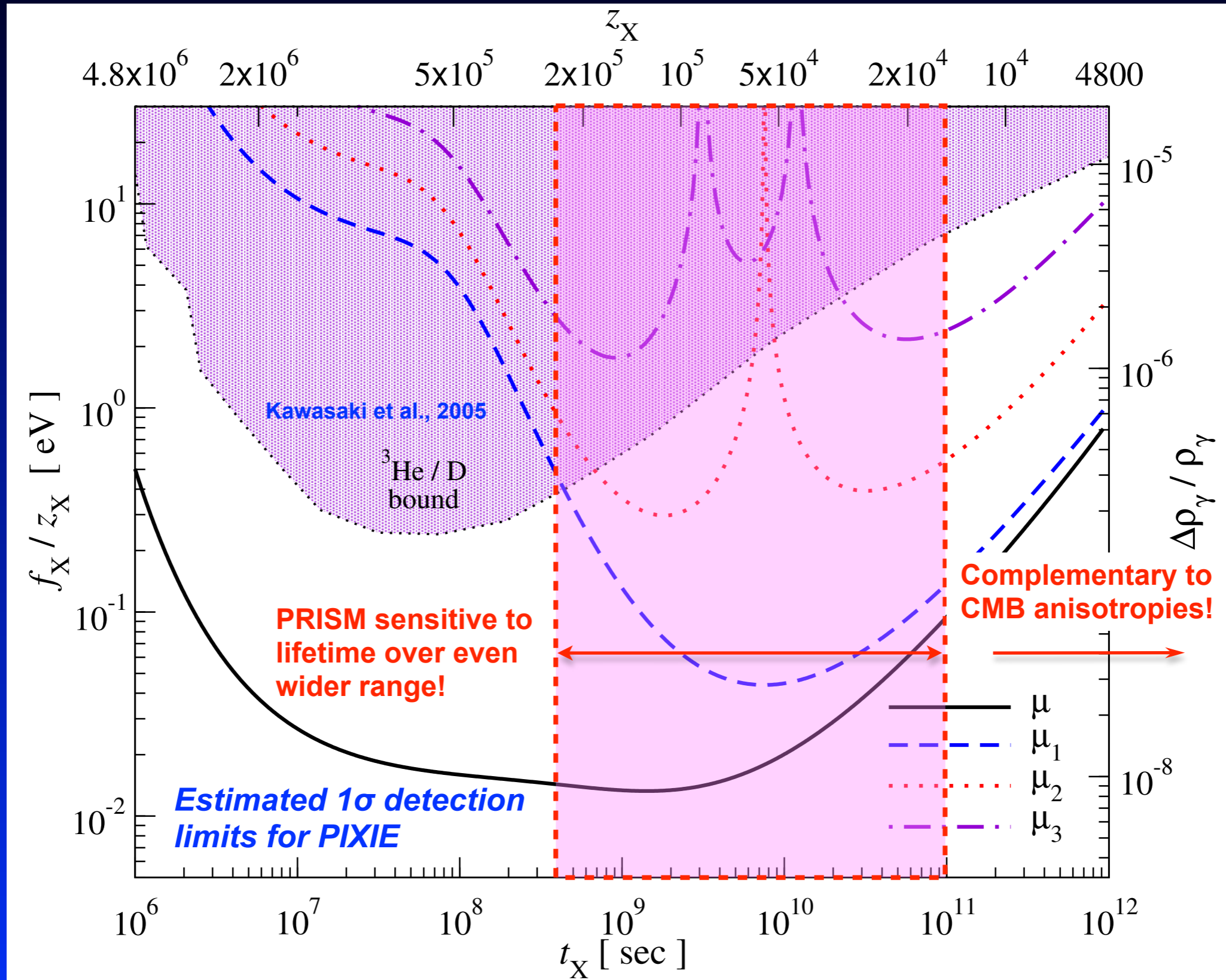
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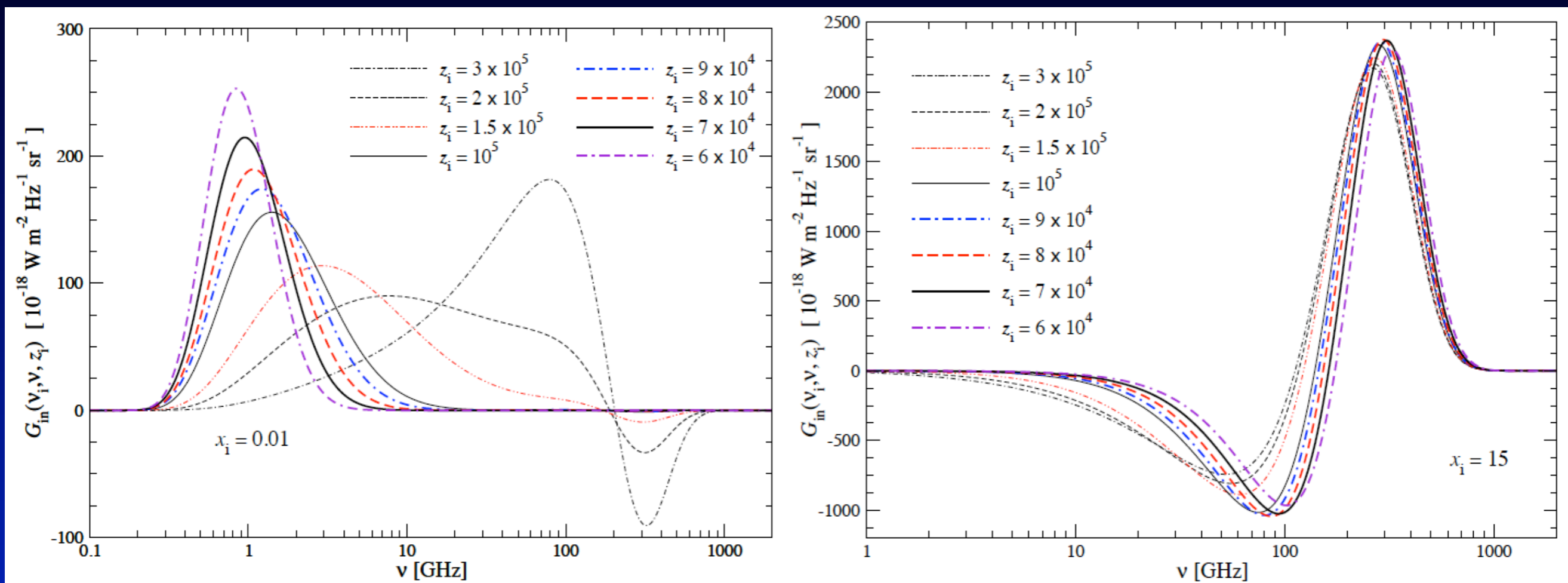
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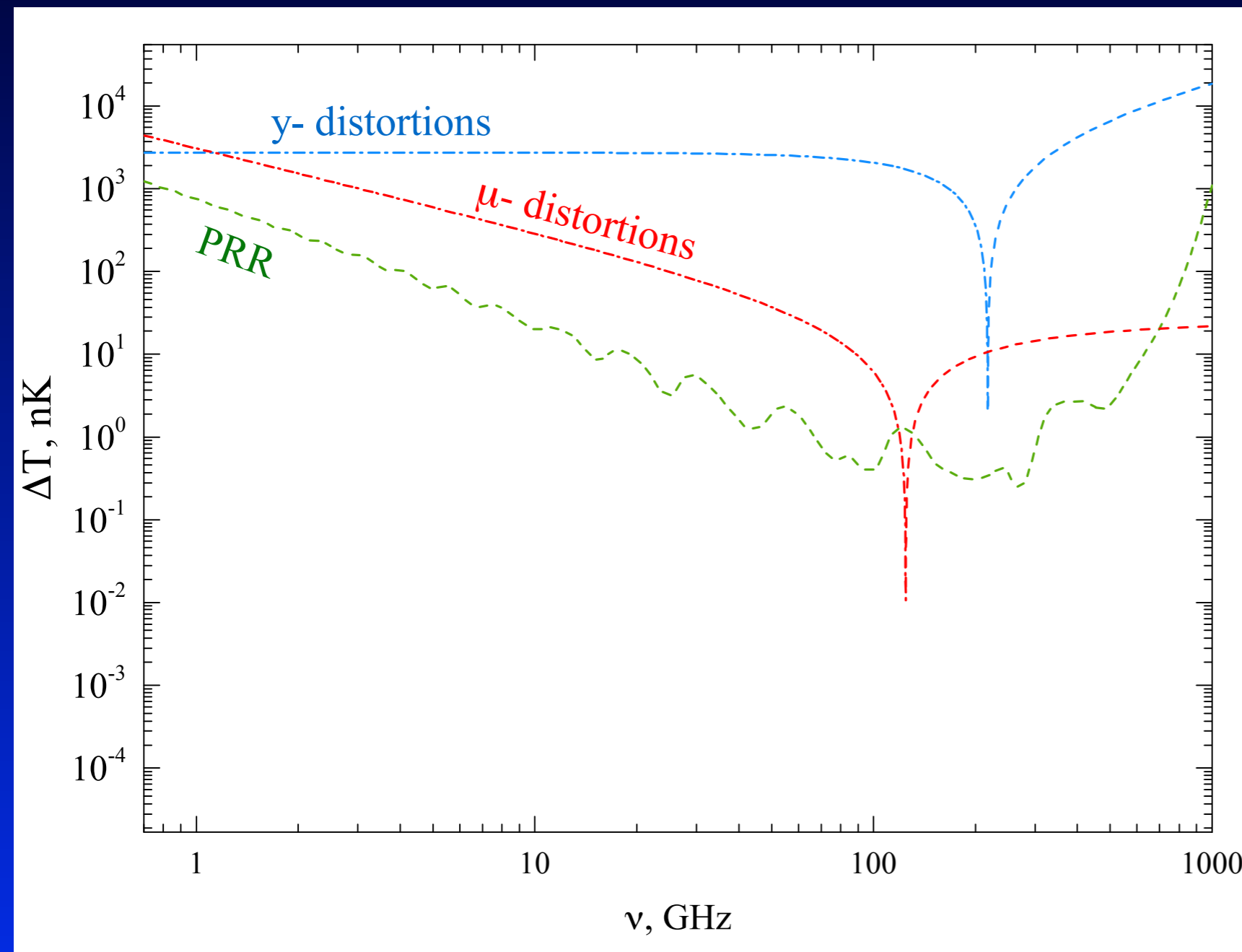


Green's function for photon injection



- Photon injection Green's function gives even richer phenomenology of distortion signals
- Depends on the details of the photon production process for redshifts $z < \text{few} \times 10^5$
- difference between high and low frequency photon injection

Spectral distortions of the CMB dipole

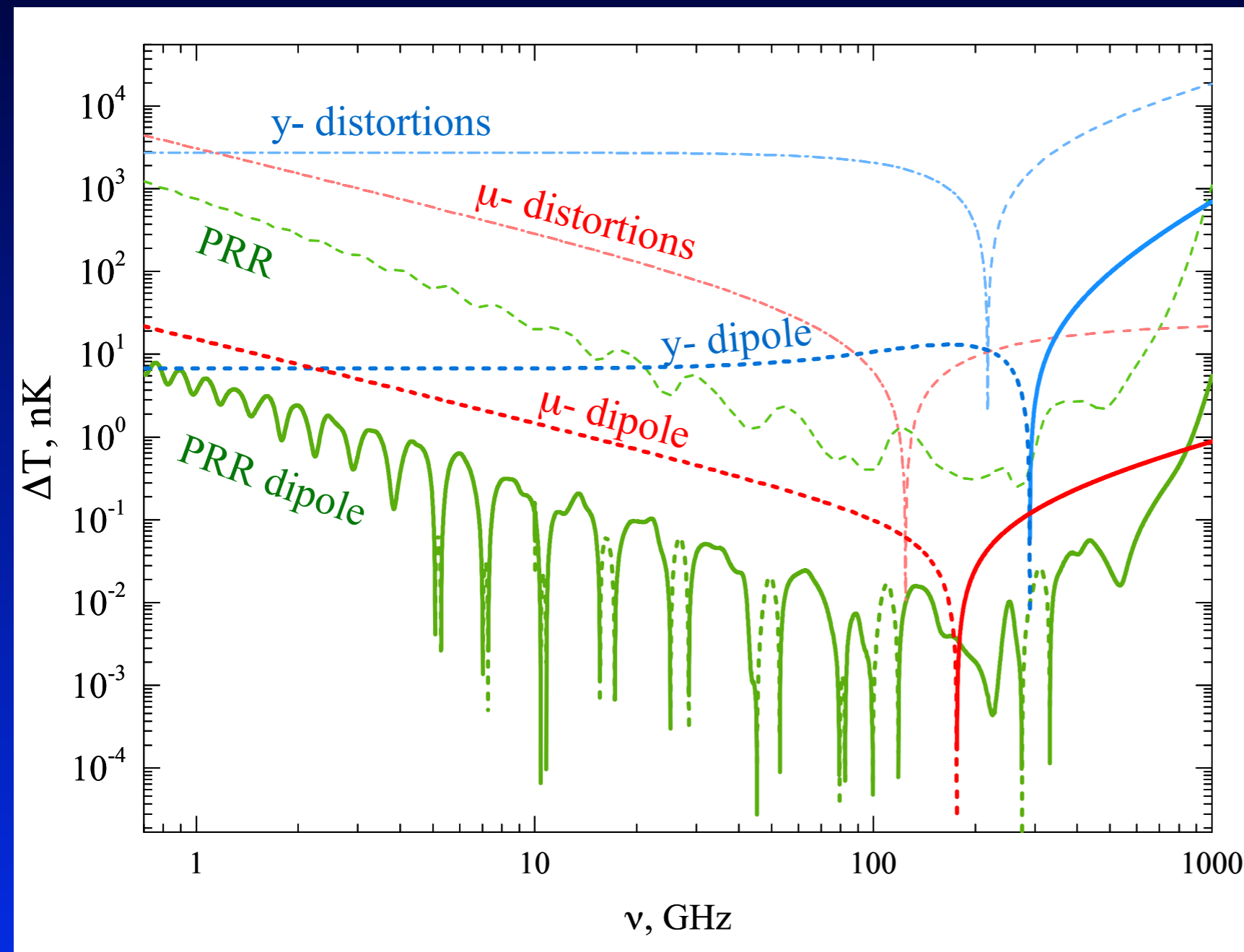


- motion with respect to CMB blackbody monopole
- ⇒ *CMB temperature dipole*
- including primordial distortions of the CMB
- ⇒ *CMB dipole is distorted*

$$\eta_d(\nu, \mathbf{n}) \approx -\nu \partial_\nu \eta_m(\nu) \beta \cos \Theta$$

- spectrum of the dipole is sensitive to the *derivative* of the monopole spectrum
- anisotropy does not need *absolute* calibration but just *inter-channel* calibration
- *but* signal is ~ 1000 times smaller...
- *foregrounds* will also leak into the dipole in this way
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Other extremely interesting new signals

- **Scattering signals from the dark ages**

(e.g., Basu et al., 2004; Hernandez-Monteagudo et al., 2007; Schleicher et al., 2009)

- constrain abundances of chemical elements at high redshift
- learn about star formation history

- **Rayleigh / HI scattering signals**

(e.g., Yu et al., 2001; Rubino-Martin et al., 2005; Lewis 2013)

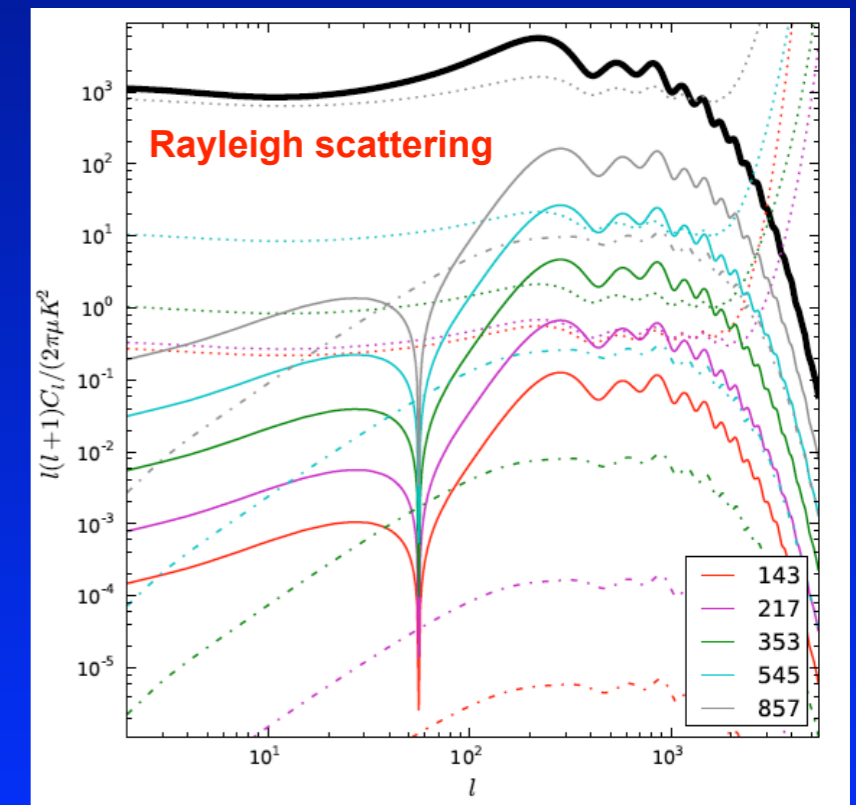
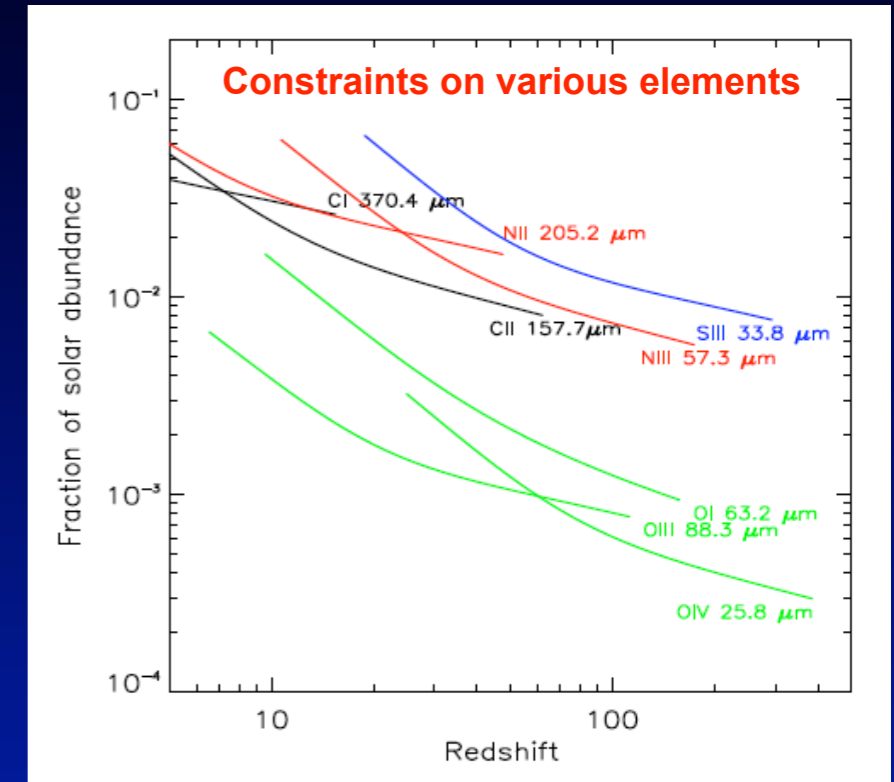
- provides way to constrain recombination history
- important when asking questions about N_{eff} and Y_p

- **Free-free signals from reionization**

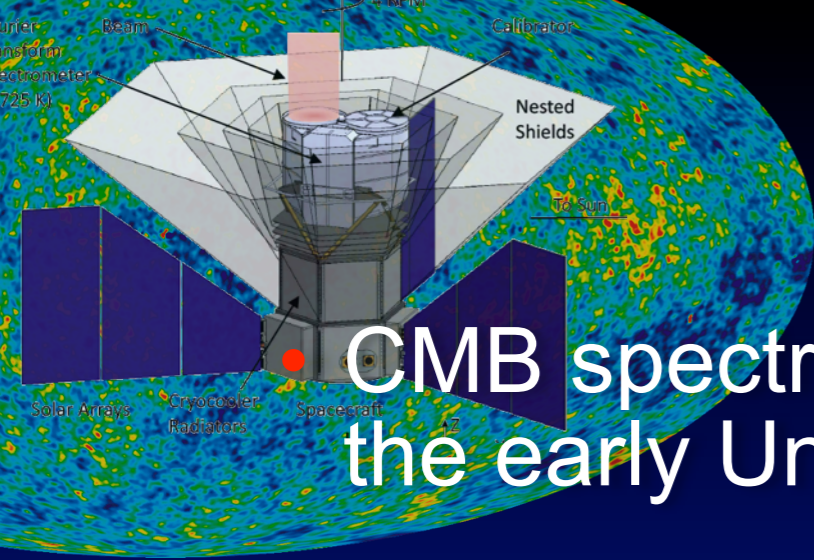
(e.g., Burigana et al. 1995; Trombetti & Burigana, 2013)

- constrains reionization history
- depends on clumpiness of the medium

All these effects give spectral-spatial signals, and an absolute spectrometer will help with channel cross calibration!

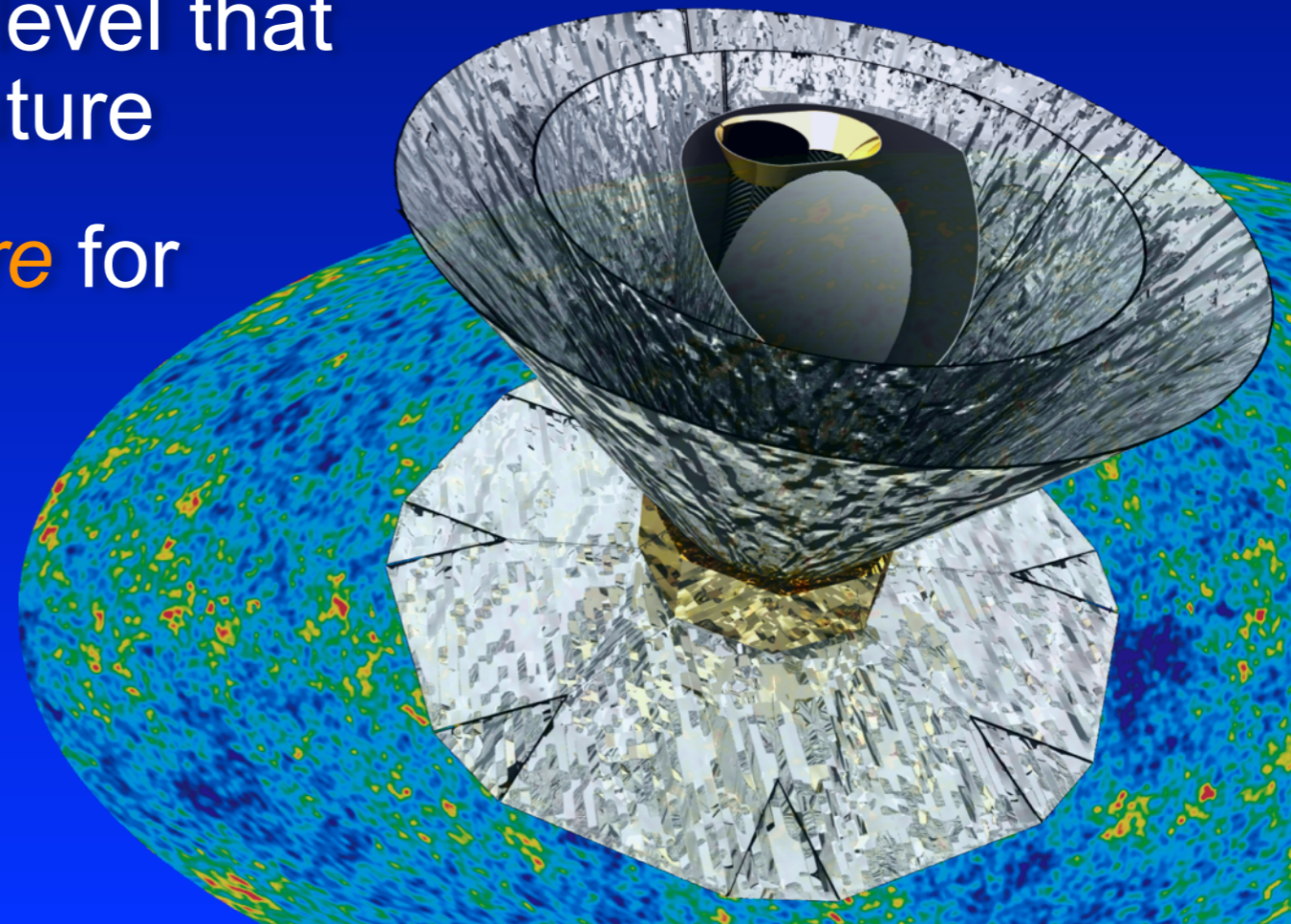


Conclusions

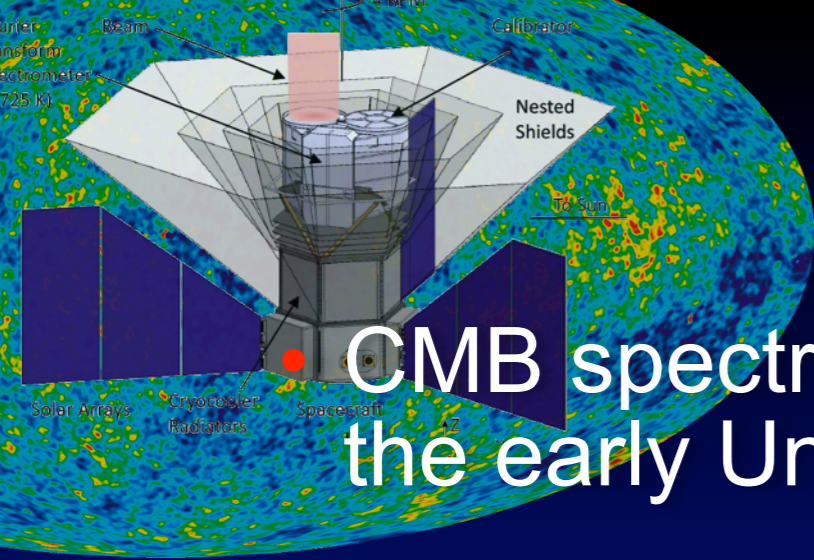


• CMB spectral distortions *will* open a *new window* to the early Universe

- new probe of the *inflation epoch* and *particle physics*
- *complementary* and *independent* source of information *not* just confirmation
- in *standard cosmology* several processes lead to *early energy release* at a level that will be detectable in the future
- extremely interesting *future* for CMB-based science!



Conclusions



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We should make use of all this information!

