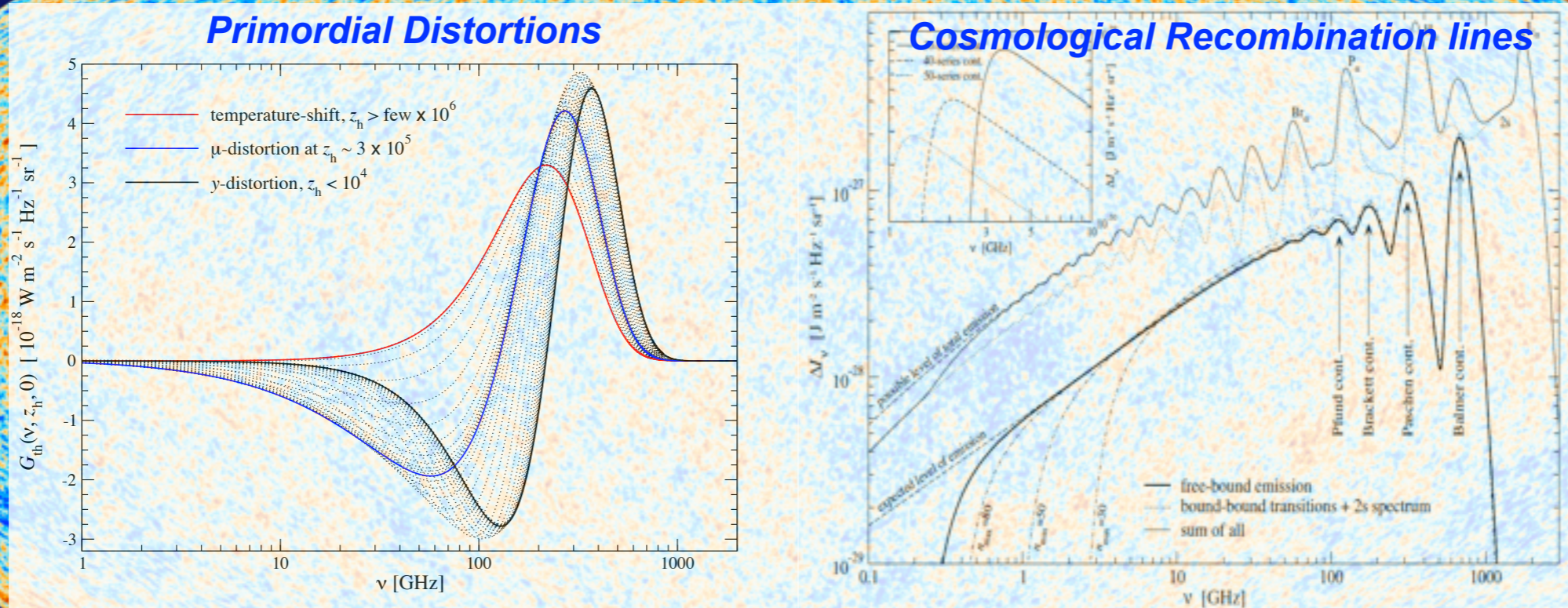


Science with Spectral Distortions of the CMB - IV

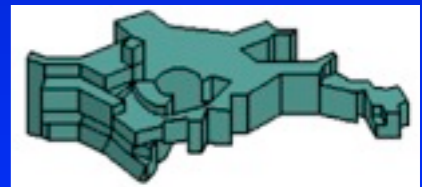


JOHNS HOPKINS
UNIVERSITY

Jens Chluba

CUSO Doctoral Program in Physics

Lausanne, November 6th, 2014



Physical mechanisms that lead to spectral distortions

- *Cooling by adiabatically expanding ordinary matter*

(JC, 2005; JC & Sunyaev 2011; Khatri, Sunyaev & JC, 2011)

*Standard sources
of distortions*

- Heating by *decaying* or *annihilating* relic particles

(Kawasaki et al., 1987; Hu & Silk, 1993; McDonald et al., 2001; JC, 2005; JC & Sunyaev, 2011; JC, 2013; JC & Jeong, 2013)

- *Evaporation of primordial black holes & superconducting strings*

(Carr et al. 2010; Ostriker & Thompson, 1987; Tashiro et al. 2012; Pani & Loeb, 2013)

- *Dissipation of primordial acoustic modes & magnetic fields*

(Sunyaev & Zeldovich, 1970; Daly 1991; Hu et al. 1994; JC & Sunyaev, 2011; JC et al. 2012 - Jedamzik et al. 2000; Kunze & Komatsu, 2013)

- *Cosmological recombination radiation*

(Zeldovich et al., 1968; Peebles, 1968; Dubrovich, 1977; Rubino-Martin et al., 2006; JC & Sunyaev, 2006; Sunyaev & JC, 2009)

„high“ redshifts

„low“ redshifts

- *Signatures due to first supernovae and their remnants*

(Oh, Cooray & Kamionkowski, 2003)

- *Shock waves arising due to large-scale structure formation*

(Sunyaev & Zeldovich, 1972; Cen & Ostriker, 1999)

- *SZ-effect from clusters; effects of reionization*

(Refregier et al., 2003; Zhang et al. 2004; Trac et al. 2008)

- *more exotic processes*

(Lochan et al. 2012; Bull & Kamionkowski, 2013; Brax et al., 2013; Tashiro et al. 2013)

pre-recombination epoch

post-recombination

Quasi-Exact Treatment: Thermalization Green's Function

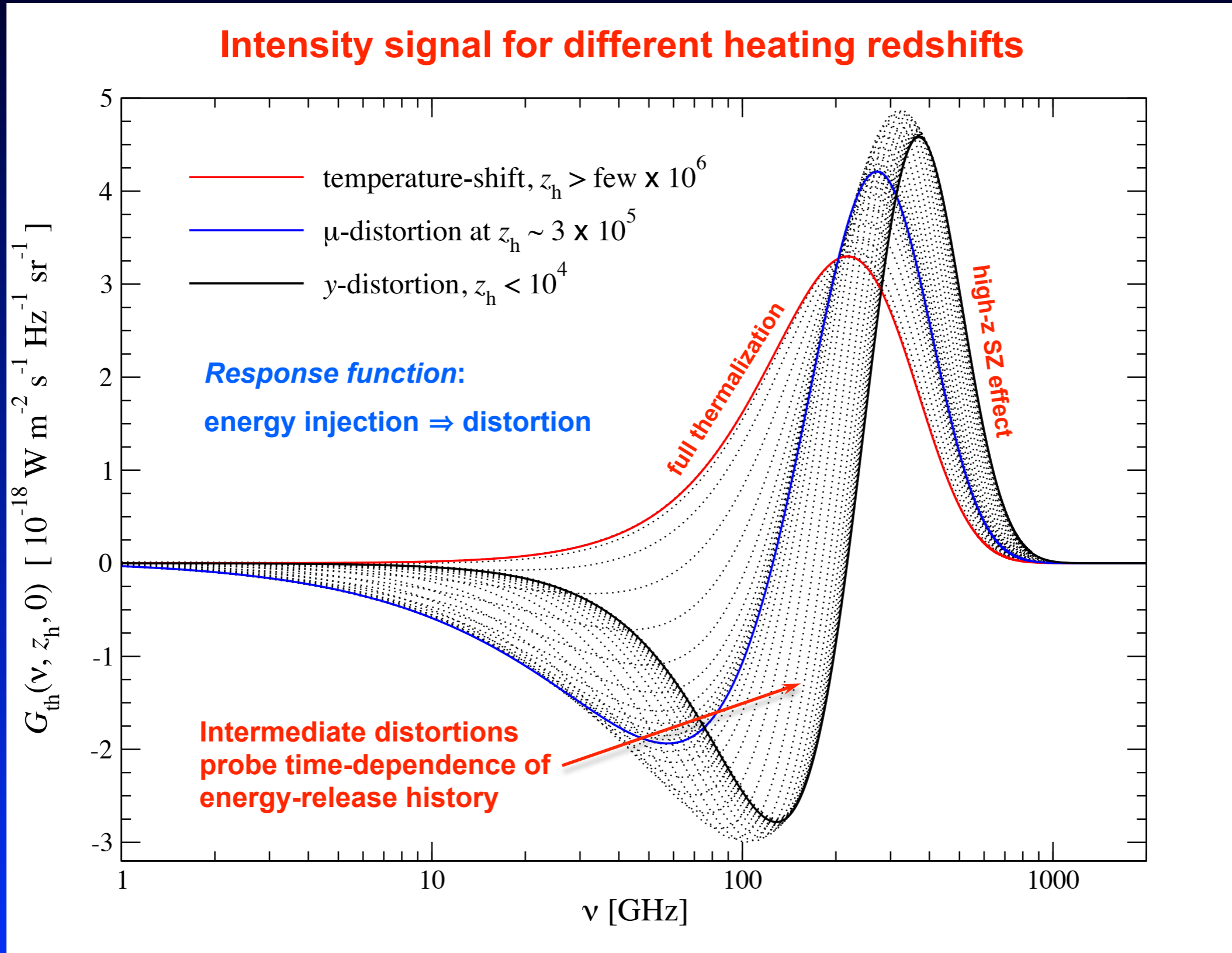
- *For real forecasts of future prospects a precise & fast method for computing the spectral distortion is needed!*
- *Case-by-case computation of the distortion (e.g., with **CosmoTherm**, JC & Sunyaev, 2012, [ArXiv:1109.6552](#)) still rather time-consuming*
- ***But:** distortions are small \Rightarrow thermalization problem becomes linear!*
- ***Simple solution:** compute “response function” of the thermalization problem \Rightarrow Green's function approach (JC, 2013, [ArXiv:1304.6120](#))*
- *Final distortion for fixed energy-release history given by*

$$\Delta I_\nu \approx \int_0^\infty G_{\text{th}}(\nu, z') \frac{d(Q/\rho_\gamma)}{dz'} dz'$$

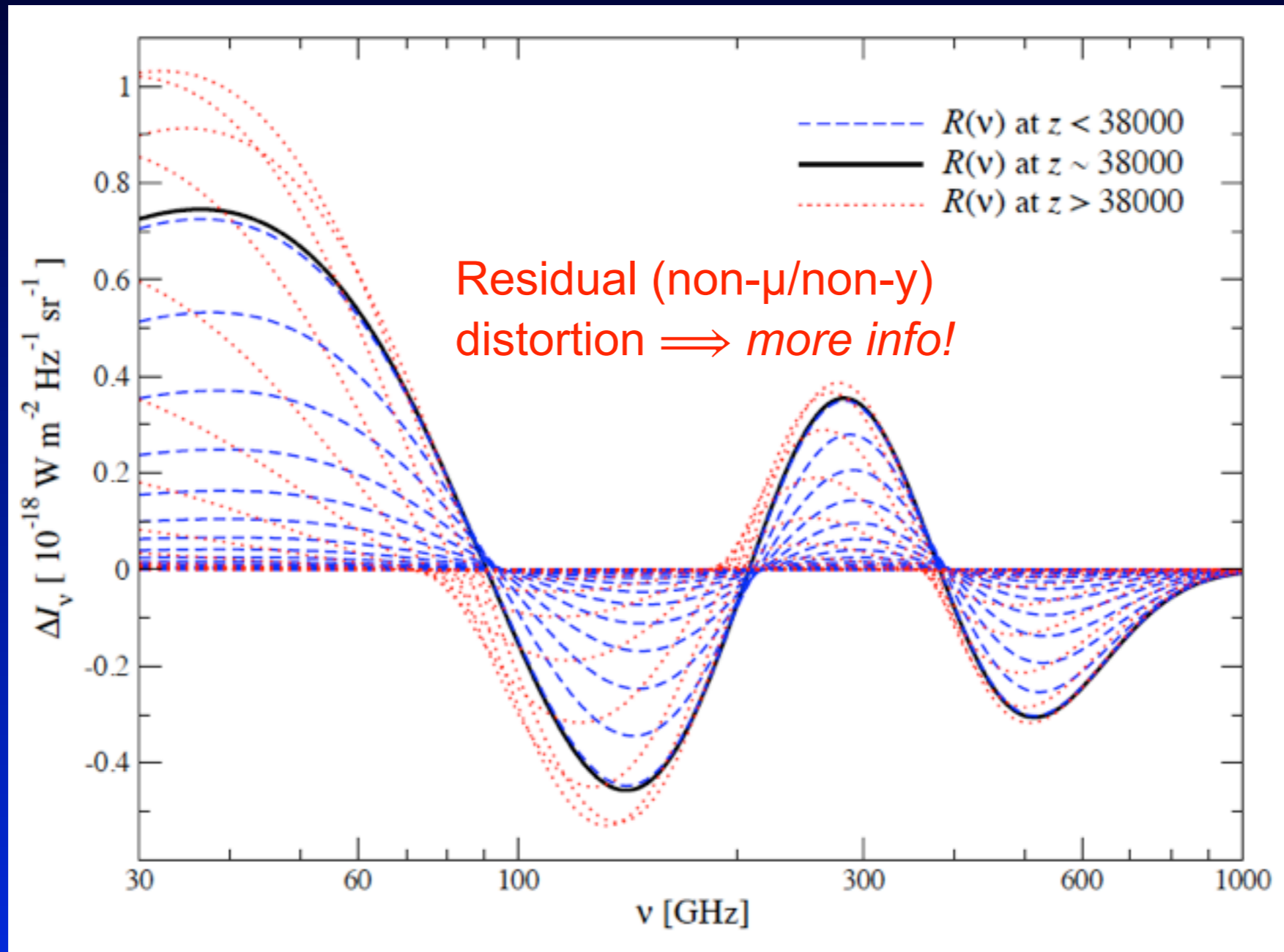
Thermalization Green's function

- *Fast and quasi-exact! No additional approximations!*

What does the spectrum look like after energy injection?

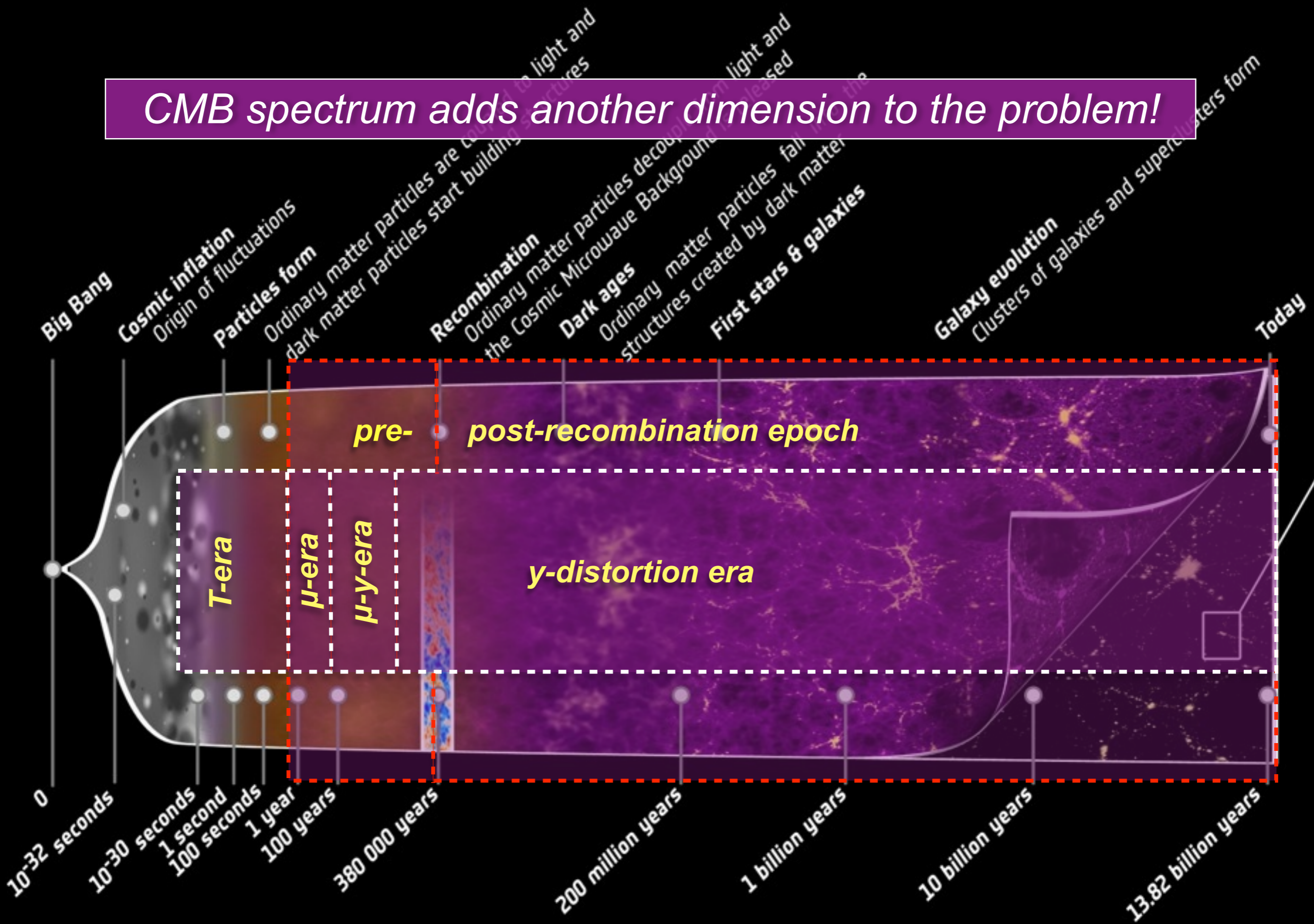


Explicitly taking out the superposition of μ & y distortion



- *Allows us to distinguish different energy release scenarios!*

CMB spectrum adds another dimension to the problem!



y - distortion

μ -y transition

μ - distortion

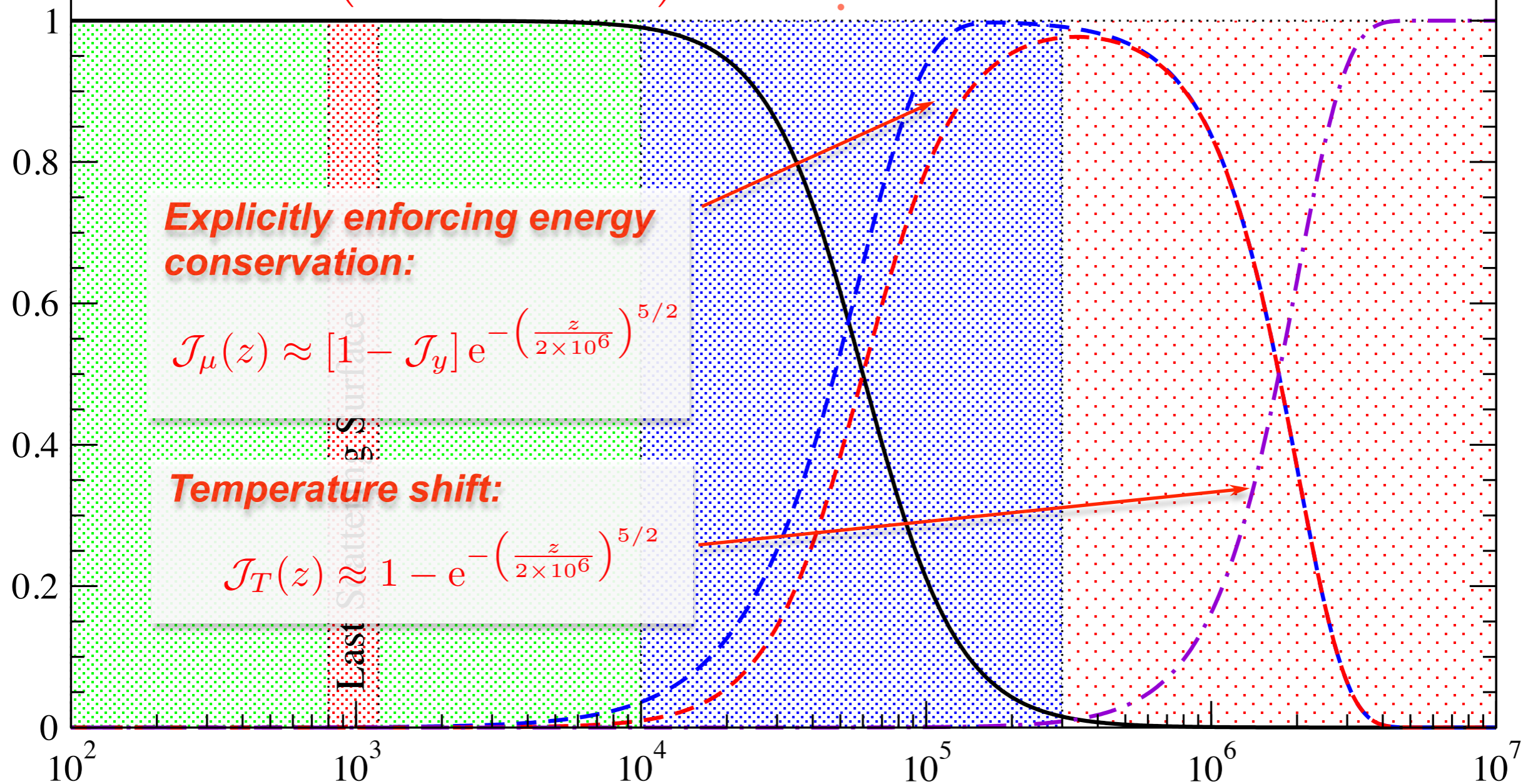
$$y \approx \frac{1}{4} \int_0^\infty \frac{d(Q/\rho_\gamma)}{dz'} \mathcal{J}_y(z') dz'$$

$$\mu \approx 1.4 \int_0^\infty \frac{d(Q/\rho_\gamma)}{dz'} \mathcal{J}_\mu(z') dz'$$

$$\mathcal{J}_y(z) \approx \left(1 + \left[\frac{1+z}{6.0 \times 10^4} \right]^{2.58} \right)^{-1}$$

$$\mathcal{J}_\mu(z) \approx \left[1 - e^{-\left[\frac{1+z}{5.8 \times 10^4} \right]^{1.88}} \right] e^{-\left[\frac{z}{2 \times 10^6} \right]^{2.5}}$$

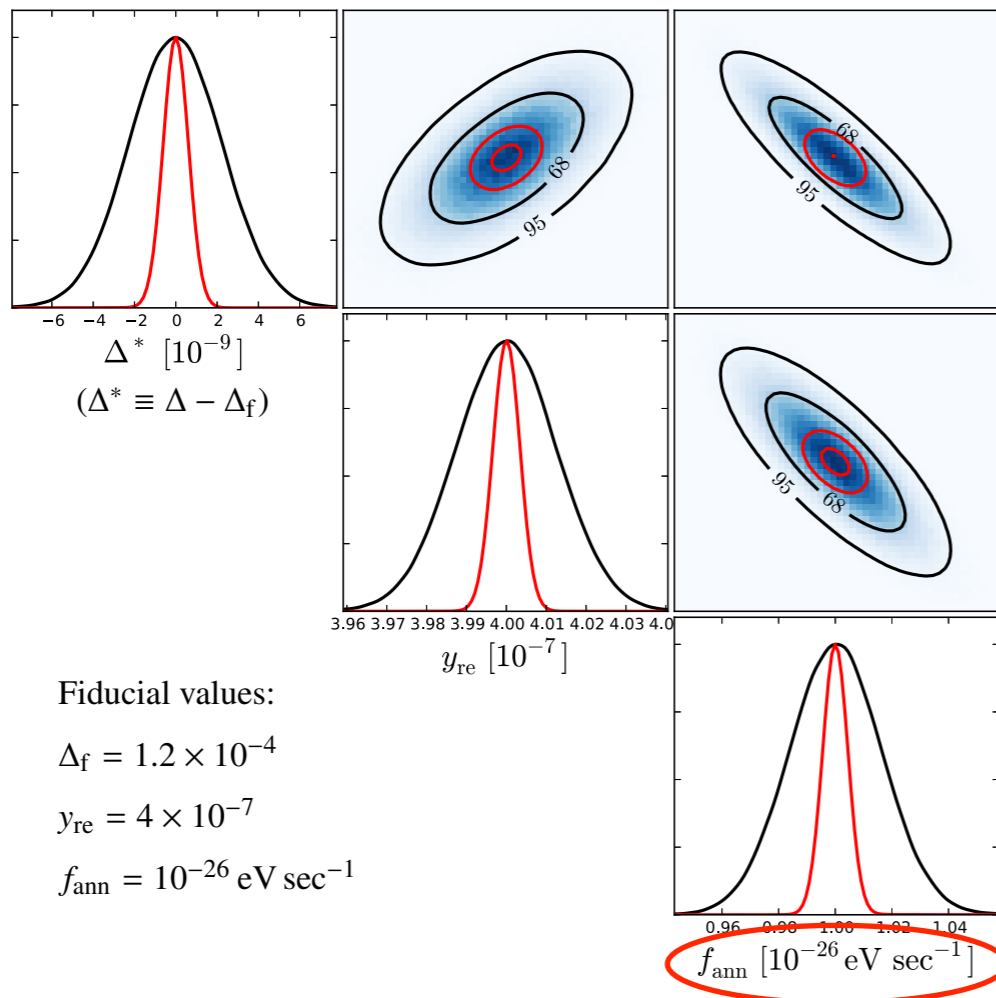
Visibility



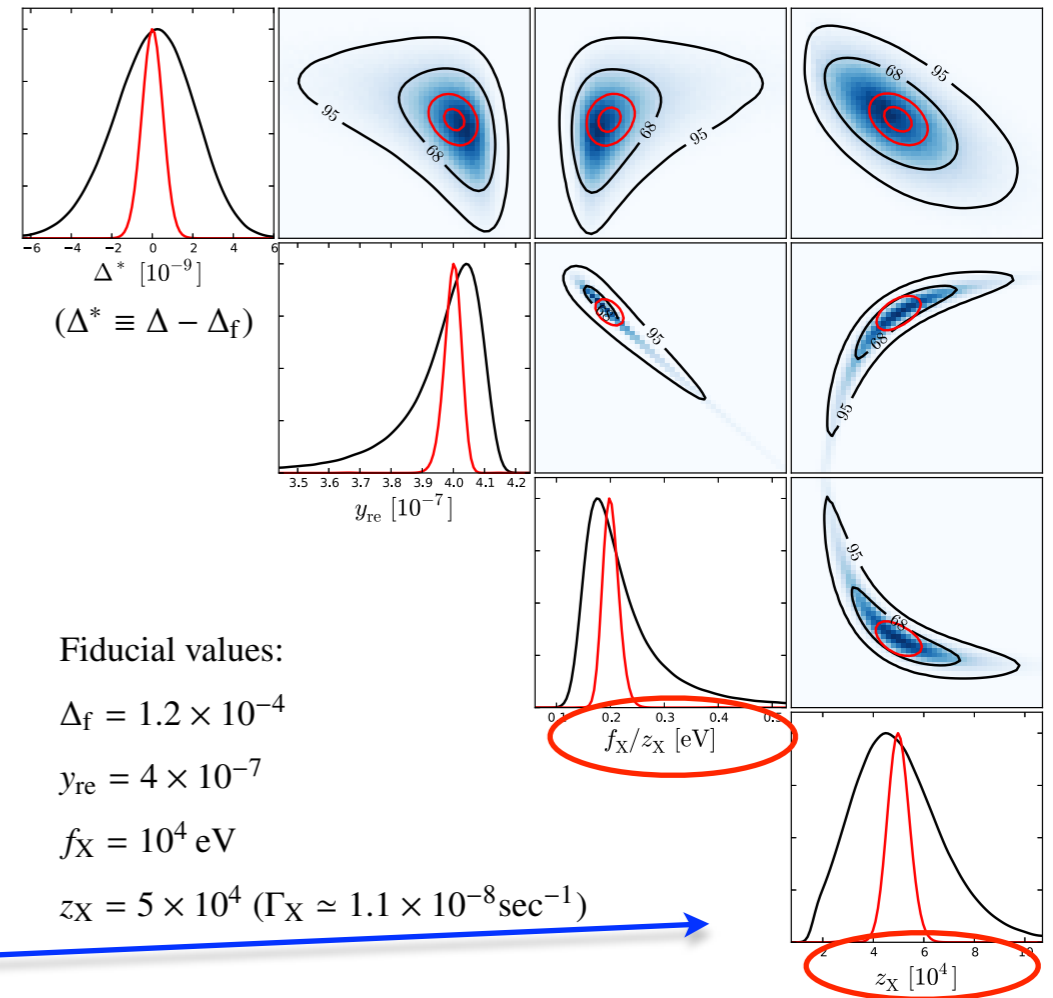
Why model-independent approach to distortion signal

- Model-dependent analysis makes model-selection non-trivial
- Real information in the distortion signal limited by sensitivity and foregrounds
- *Principle Component Analysis* (PCA) can help optimizing this!
- useful for optimizing experimental designs (*frequencies; sensitivities, ...*)!

Annihilation scenario



Decaying particle scenario



How do we compare these?

Eigenmodes for a *PIXIE*-type experiment

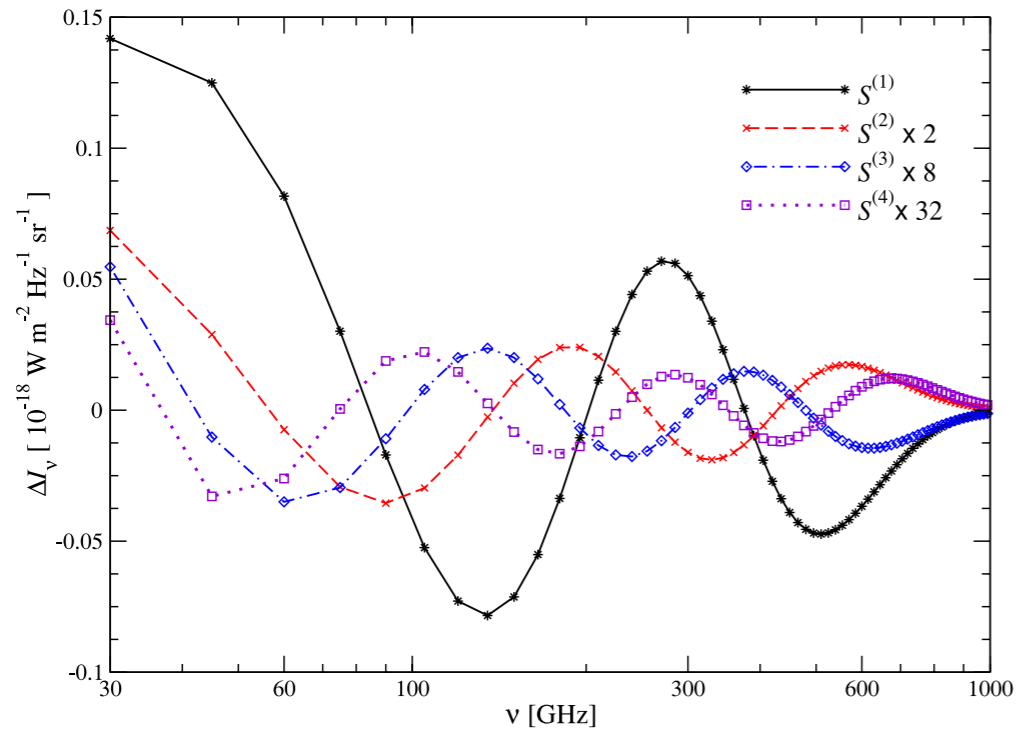
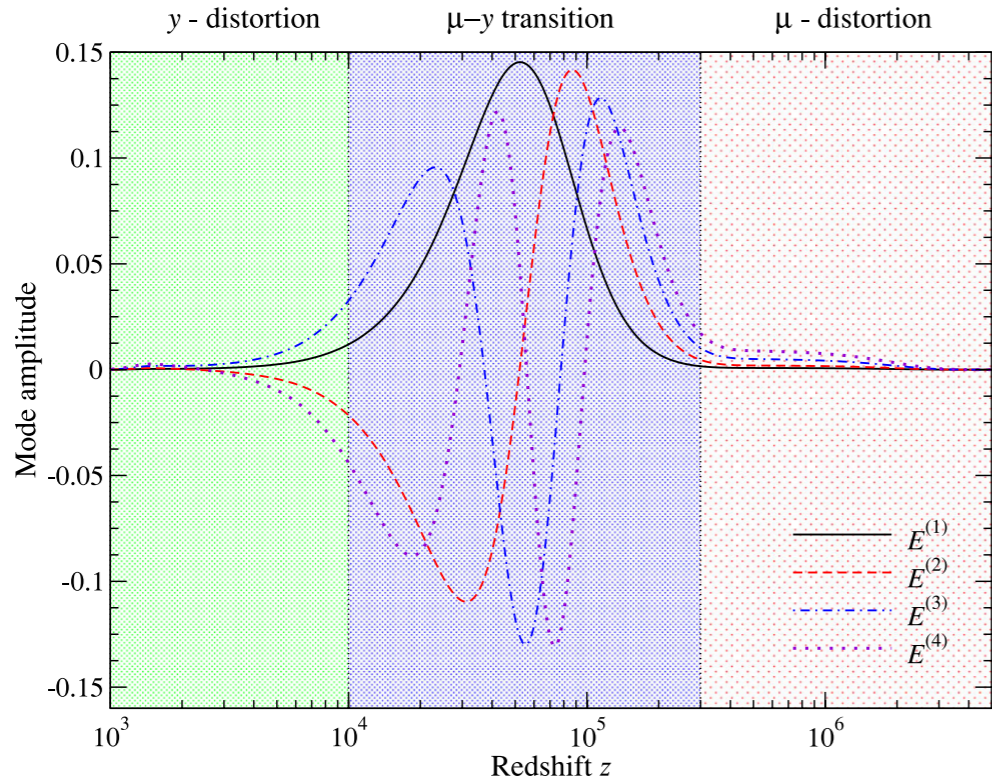


Figure 4. First few eigenmodes $E^{(k)}$ and $S^{(k)}$ for *PIXIE*-type settings ($\nu_{\min} = 30$ GHz, $\nu_{\max} = 1000$ GHz and $\Delta\nu_s = 15$ GHz). In the mode construction, we assumed that energy release only occurred at $10^3 \leq z \leq 5 \times 10^6$.

Estimated error bars

(under idealistic assumptions...)

$$\frac{\Delta T}{T} \simeq 2 \text{ nK} \left(\frac{\Delta I_c}{5 \text{ Jy sr}^{-1}} \right)$$

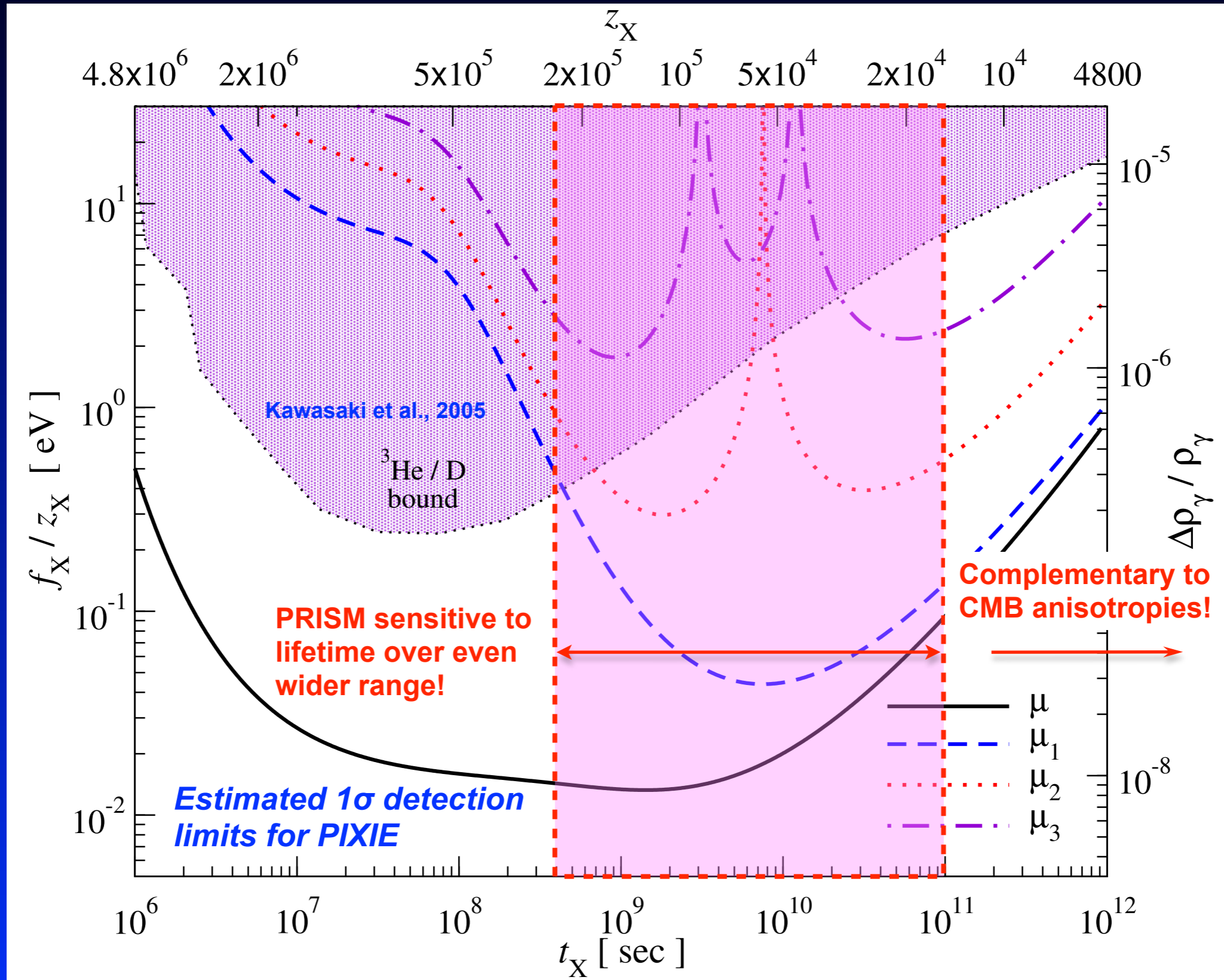
$$\Delta y \simeq 1.2 \times 10^{-9} \left(\frac{\Delta I_c}{5 \text{ Jy sr}^{-1}} \right)$$

$$\Delta \mu \simeq 1.4 \times 10^{-8} \left(\frac{\Delta I_c}{5 \text{ Jy sr}^{-1}} \right)$$

Table 1. Forecasted 1σ errors of the first six eigenmode amplitudes, $E^{(k)}$. We also give $\varepsilon_k = 4 \sum_i S_i^{(k)} / \sum_i G_{i,T}$, and the scalar products $S^{(k)} \cdot S^{(k)}$ (in units of $[10^{-18} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}]^2$). The fraction of energy release to the residual distortion and its uncertainty are given by $\varepsilon \approx \sum_k \varepsilon_k \mu_k$ and $\Delta\varepsilon \approx (\sum_k \varepsilon_k^2 \Delta\mu_k^2)^{1/2}$, respectively. For the mode construction we used *PIXIE*-settings ($\{\nu_{\min}, \nu_{\max}, \Delta\nu_s\} = \{30, 1000, 15\}$ GHz and channel sensitivity $\Delta I_c = 5 \times 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$). The errors roughly scale as $\Delta\mu_k \propto \Delta I_c / \sqrt{\Delta\nu_s}$.

k	$\Delta\mu_k$	$\Delta\mu_k / \Delta\mu_1$	ε_k	$S^{(k)} \cdot S^{(k)}$
1	1.48×10^{-7}	1	-6.98×10^{-3}	1.15×10^{-1}
2	7.61×10^{-7}	5.14	2.12×10^{-3}	4.32×10^{-3}
3	3.61×10^{-6}	24.4	-3.71×10^{-4}	1.92×10^{-4}
4	1.74×10^{-5}	1.18×10^2	8.29×10^{-5}	8.29×10^{-6}
5	8.52×10^{-5}	5.76×10^2	-1.55×10^{-5}	3.45×10^{-7}
6	4.24×10^{-4}	2.86×10^3	2.75×10^{-6}	1.39×10^{-8}

Distortions could shed light on decaying (DM) particles!



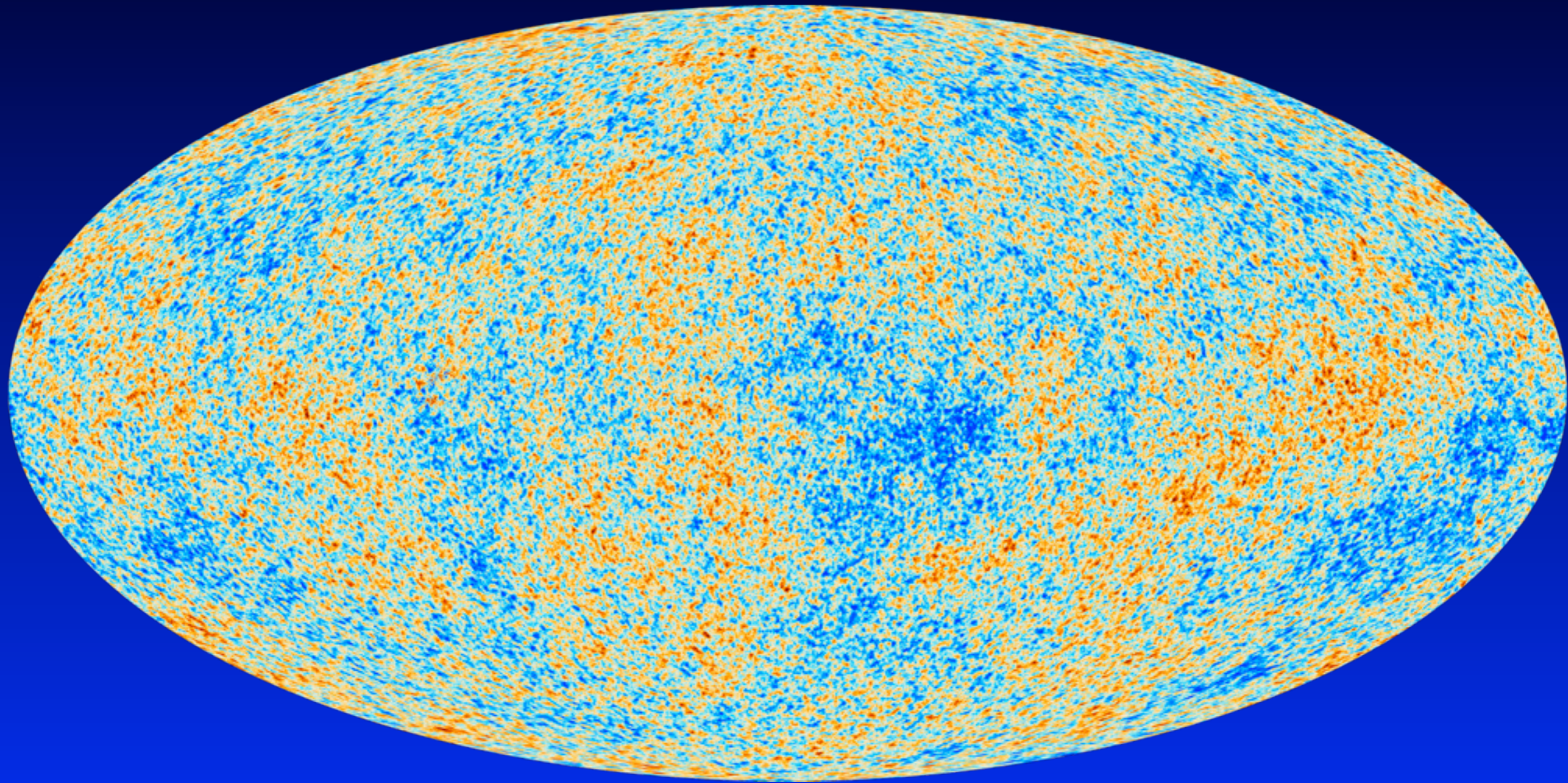
Structure of the Lectures (cont.)

Lecture III:

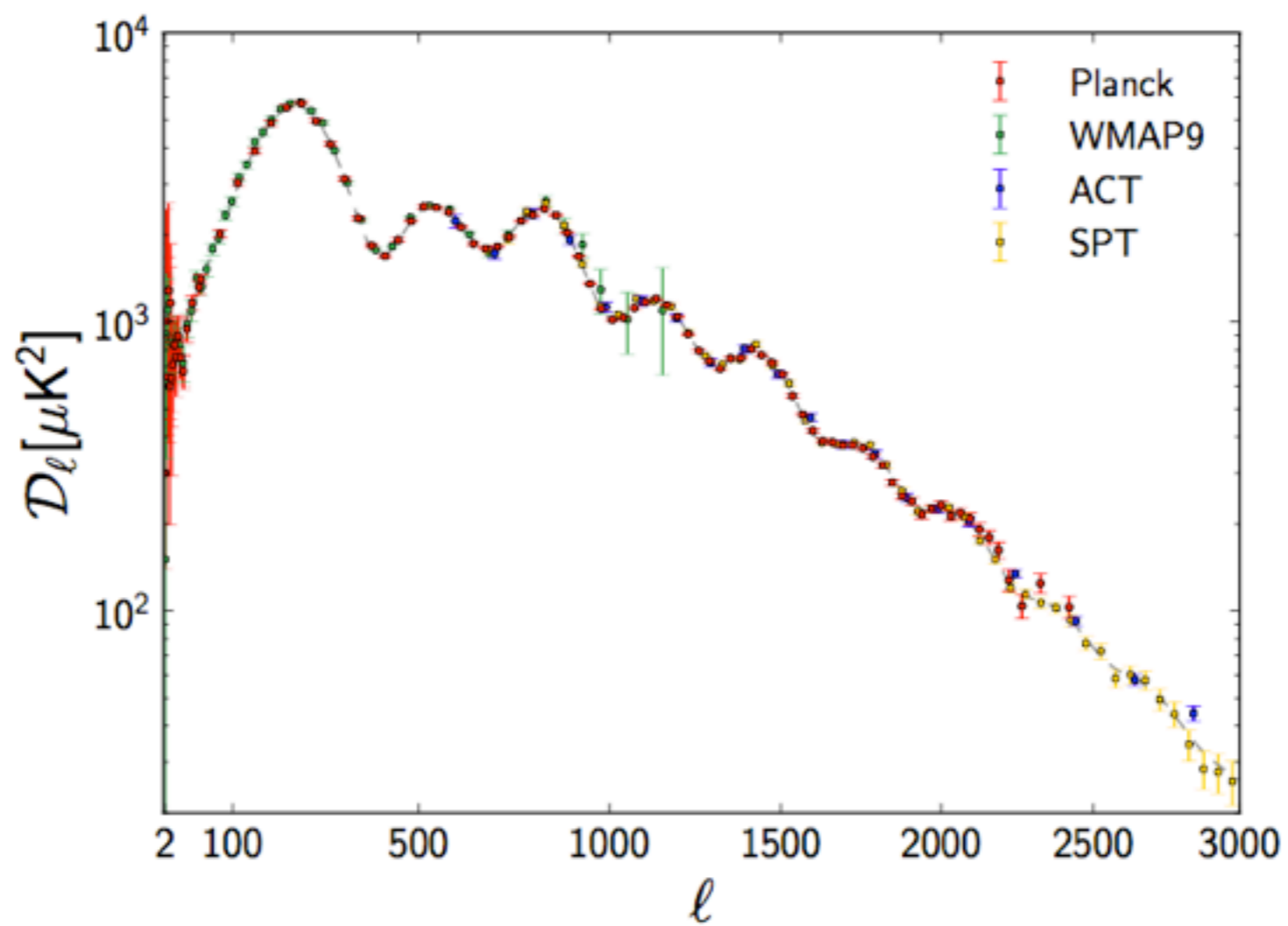
- Overview of different sources of distortions
- Decaying particles
- Dissipation of acoustic modes

The dissipation of small-scale acoustic modes

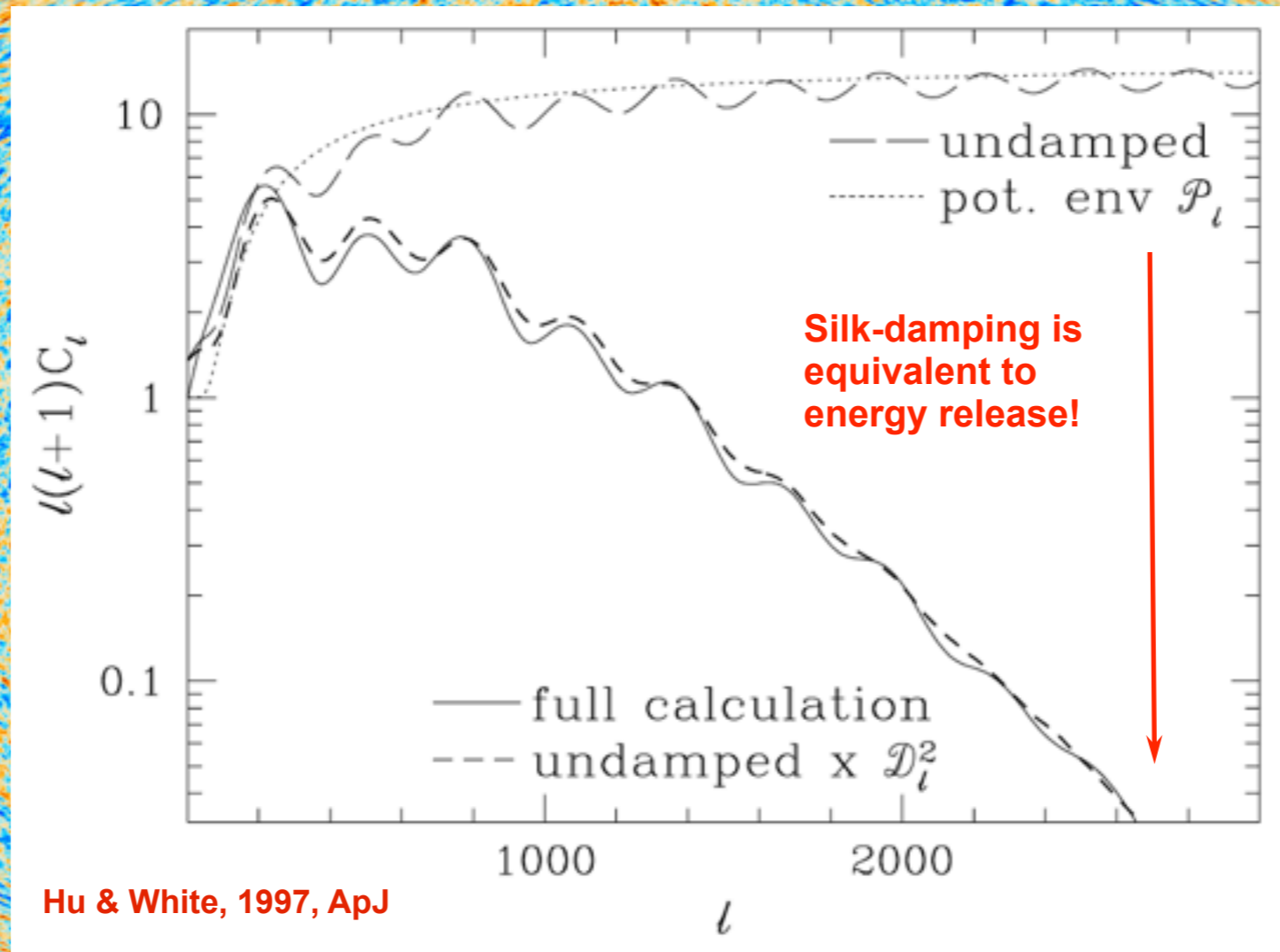
Dissipation of small-scale acoustic modes



Dissipation of small-scale acoustic modes



Dissipation of small-scale acoustic modes



Energy release caused by dissipation process

‘Obvious’ dependencies:

- *Amplitude* of the small-scale power spectrum
- *Shape* of the small-scale power spectrum
- *Dissipation scale* $\rightarrow k_D \sim (H_0 \Omega_{\text{rel}}^{1/2} N_{e,0})^{1/2} (1+z)^{3/2}$ at early times

not so ‘obvious’ dependencies:

- *primordial non-Gaussianity* in the ultra squeezed limit
(Pajer & Zaldarriaga, 2012; Ganc & Komatsu, 2012)
- *Type* of the perturbations (adiabatic \leftrightarrow isocurvature)
(Barrow & Coles, 1991; Hu et al., 1994; Dent et al, 2012, JC & Grin, 2012)
- *Neutrinos* (or any extra relativistic degree of freedom)

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*CMB Spectral distortions could add additional numbers beyond
‘just’ the tensor-to-scalar ratio from B-modes!*

Handwavy derivation of the heating rate

Dissipation of acoustic modes: 'classical treatment'

- energy stored in plane sound waves

$$\text{Landau \& Lifshitz, 'Fluid Mechanics', \S 65} \Rightarrow Q \sim c_s^2 \rho (\delta\rho/\rho)^2$$

- expression for normal ideal gas where ρ is '*mass density*' and c_s denotes '*sounds speed*'

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- photon-baryon fluid with baryon loading $R \ll 1$

$$(c_s/c)^2 = [3(1+R)]^{-1} \sim 1/3$$

$$\rho \rightarrow \rho_Y = a_R T^4$$

$$\delta\rho/\rho \rightarrow 4(\delta T_0/T) \equiv 4\Theta_0 \leftarrow \text{only perturbation in the monopole accounted for}$$

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$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt = -16/3 d\langle \Theta_0^2 \rangle / dt$$

'minus' because *decrease* of Θ at small scales means *increase* for average spectrum

can be calculated using first order perturbation theory

Dissipation of acoustic modes: 'classical treatment'

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Landau & Lifshitz, 'Fluid Mechanics', § 65 $\Rightarrow Q \sim c_s^2 \rho (\delta\rho/\rho)^2$

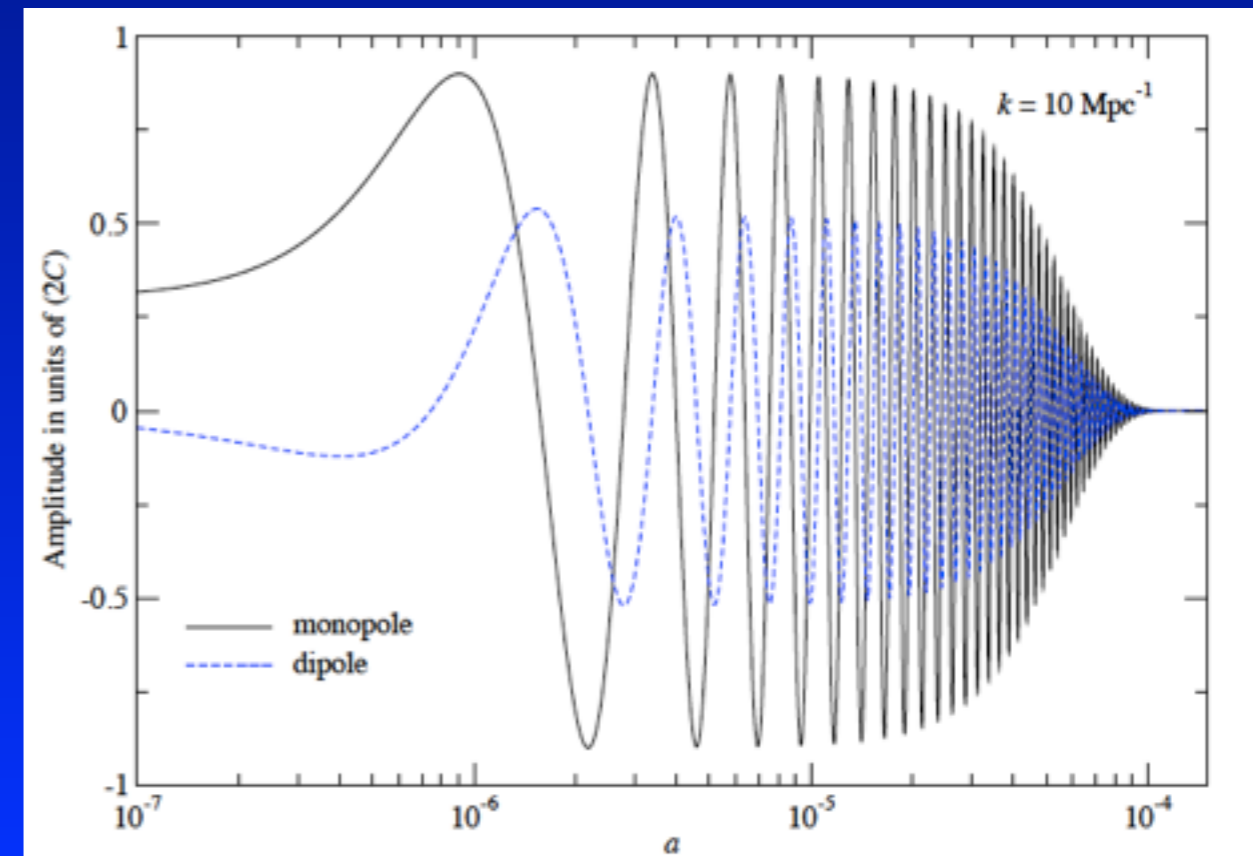
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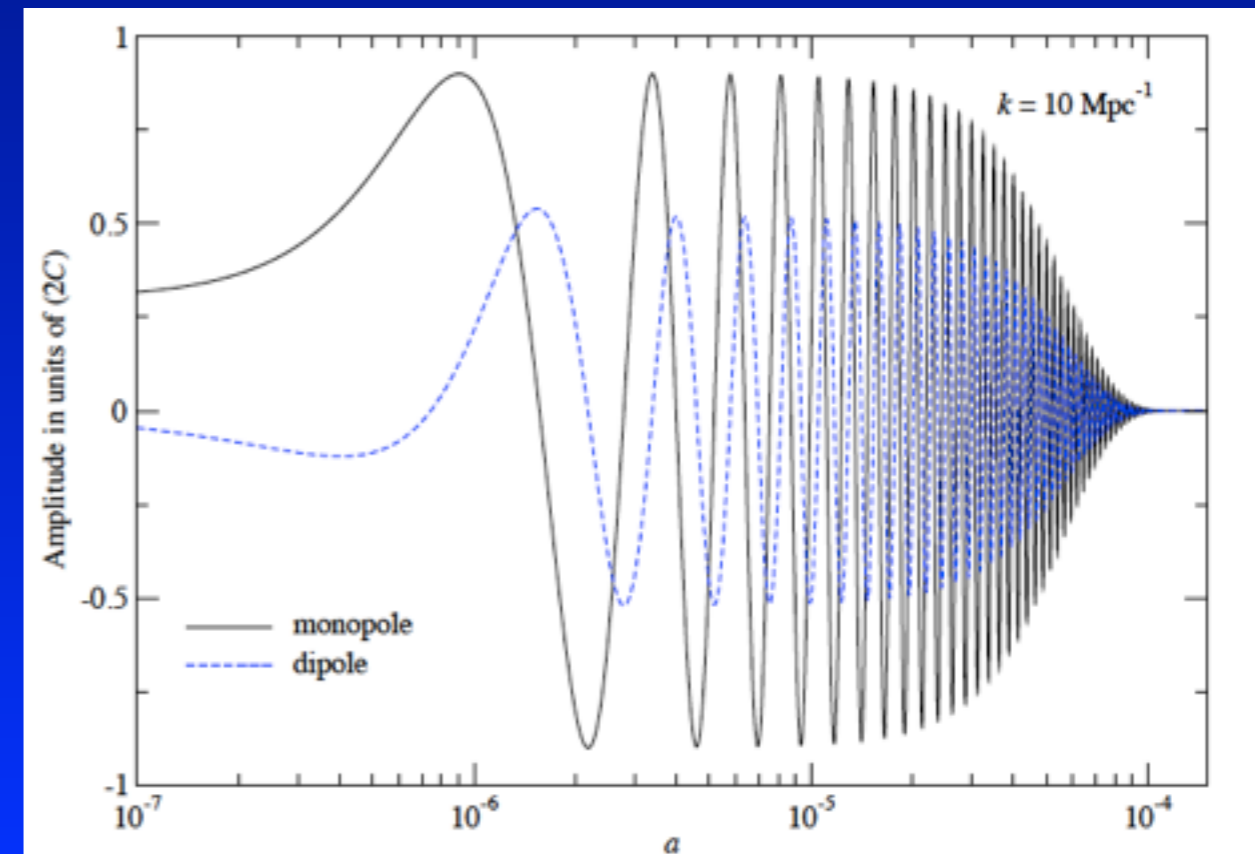
$$\rho \rightarrow \rho_Y = a_R T^4 \quad \Rightarrow \quad (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt = -16/3 d\langle \Theta_0^2 \rangle / dt$$

$$\delta\rho/\rho \rightarrow 4(\delta T_0/T) \equiv 4\Theta_0$$

- Simple estimate does *not* capture all the physics of the problem:

(JC, Khatri & Sunyaev, 2012)

- ▶ *total energy release is 9/4 ~ 2.25 times larger!*
- ▶ *only 1/3 of the released energy goes into distortions*



Early power spectrum constraints from FIRAS

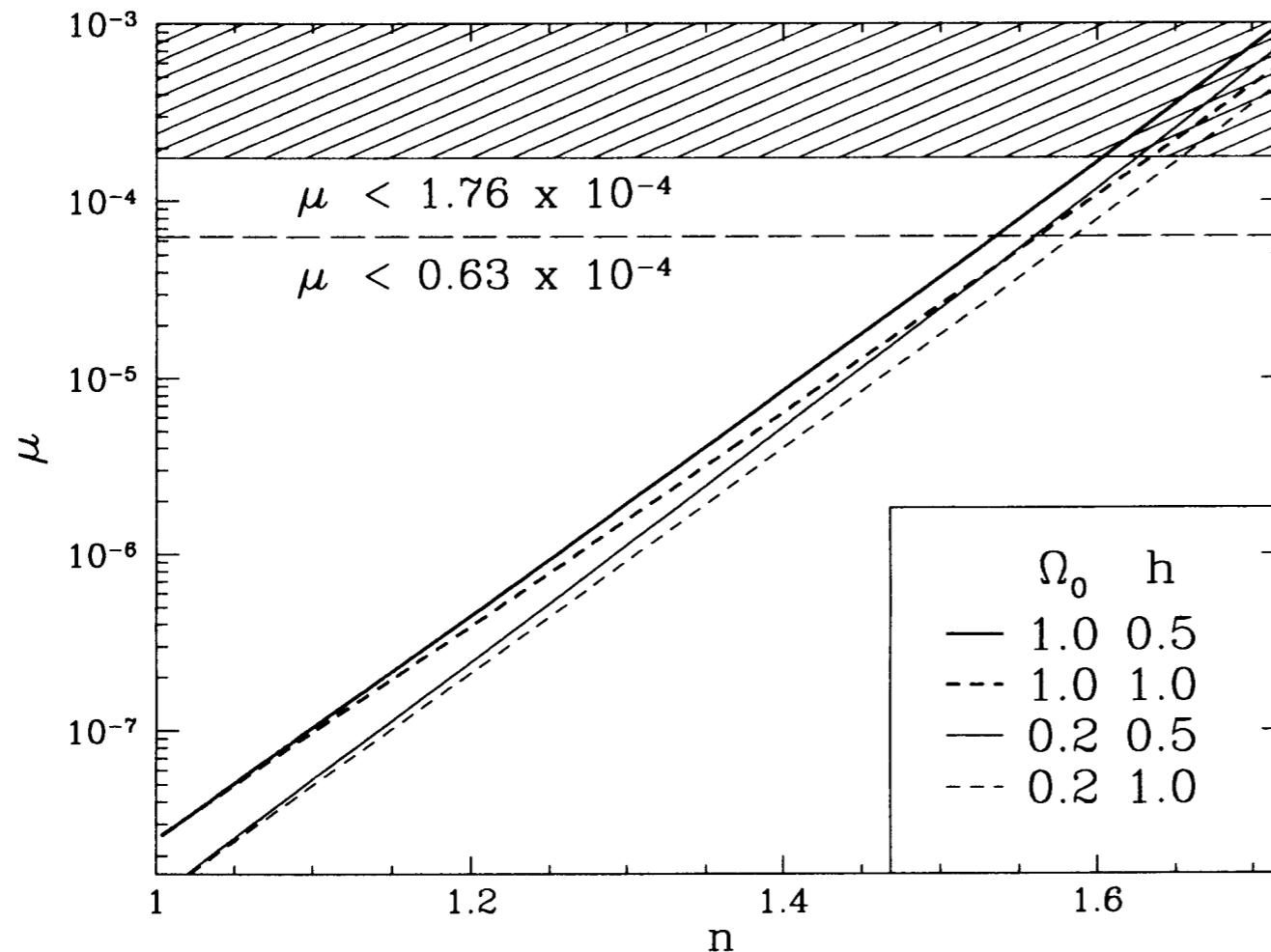


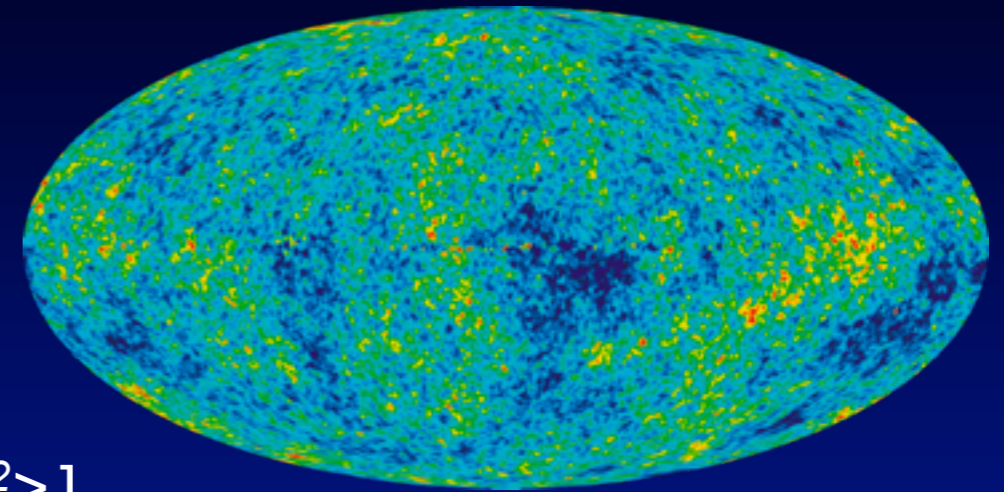
FIG. 1.—Spectral distortion μ , predicted from the full eq. (11), as a function of the power index n for a normalization at the mean of the *COBE* DMR detection $(\Delta T/T)_{10^\circ} = 1.12 \times 10^{-5}$. With the uncertainties on *both* the DMR and FIRAS measurements, the conservative 95% upper limit is effectively $\mu < 1.76 \times 10^{-4}$ (see text). The corresponding constraint on n is relatively weakly dependent on cosmological parameters: $n < 1.60$ ($h = 0.5$) and $n < 1.63$ ($h = 1.0$) for $\Omega_0 = 1$ and quite similar for $0.2 < \Omega_0 = 1 - \Omega_\Lambda < 1$ universes. These limits are nearly independent of Ω_B . We have also plotted the optimistic 95% upper limit on $\mu < 0.63 \times 10^{-4}$ for comparison as discussed in the text.

- based on classical estimate for heating rate
- Tightest / cleanest constraint at that point!
- simple power-law spectrum assumed
- $\mu \sim 10^{-8}$ for scale-invariant power spectrum
- $n_s \lesssim 1.6$

Dissipation of acoustic modes: 'microscopic picture'

- after inflation: photon field has spatially varying temperature T
- average energy stored in photon field at any given moment

$$\langle \rho_\gamma \rangle = a_R \langle T^4 \rangle \approx a_R \langle T \rangle^4 [1 + \underbrace{4\langle \Theta \rangle}_{=0} + 6\langle \Theta^2 \rangle]$$



E.g., our snapshot at $z=0$

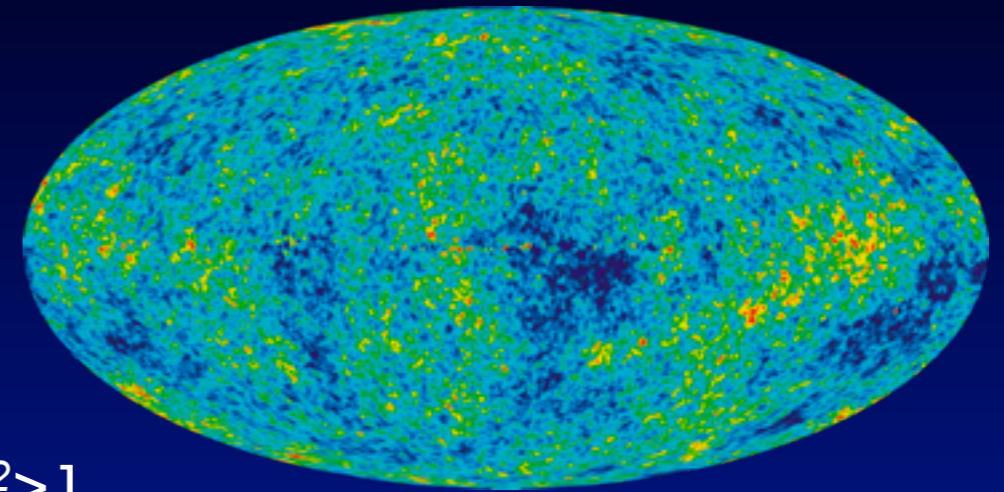
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$$\Rightarrow (a^4 \rho_\gamma)^{-1} da^4 Q_{ac}/dt = -6 d\langle \Theta^2 \rangle/dt$$

- Monopole actually **drops** out of the equation!
- In principle *all* higher multipoles contribute to the energy release



E.g., our snapshot at $z=0$

Dissipation of acoustic modes: 'microscopic picture'

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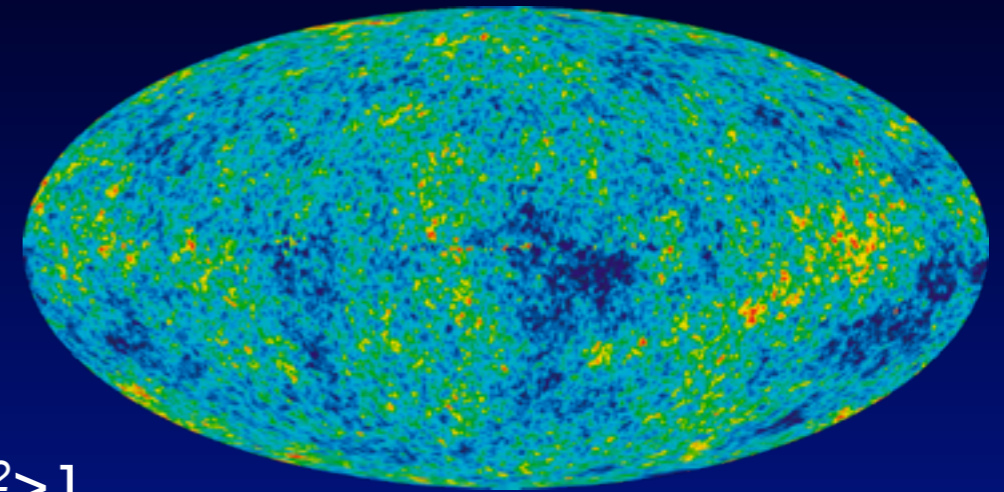
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- Monopole actually **drops** out of the equation!
- In principle **all** higher multipoles contribute to the energy release
- At high redshifts ($z \geq 10^4$):

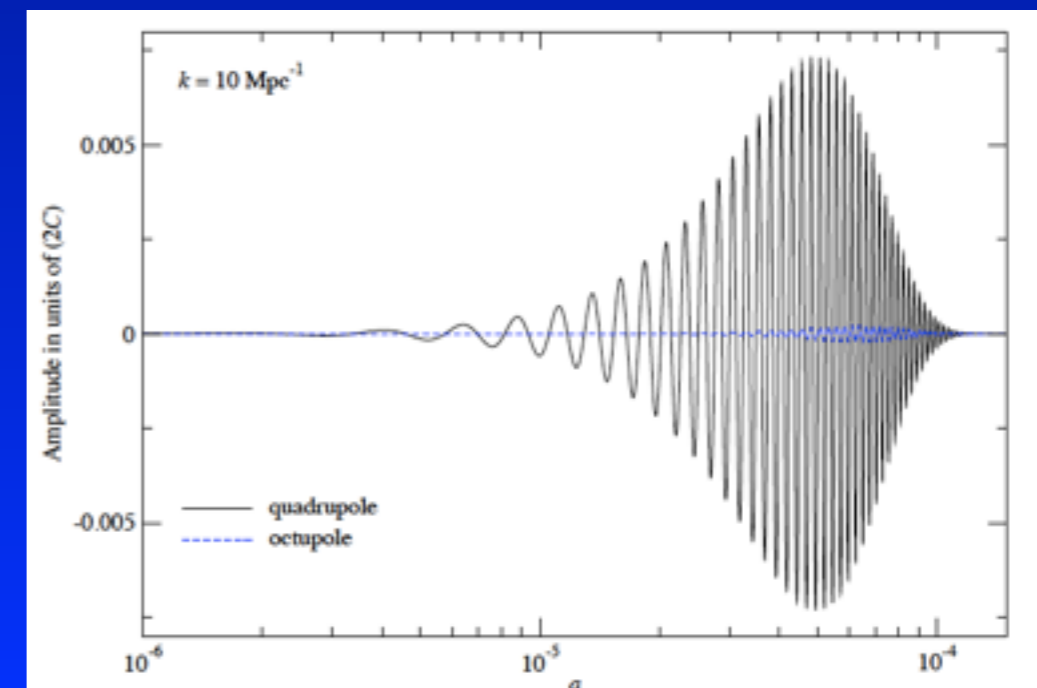
- ▶ *net (gauge-invariant) dipole and contributions from higher multipoles are negligible*
- ▶ *dominant term caused by quadrupole anisotropy*

$$\Rightarrow (a^4 \rho_Y)^{-1} da^4 Q_{ac}/dt \approx -12 d\langle \Theta_0^2 \rangle/dt$$

9/4 larger than classical estimate

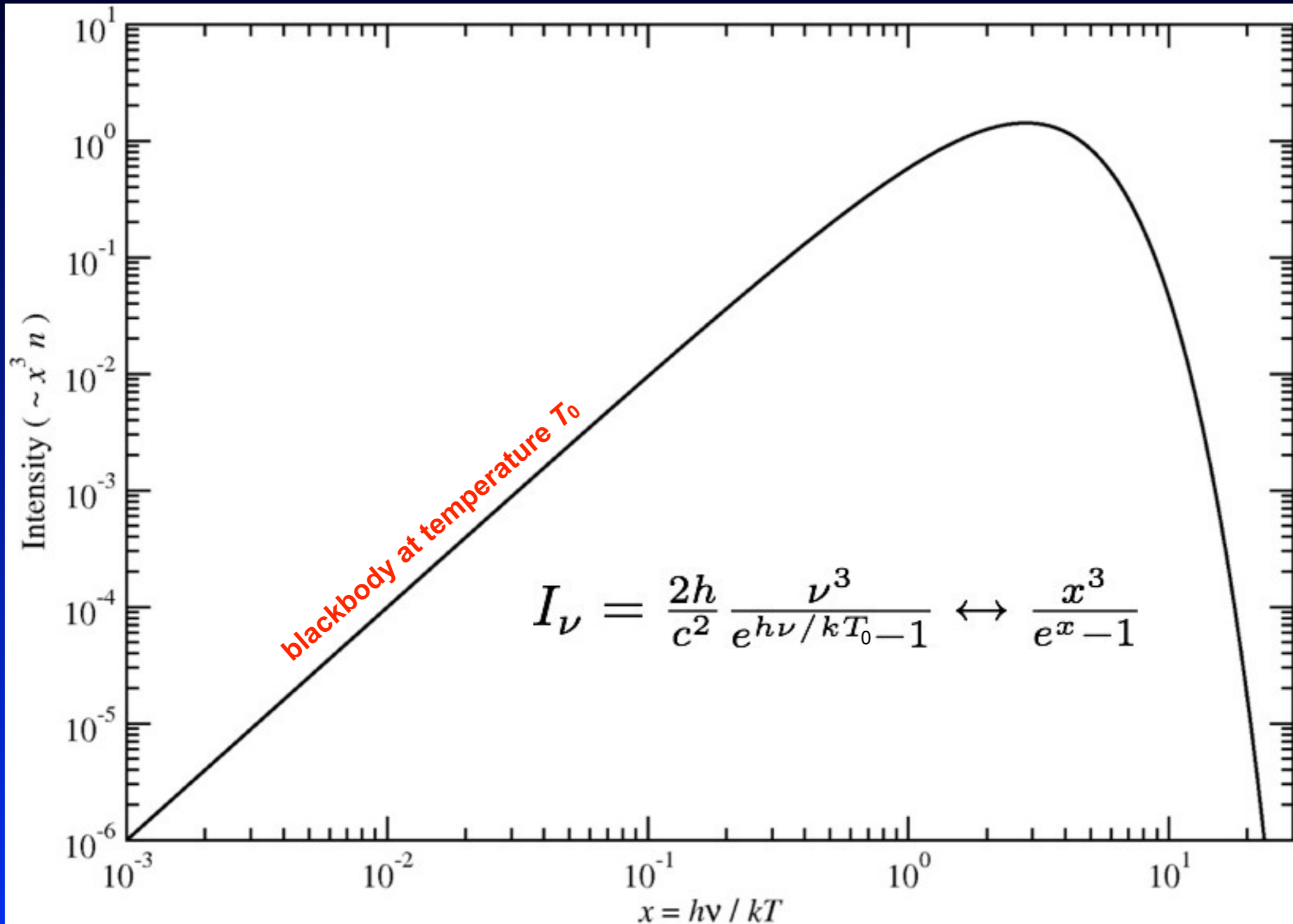


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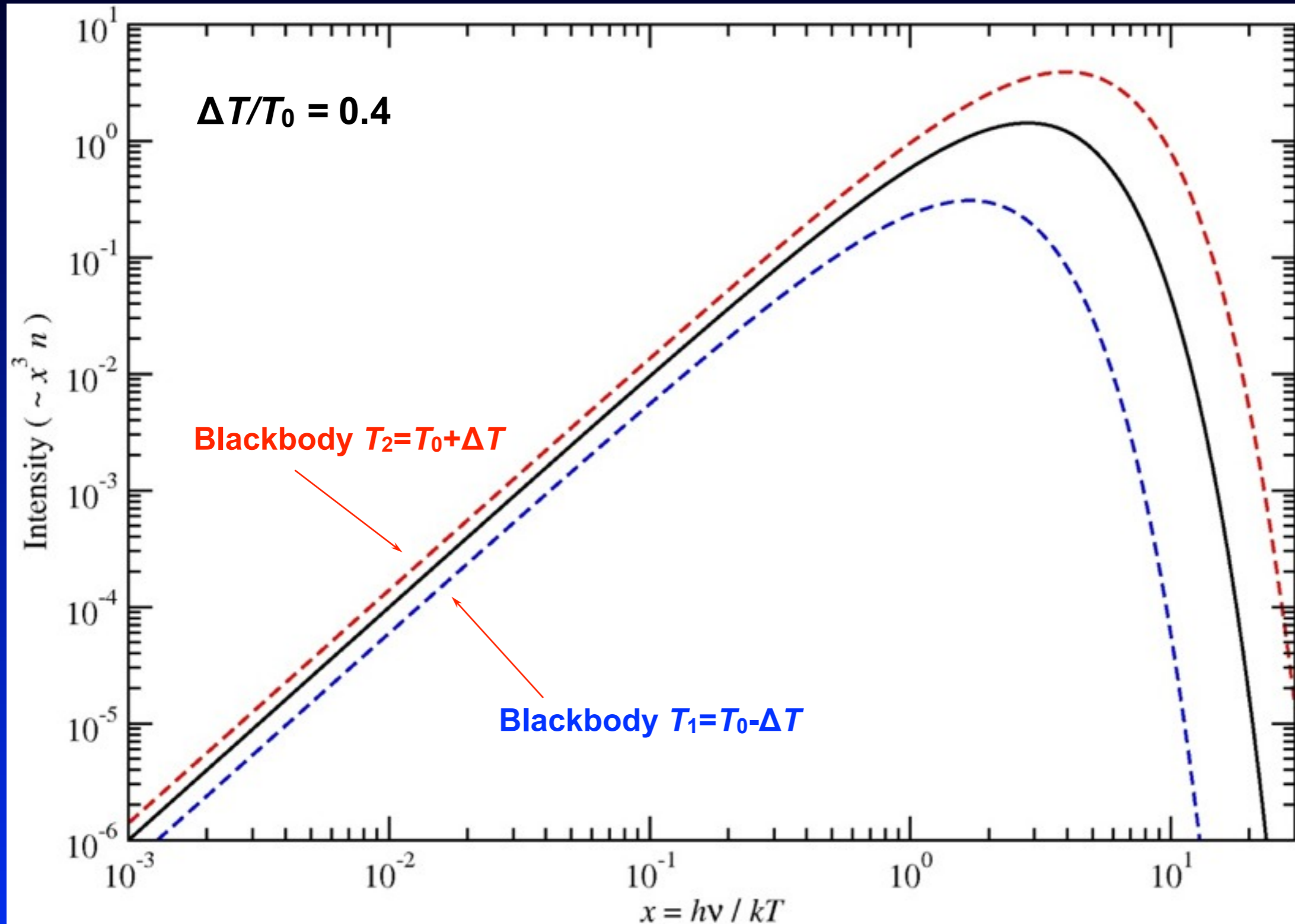


Where does the 2:1 ratio come from?

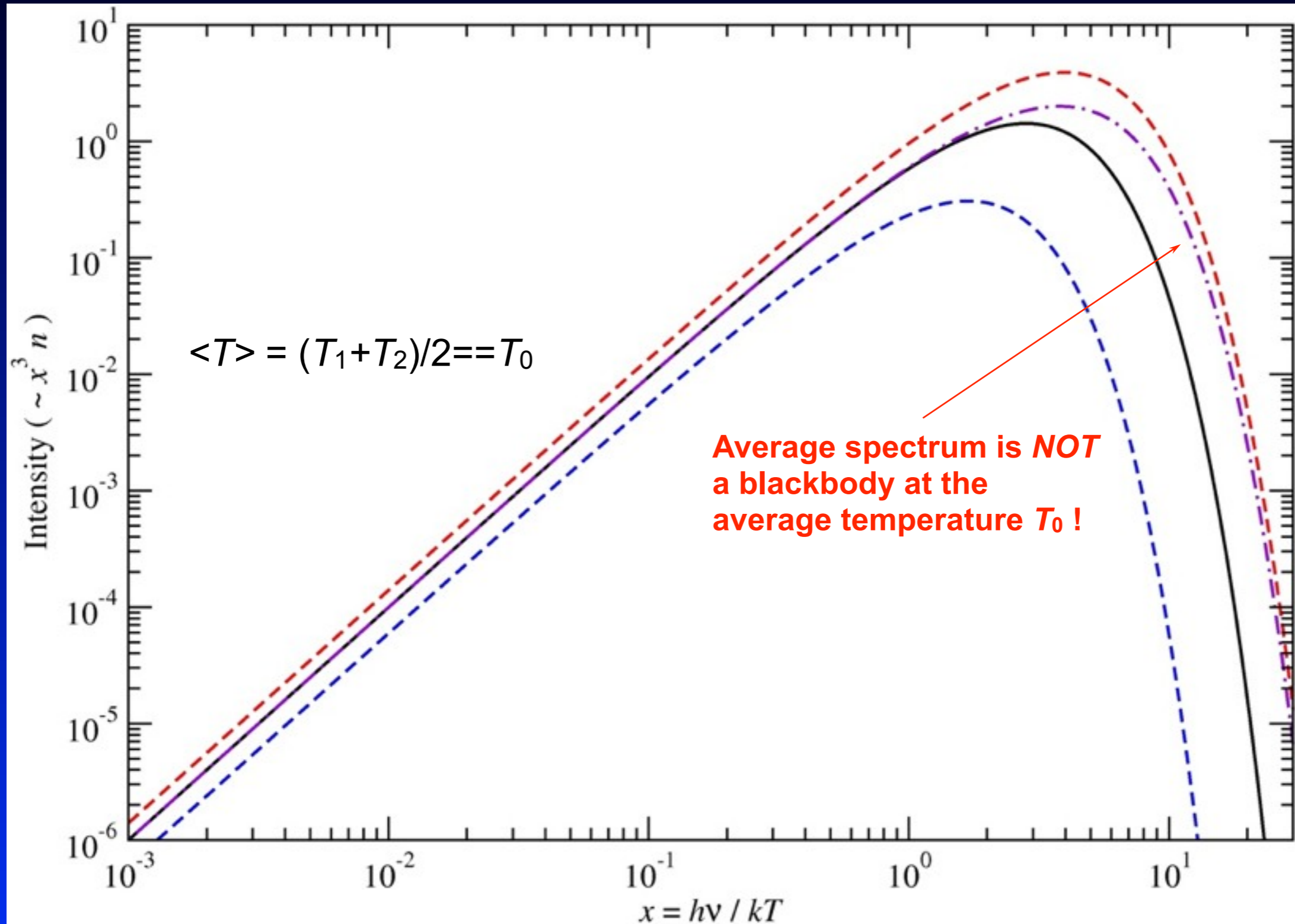
Superpositions of blackbody spectra



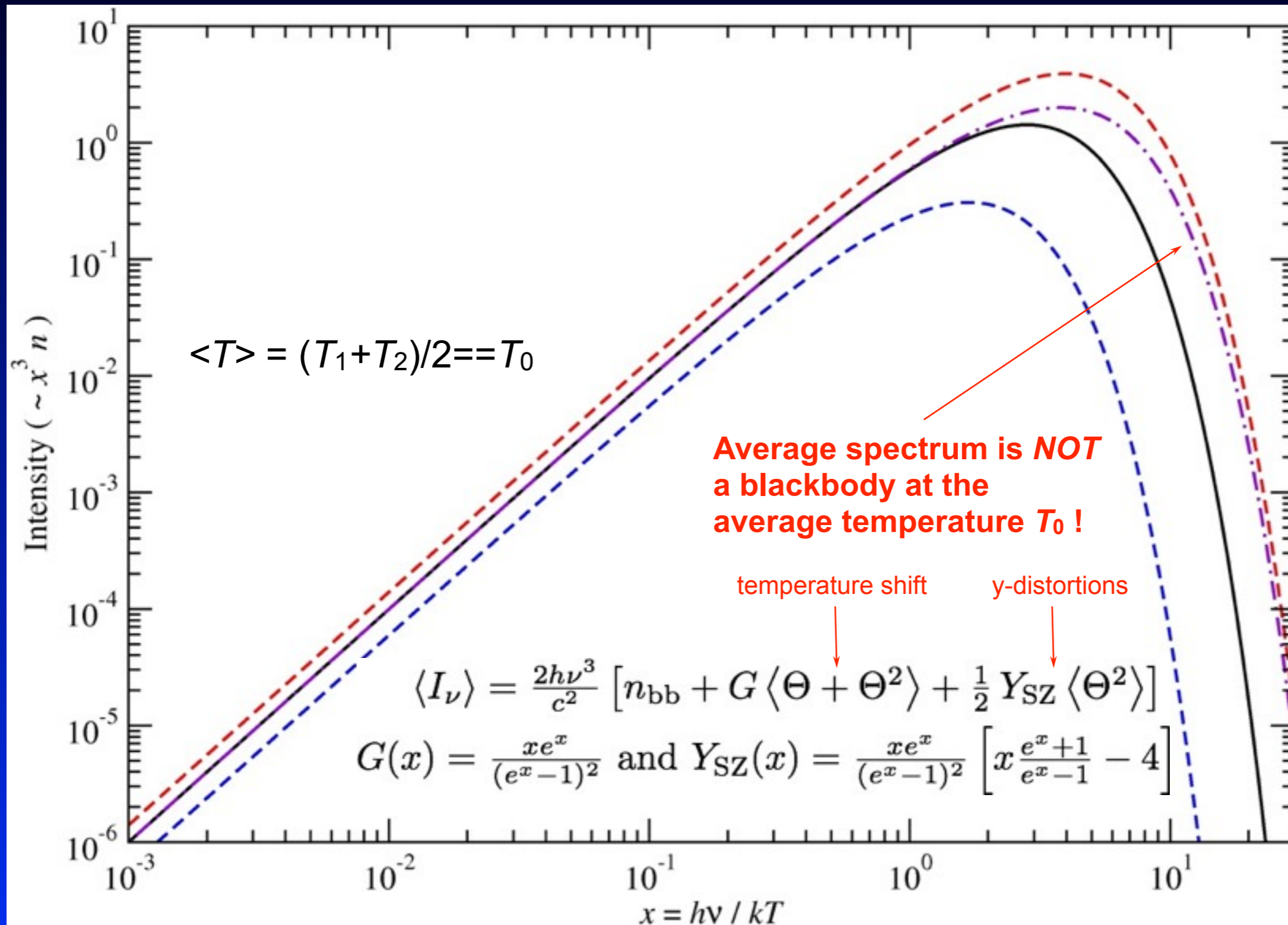
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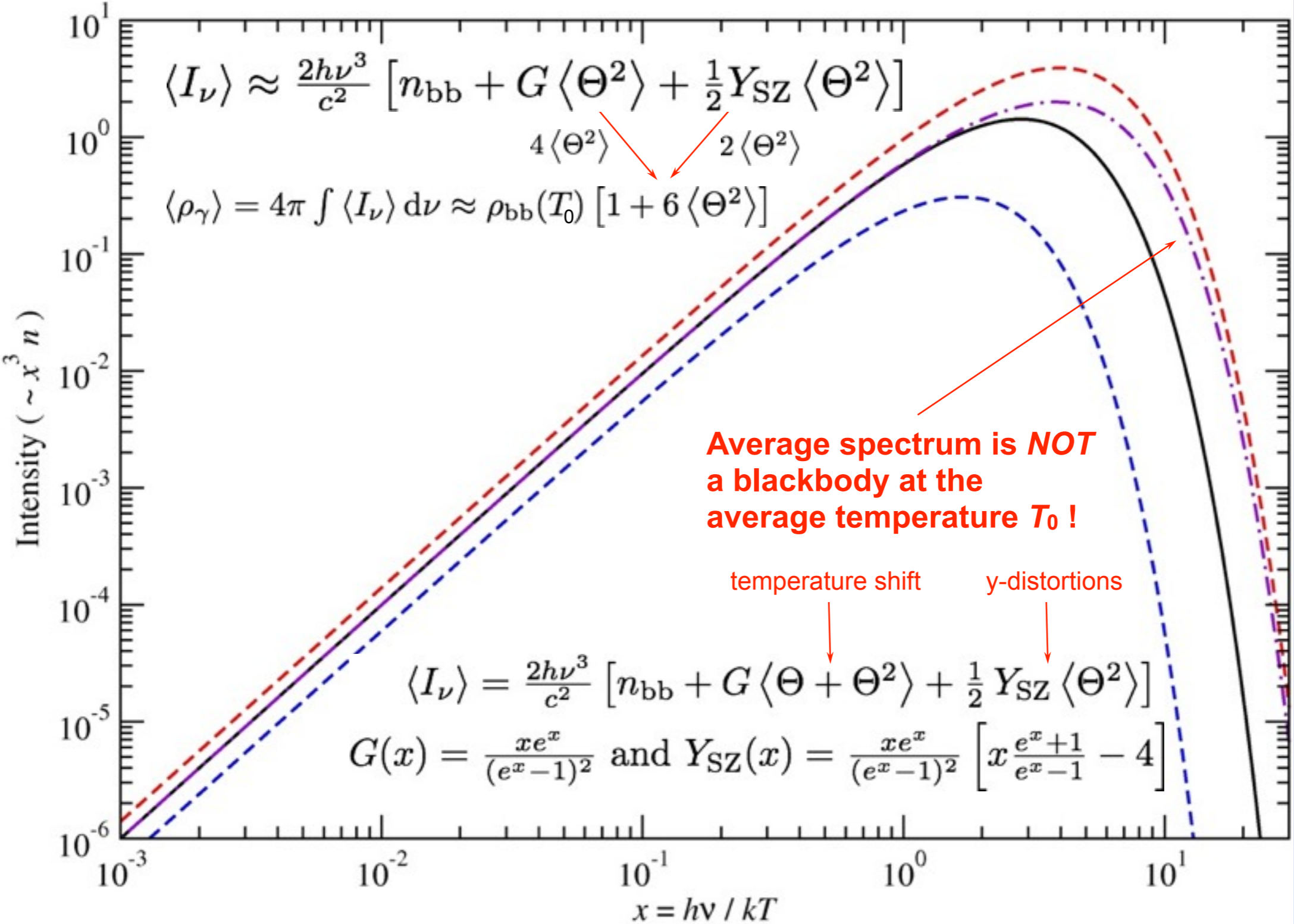
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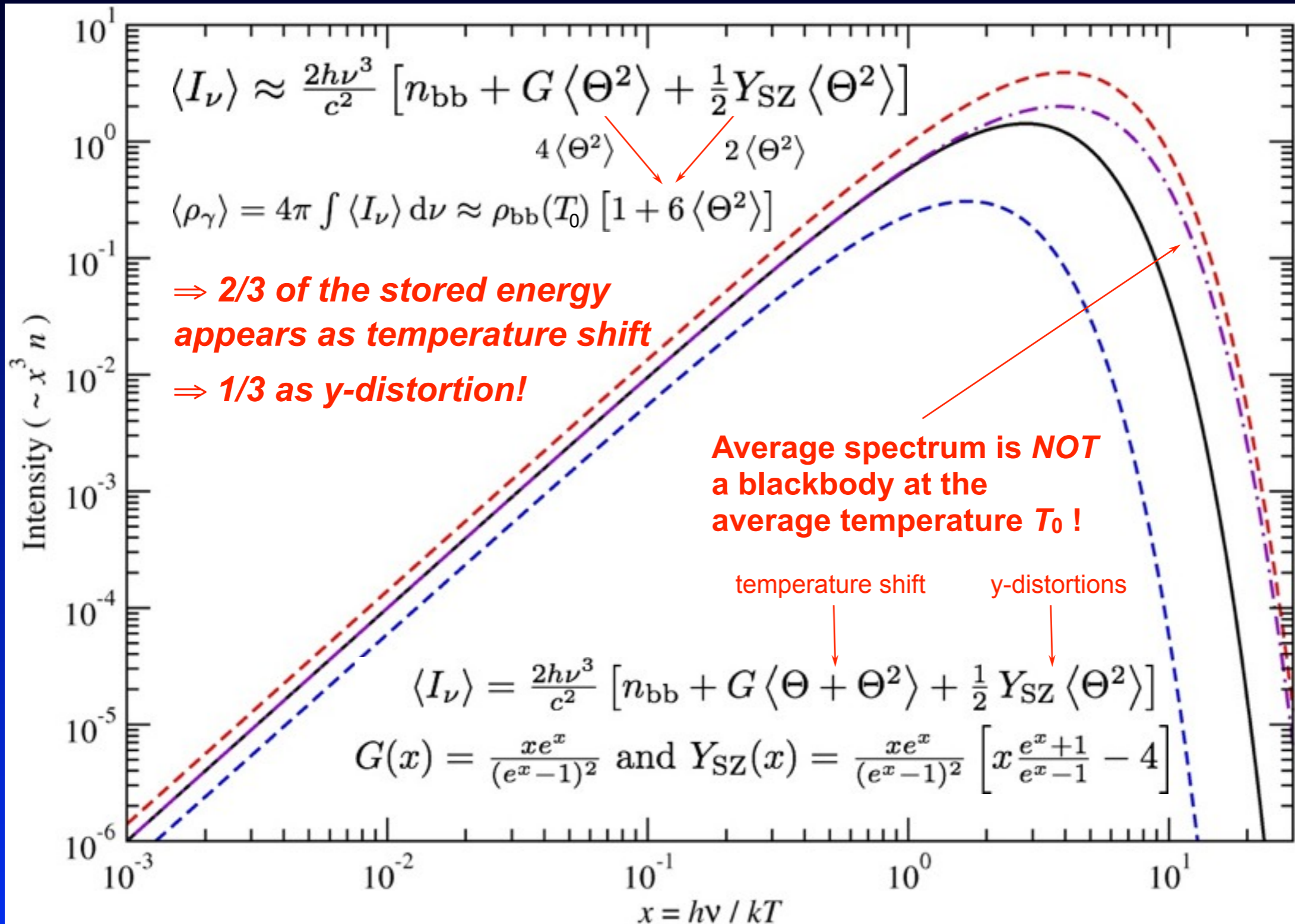
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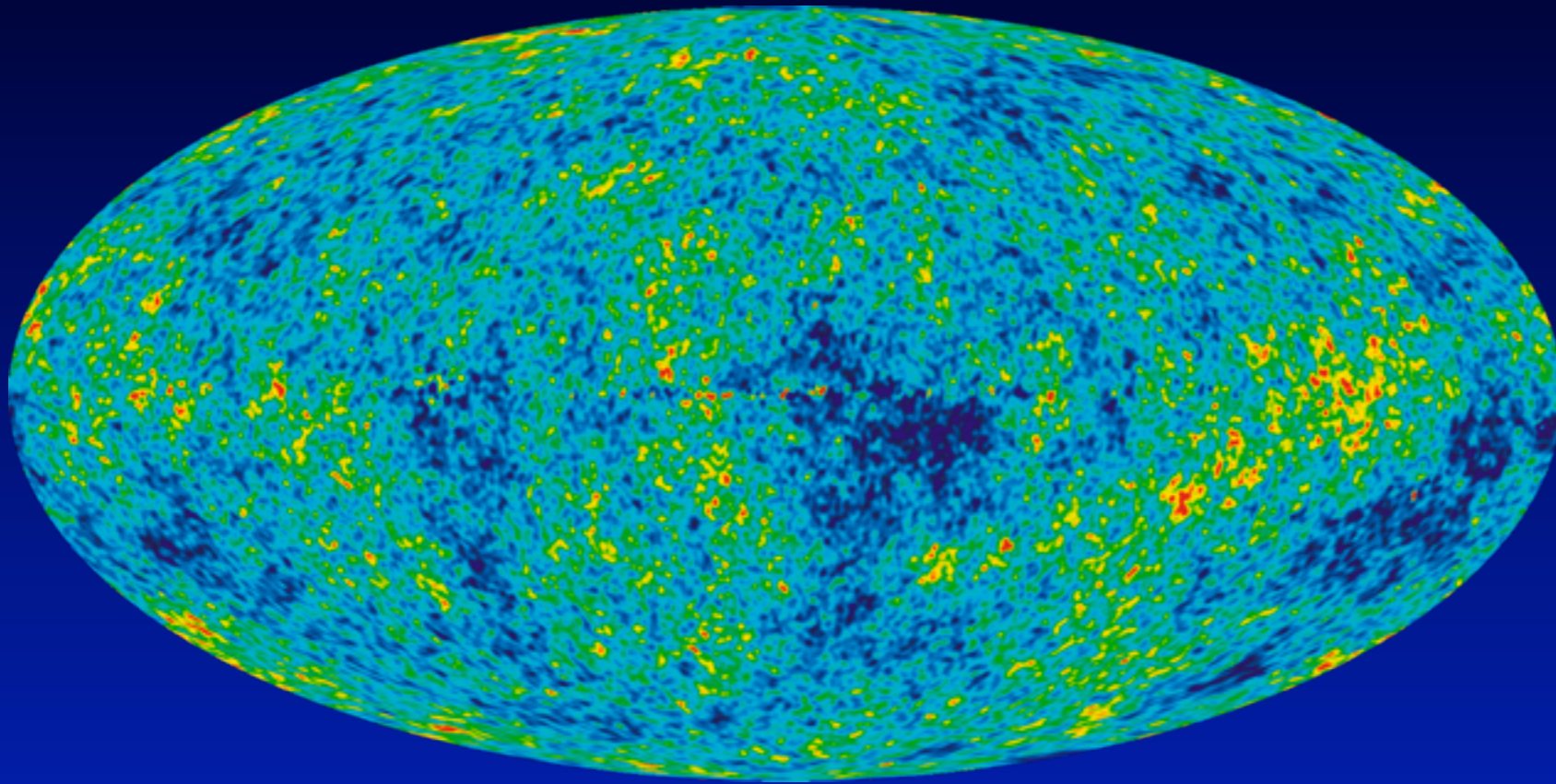
Superpositions of blackbody spectra



Superpositions of blackbody spectra



Distortions caused by superposition of blackbodies



- average spectrum

$$\Rightarrow y \simeq \frac{1}{2} \left\langle \left(\frac{\Delta T}{T} \right)^2 \right\rangle \approx 8 \times 10^{-10}$$

$$\Delta T_{\text{sup}} \simeq T \left\langle \left(\frac{\Delta T}{T} \right)^2 \right\rangle \approx 4.4 \text{ nK}$$

- known with very high precision

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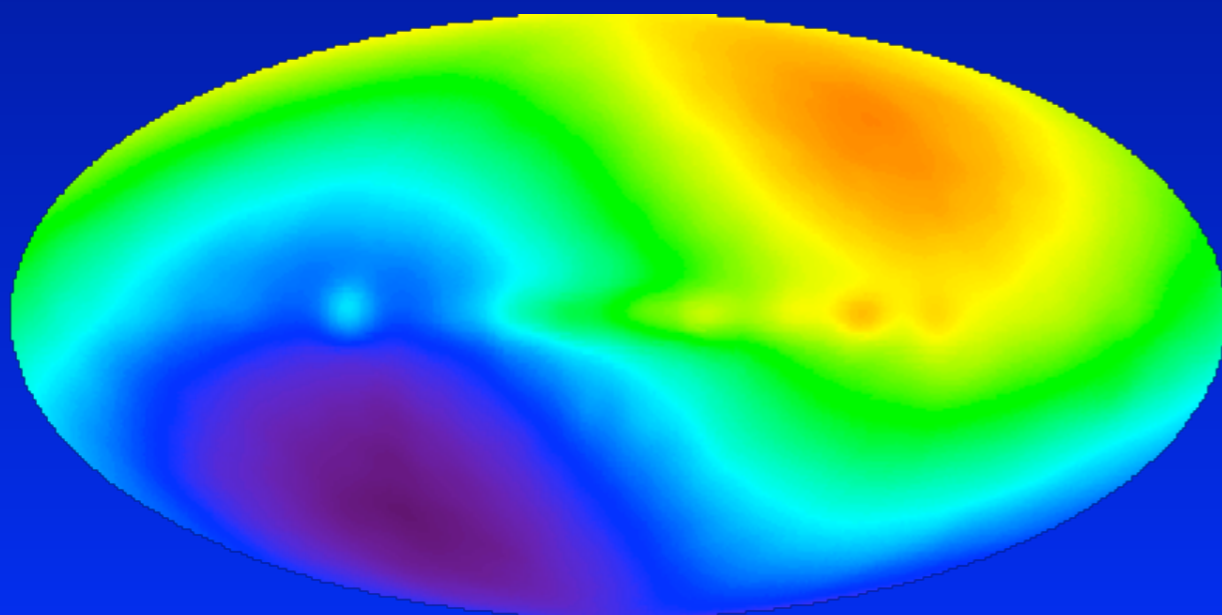
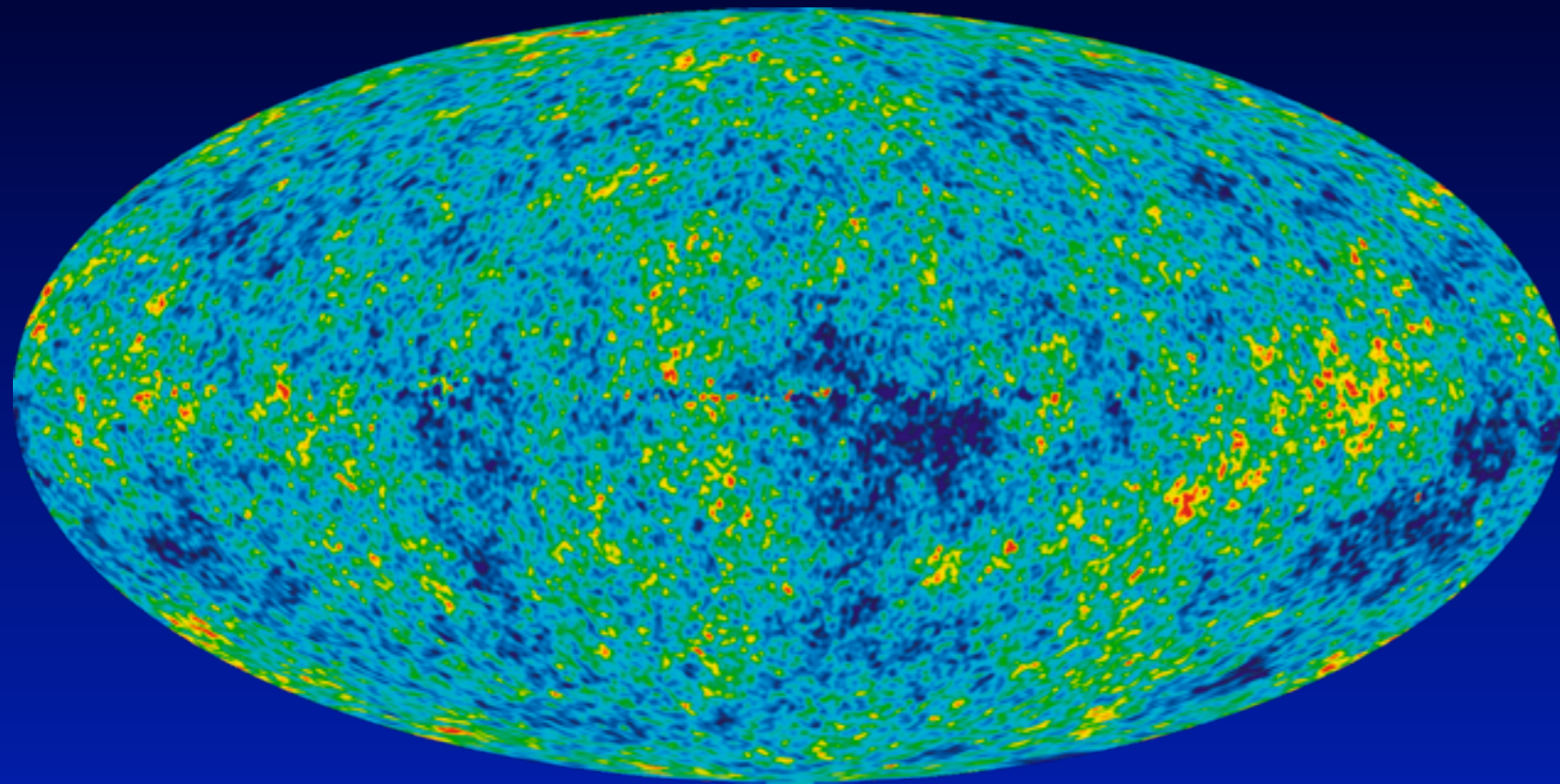
- known with very high precision

- CMB dipole ($\beta_c \sim 1.23 \times 10^{-3}$)

$$\Rightarrow y \simeq \frac{\beta_c^2}{6} \approx 2.6 \times 10^{-7}$$

$$\Delta T_{\text{sup}} \simeq T \frac{\beta_c^2}{3} \approx 1.4 \mu\text{K}$$

- electrons are up-scattered
- can be taken out at the level of $\sim 10^{-9}$



Effective energy release caused by damping effect

- Effective heating rate from full 2x2 Boltzmann treatment (JC, Khatri & Sunyaev, 2012)

$$\frac{1}{a^4 \rho_\gamma} \frac{da^4 Q_{ac}}{dt} = 4\sigma_T N_e c \left\langle \frac{(3\Theta_1 - \beta)^2}{3} + \frac{9}{2}\Theta_2^2 - \frac{1}{2}\Theta_2(\Theta_0^P + \Theta_2^P) + \sum_{l \geq 3} (2l + 1)\Theta_l^2 \right\rangle$$

$$\Theta_l = \frac{1}{2} \int \Theta(\mu) P_l(\mu) d\mu$$

gauge-independent dipole

effect of polarization

higher multipoles

$$\langle XY \rangle = \int \frac{k^2 dk}{2\pi^2} P(k) X(k) Y(k)$$

Primordial power spectrum

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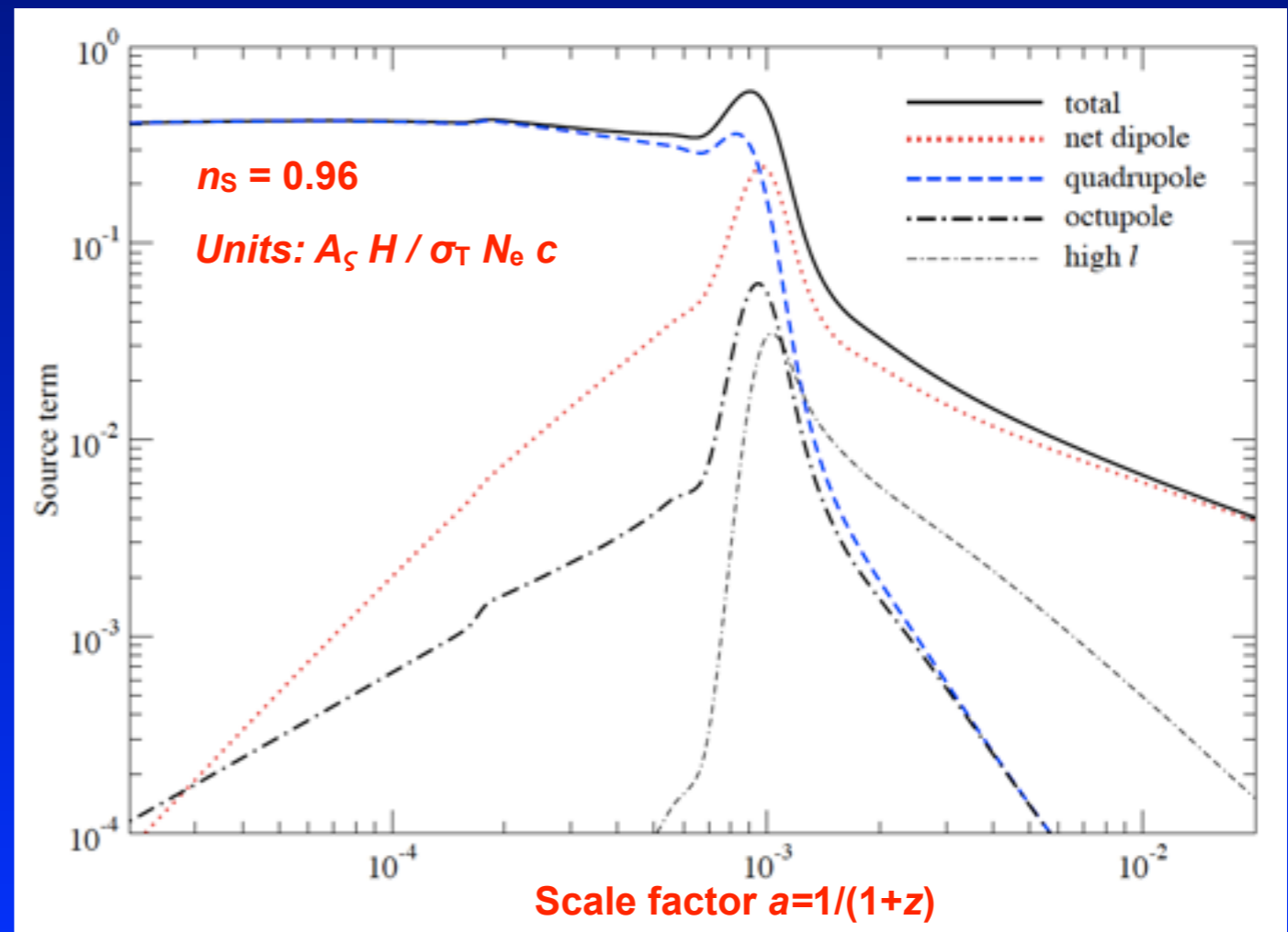
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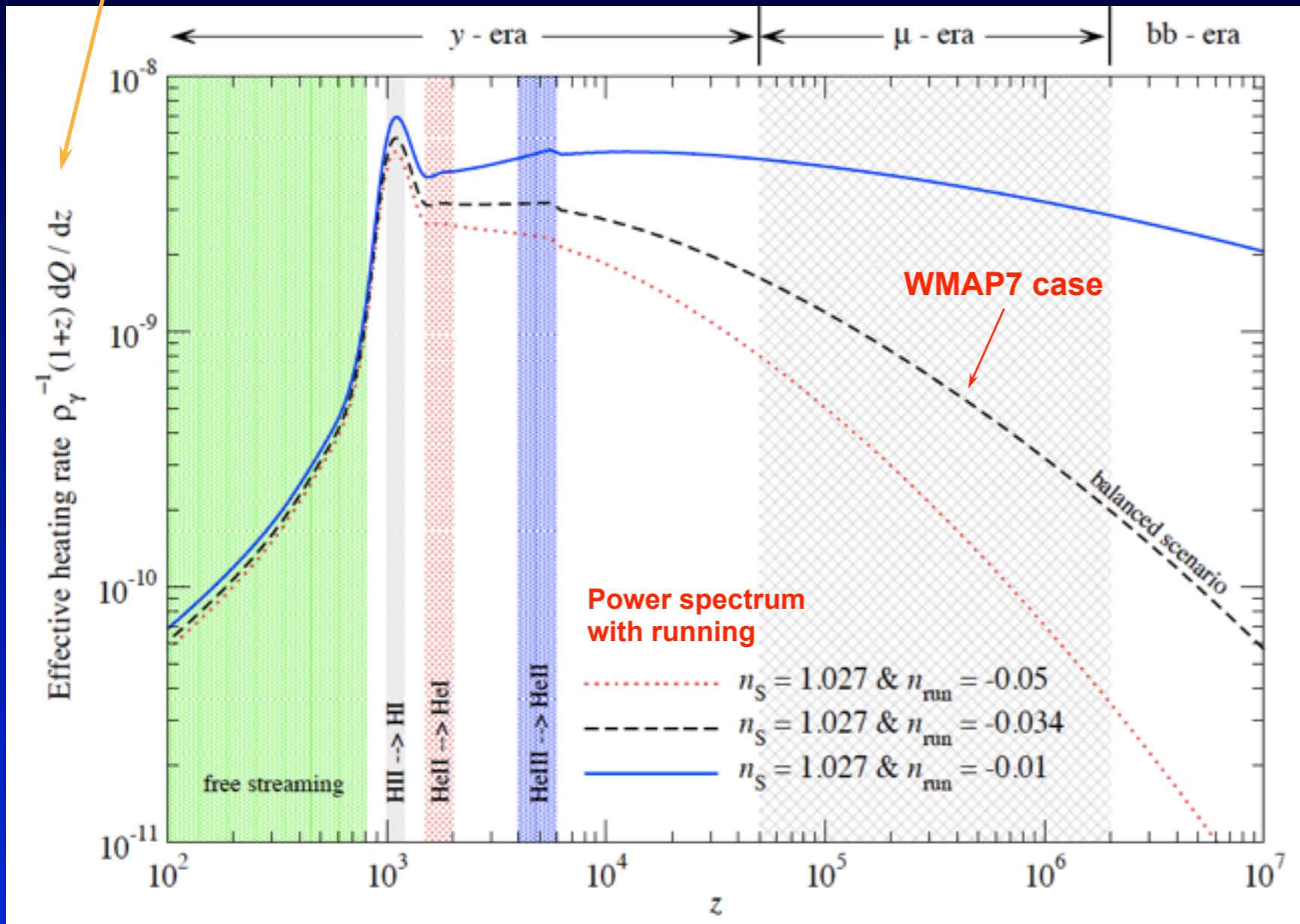
Primordial power spectrum

- quadrupole dominant at high z
- net dipole important only at low redshifts
- polarization $\sim 5\%$ effect
- contribution from higher multipoles rather small



Our computation for the effective energy release

scaled such that constant for $n_s = 1$



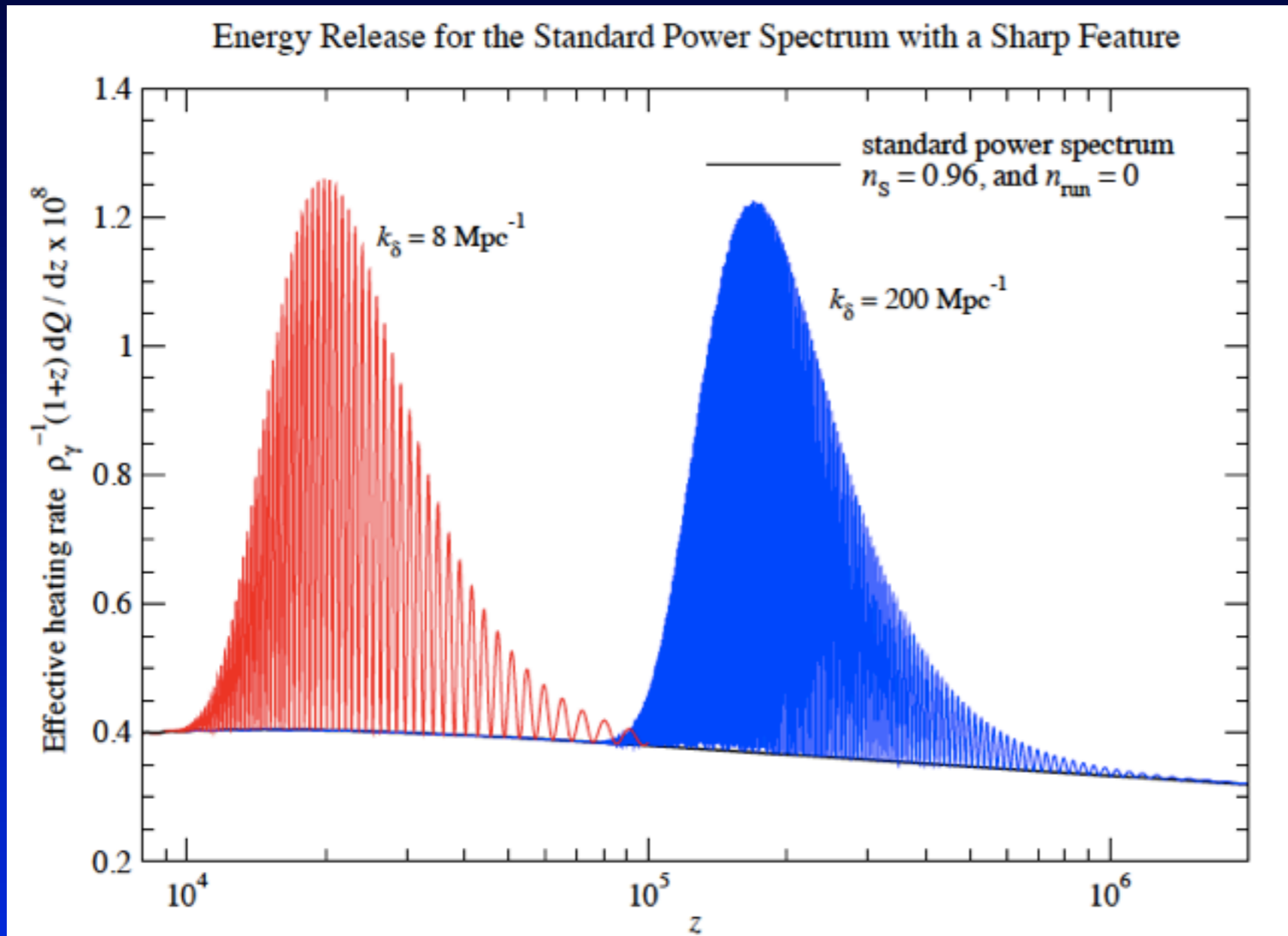
- Our 2. order perturbation calculation showed that the *classical* picture was slightly inconsistent
- Amplitude of the distortion depends on the small-scale power spectrum
- Computation carried out with **CosmoTherm** (JC & Sunyaev 2011)

JC, Khatri & Sunyaev, 2012

$$P_{\zeta}(k) = 2\pi^2 A_{\zeta} k^{-3} (k/k_0)^{n_s - 1 + \frac{1}{2} n_{\text{run}} \ln(k/k_0)}$$

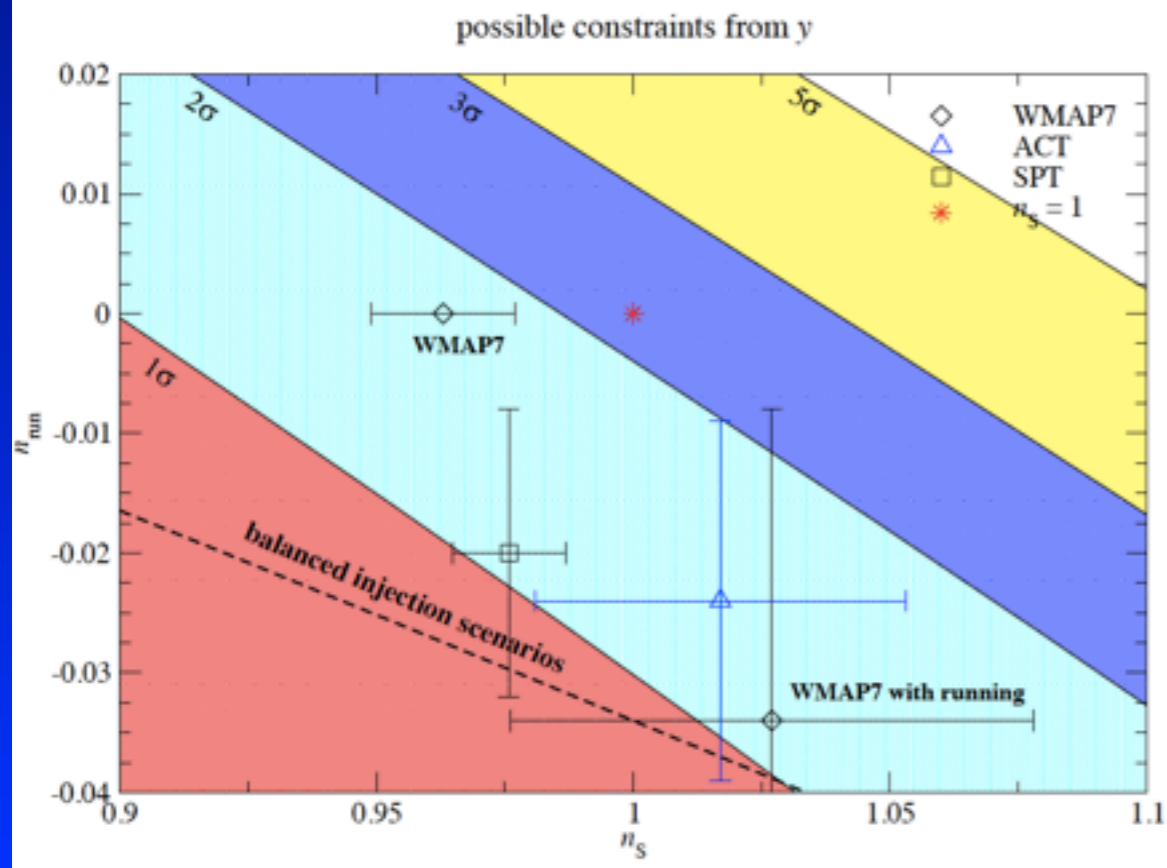
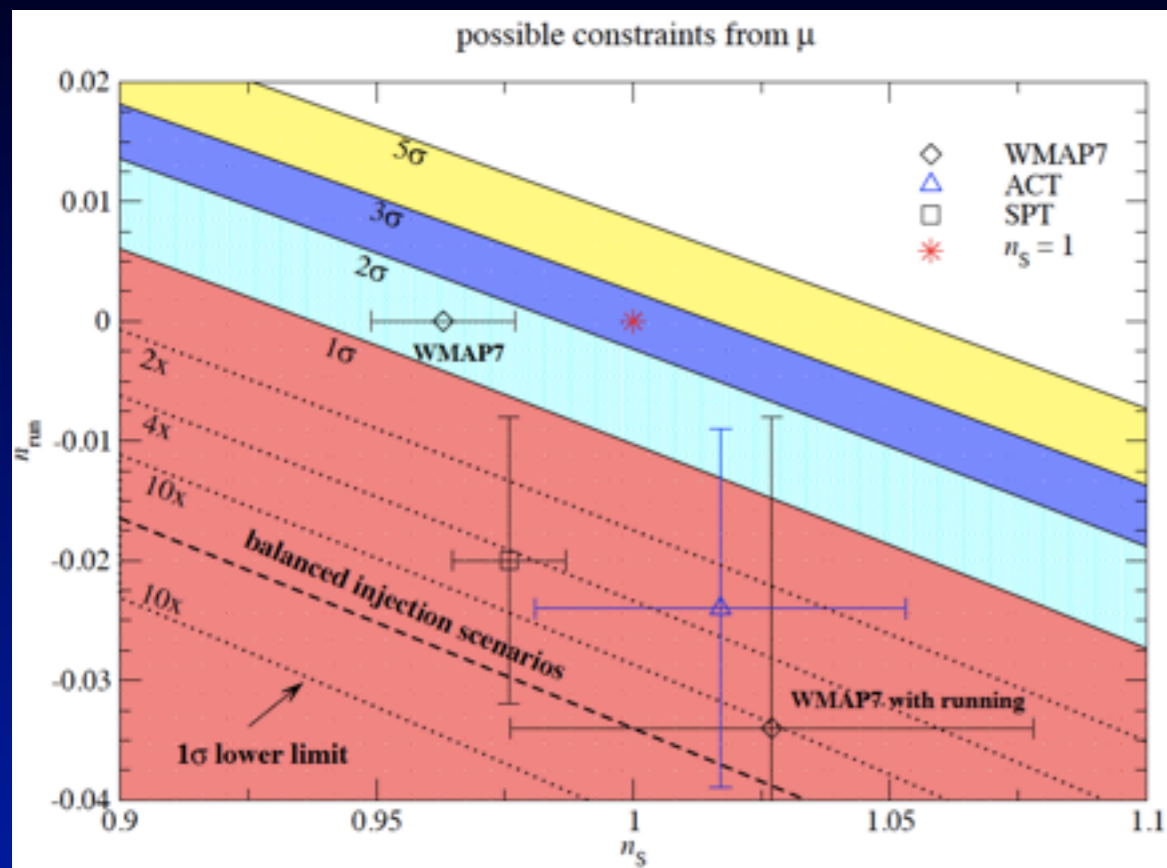
Primordial power spectrum of curvature perturbations is input for the calculation

Which modes dissipate in the μ and y -eras?



- Single mode with wavenumber k dissipates its energy at $z_d \sim 4.5 \times 10^5 (k \text{ Mpc}/10^3)^{2/3}$
- Modes with wavenumber $50 \text{ Mpc}^{-1} < k < 10^4 \text{ Mpc}^{-1}$ dissipate their energy during the μ -era
- Modes with $k < 50 \text{ Mpc}^{-1}$ cause y -distortion

Constraints on the standard primordial power spectrum

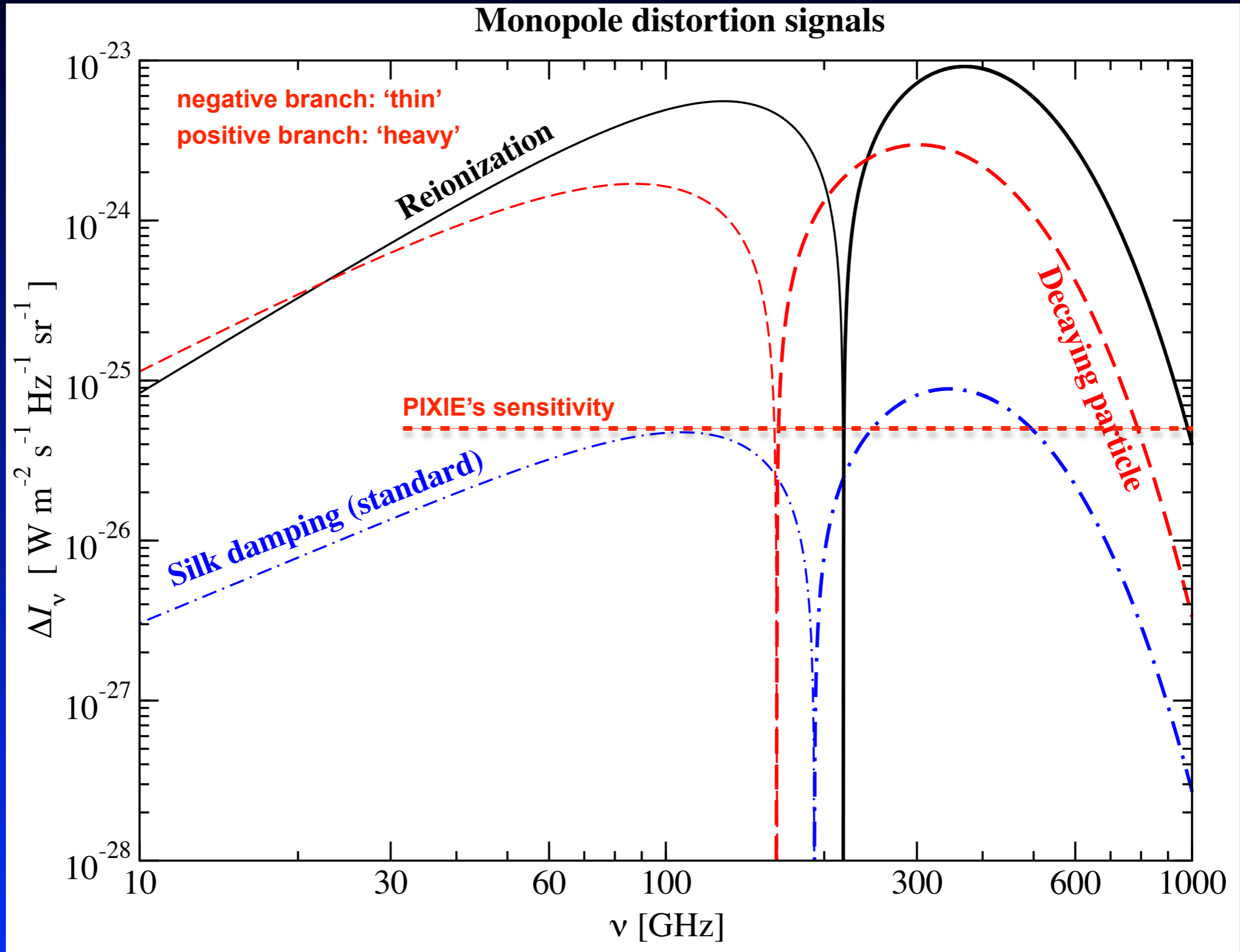


- For *any* given power spectrum very precise predictions are possible!
- The *physics* going into the computation are *well understood*
- For the standard power spectrum PIXIE might detect the μ -distortion caused by acoustic damping at $\sim 1.5\sigma$ level
- PIXIE could *independently* rule out a scale-invariant power spectrum at $\sim 2.5\sigma$ level
- γ -distortion will be harder to measure, since many *other astrophysical processes* cause γ -distortions at low redshift

$$P_{\zeta}(k) = 2\pi^2 A_{\zeta} k^{-3} (k/k_0)^{n_s - 1 + \frac{1}{2} n_{\text{run}} \ln(k/k_0)}$$

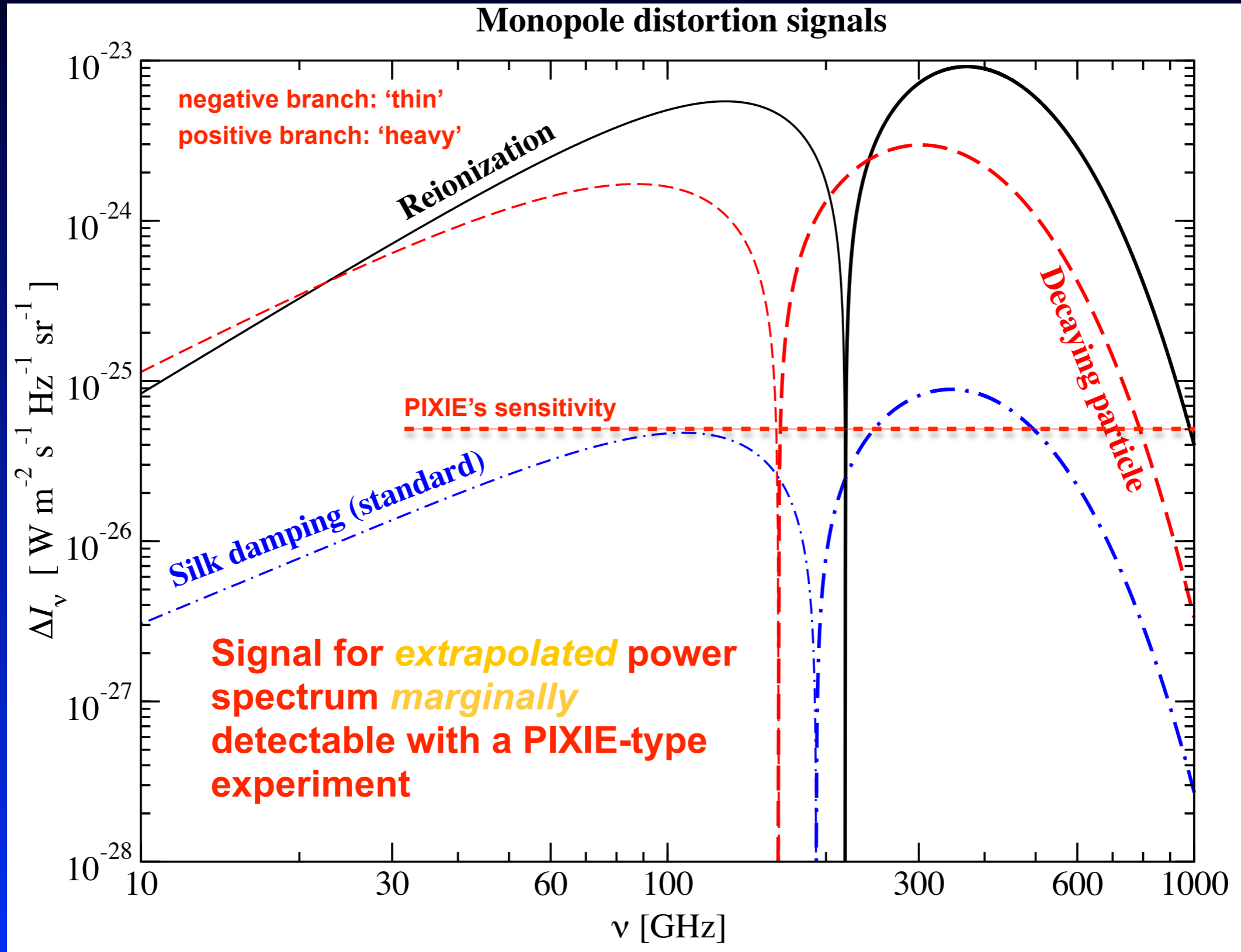
Average CMB spectral distortions

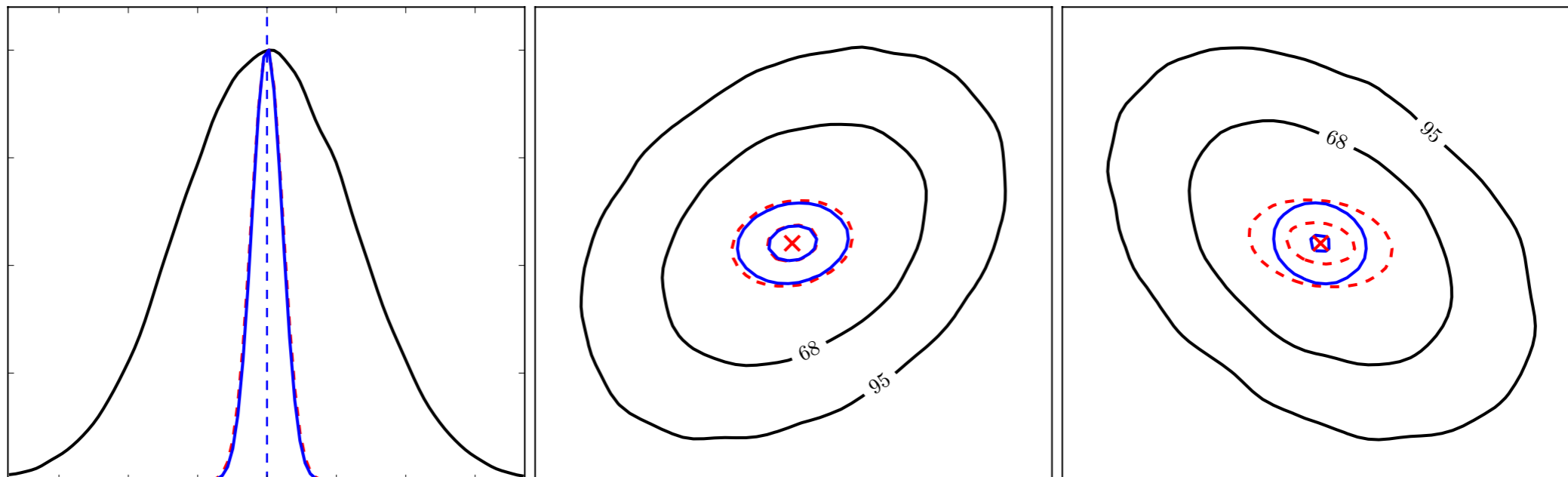
Absolute value of Intensity signal



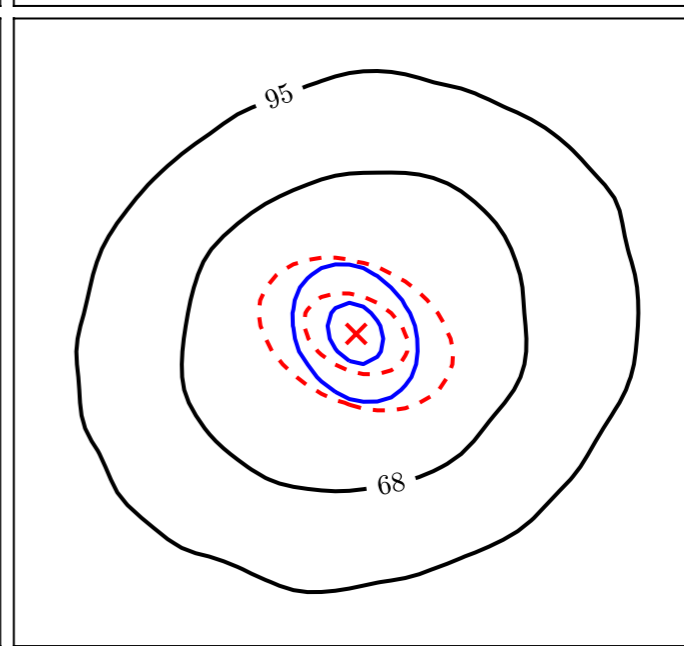
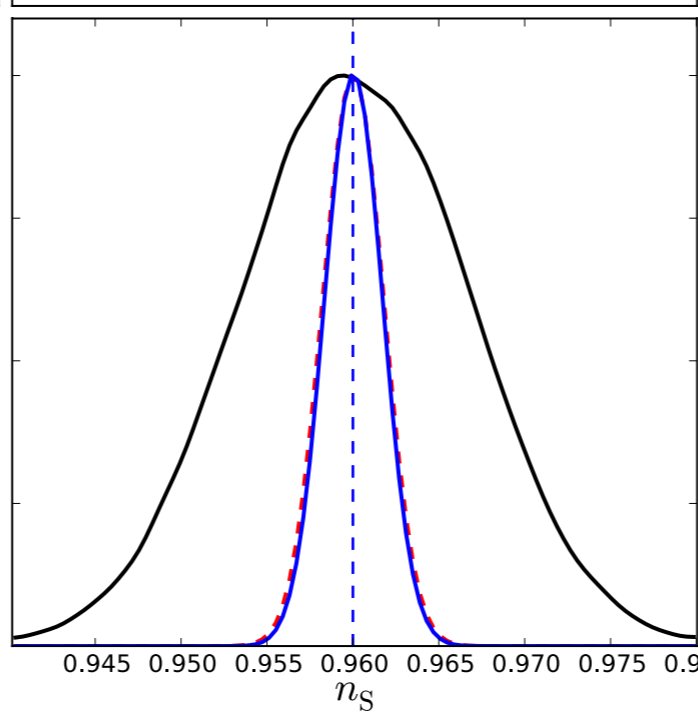
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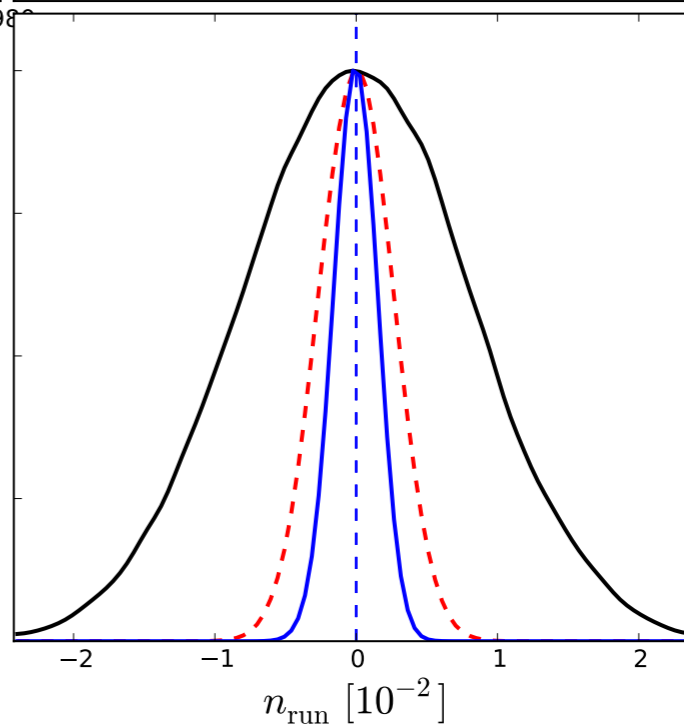


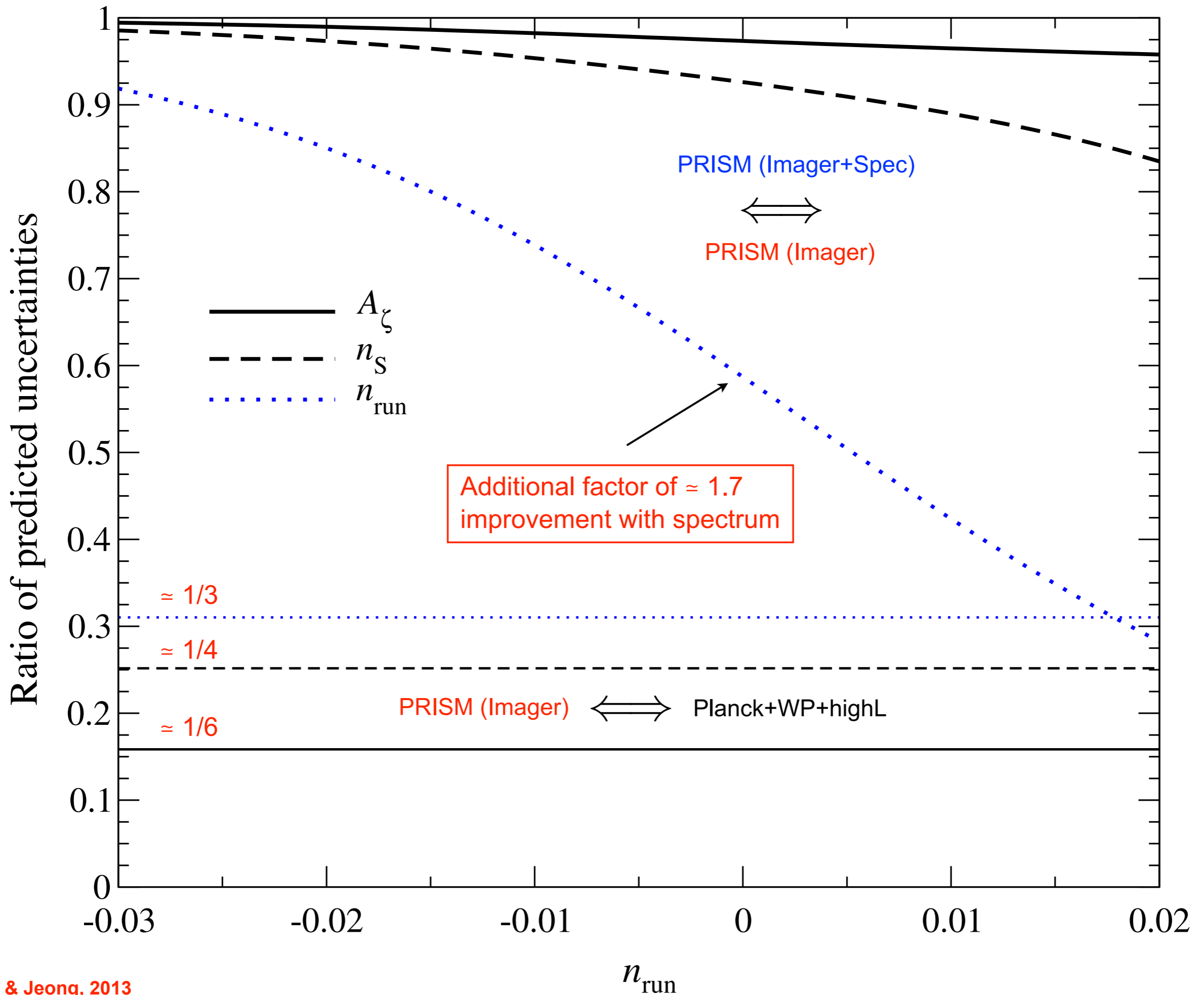


Fiducial model
 $k_0 = 0.05 \text{ Mpc}^{-1}$
 $A_\zeta = 2.2 \times 10^{-9}$
 $n_S = 0.96$
 $n_{\text{run}} = 0$



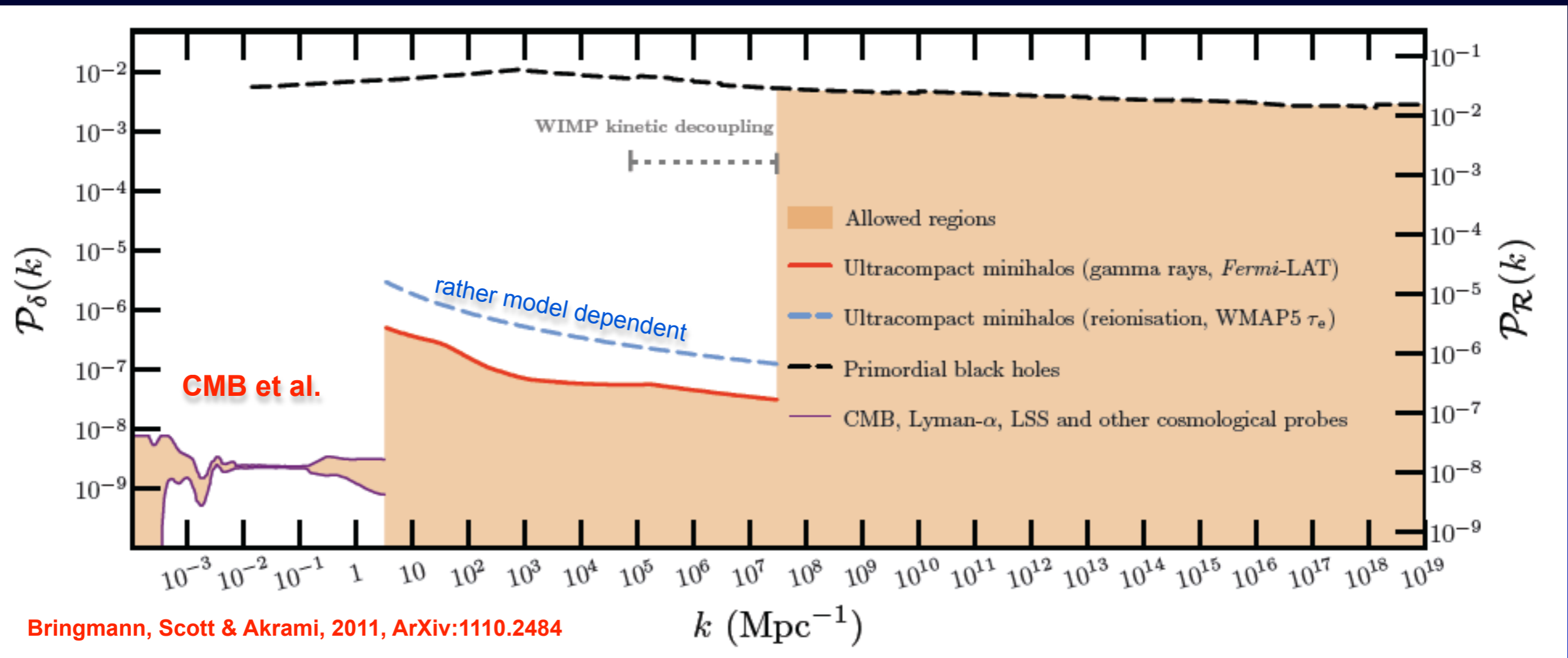
Planck+WP+highL —————
 PRISM (Imager) - - - - -
 PRISM (Imager+Spec) ————





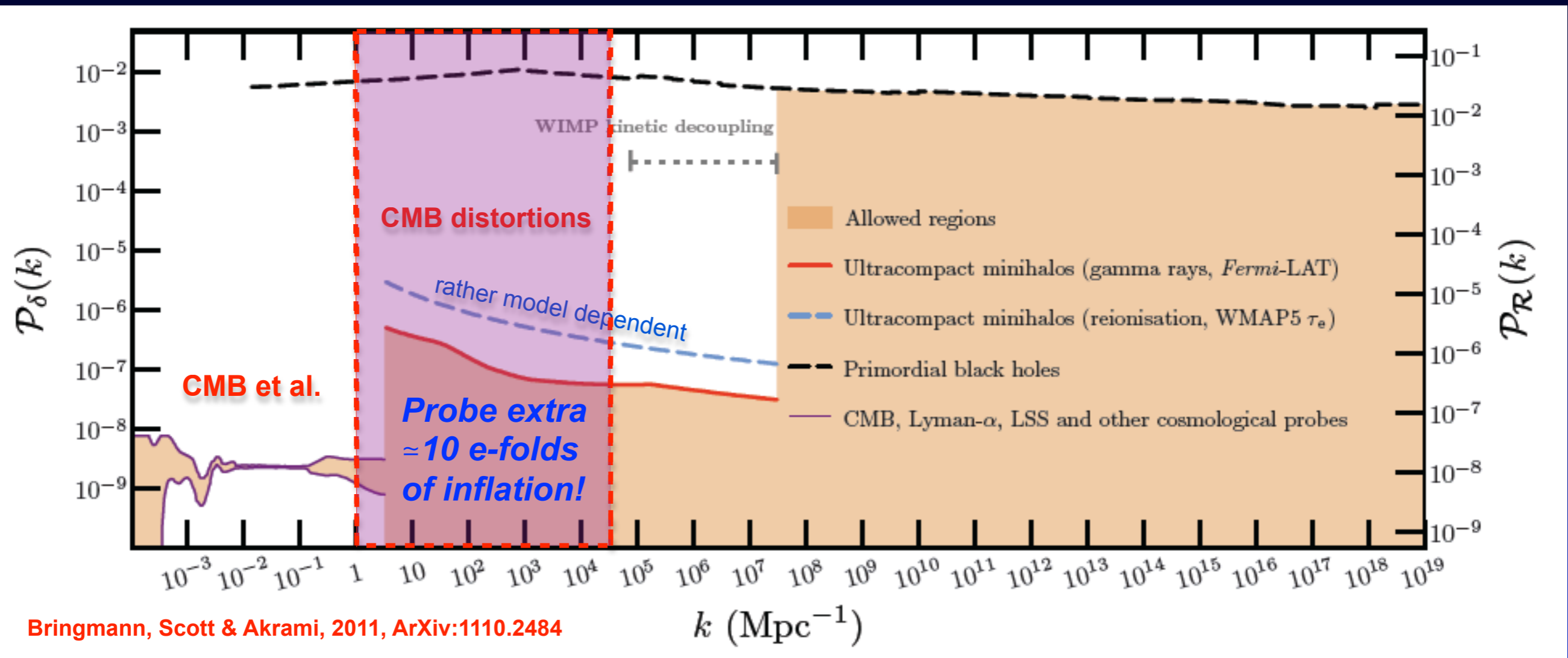
But this is not all that one could look at !!!

Distortions provide additional power spectrum constraints!



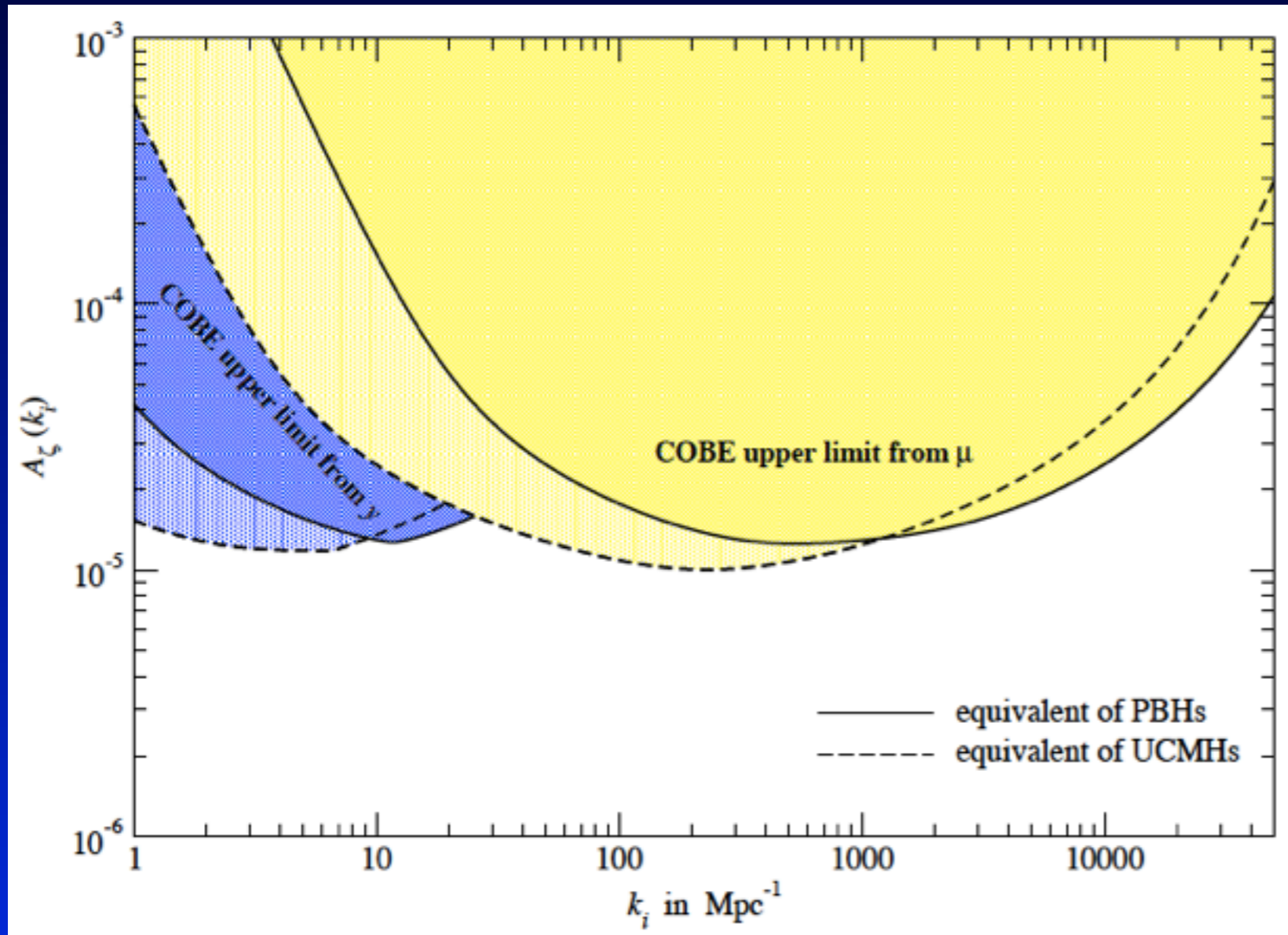
- Amplitude of power spectrum rather uncertain at $k > 3 \text{ Mpc}^{-1}$
- improved limits at smaller scales can *rule out* many *inflationary models*

Distortions provide additional power spectrum constraints!



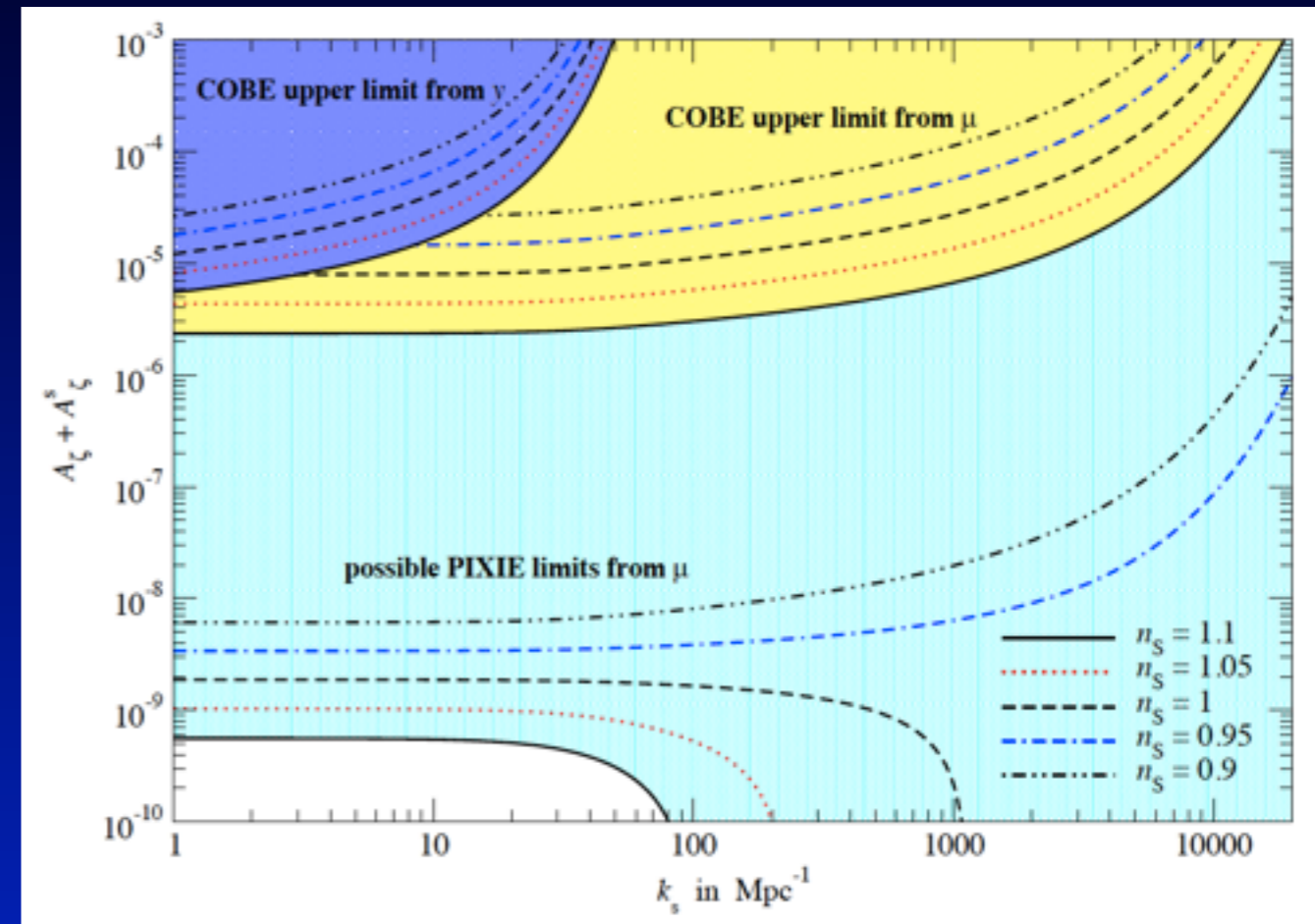
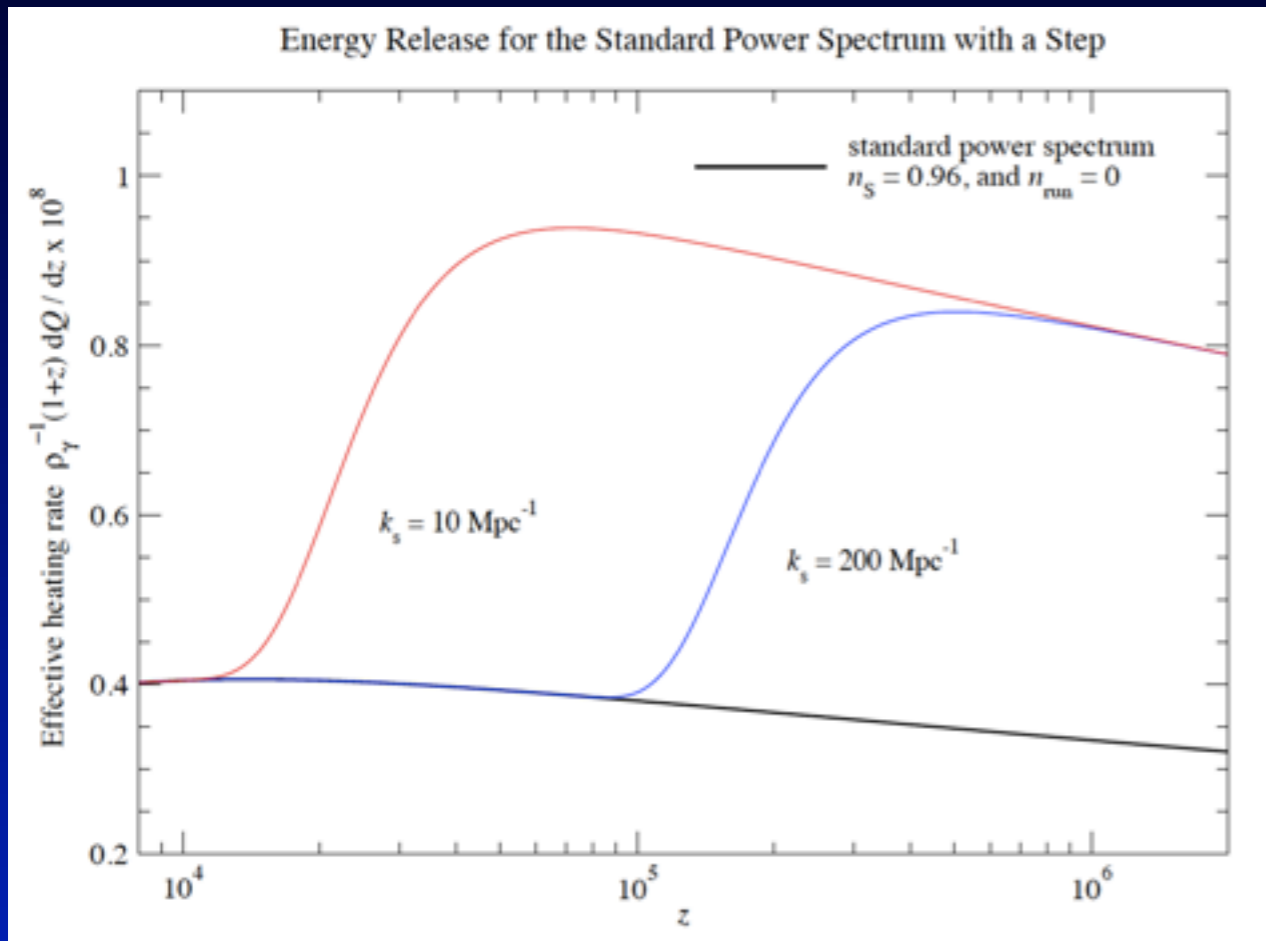
- Amplitude of power spectrum rather uncertain at $k > 3 \text{ Mpc}^{-1}$
- improved limits at smaller scales can *rule out* many *inflationary models*
- CMB spectral distortions would *extend* our *lever arm* to $k \sim 10^4 \text{ Mpc}^{-1}$
- very *complementary* piece of information about early-universe physics

COBE/FIRAS limits on the amplitude of the small-scale power spectrum



- 'optimistic' limit $P(k) < 8.4 \times 10^{-6}$
- Conservative constraint
- $\sim 10^3$ stronger than PBHs limit
- UCMHs limit still ~ 10 times stronger but more uncertain
- PIXIE could improve limit to $P(k) < 10^{-8}$
- constant power limit even $P(k) < 10^{-9}$

Primordial power spectra with 'step' at small scales



$$\mu \approx 2.2 \int_{k_{\min}}^{\infty} \mathcal{P}_\zeta(k) \left[\exp\left(-\frac{\hat{k}}{5400}\right) - \exp\left(-\left[\frac{\hat{k}}{31.6}\right]^2\right) \right] d \ln k$$

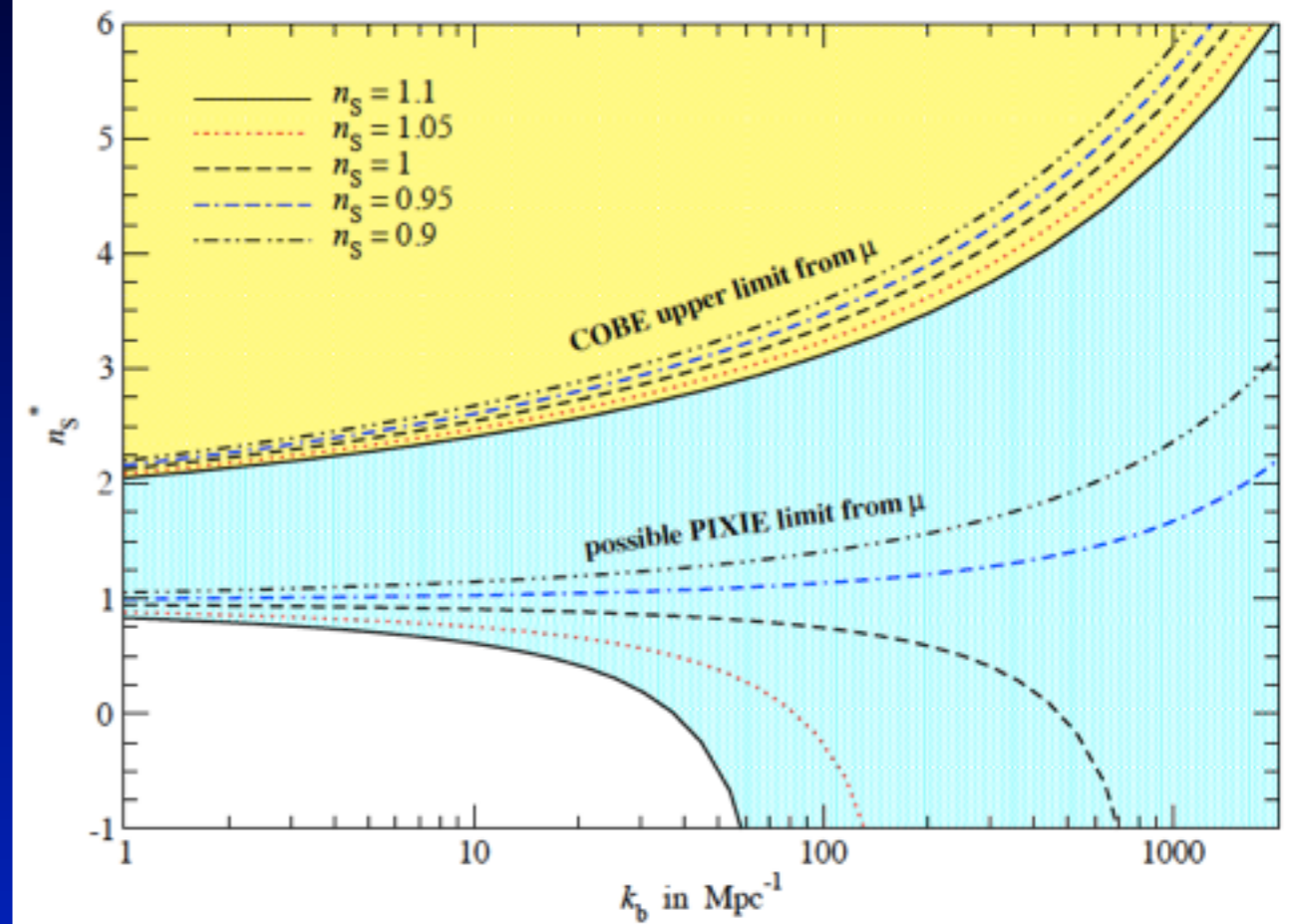
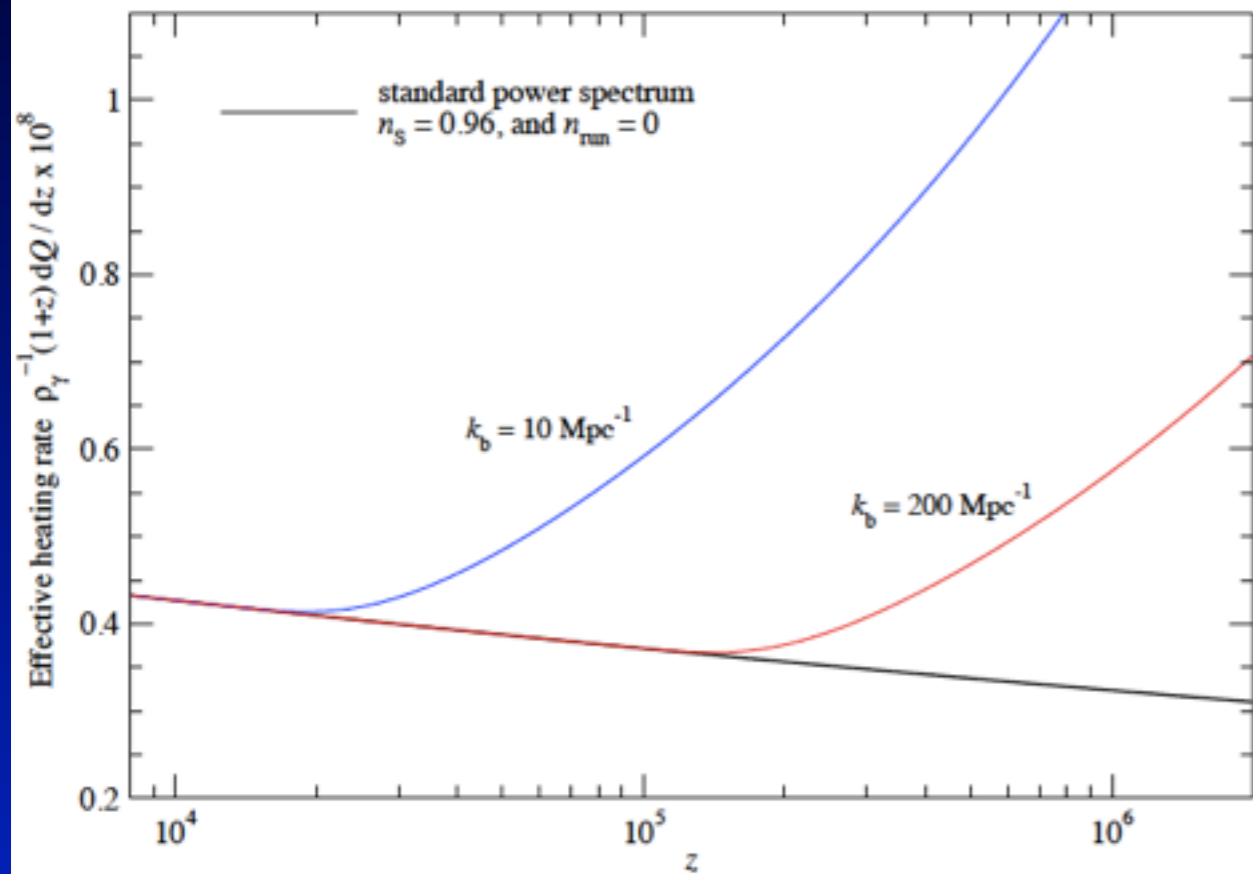
$$y \approx 0.4 \int_{k_{\min}}^{\infty} \mathcal{P}_\zeta(k) \exp\left(-\left[\frac{\hat{k}}{31.6}\right]^2\right) d \ln k,$$

Integral constraint on small-scale power

- simple formula to compute the effective μ and y -parameter
- COBE/FIRAS \Rightarrow amplitude of the small-scale power spectrum can't change by more than $\sim 2 \times 10^{-6}$ at wavenumber $k \sim 1 \text{ Mpc}^{-1}$

Primordial power spectra with 'bend' at small scales

Energy Release for the Standard Power Spectrum with a Kink



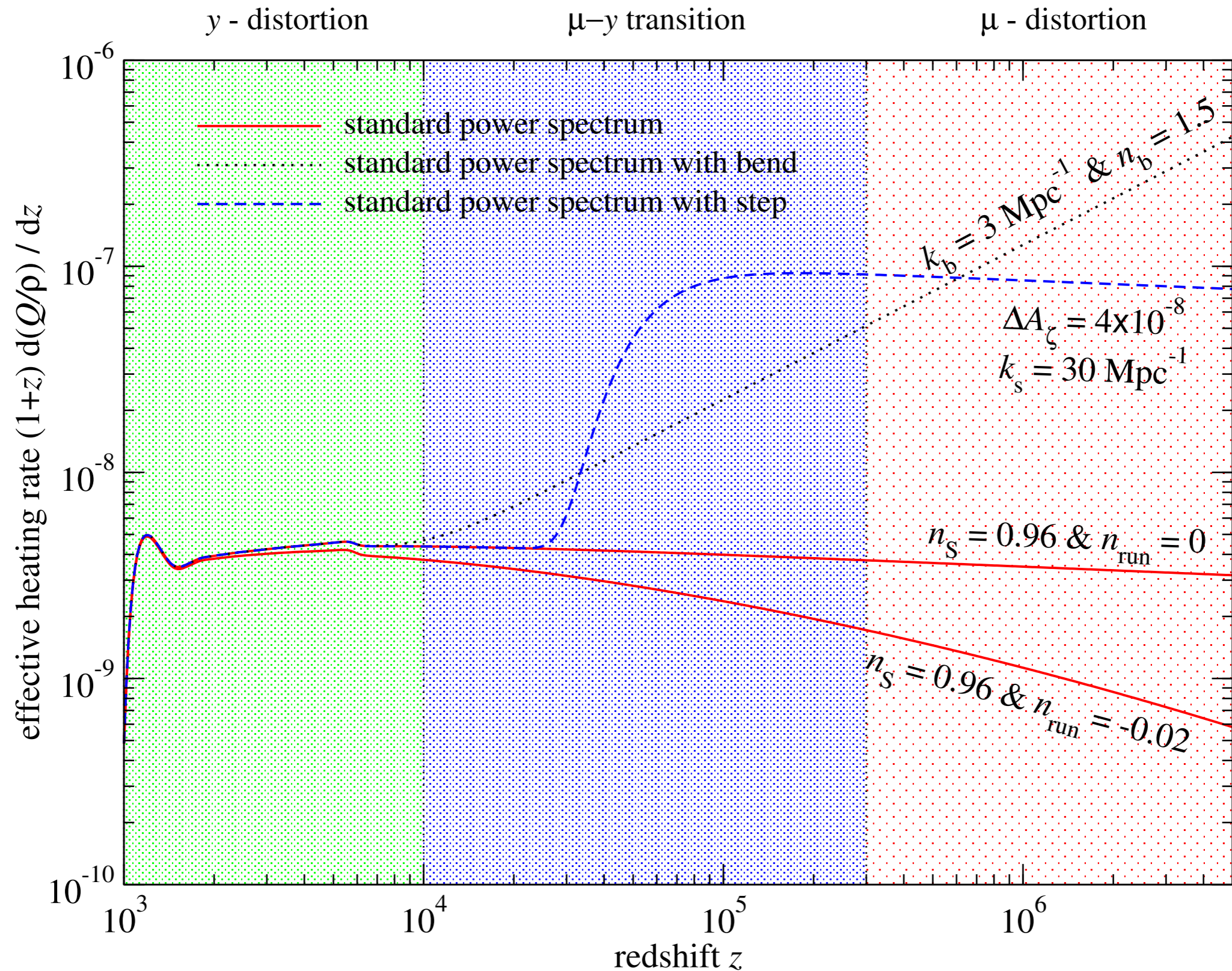
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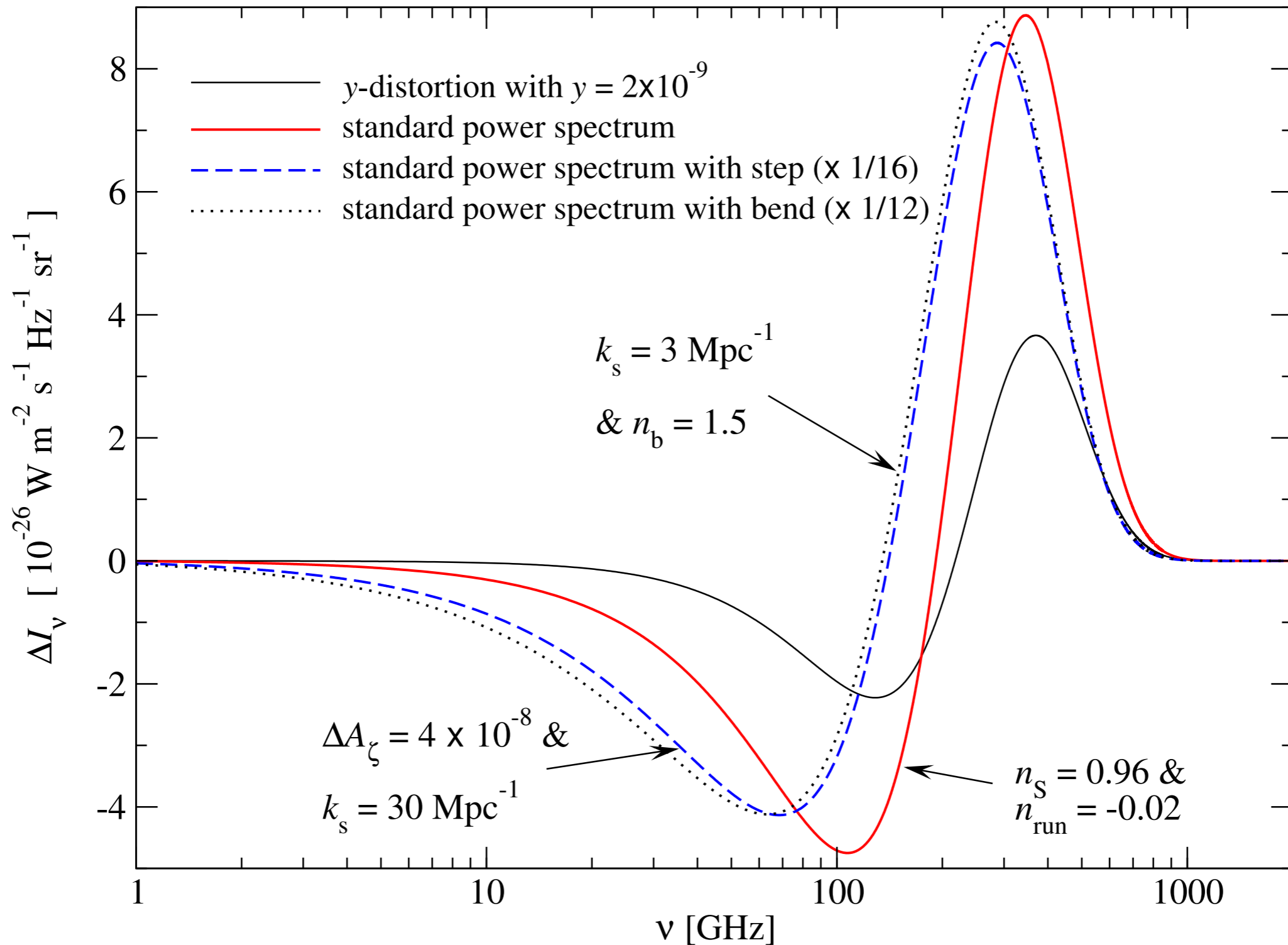
Integral constraint on small-scale power

- COBE/FIRAS \Rightarrow spectral index at $k \sim 1 \text{ Mpc}^{-1}$ cannot change by more than $\Delta n \sim 1$
- PIXIE will place very tight constraints on such models

Probing the small-scale power spectrum

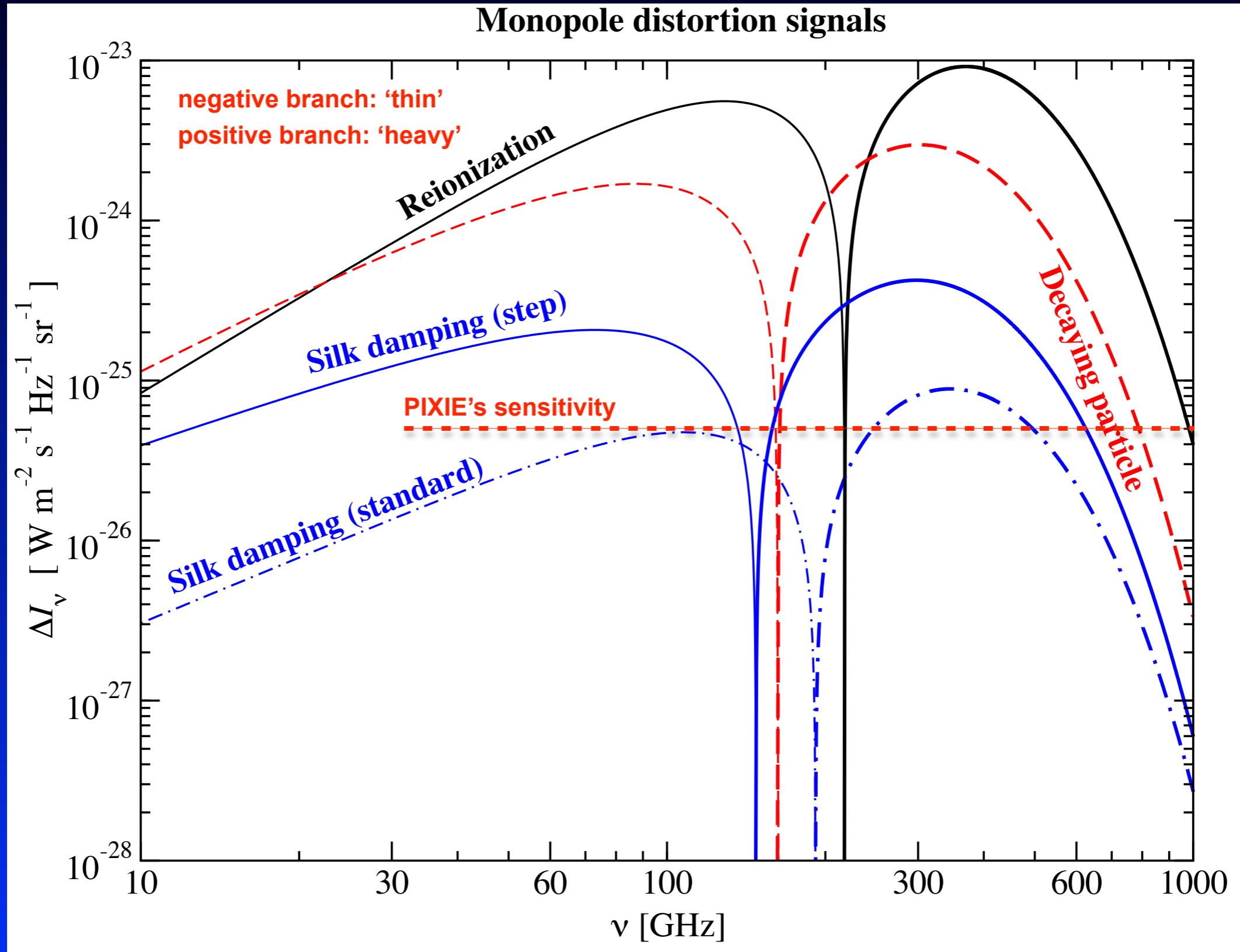


Probing the small-scale power spectrum



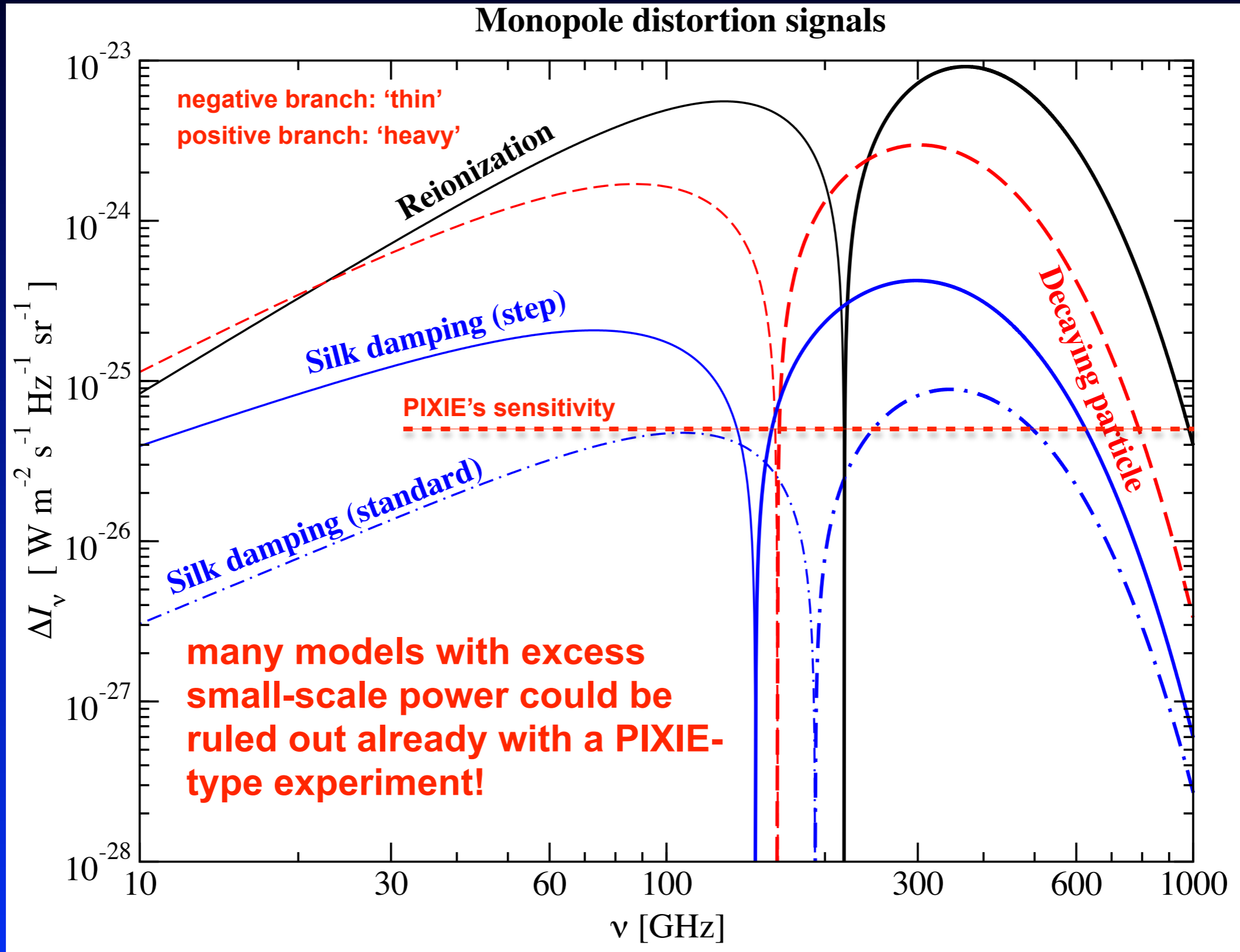
Average CMB spectral distortions

Absolute value of Intensity signal

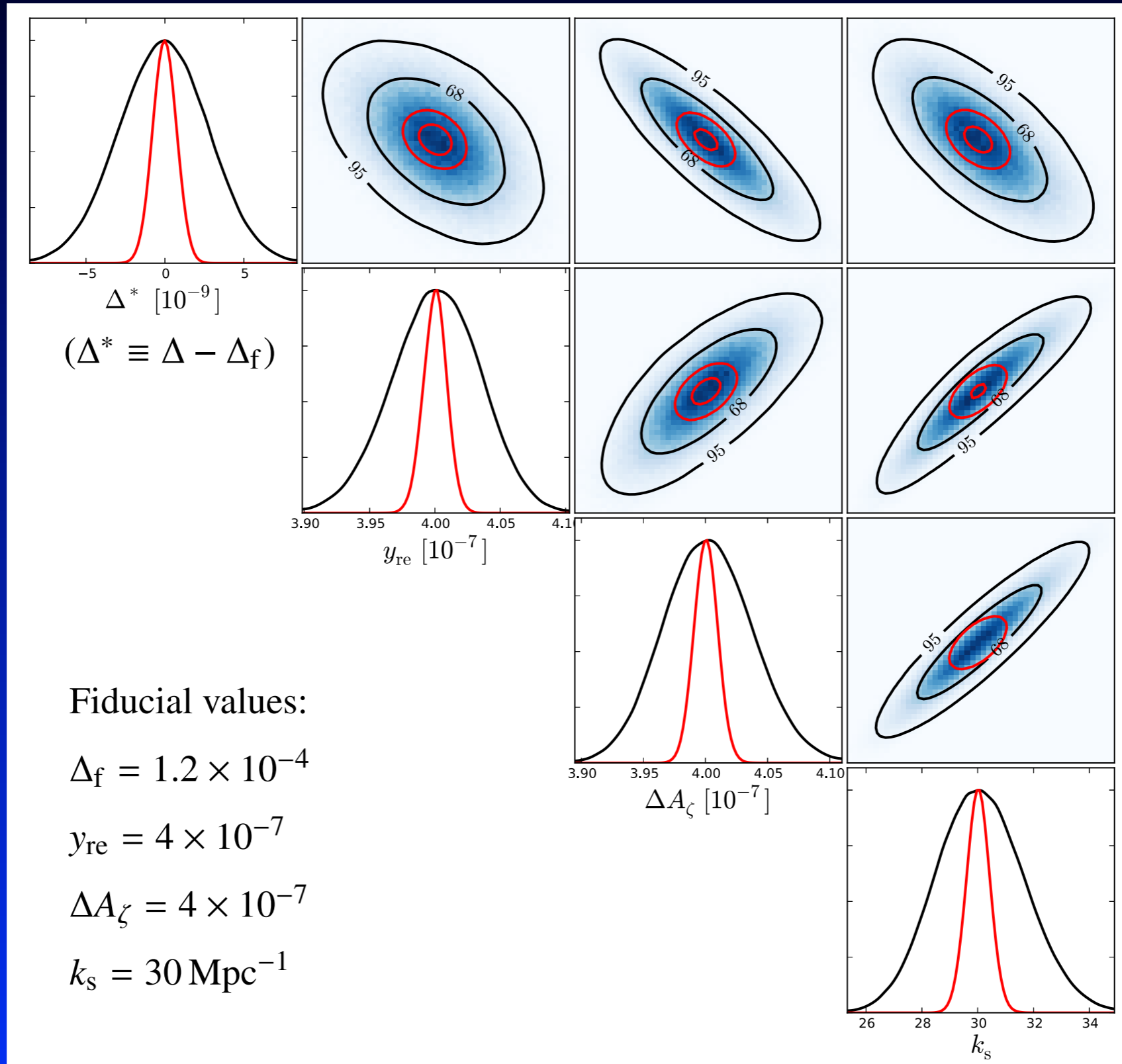


Average CMB spectral distortions

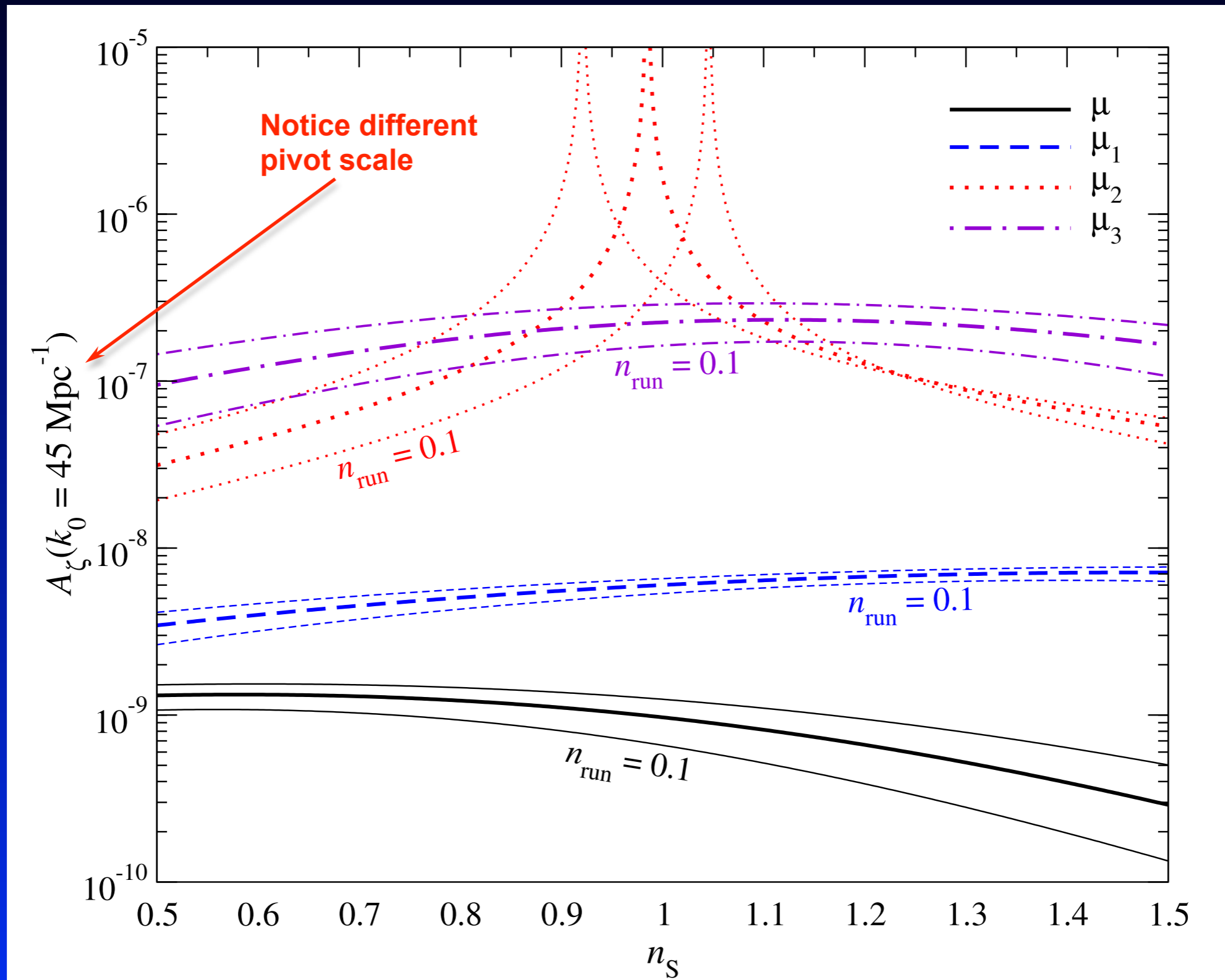
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Probing the small-scale power spectrum

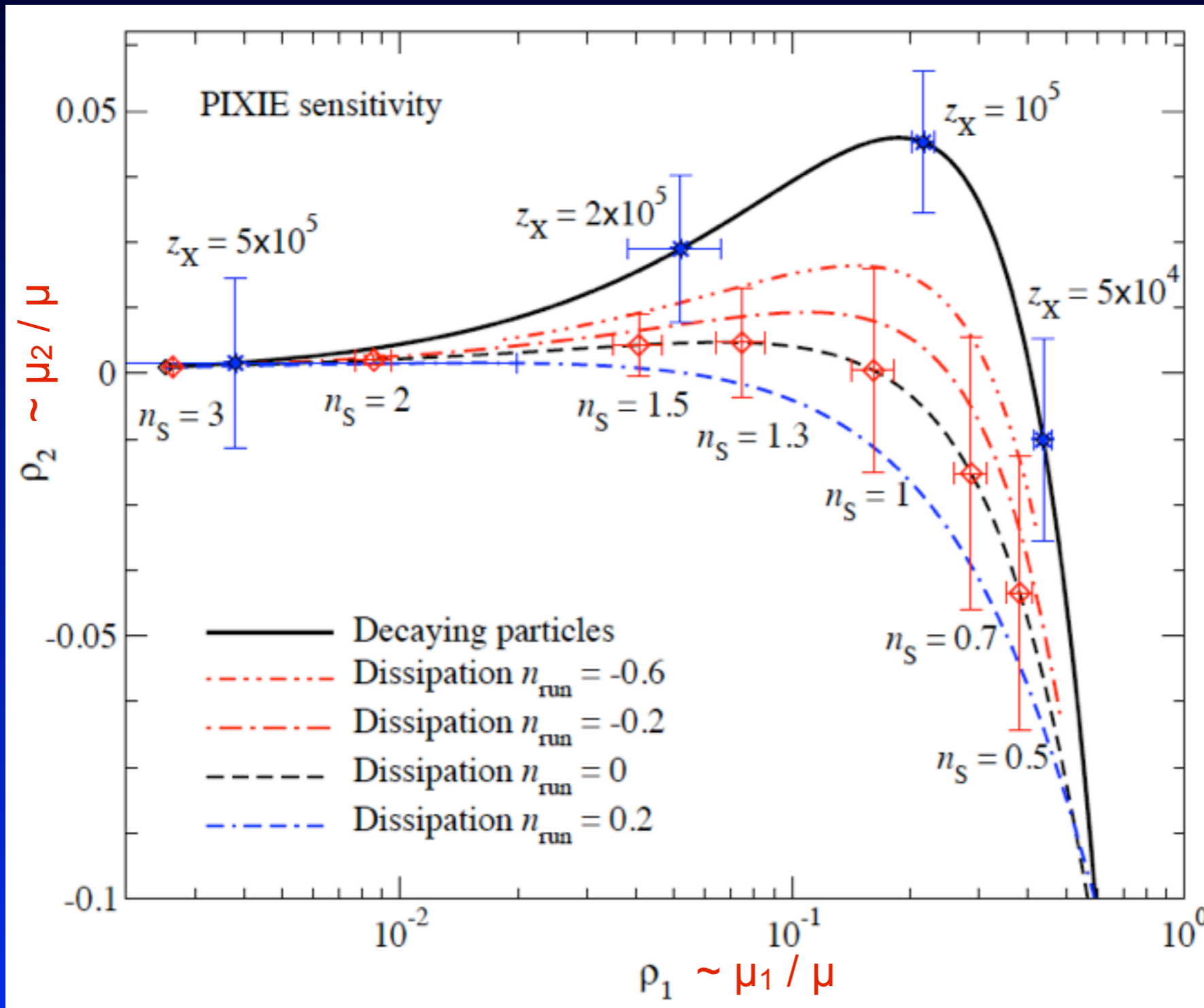


Dissipation scenario: 1σ -detection limits for PIXIE



$$P_\zeta(k) = 2\pi^2 A_\zeta k^{-3} (k/k_0)^{n_s - 1 + \frac{1}{2}n_{\text{run}} \ln(k/k_0)}$$

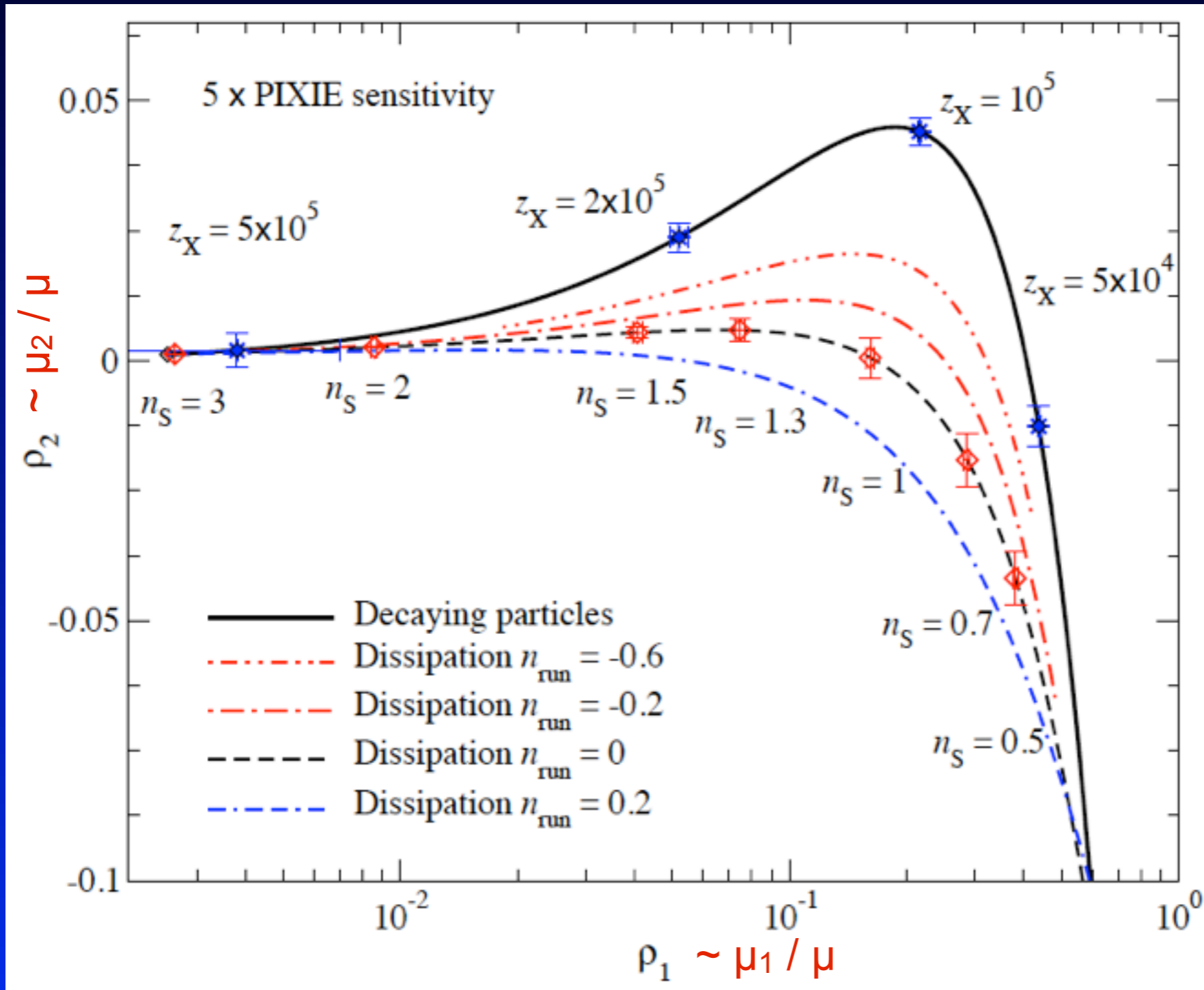
Distinguishing dissipation and decaying particle scenarios



- measurement of μ , μ_1 & μ_2
- trajectories of decaying particle and dissipation scenarios differ!
- scenarios can in principle be distinguished

$$A_\zeta = 5 \times 10^{-8}$$

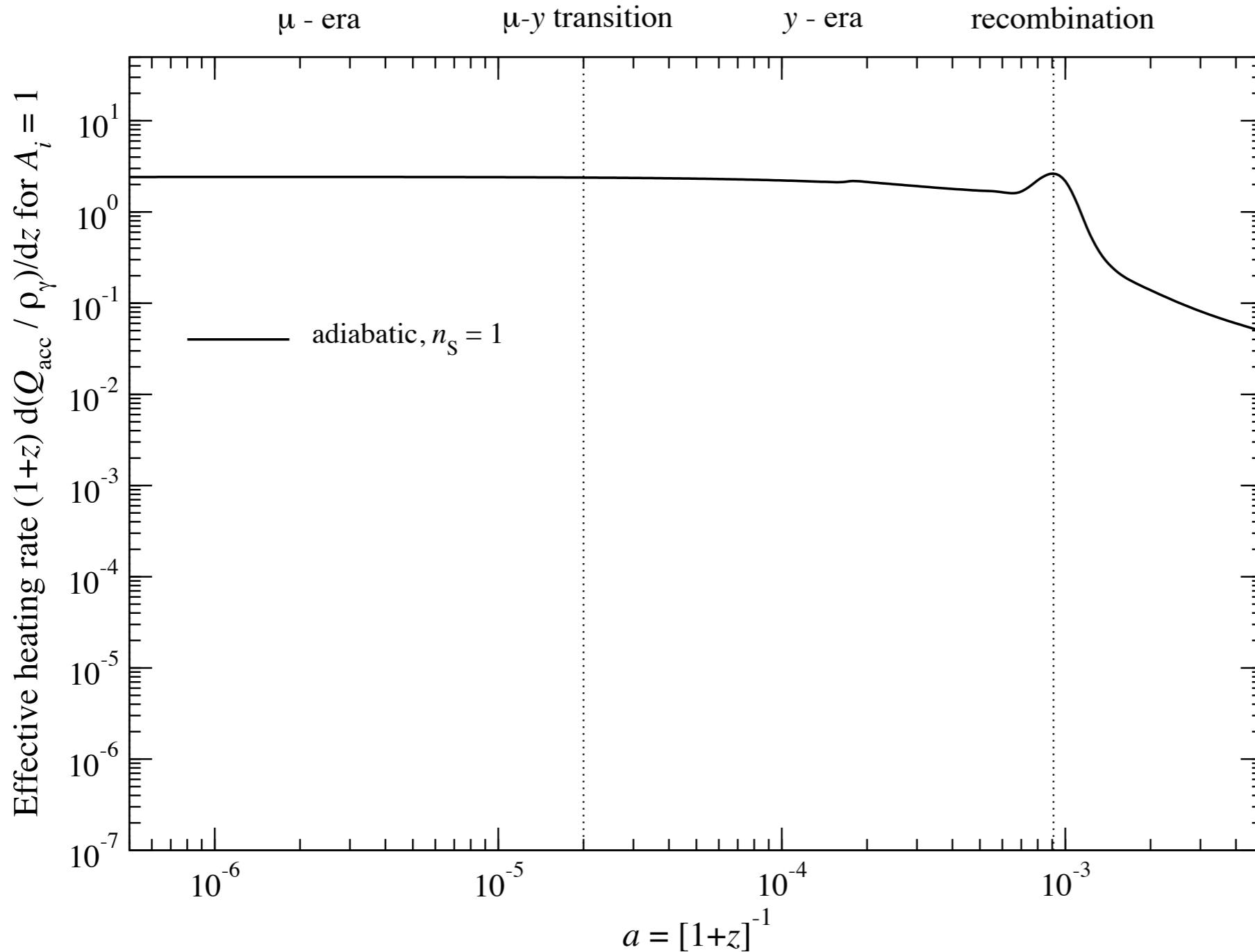
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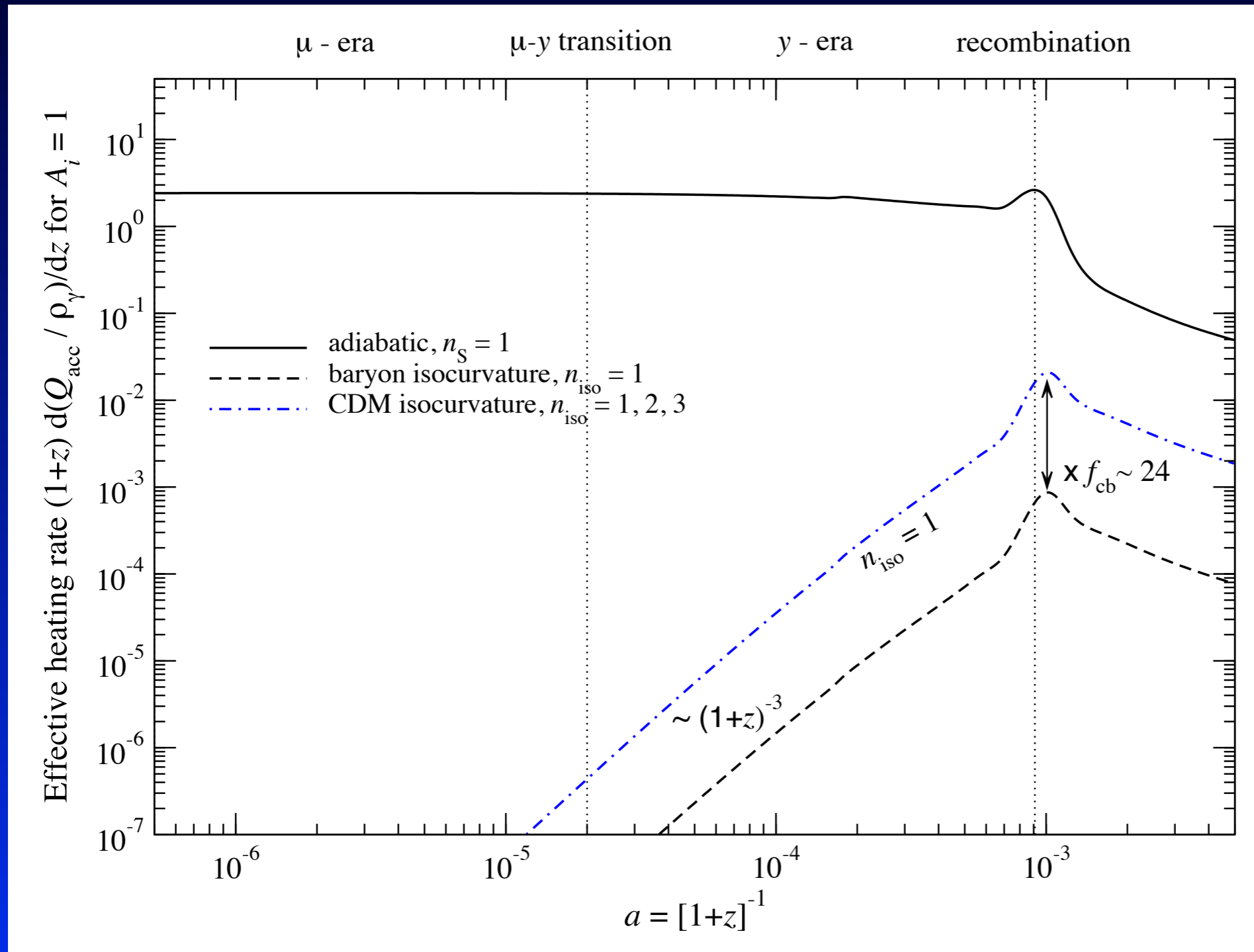
Dependence of heating rate on the perturbation type



- Adiabatic modes: heating rate $\sim 1/z$ at high z

$$P_i(k) = 2\pi^2 A_i k^{-3} (k/k_0)^{n_i-1}$$

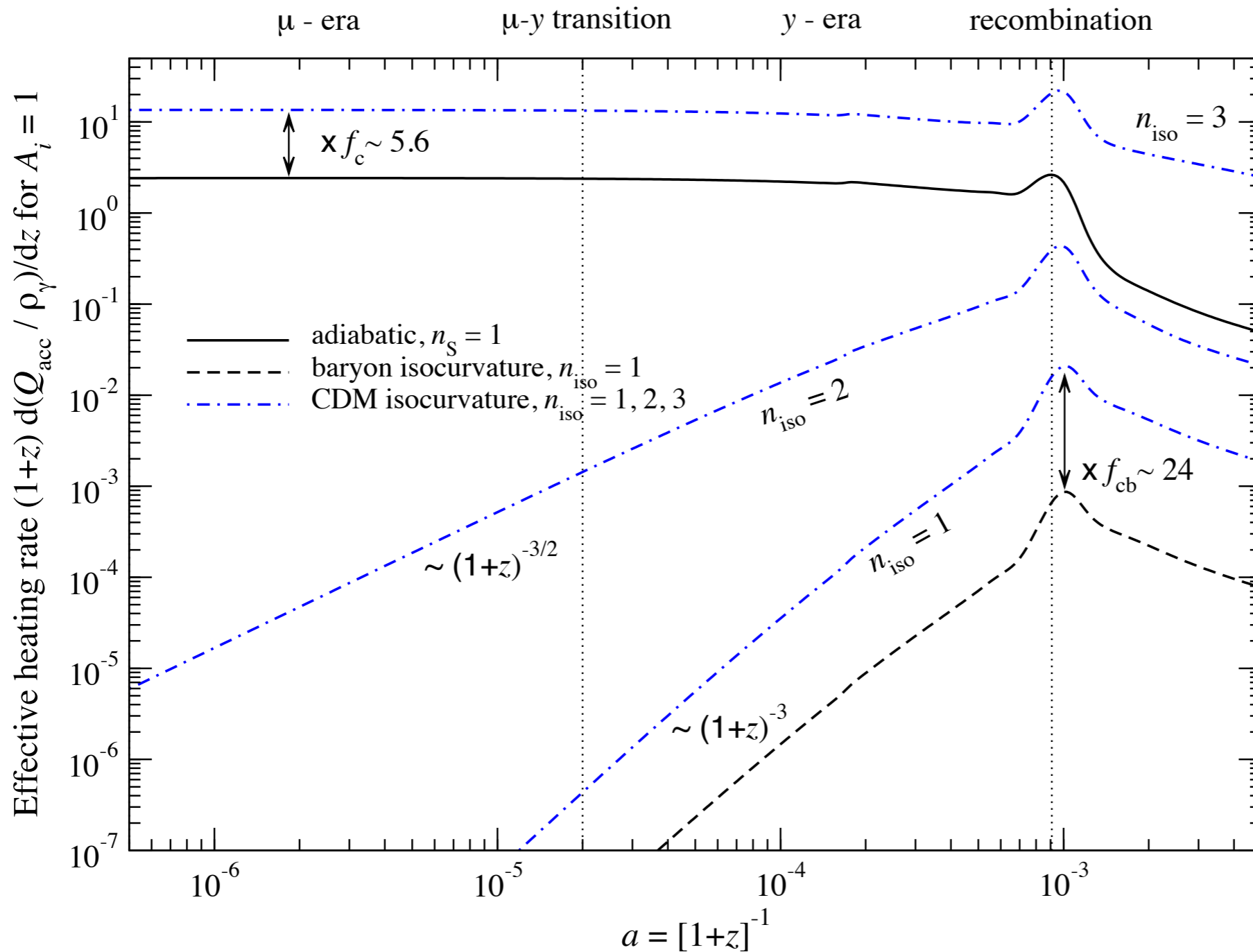
Dependence of heating rate on the perturbation type



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- baryon/CDM isocurvature modes:
 $A \sim k/k_{\text{eq}}$
 during radiation dominated epoch

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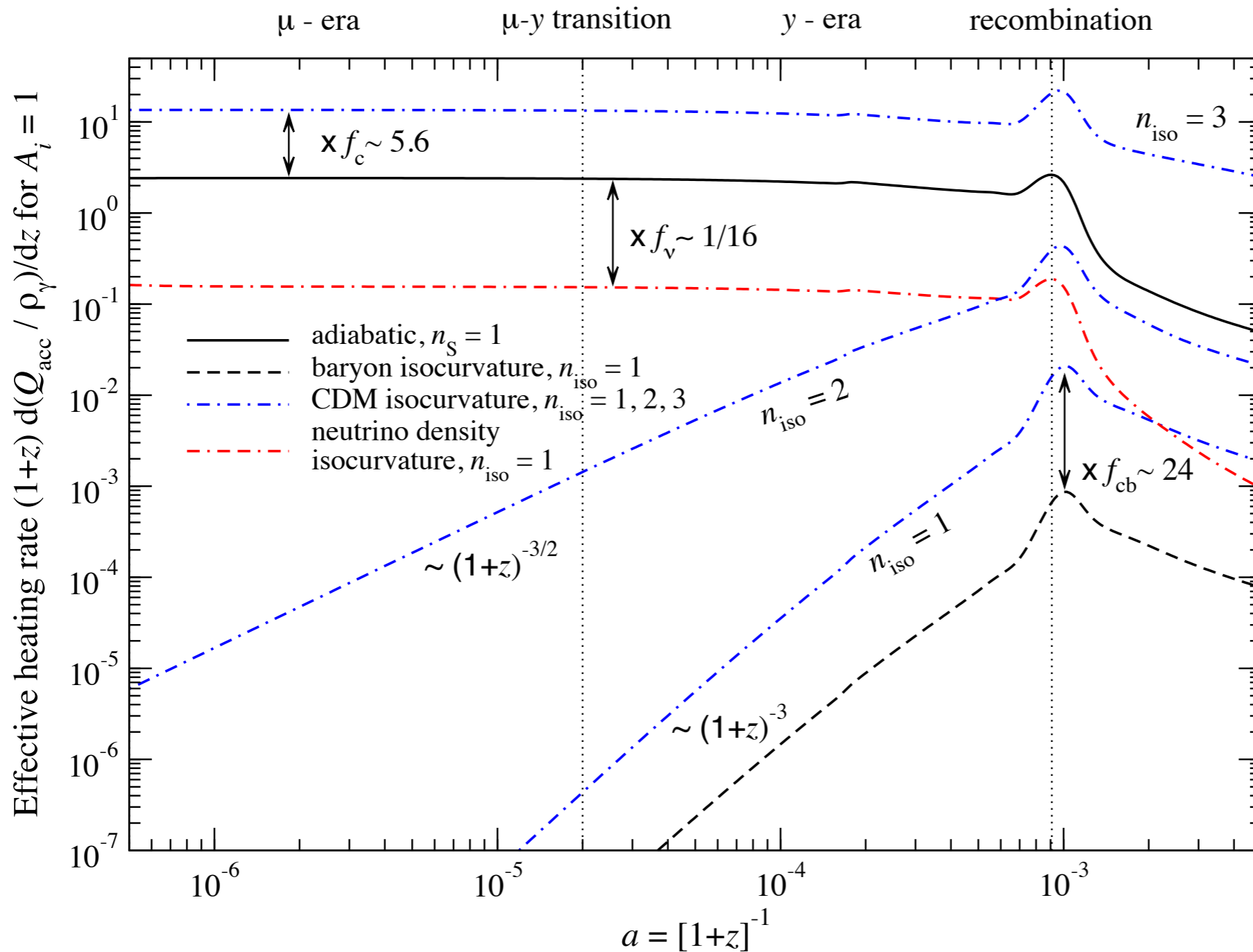
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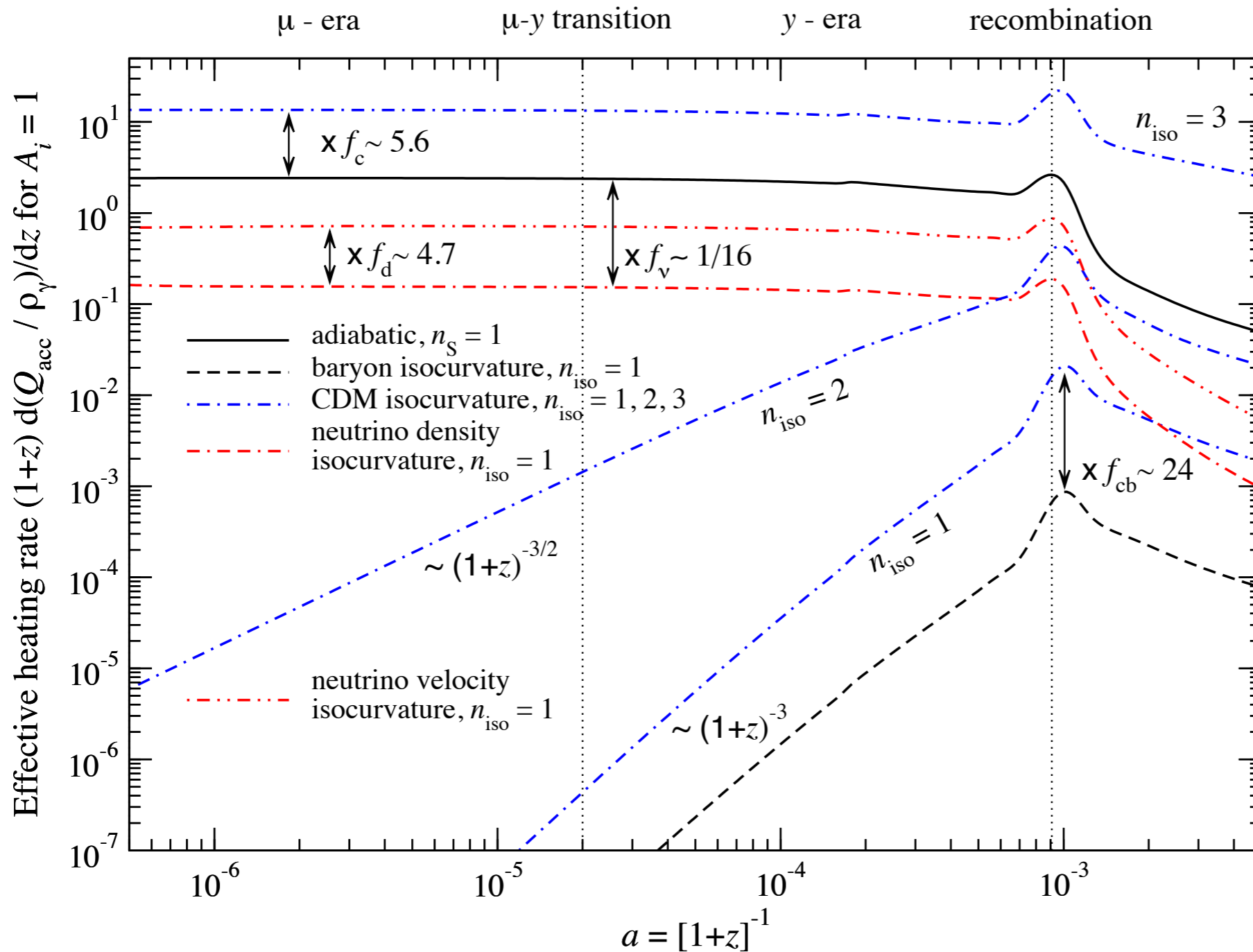
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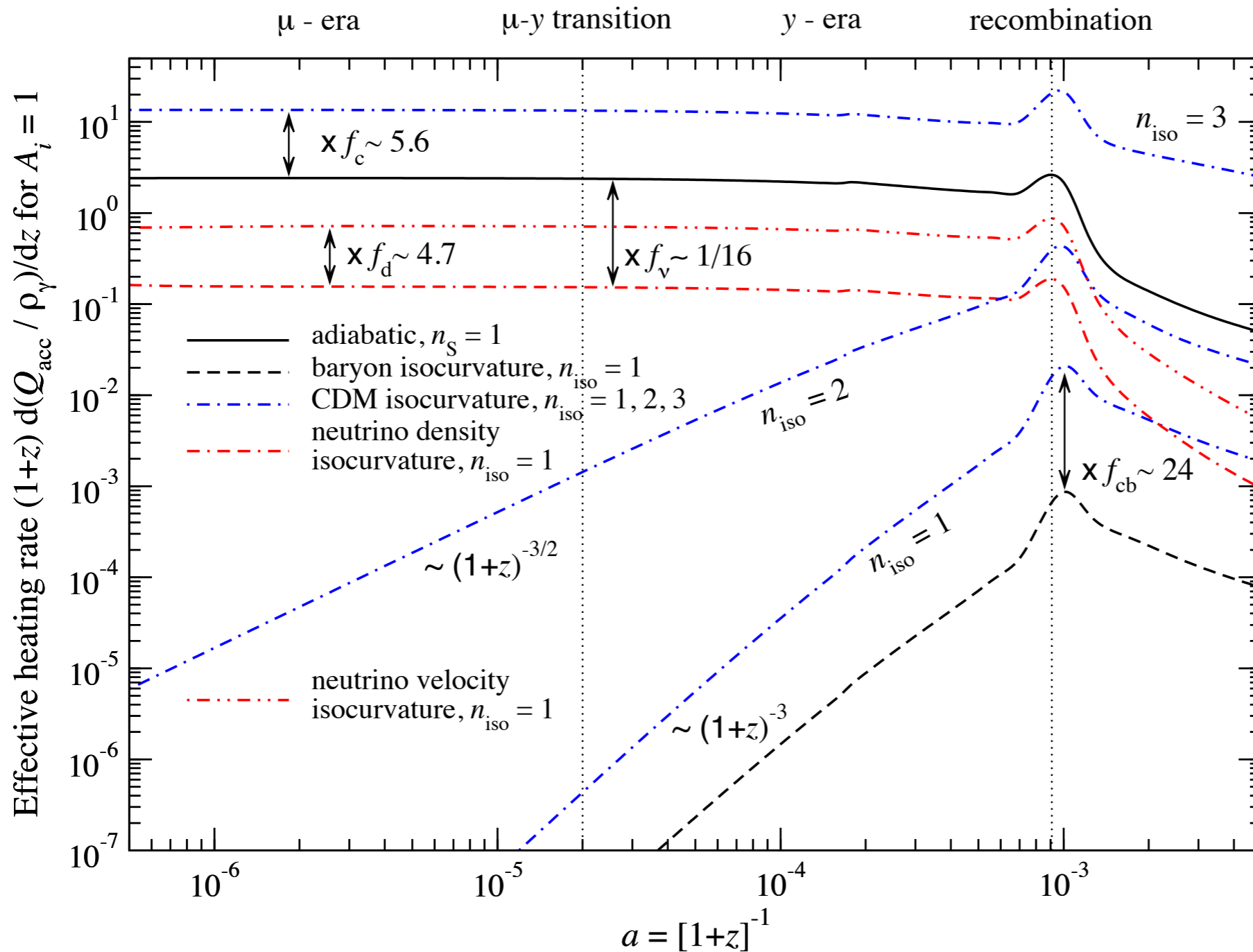
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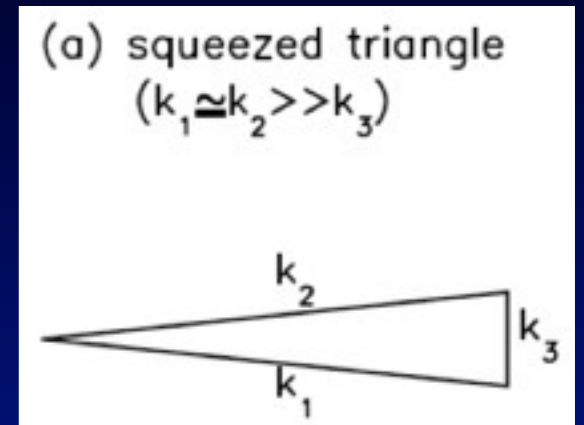


- Adiabatic modes: heating rate $\sim 1/z$ at high z
- baryon/CDM isocurvature modes:
 $A \sim k/k_{eq}$
 during radiation dominated epoch
- $n_{iso} \sim 3 \Rightarrow$ heating rate $\sim 1/z$
- neutrino isocurvature modes very similar to adiabatic modes
- compensated isocurvature modes: *practically no heating*

$$P_i(k) = 2\pi^2 A_i k^{-3} (k/k_0)^{n_i-1}$$

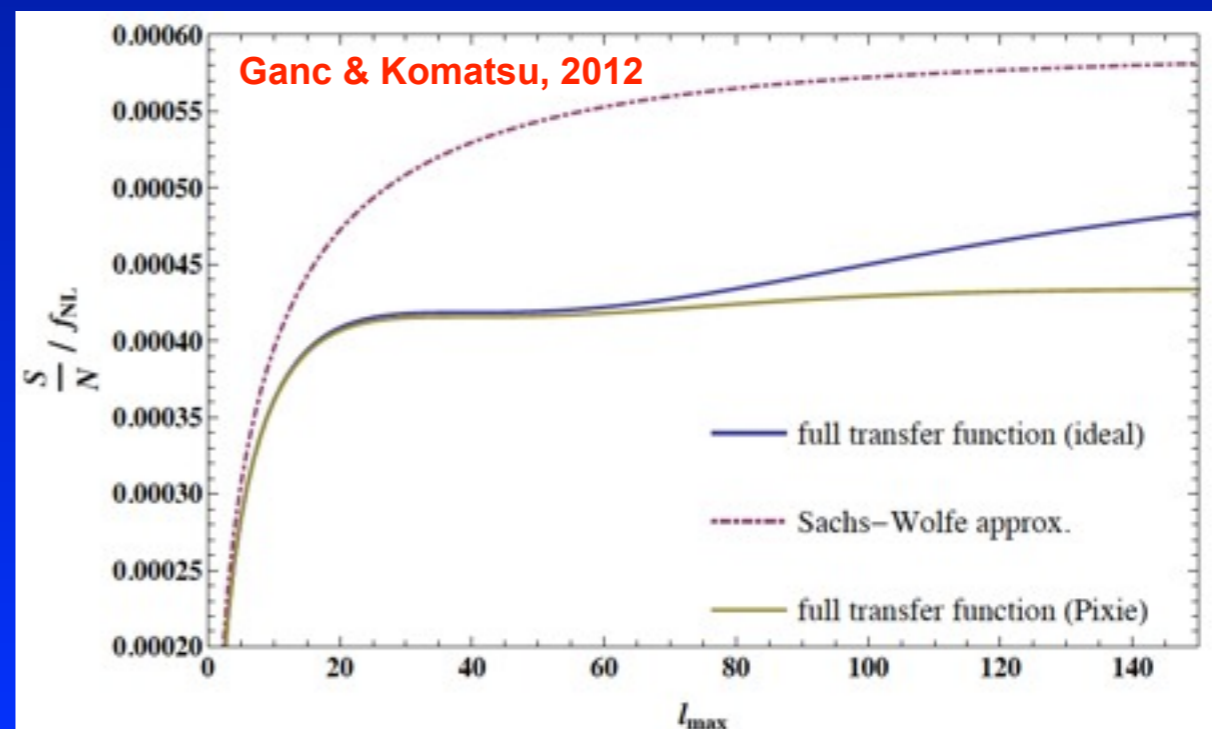
Anisotropic μ -distortions from non-Gaussianity

- Modes that dissipate energy have $k_1 \approx k_2 \gg k_3$
- Non-Gaussian power spectrum \rightarrow presence of positive long-wavelength mode enhances small-scale power
- More small-scale power \rightarrow larger μ -distortion
- \rightarrow Spatially varying μ -distortion caused by non-Gaussianity!
(Pajer & Zaldarriaga, 2012; Ganc & Komatsu, 2012)
- Non-vanishing μ -T correlation at large scales
- Might be detectable with PIXIE-type experiment for $f_{\text{NL}} > 10^3$

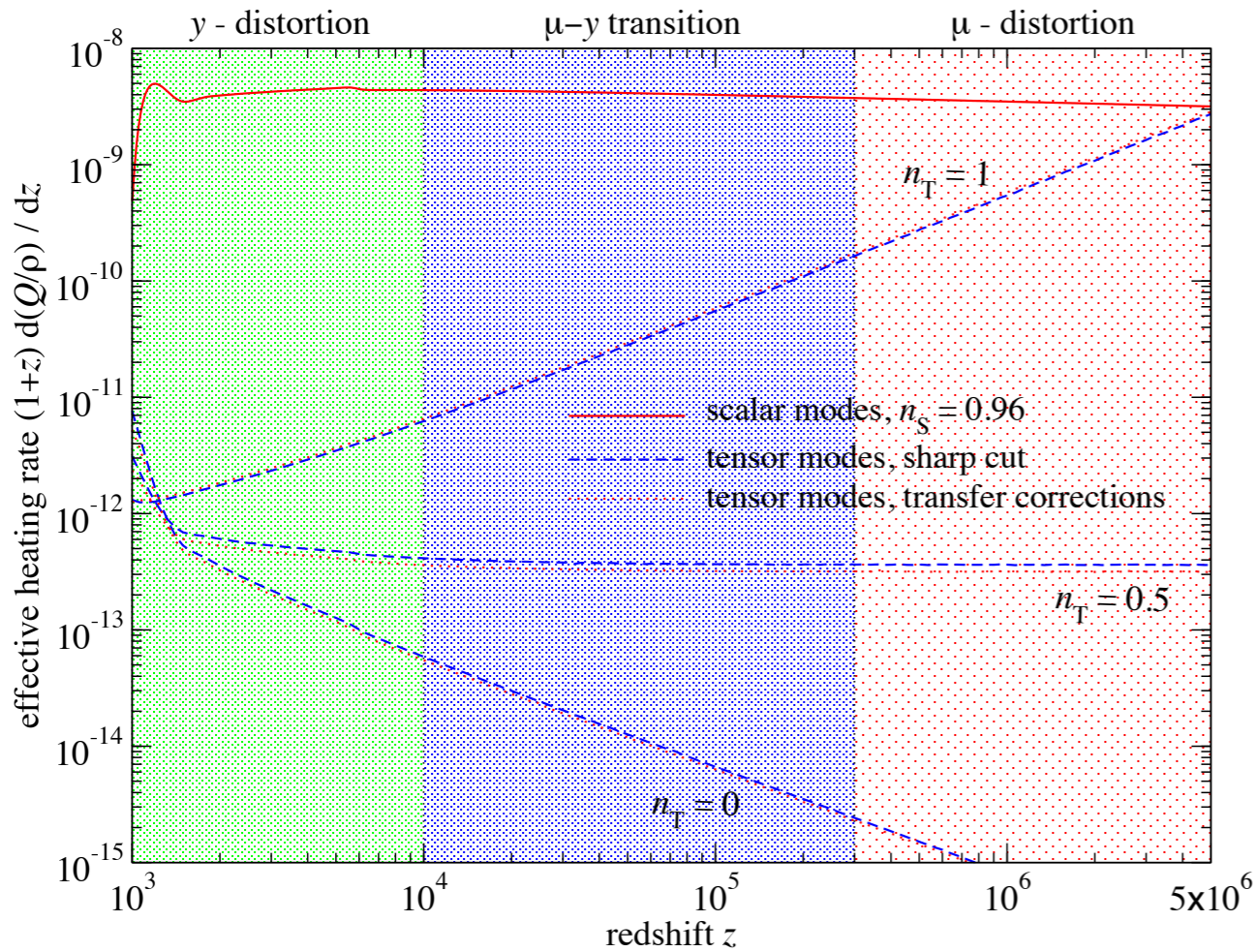


Requirements

- precise cross-calibration of frequency channels
- higher angular resolution does not improve cumulative S/N

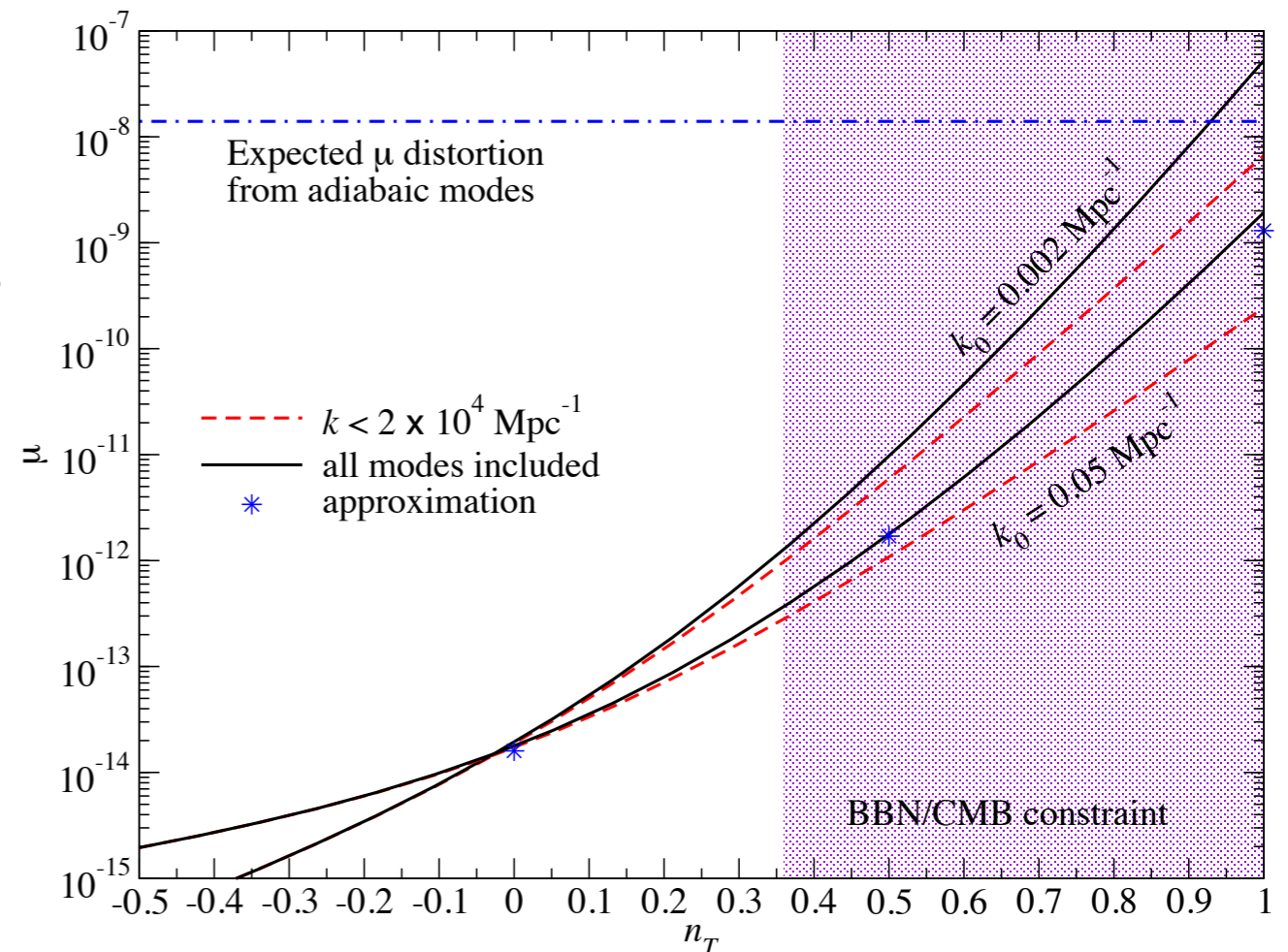


Dissipation of tensor perturbations

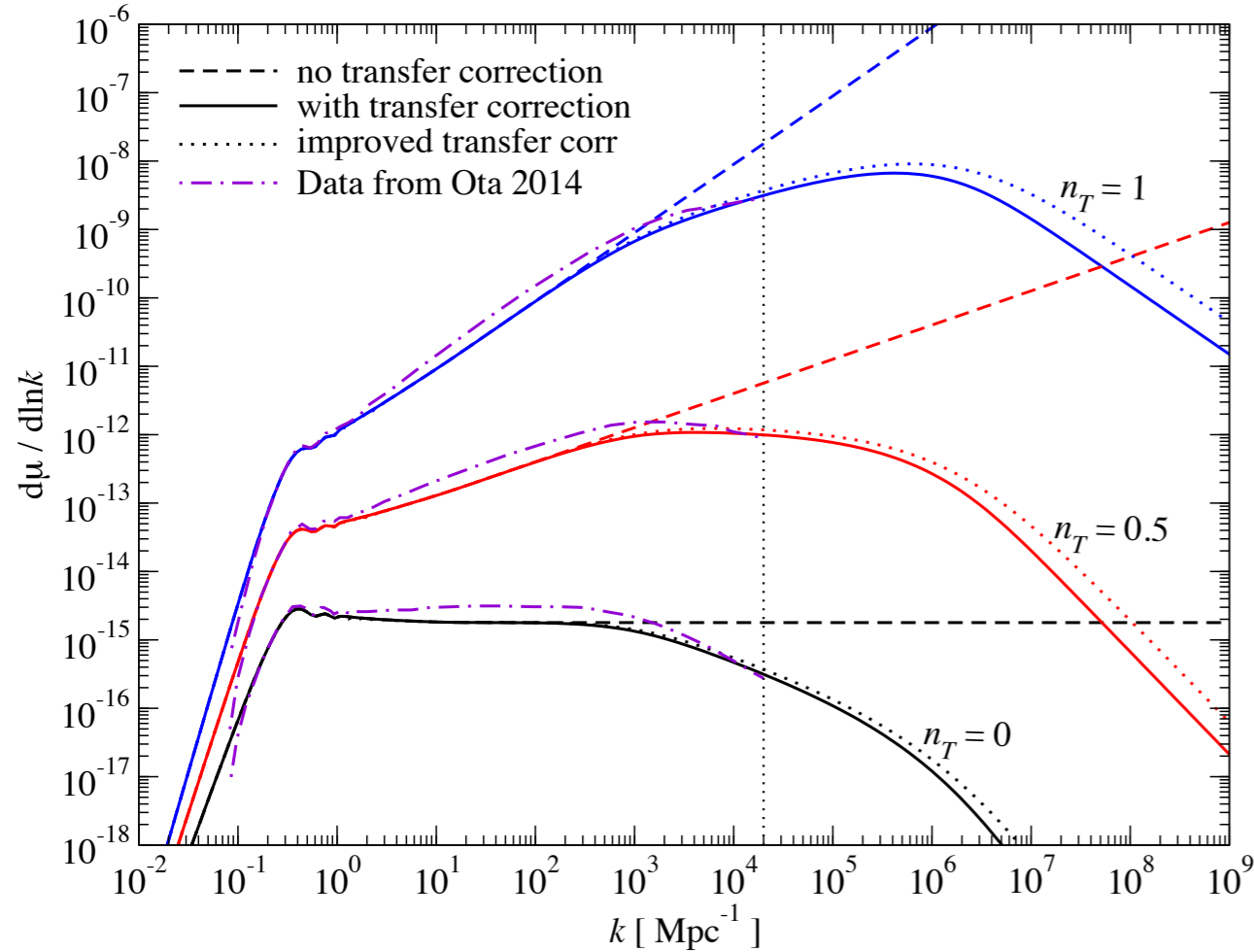


- heating rate can be computed similar to adiabatic modes
- heating rate much smaller than for scalar perturbations
- roughly constant per $d \ln z$ for $n_T \sim 0.5$

- distortion signal very small compared to adiabatic modes
- no severe contamination in simplest cases
- models with 'large' distortion already constrained by BBN/CMB



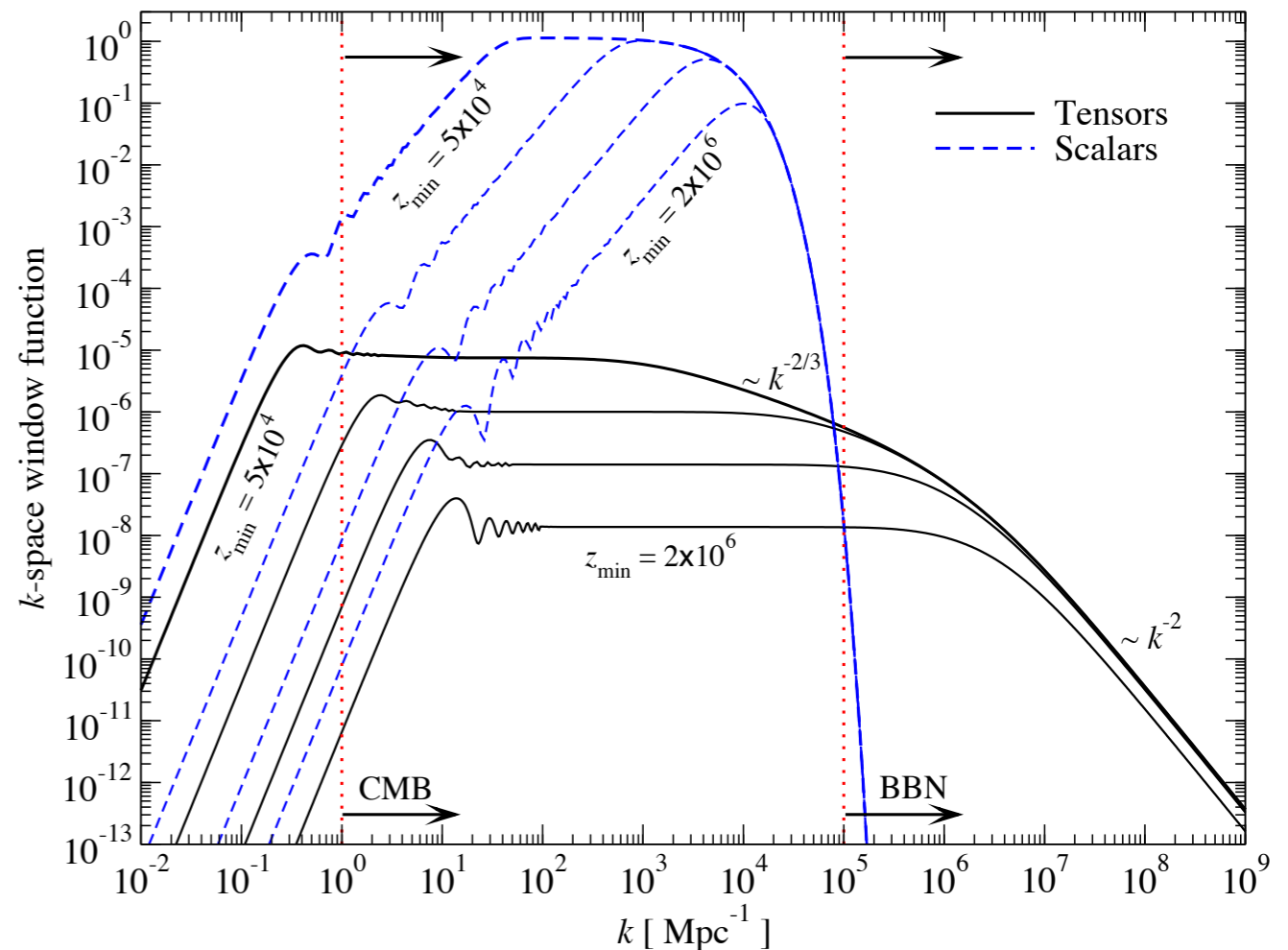
Comparison of the distortion window functions



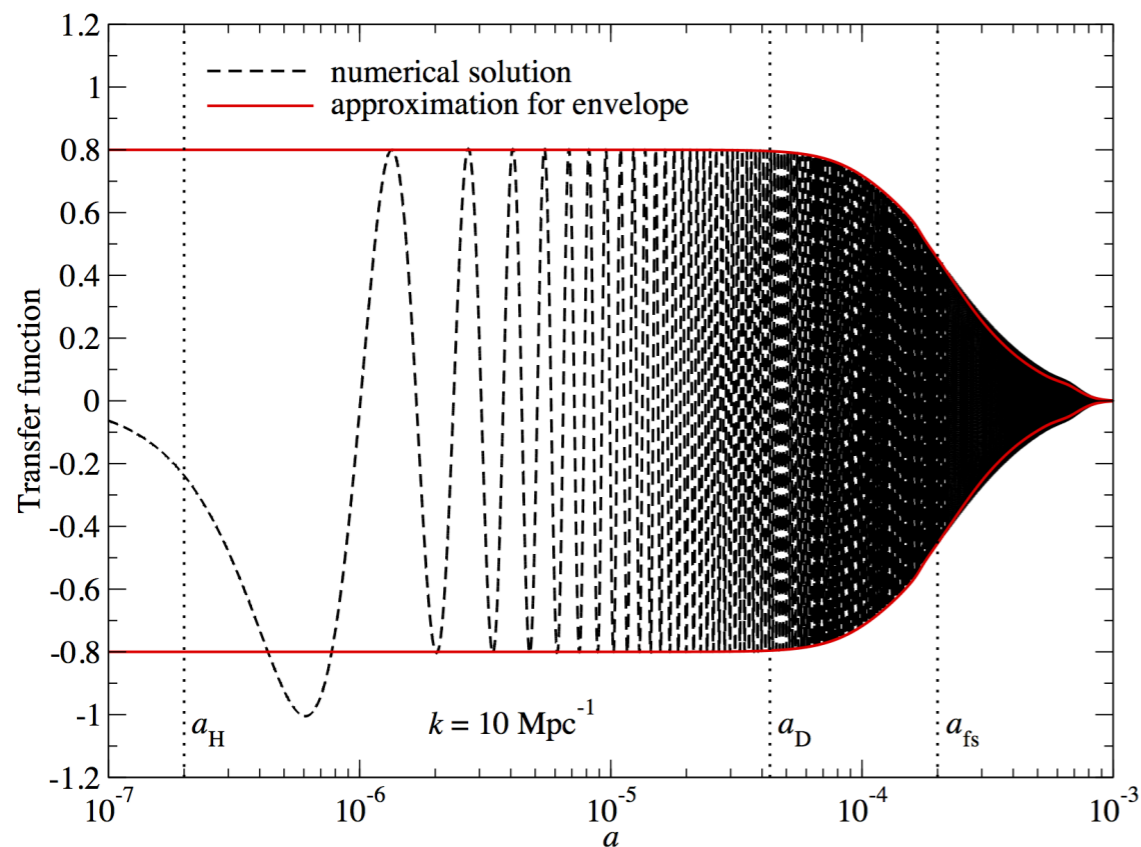
- small-scale modes important for blue tensor power spectra
- Ota et al. underestimated distortion in this case ~ 7 times

$$\mu_i \approx \int_0^\infty \frac{k^2 dk}{2\pi^2} P_i(k) W_i(k)$$

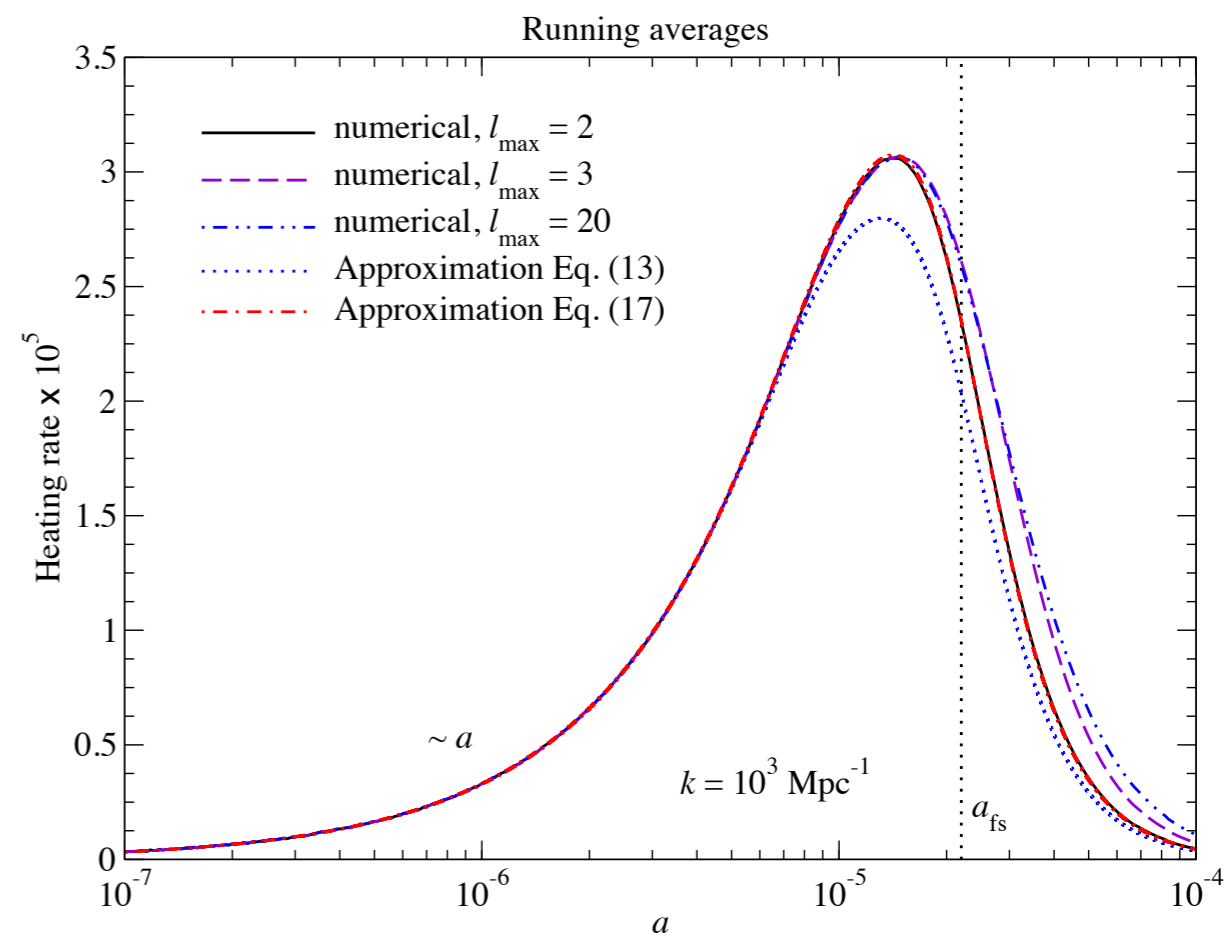
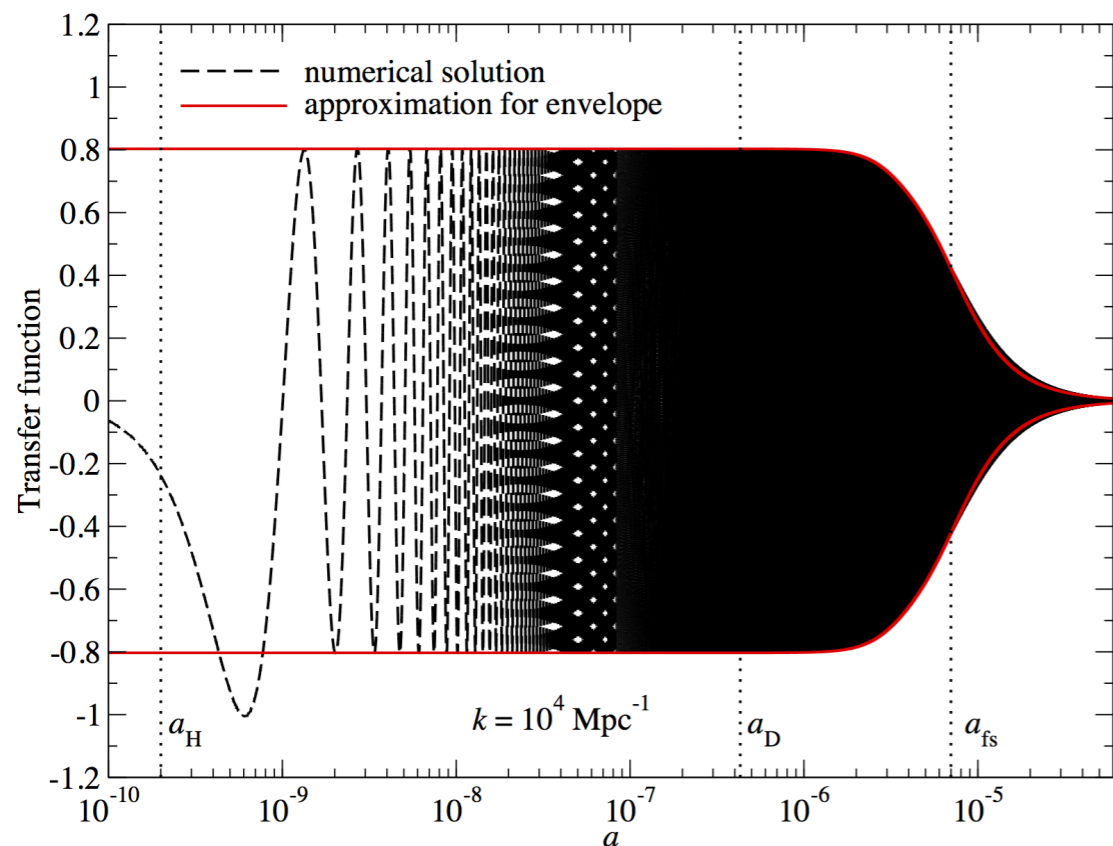
- adiabatic modes sensitive to a smaller range of scales
- tensors even have contributions from close to the horizon scale
- power-law decay at small scales



Small-scale photon transfer function for tensors



- simple analytic expressions for the envelope and phase
- tensors never really disappear at small scales
- decay of amplitude only power-law instead of exponential as for adiabatic modes



Structure of the Lectures (cont.)

Lecture III:

- Overview of different sources of distortions
- Dissipation of acoustic modes
- Decaying particles

Structure of the Lectures (cont.)

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- Recombination physics and why it is important
- The cosmological recombination radiation
- Sunyaev-Zeldovich effect and what the signals could tell us

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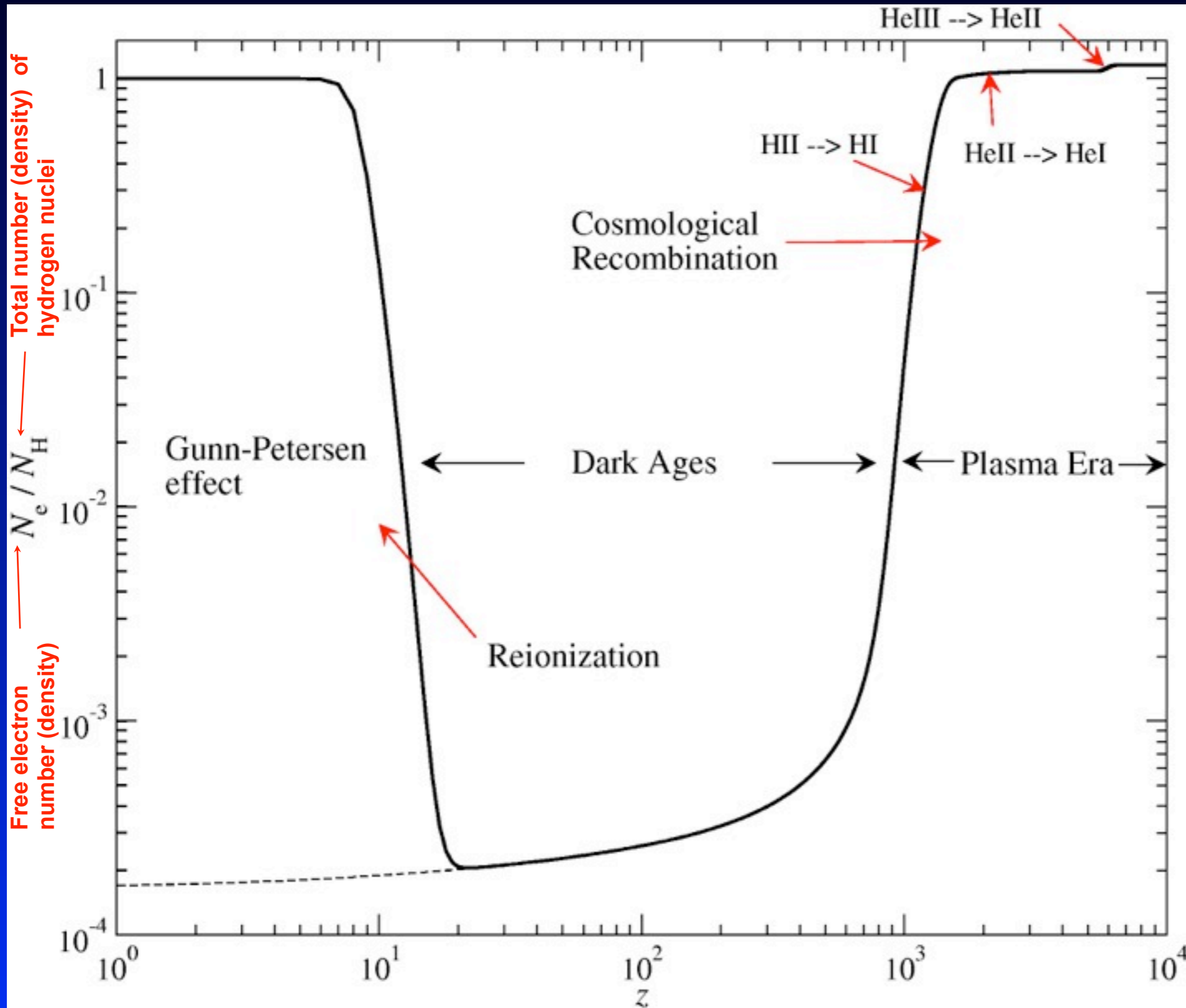
- Recombination physics and why it is important
- The cosmological recombination radiation
- Sunyaev-Zeldovich effect and what the signals could tell us



Sadly we won't have time for this...

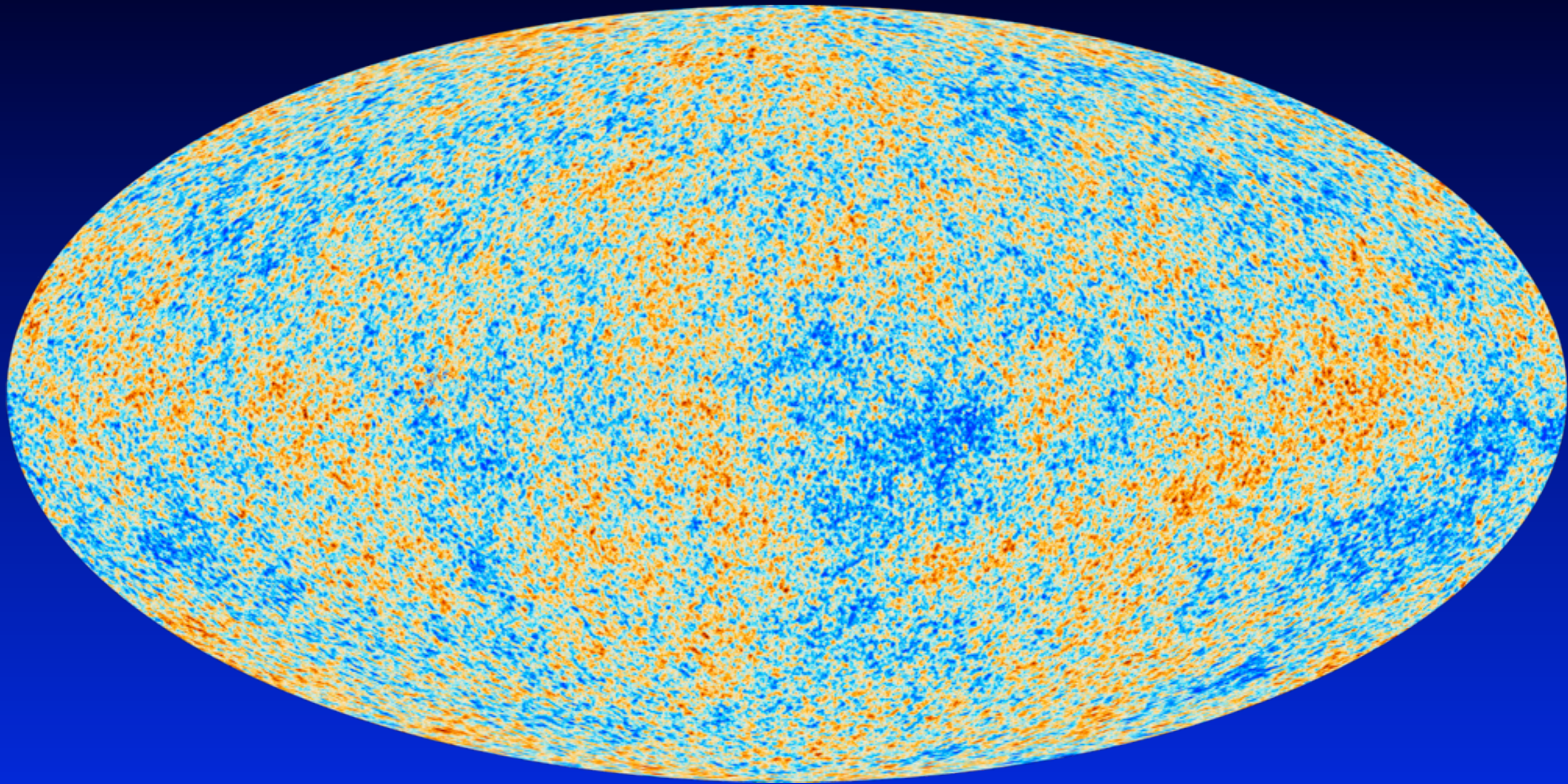
The cosmological recombination radiation & ionization history and why they are so important

Sketch of the Cosmic Ionization History



- at redshifts higher than $\sim 10^4$ Universe \rightarrow fully ionized
- $z \geq 10^4 \rightarrow$ free electron fraction $N_e/N_H \sim 1.16$ (Helium has 2 electrons and abundance $\sim 8\%$)
- $\text{HeIII} \rightarrow \text{HeII}$ recombination at $z \sim 6000$
- $\text{HeII} \rightarrow \text{HeI}$ recombination at $z \sim 2000$
- $\text{HII} \rightarrow \text{HI}$ recombination at $z \sim 1000$

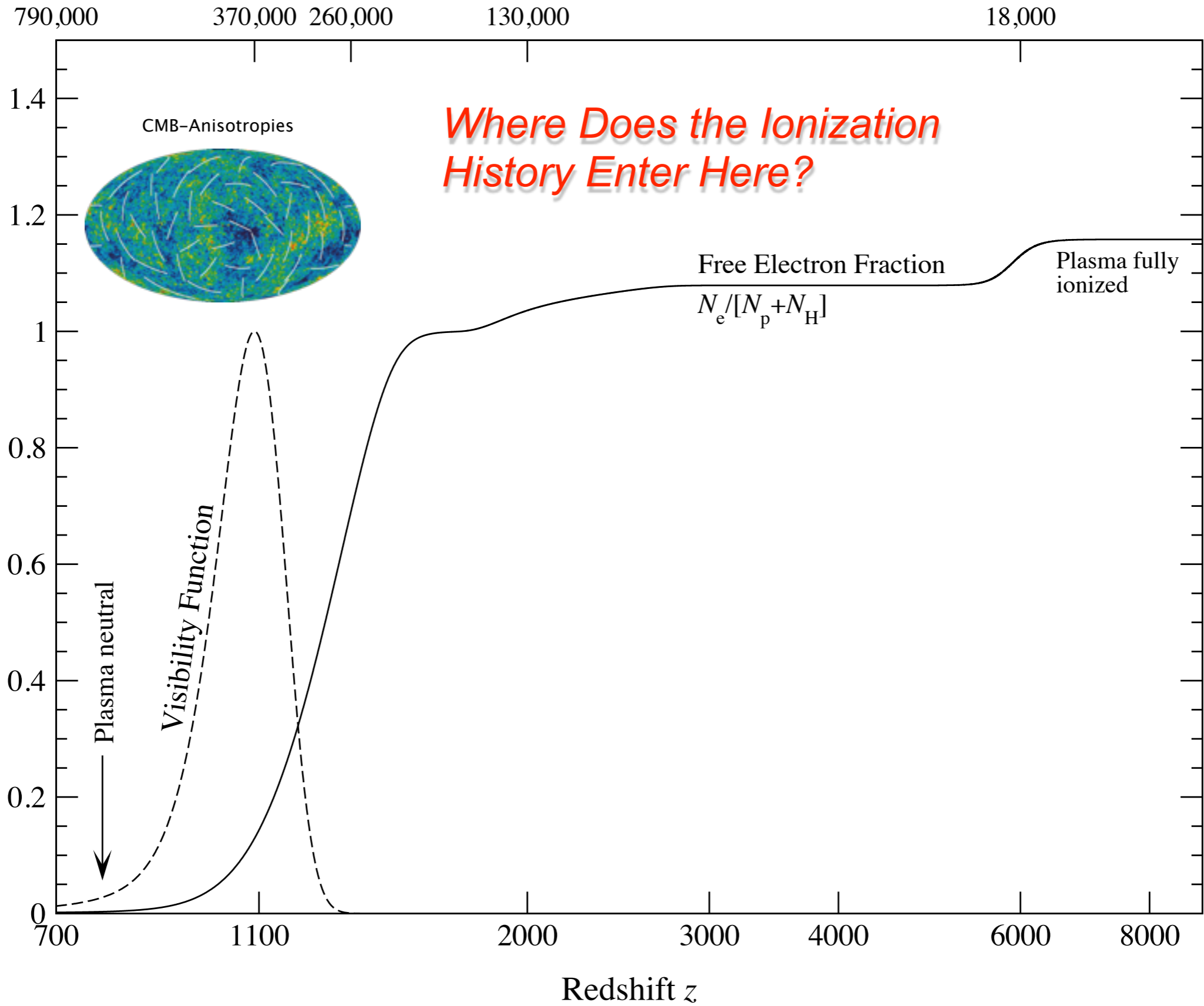
Cosmic Microwave Background Anisotropies



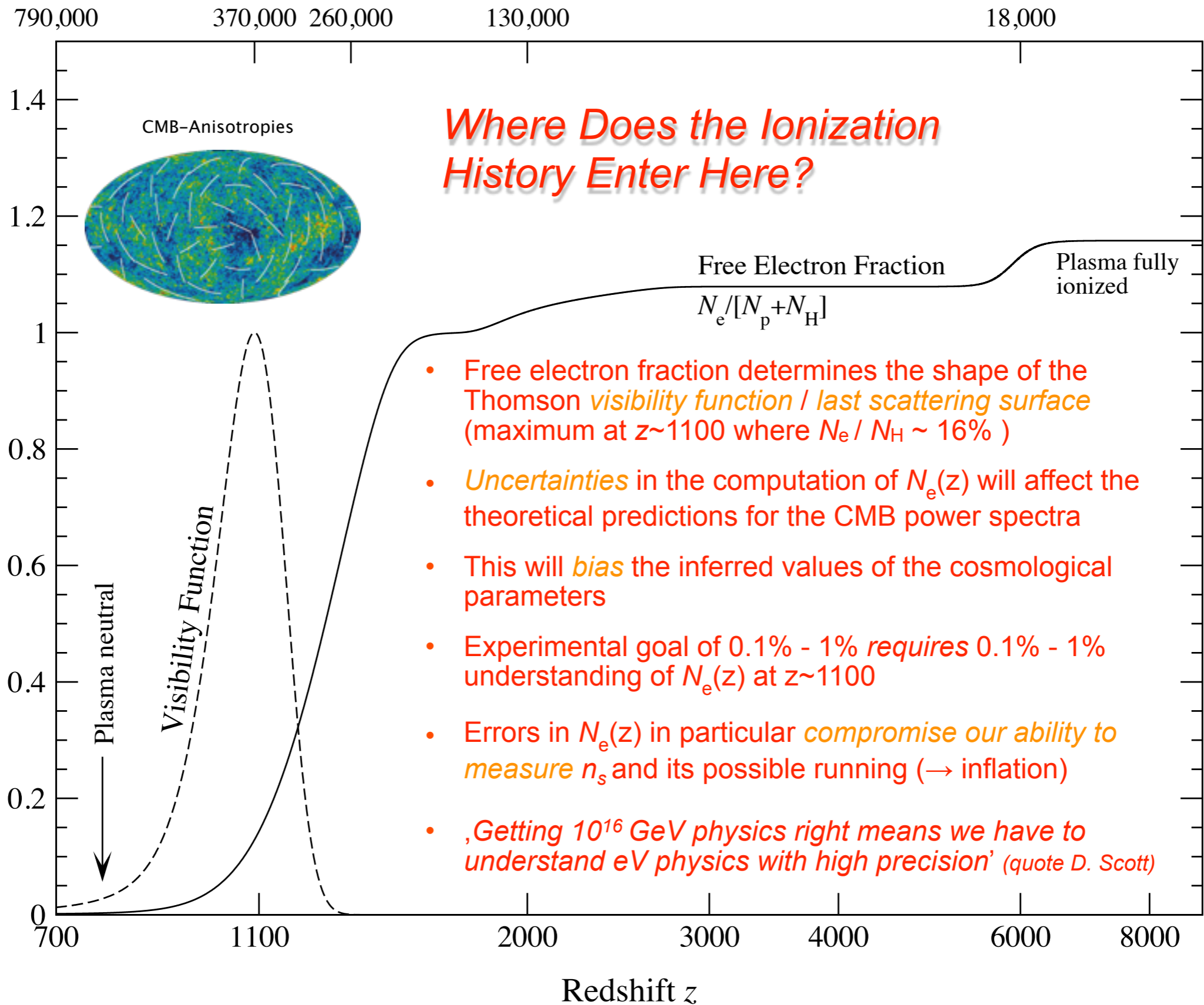
Planck all sky map

- CMB has a blackbody spectrum in every direction
- tiny variations of the CMB temperature $\Delta T/T \sim 10^{-5}$

Cosmological Time in Years

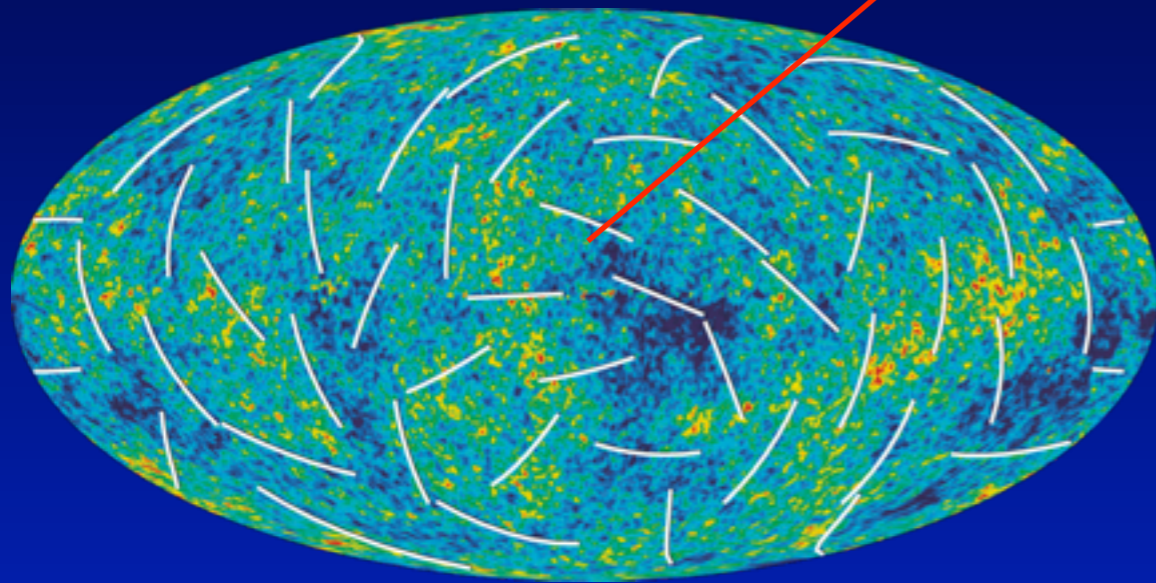


Cosmological Time in Years



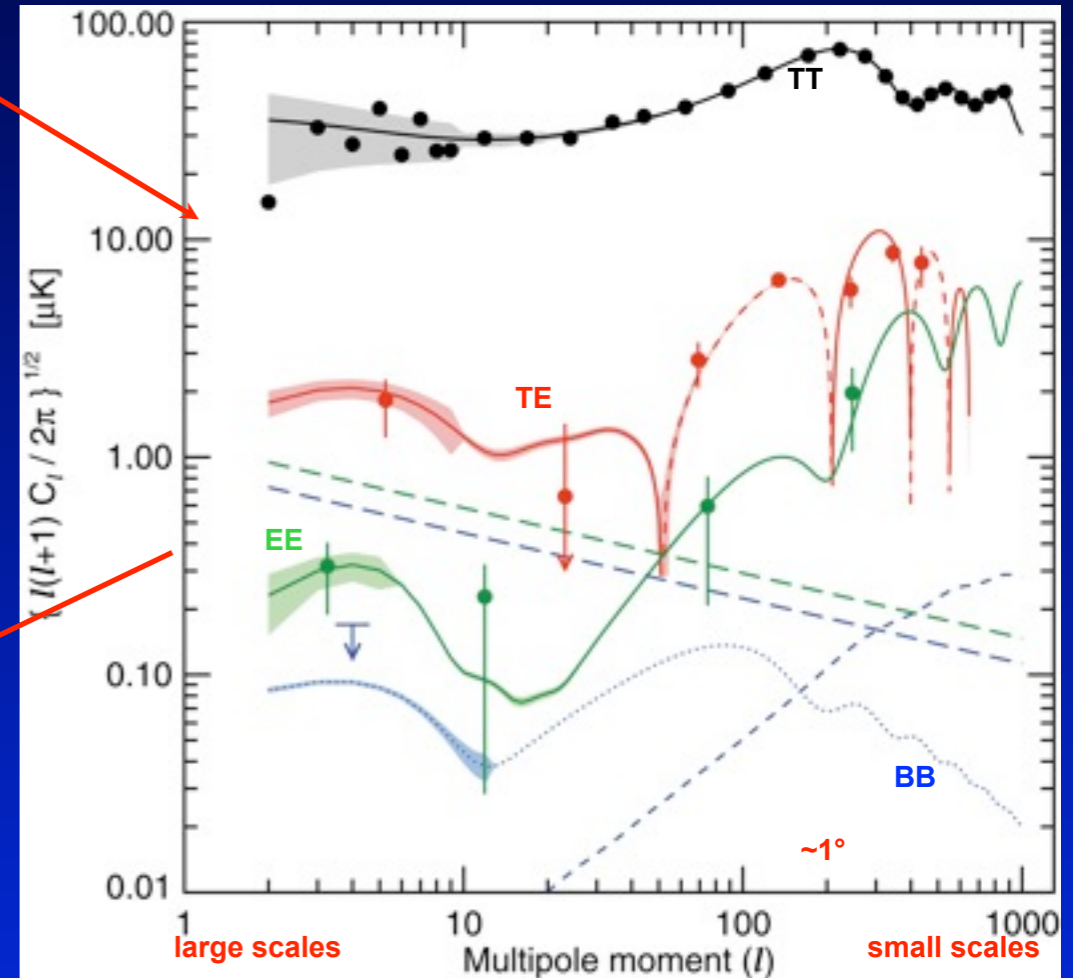
CMB Sky \rightarrow Cosmology

WMAP CMB Sky



a_{lm}

Power spectra



Cosmological Parameters

$\Omega_{\text{tot}}, \Omega_{\text{m}}, \Omega_{\text{b}}, \Omega_{\Lambda},$
 $h, \tau, n_{\text{S}}, \dots$

(Joint) analysis

Other cosmological Dataset:

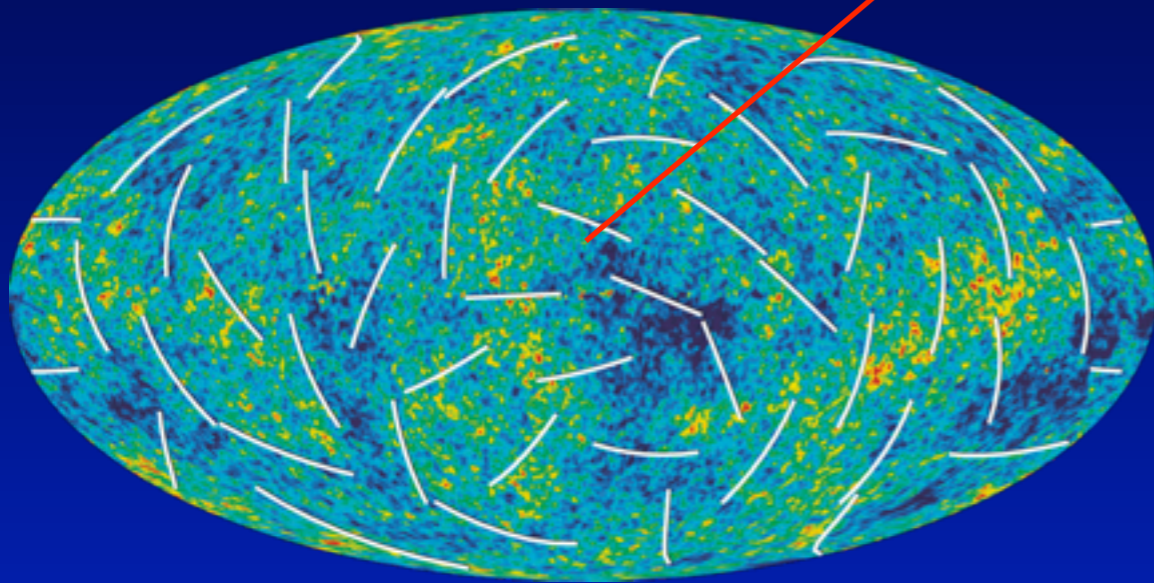
small-scale CMB, Supernovae, large-scale structure/
BAO, Lyman- α forest, lensing, ...

CMB Sky \rightarrow Cosmology

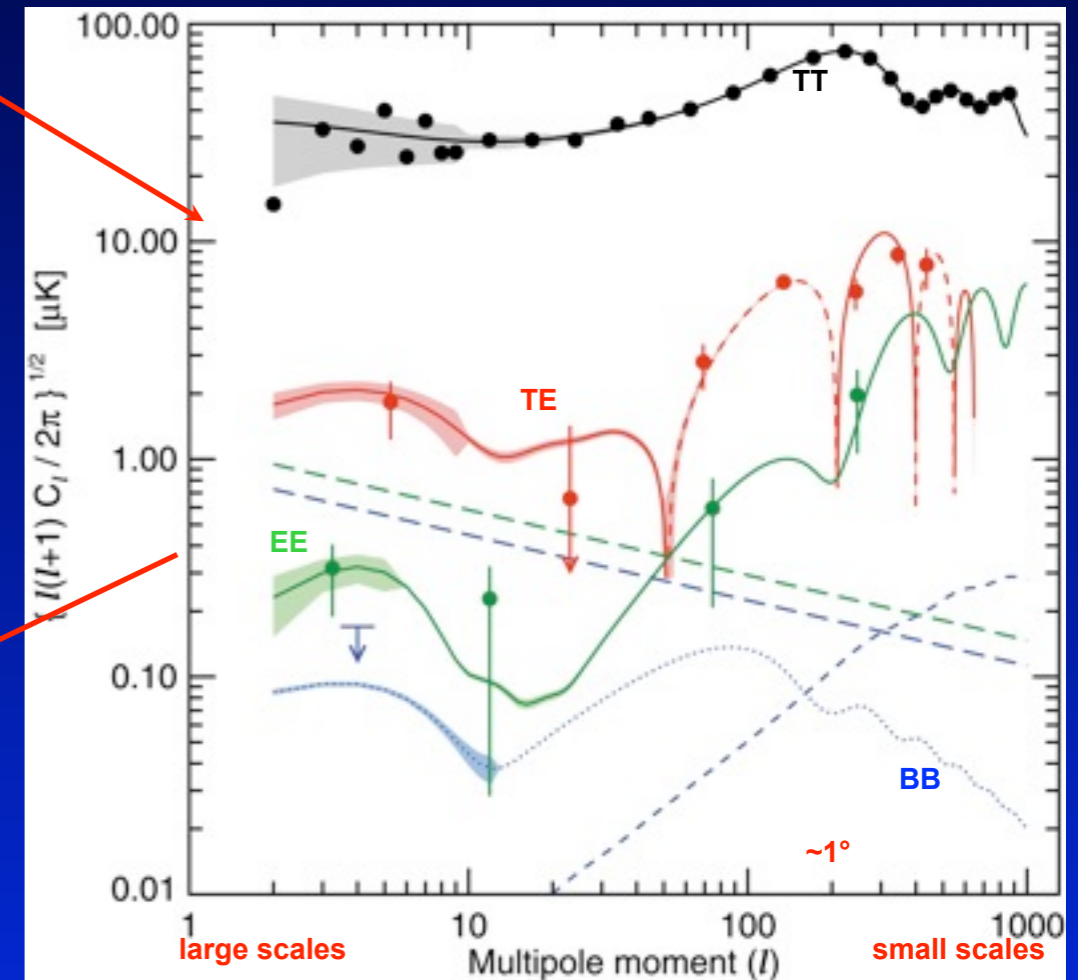
$N_e(z)$ is a *crucial* input

Power spectra

WMAP CMB Sky



a_{lm}



Cosmological Parameters

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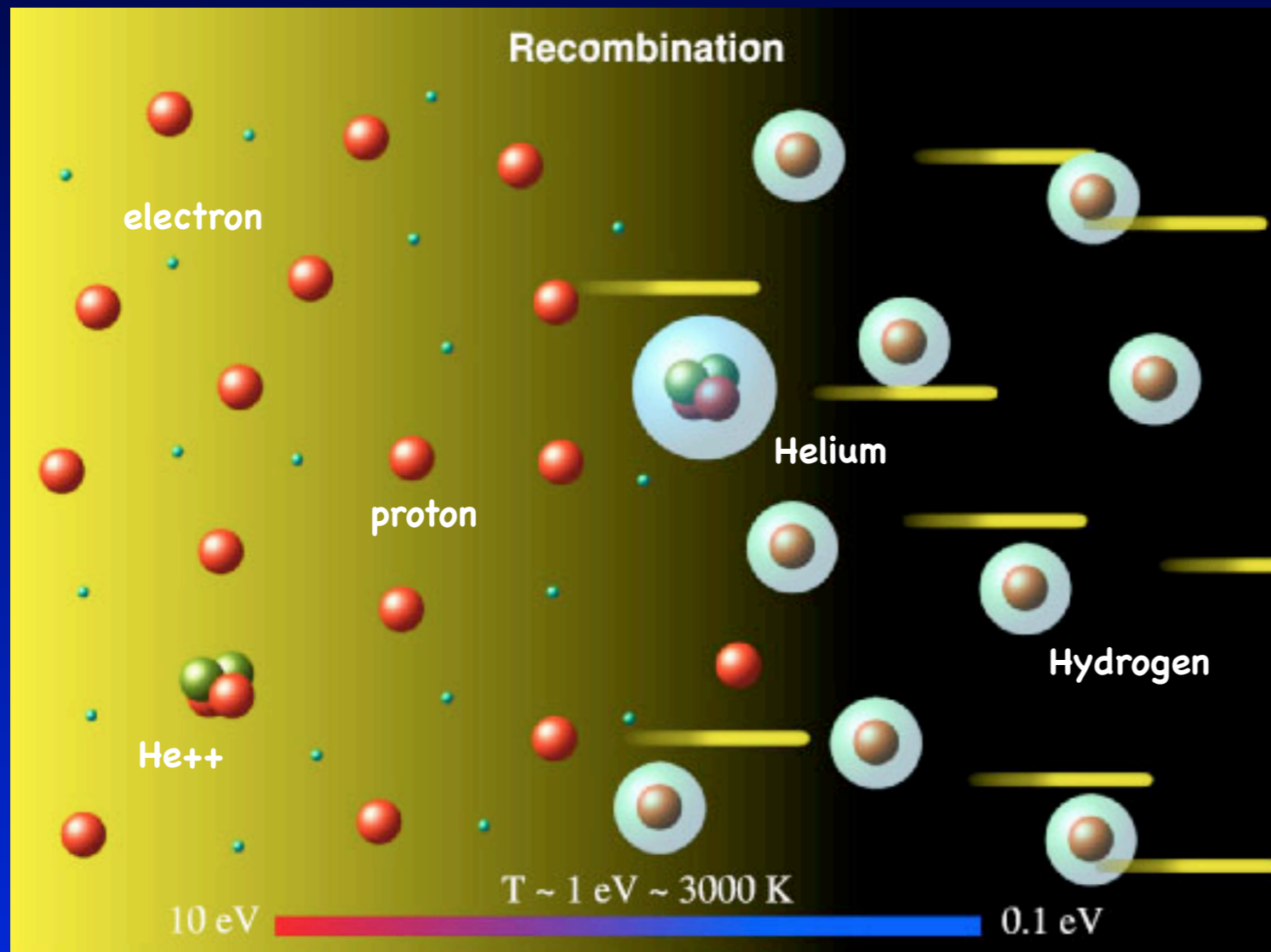
small-scale CMB, Supernovae, large-scale structure/
BAO, Lyman- α forest, lensing, ...

Why are the ionization history and recombination radiation connected?

- To interpret high-precision CMB data we need to understand the *ionization history* very well!
- The recombination radiation is a direct *record* of the recombination process
- measuring the recombination radiation allows us to directly *check our understanding* of the recombination process!
- *High-frequency distortion* actually controls recombination dynamics, so we need to understand both well!

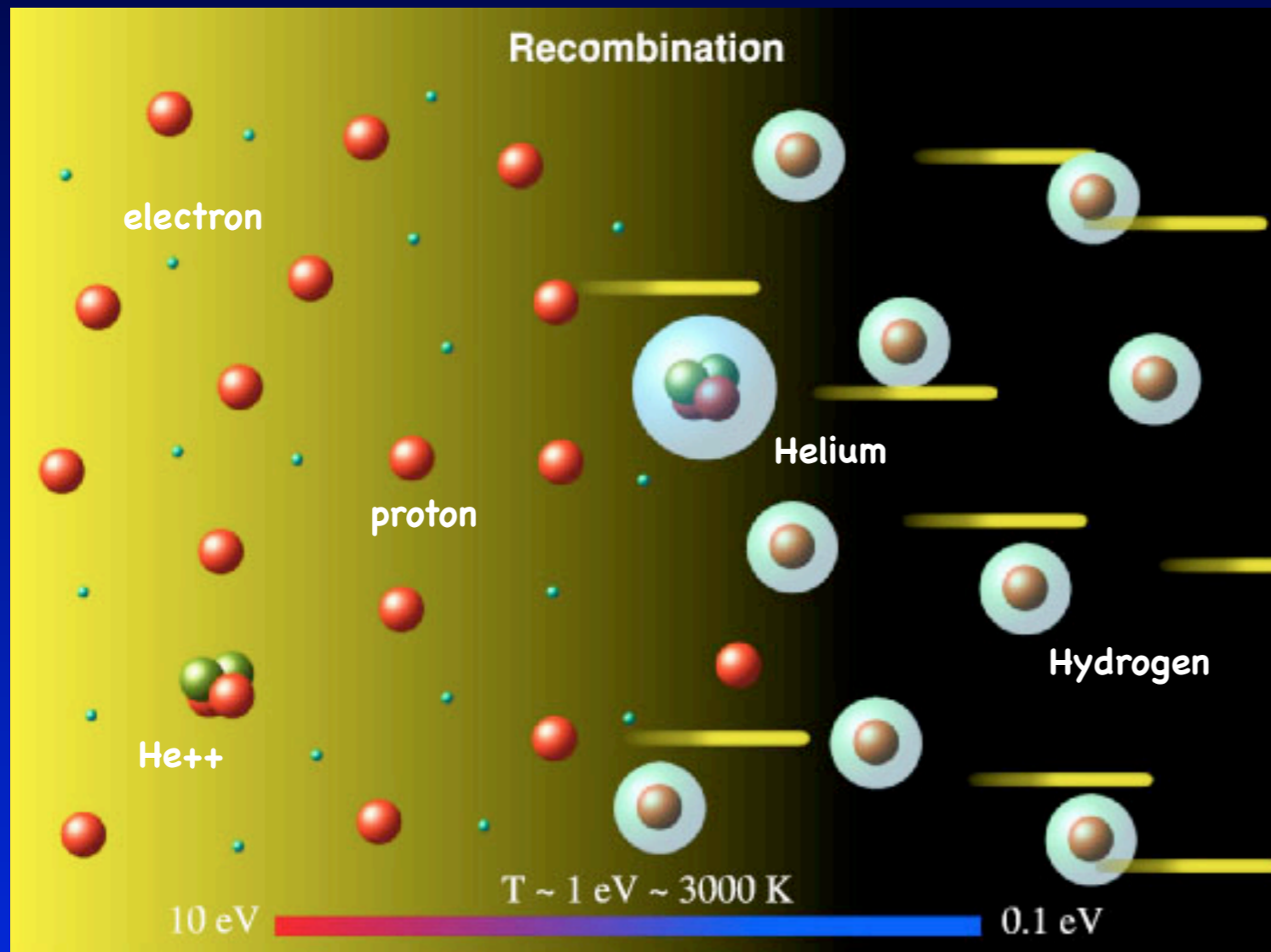
How does cosmological recombination work?

What is the recombination problem about?



- coupled system describing the interaction of *matter* with the ambient CMB *photon* field
- atoms can be in different excitation states
⇒ *lots of levels to worry about*
- recombination process changes Wien tail of CMB and this affects the recombination dynamics
⇒ *radiative transfer problem*

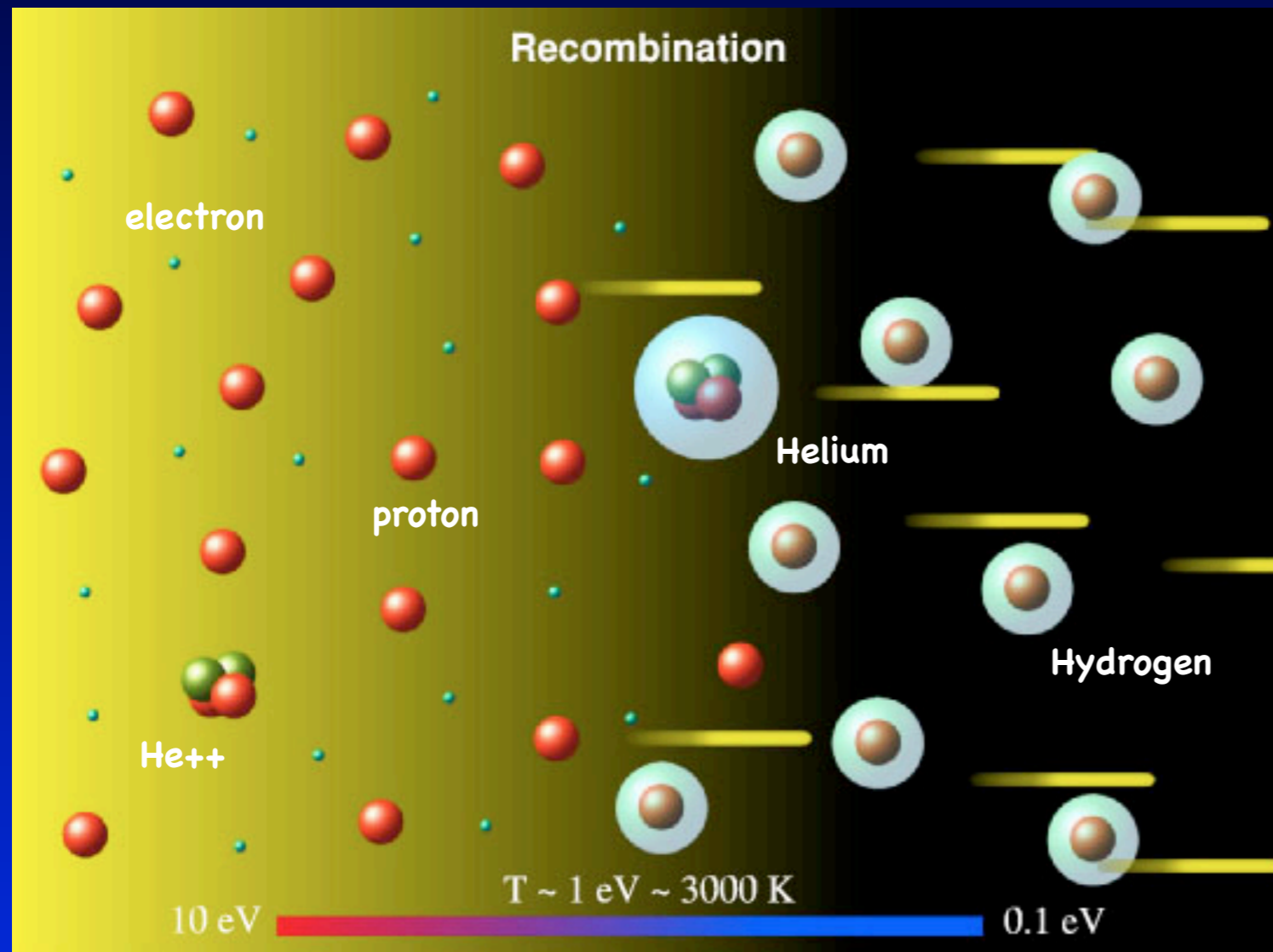
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Have to follow evolution of: N_e, T_e, N_p, N_i and ΔI_ν

What is the recombination problem about?

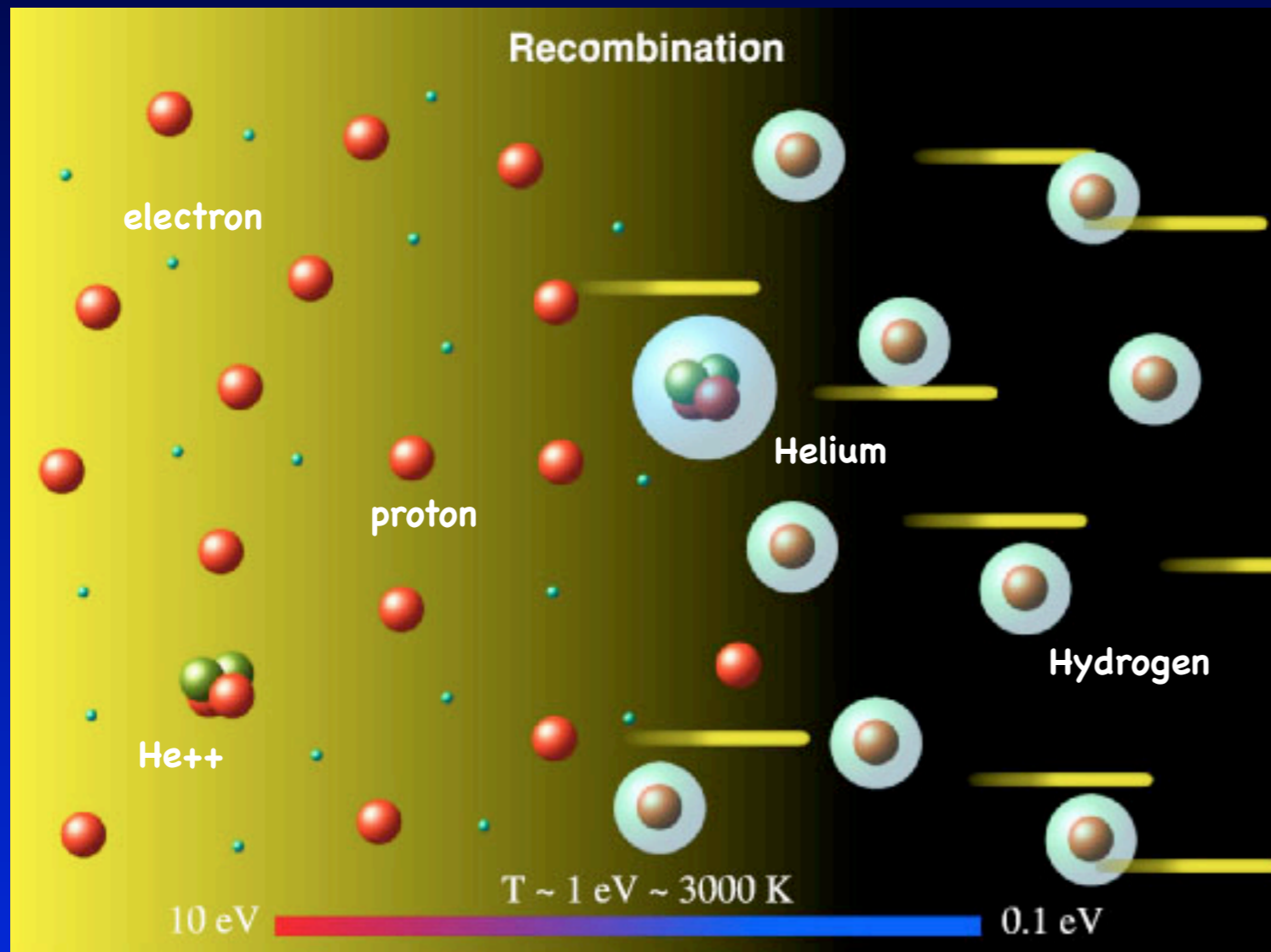


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⇒ *radiative transfer problem*

Have to follow evolution of: N_e, T_e, N_p, N_i and ΔI_ν

↑ electron temperature
↑ number densities
↑ non-thermal photons

What is the recombination problem about?



- coupled system describing the interaction of *matter* with the ambient CMB *photon* field
- atoms can be in different excitation states
⇒ *lots of levels to worry about*
- recombination process changes Wien tail of CMB and this affects the recombination dynamics
⇒ *radiative transfer problem*

Have to follow evolution of: N_e, T_e, N_p, N_i and ΔI_ν

Arrows point from the text to the variables: T_e is labeled 'electron temperature', N_e, N_p, N_i are collectively labeled 'number densities', and ΔI_ν is labeled 'non-thermal photons'.

Only problem in time!

Physical Conditions during Recombination

- Temperature $T_\gamma \sim 2.725 (1+z) \text{ K} \sim 3000 \text{ K}$
- Baryon number density $N_b \sim 2.5 \times 10^{-7} \text{ cm}^{-3} (1+z)^3 \sim 330 \text{ cm}^{-3}$
- Photon number density $N_\gamma \sim 410 \text{ cm}^{-3} (1+z)^3 \sim 2 \times 10^9 N_b$
⇒ photons in very distant Wien tail of blackbody spectrum can keep hydrogen ionized until $h\nu_\alpha \sim 40 kT_\gamma \iff T_\gamma \sim 0.26 \text{ eV}$
- Collisional processes negligible (*completely different in stars!!!*)
- Rates dominated by radiative processes
(e.g. stimulated emission & stimulated recombination)
- Compton interaction couples electrons very tightly to photons until $z \sim 200 \Rightarrow T_\gamma \sim T_e \sim T_m$

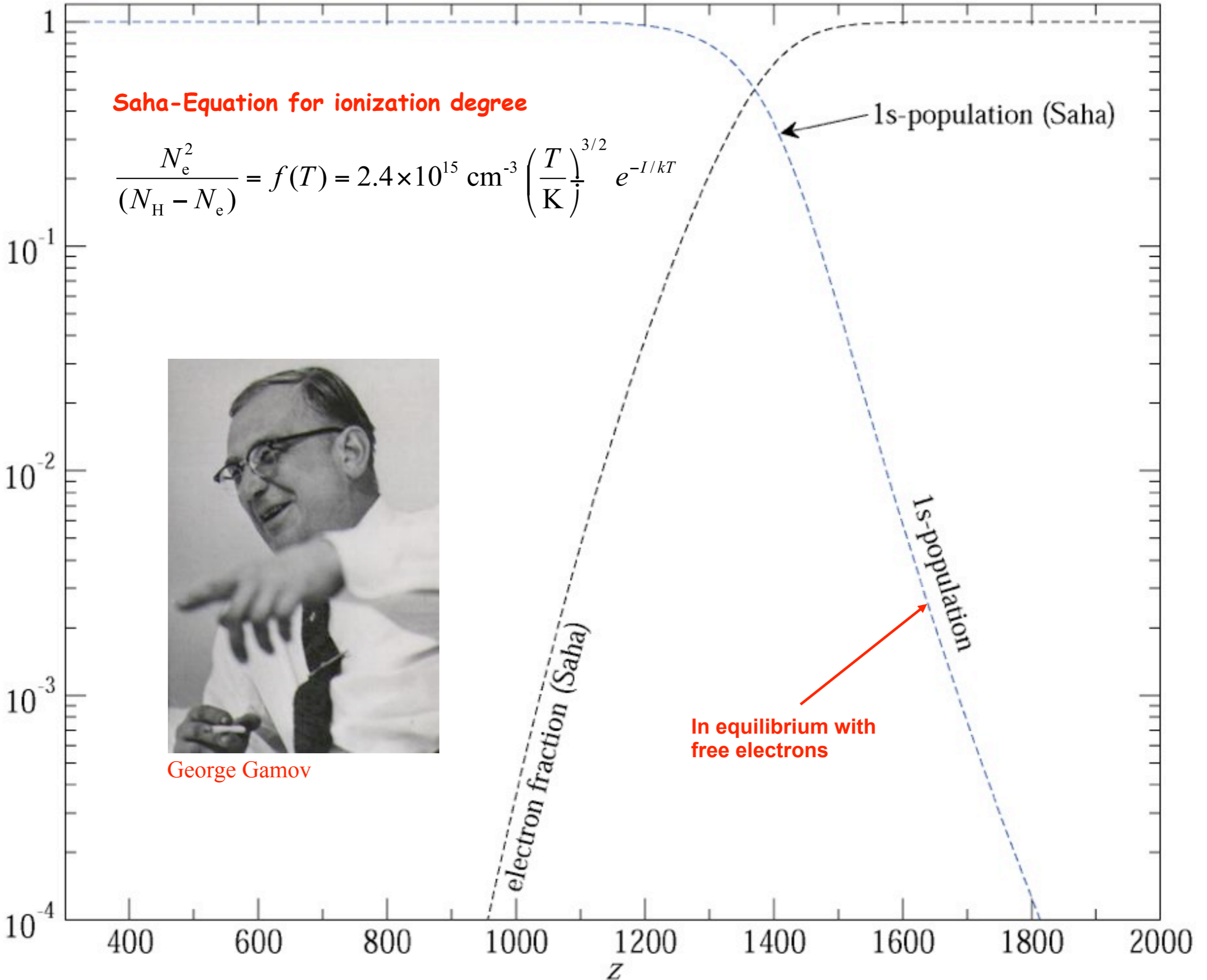
(number) density of given species i $\rightarrow N_i/N_H$ \rightarrow Total number (density) of hydrogen nuclei

Saha-Equation for ionization degree

$$\frac{N_e^2}{(N_H - N_e)} = f(T) = 2.4 \times 10^{15} \text{ cm}^{-3} \left(\frac{T}{\text{K}} \right)^{3/2} e^{-I/kT}$$



George Gamov

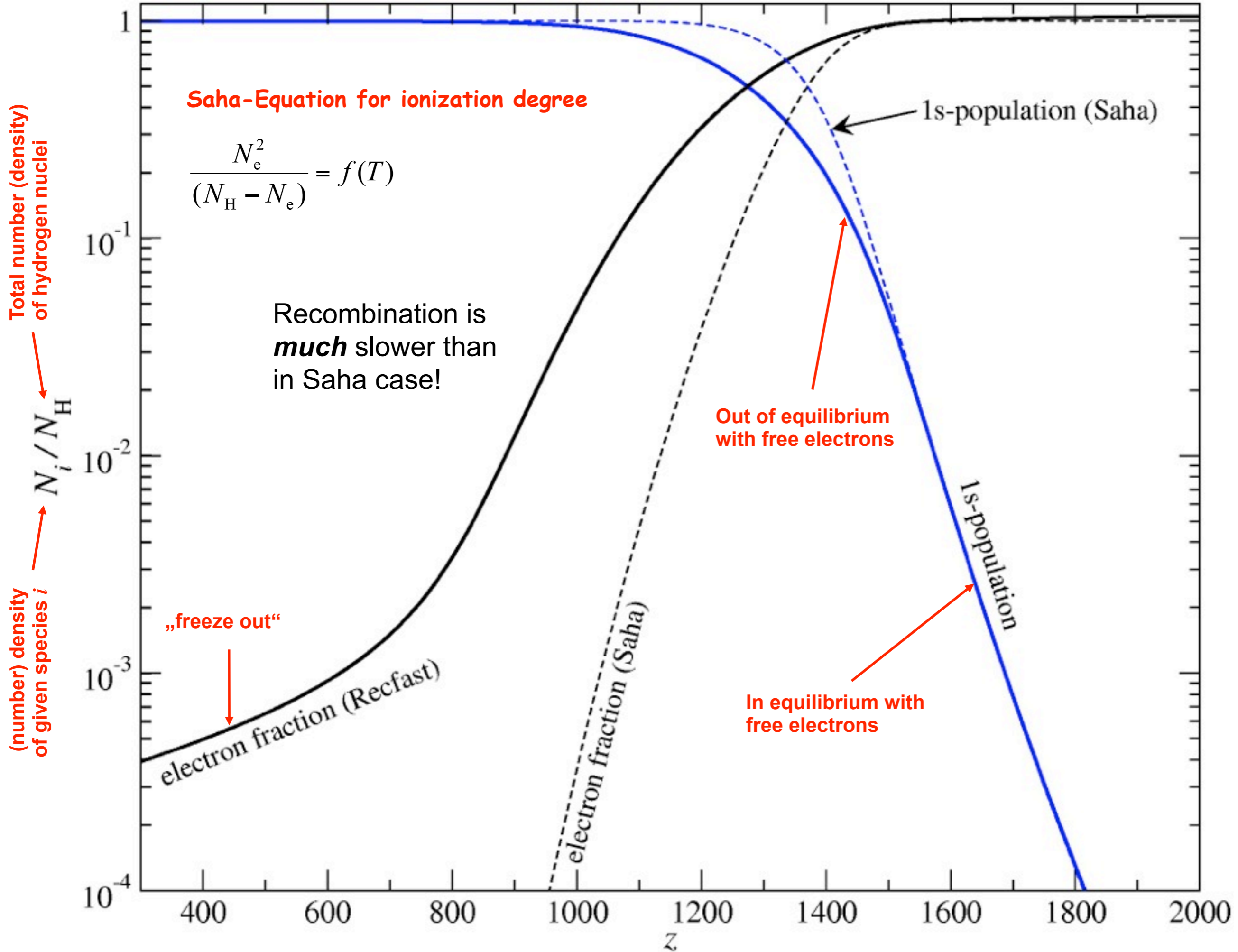


electron fraction (Saha)

In equilibrium with free electrons

1s-population (Saha)

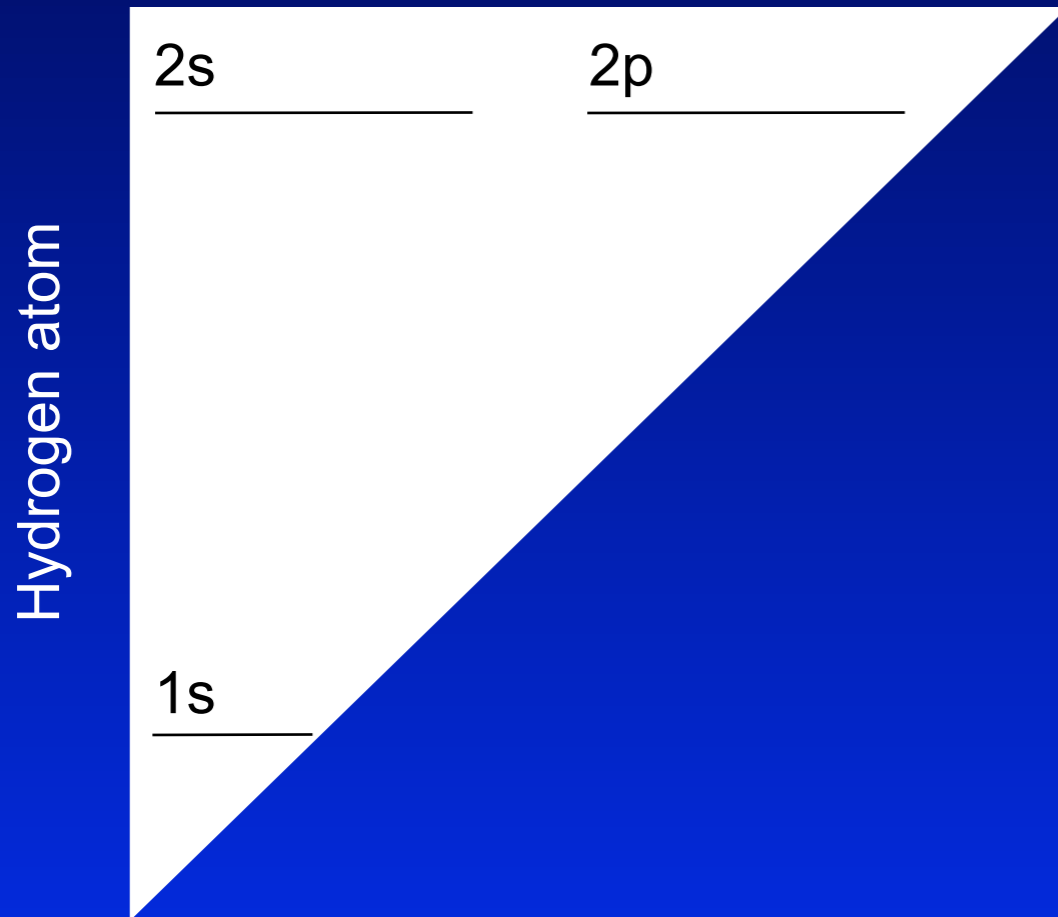
1s-population



3-level Hydrogen Atom and Continuum

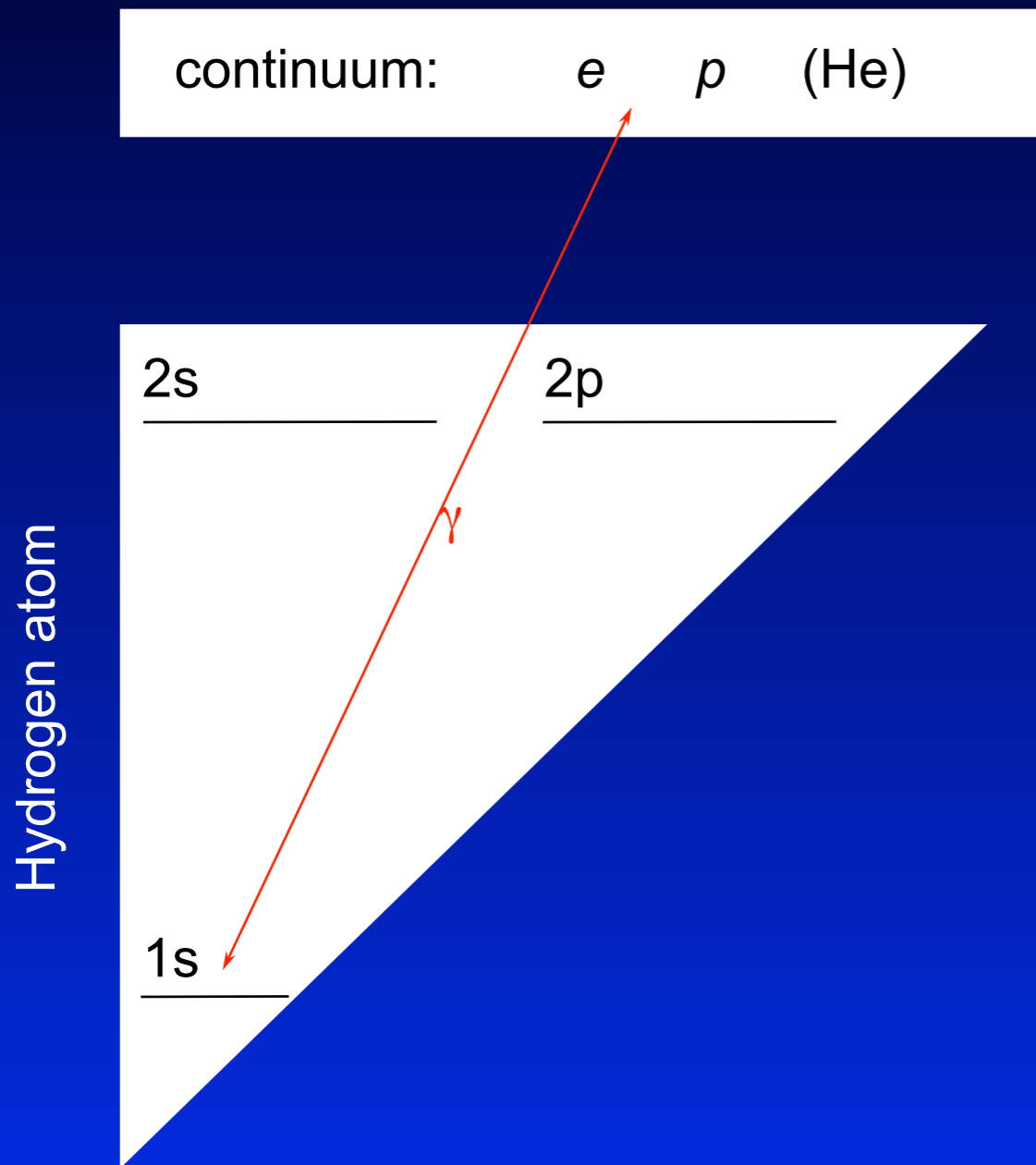
continuum: e p (He)

Routes to the ground state ?



Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278
Peebles, 1968, ApJ, 153, 1

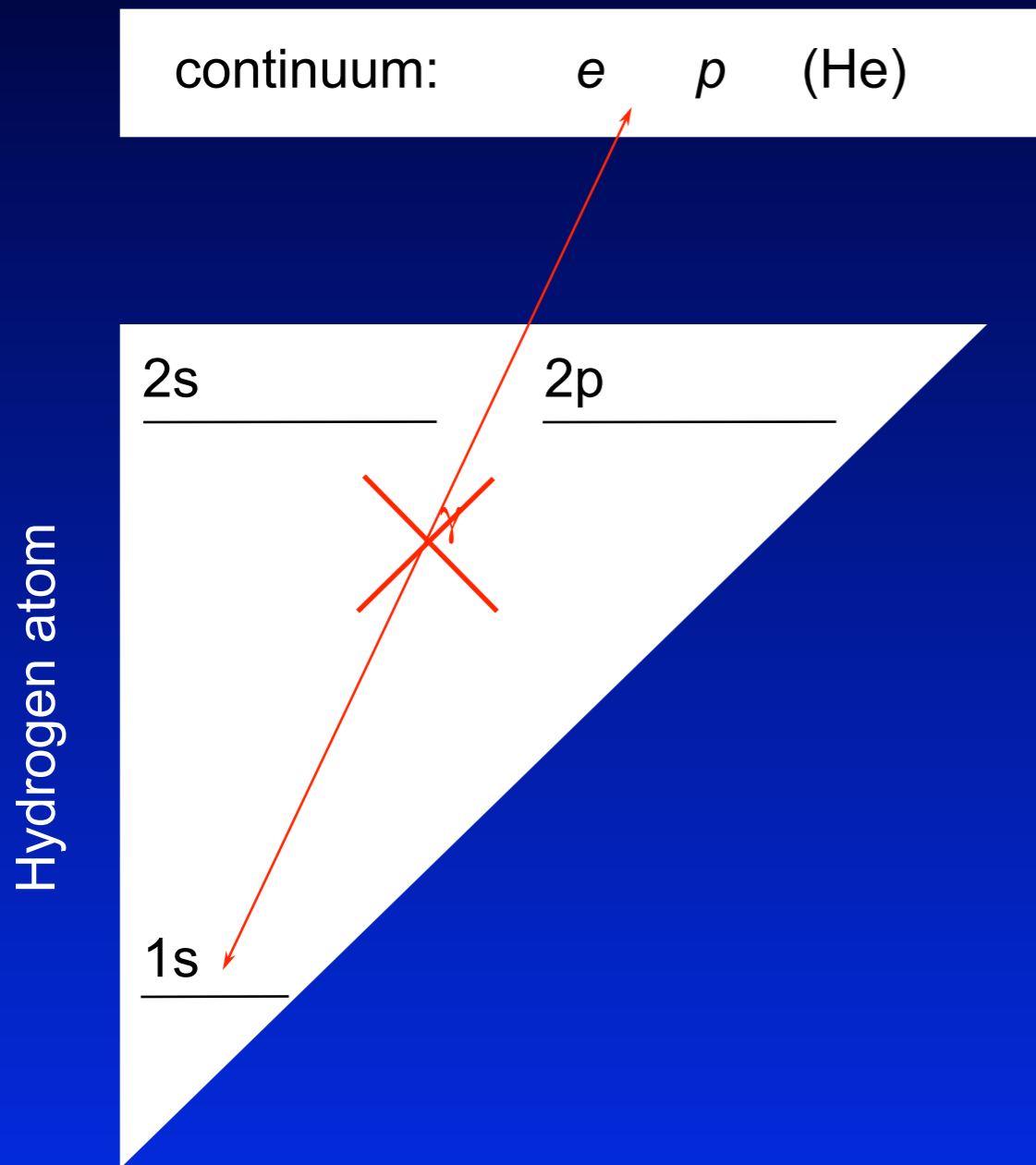
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Routes to the ground state ?

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 - Emission of photon is followed by immediate re-absorption

3-level Hydrogen Atom and Continuum

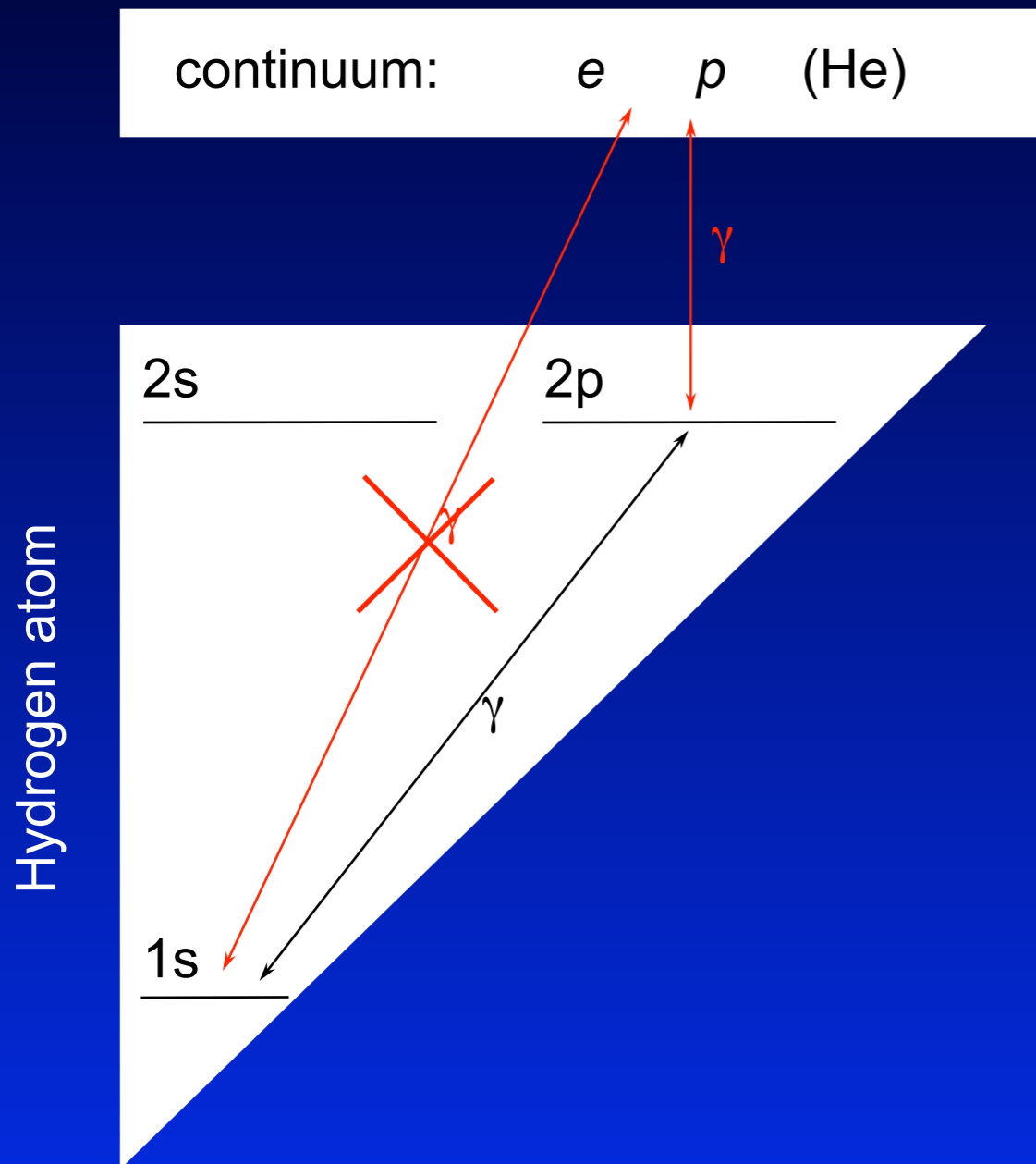


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No

3-level Hydrogen Atom and Continuum

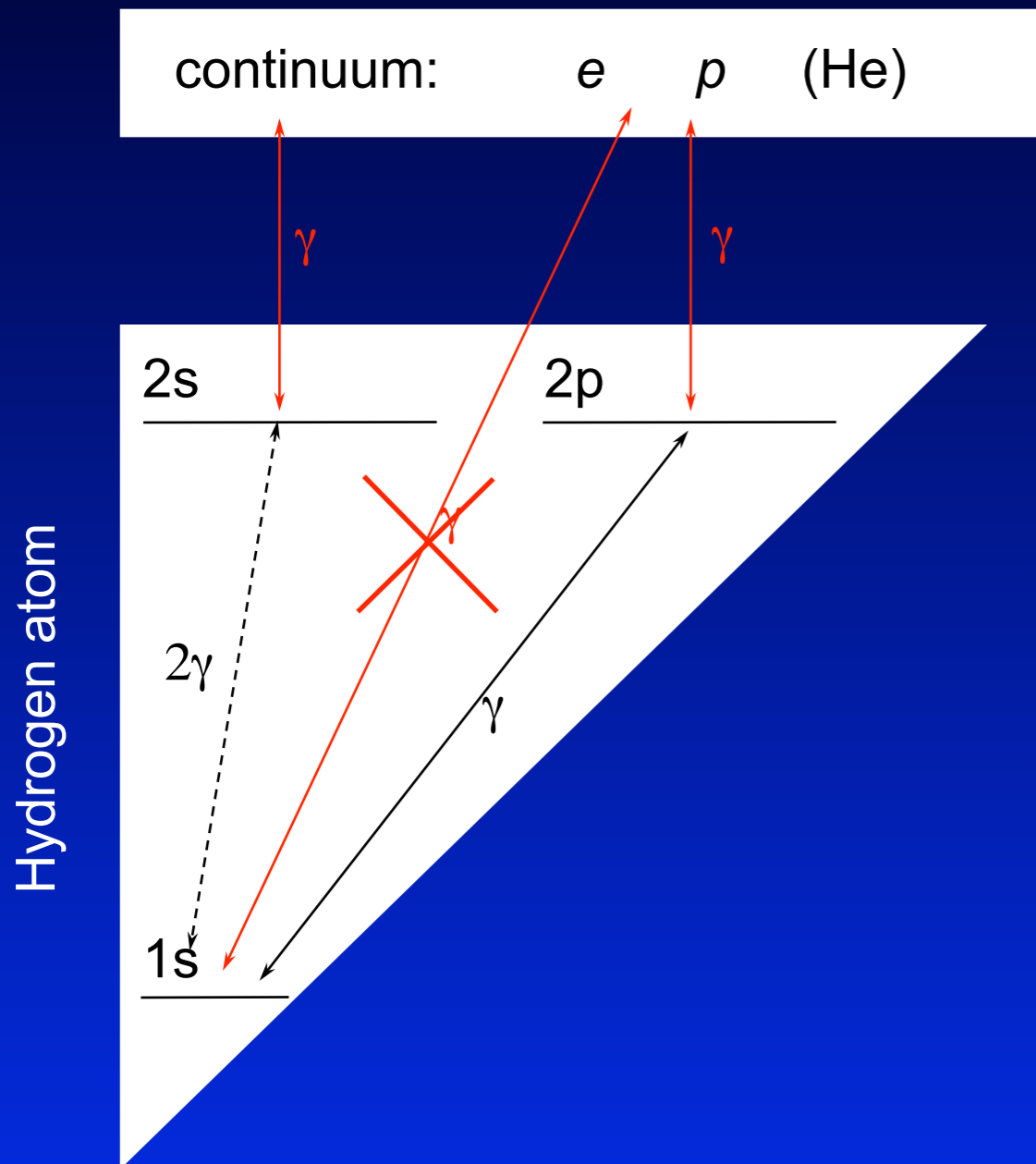


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 - medium optically thick to Ly- α phot.
 - many resonant scatterings
 - escape very hard ($p \sim 10^{-9}$ @ $z \sim 1100$)

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3-level Hydrogen Atom and Continuum

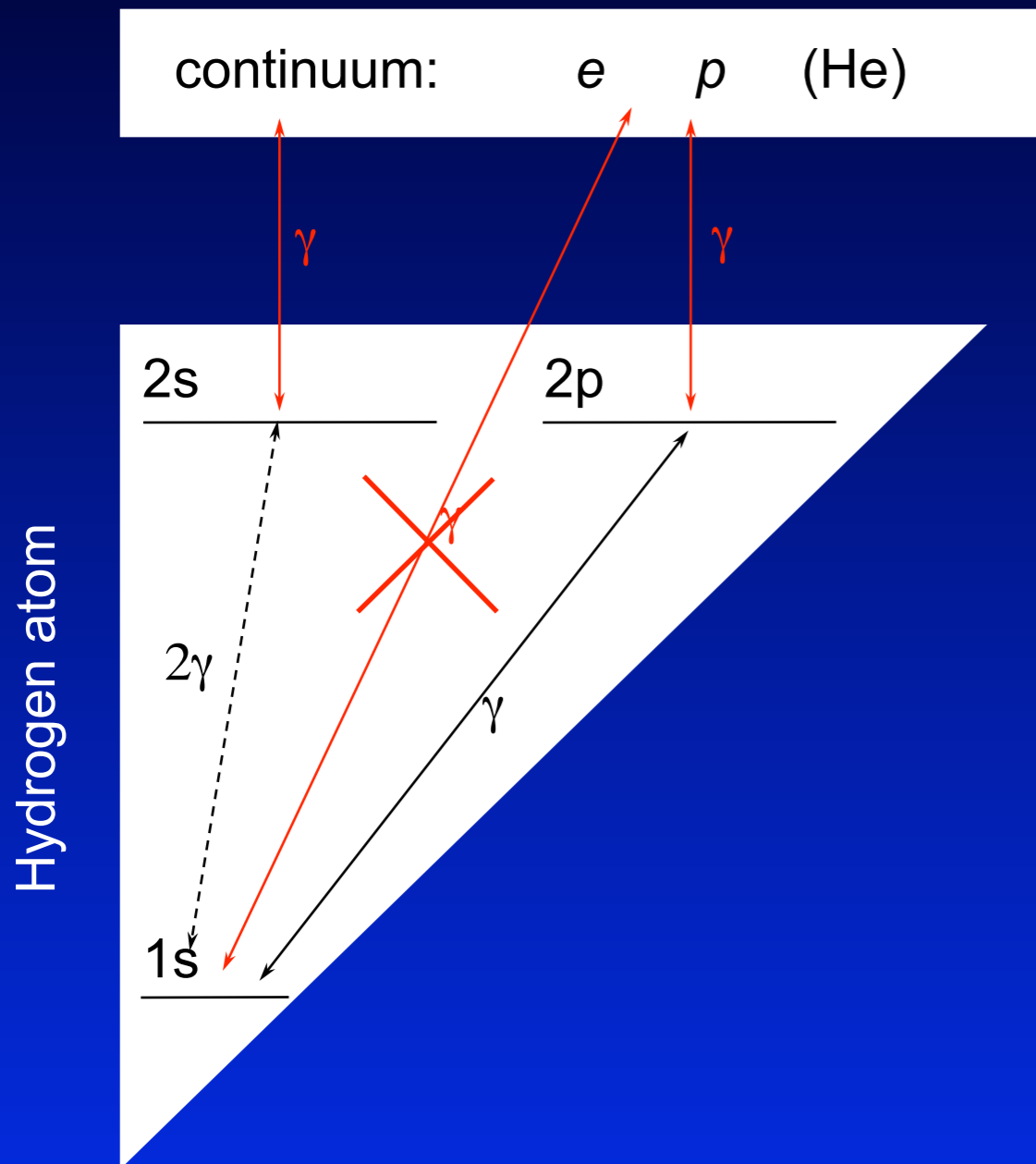


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 - $2s \rightarrow 1s \sim 10^8$ times slower than Ly- α
 - 2s two-photon decay profile \rightarrow maximum at $\nu \sim 1/2 \nu_\alpha$
 - immediate escape

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3-level Hydrogen Atom and Continuum



Routes to the ground state ?

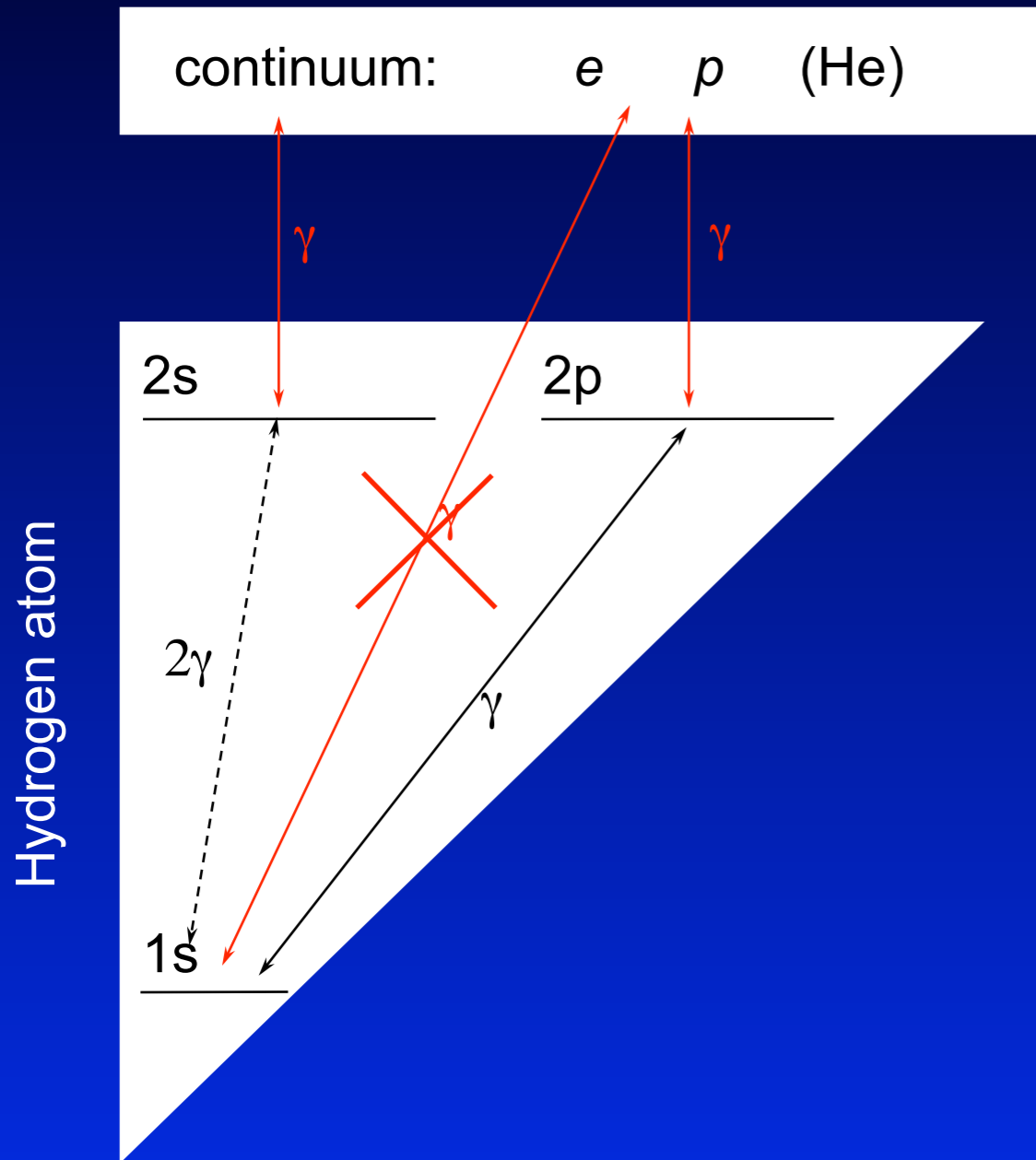
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~ 43%

~ 57%

3-level Hydrogen Atom and Continuum



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- } **~ 43%**
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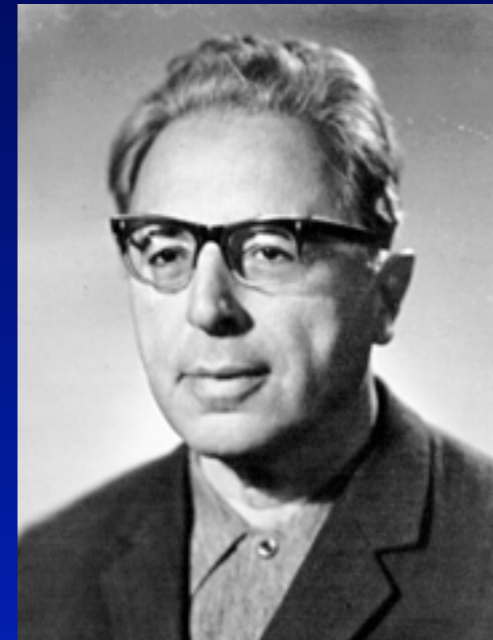
$$\Delta N_e / N_e \sim 10\% - 20\%$$

These first computations were completed in 1968!



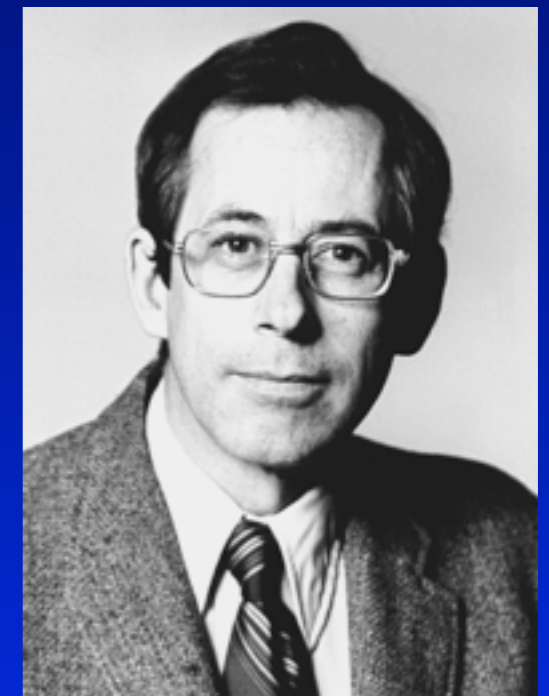
Moscow

Yakov Zeldovich



Iosif Shklovskii

Princeton



Jim Peebles

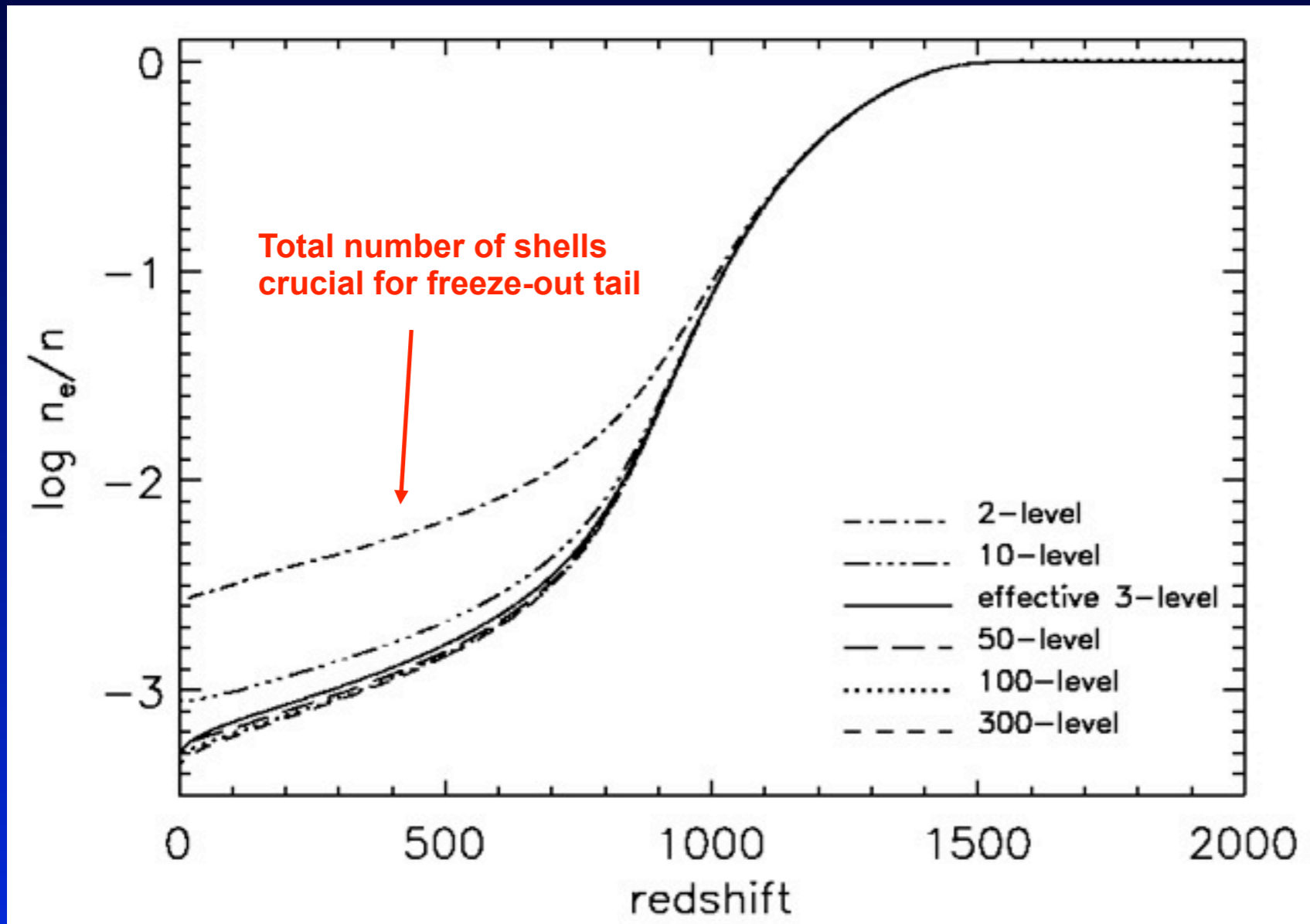


Vladimir Kurt
(UV astronomer)



Rashid Sunyaev

Multi-level Atom \iff Recfast-Code



Output of N_e/N_H

Hydrogen:

- up to 300 levels (shells)
- $n \geq 2 \rightarrow$ full SE for l -sub-states

Helium:

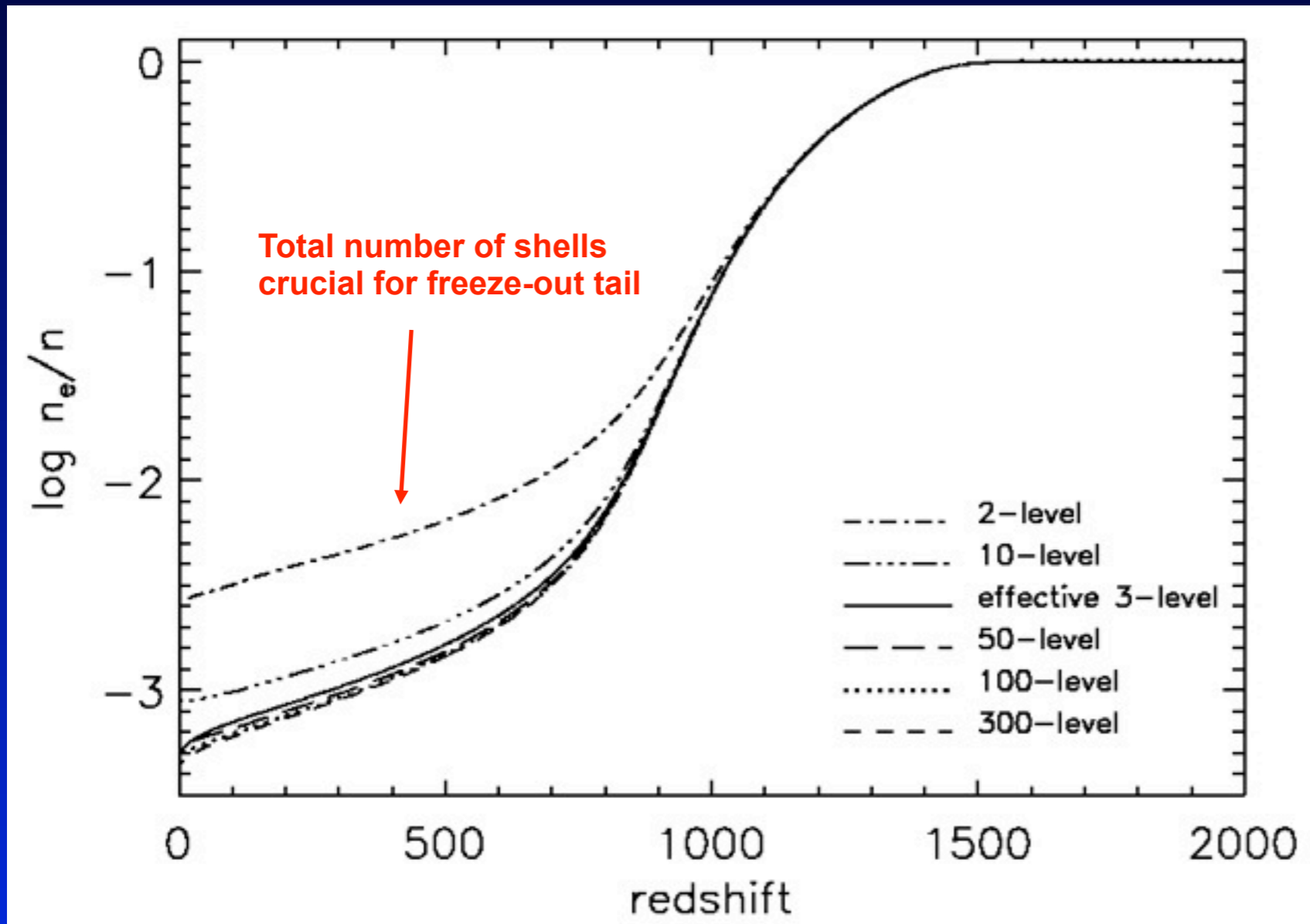
- HeI 200-levels ($z \sim 1400-1500$)
- HeII 100-levels ($z \sim 6000-6500$)
- HeIII 1 equation

Low Redshifts:

- H chemistry (only at low z)
- cooling of matter (Bremsstrahlung, collisional cooling, line cooling)

Seager, Sasselov & Scott, 1999, ApJL, 523, L1
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Seager, Sasselov & Scott, 2000, ApJS, 128, 407

$$\Delta N_e / N_e \sim 1\% - 3\%$$

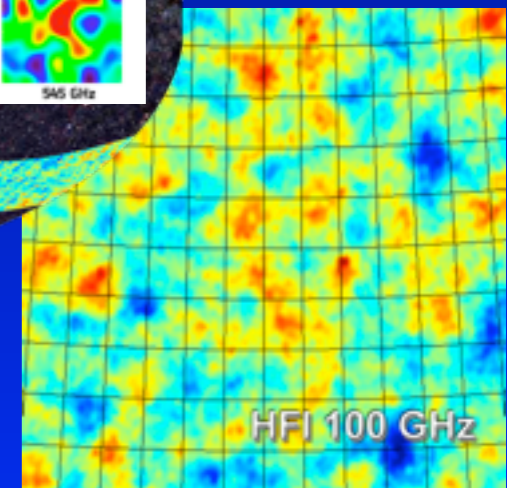
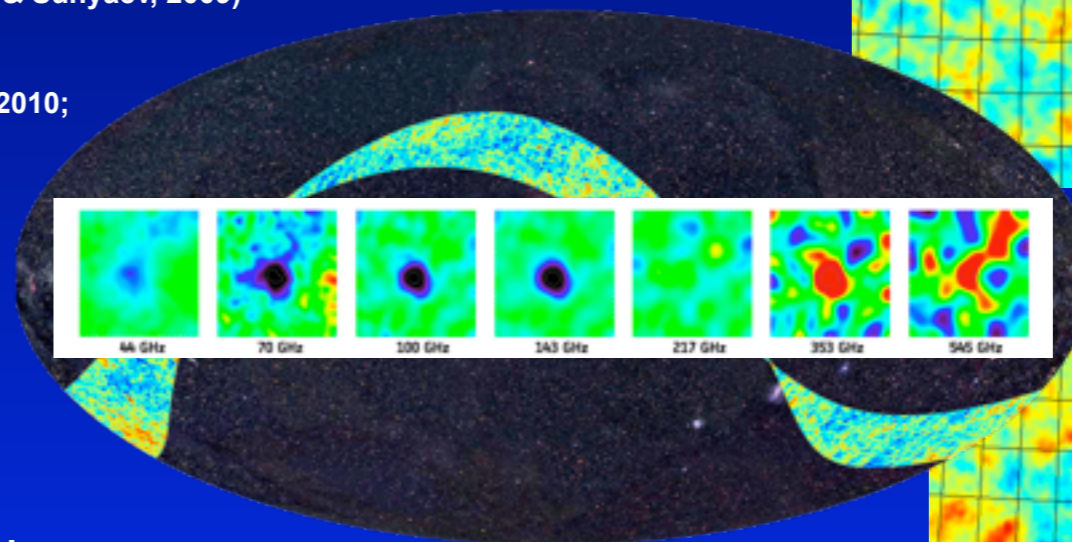
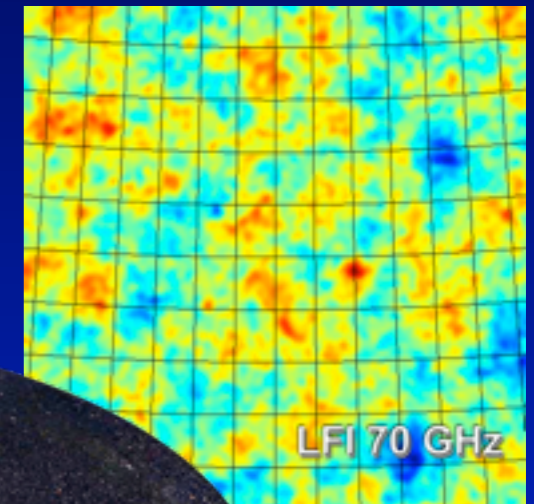
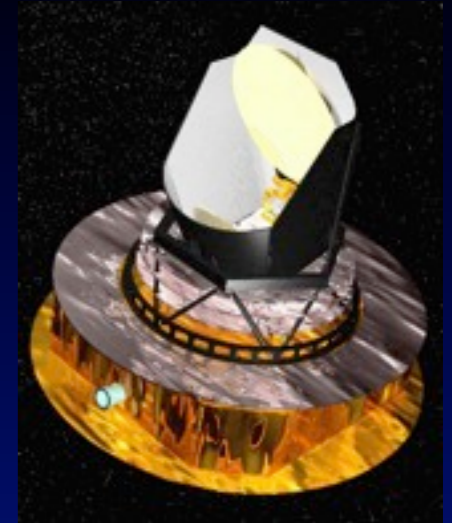
Getting the job done for Planck

Hydrogen recombination

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Helium recombination

- Similar list of processes as for hydrogen
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$$\Delta N_e / N_e \sim 0.1 \%$$

Solving the problem for the Planck Collaboration was a common effort!

Recombination Physics Meeting in Orsay 2008

see: <http://www.b-pol.org/RecombinationConference/>



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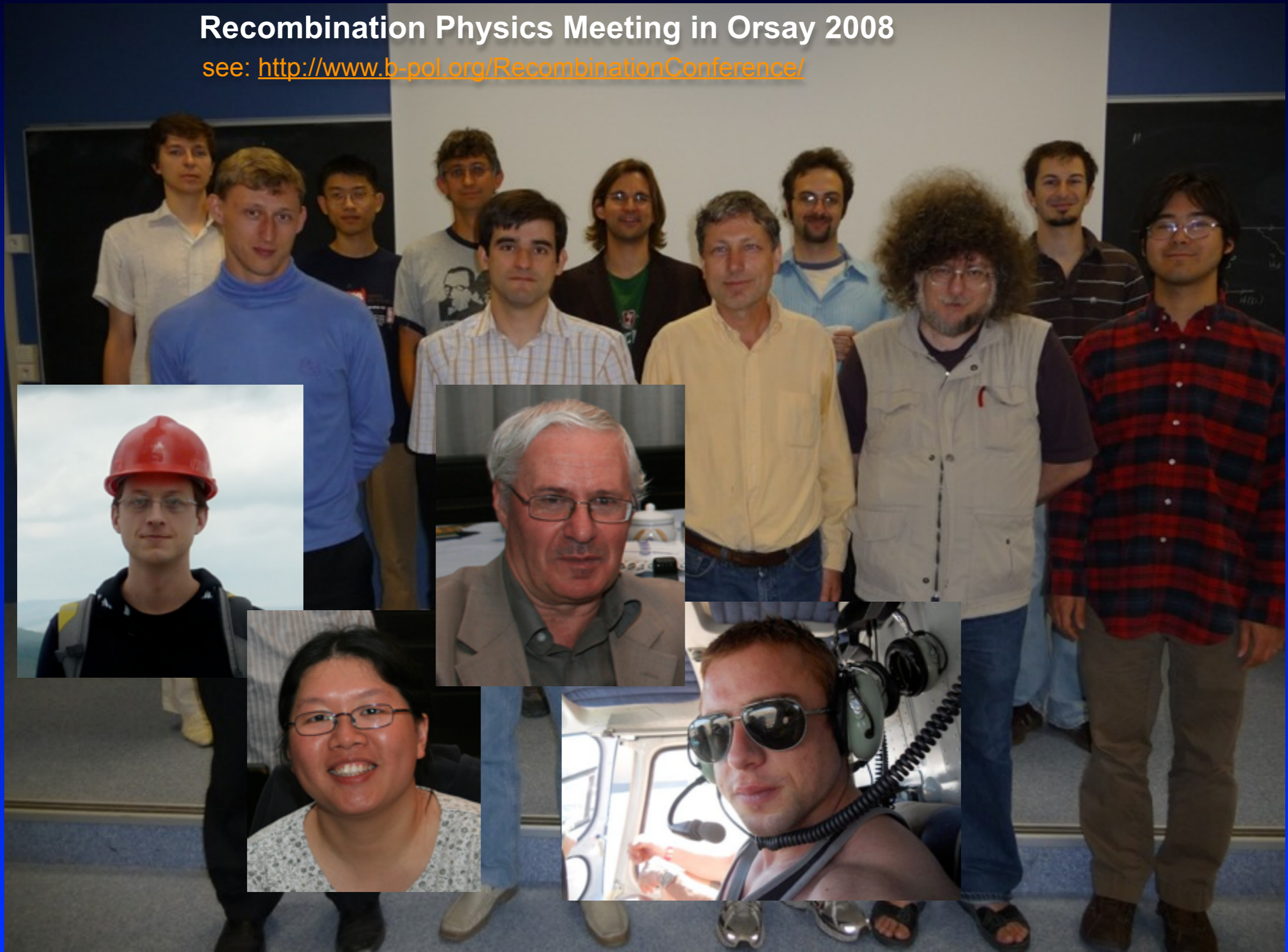
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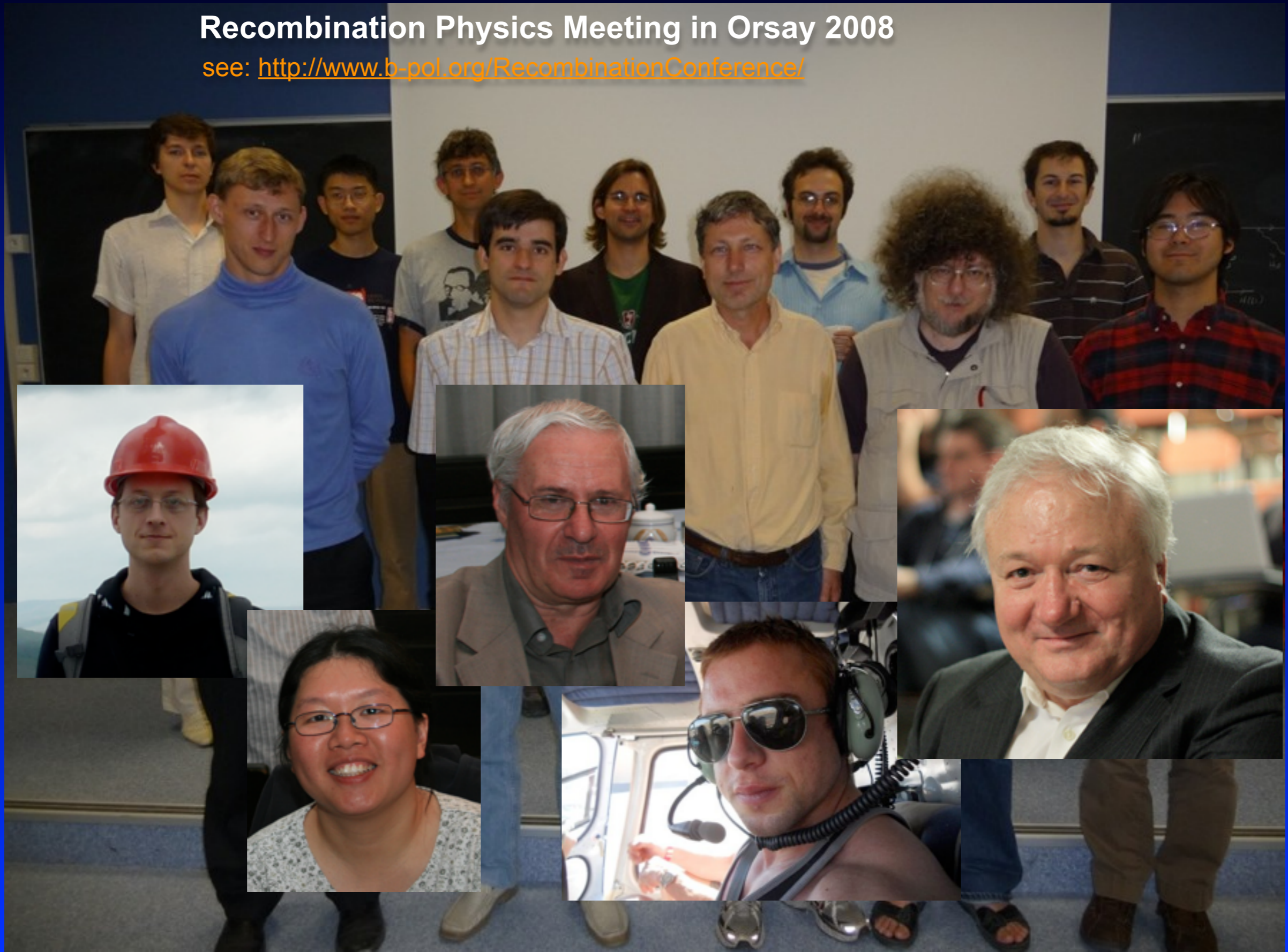
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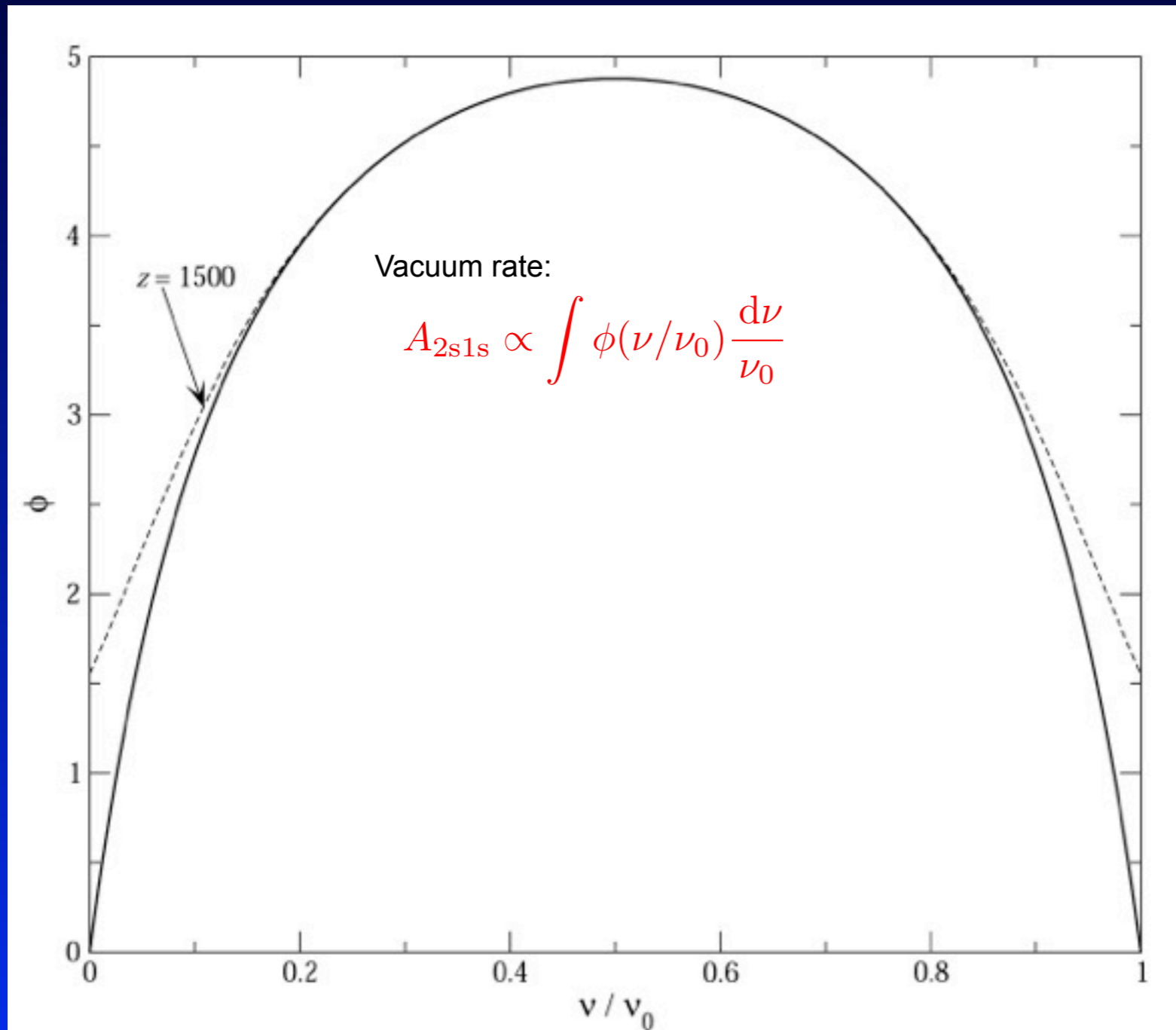
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Simple example: stimulated 2s \rightarrow 1s decay



2s-1s emission profile

Transition rate in vacuum

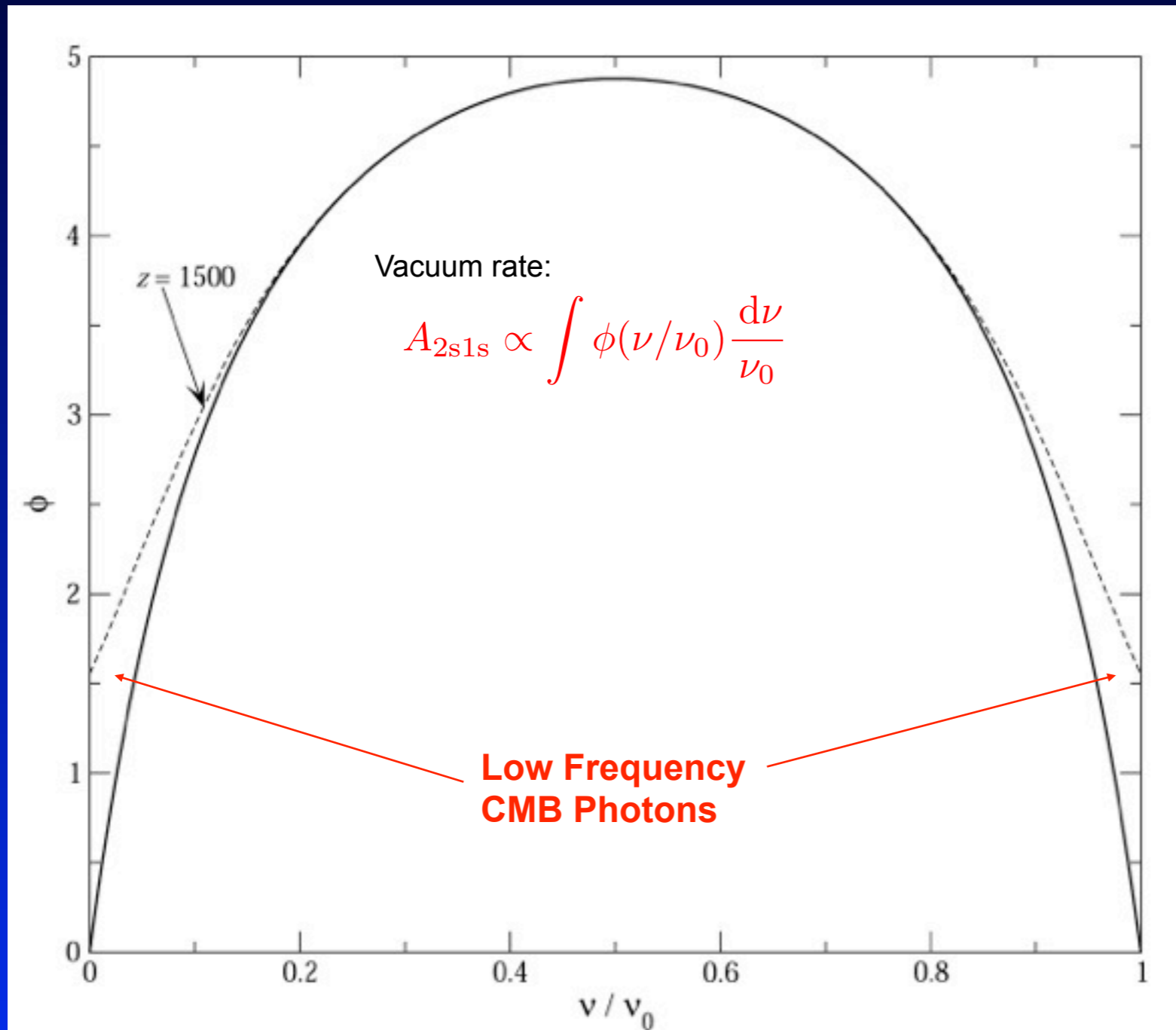
$$\rightarrow A_{2s1s} \sim 8.22 \text{ sec}^{-1}$$

CMB ambient photons field

$$\rightarrow A_{2s1s} \text{ increased by } \sim 1\%-2\%$$

\rightarrow HI - recombination faster
by $\Delta N_e/N_e \sim 1.3\%$

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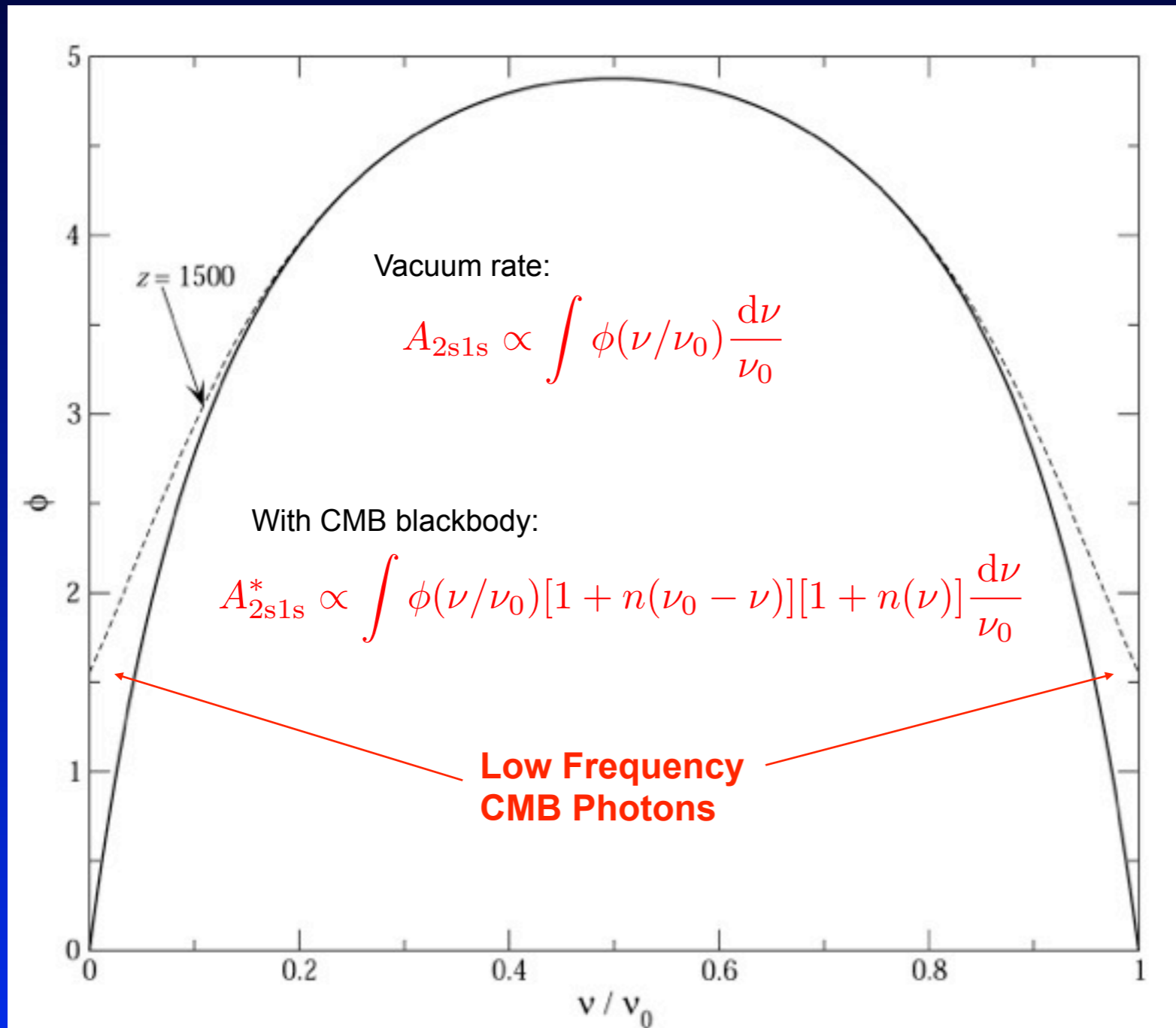
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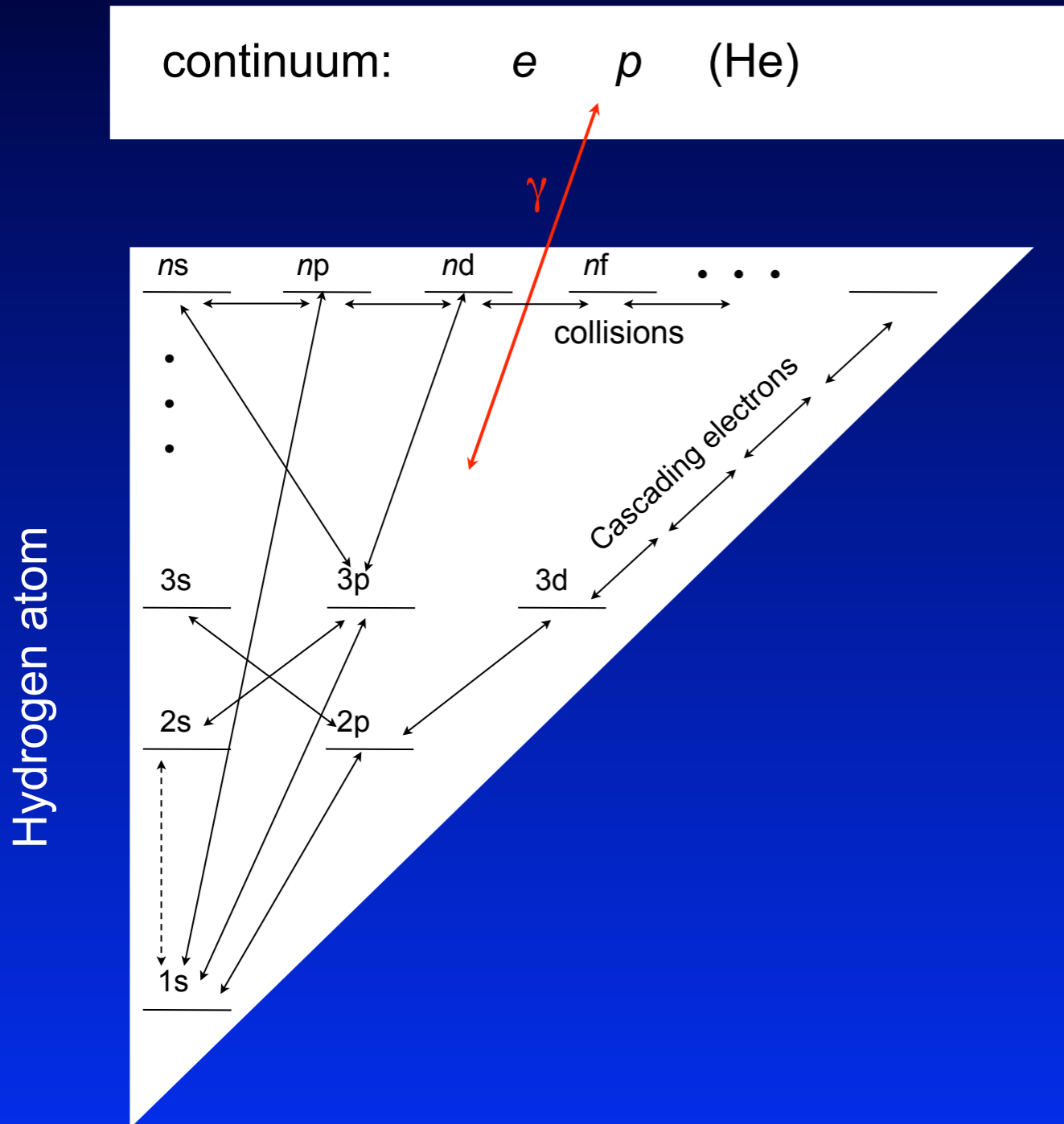
→ $A_{2s1s} \sim 8.22 \text{ sec}^{-1}$

CMB ambient photons field

→ A_{2s1s} increased by ~1%-2%

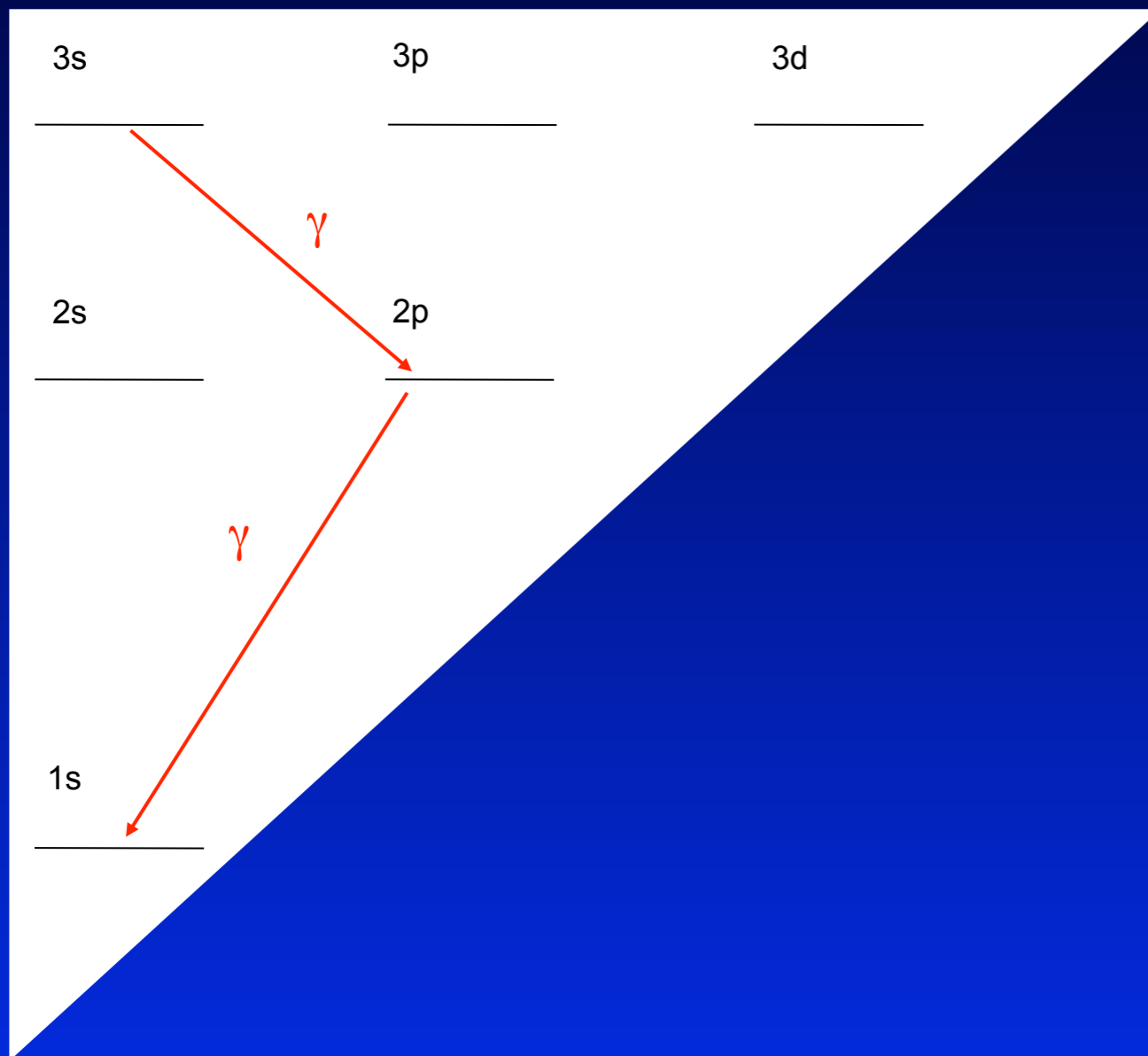
→ HI - recombination faster
 by $\Delta N_e/N_e \sim 1.3\%$

Processes for the upper levels



- **recombination & photoionization**
 - n small \rightarrow l -dependence not drastic
 - high shells \rightarrow more likely to $l \ll n$
 - large $n \rightarrow$ *induced* recombination
 - **many radiative dipole transitions**
 - Lyman-series optically thick
 - $\Delta l = \pm 1$ restriction (electron cascade)
 - large n & small $\Delta n \rightarrow$ *induced* emission
 - **l -changing collisions**
 - help to establish full SE within the shell
 - only effective for $n > 25-30$
- **n -changing collisions**
 - **Collisional photoionization**
 - **Three-body-recombination**

Two-photon emission profile



Seaton cascade (1+1 photon)

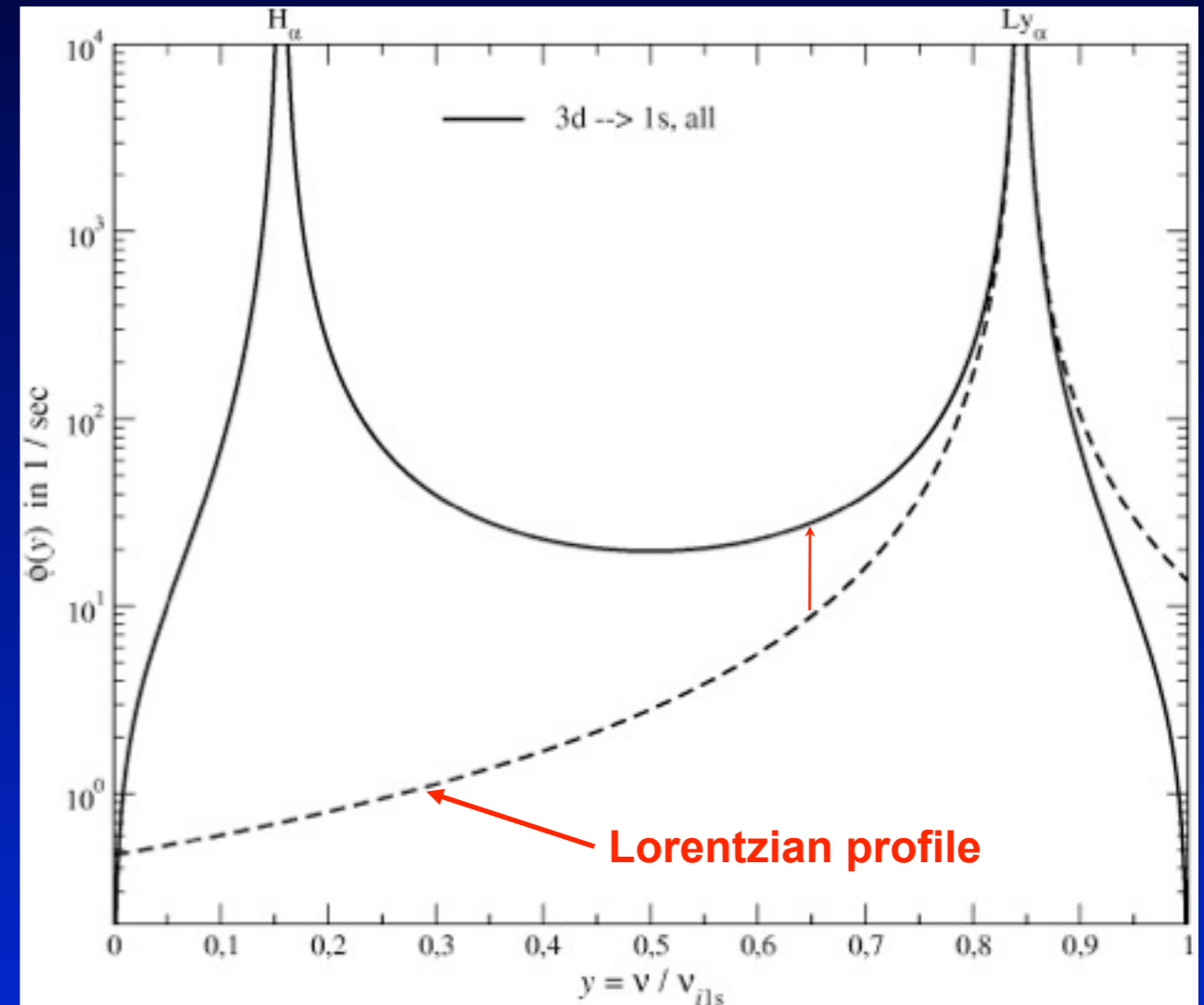
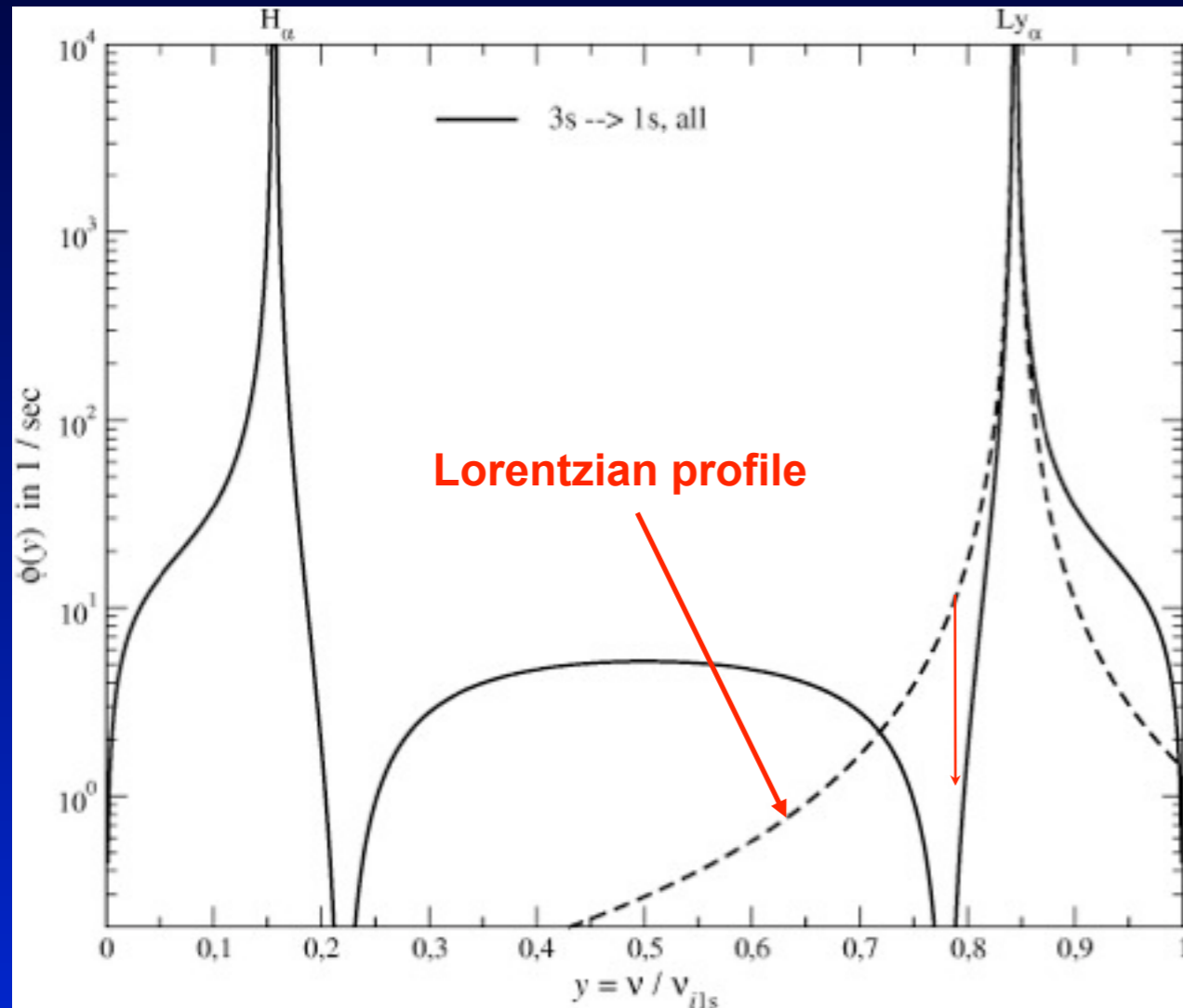
No collisions \rightarrow two photons (mainly H- α and Ly- α) are emitted!

Maria-Göppert-Mayer (1931): description of two-photon emission as single process in Quantum Mechanics

\rightarrow Deviations of the *two-photon line profile* from the Lorentzian in the damping wings

\rightarrow Changes in the optically thin (below ~ 500 - 5000 Doppler width) parts of the line spectra

3s and 3d two-photon decay spectrum

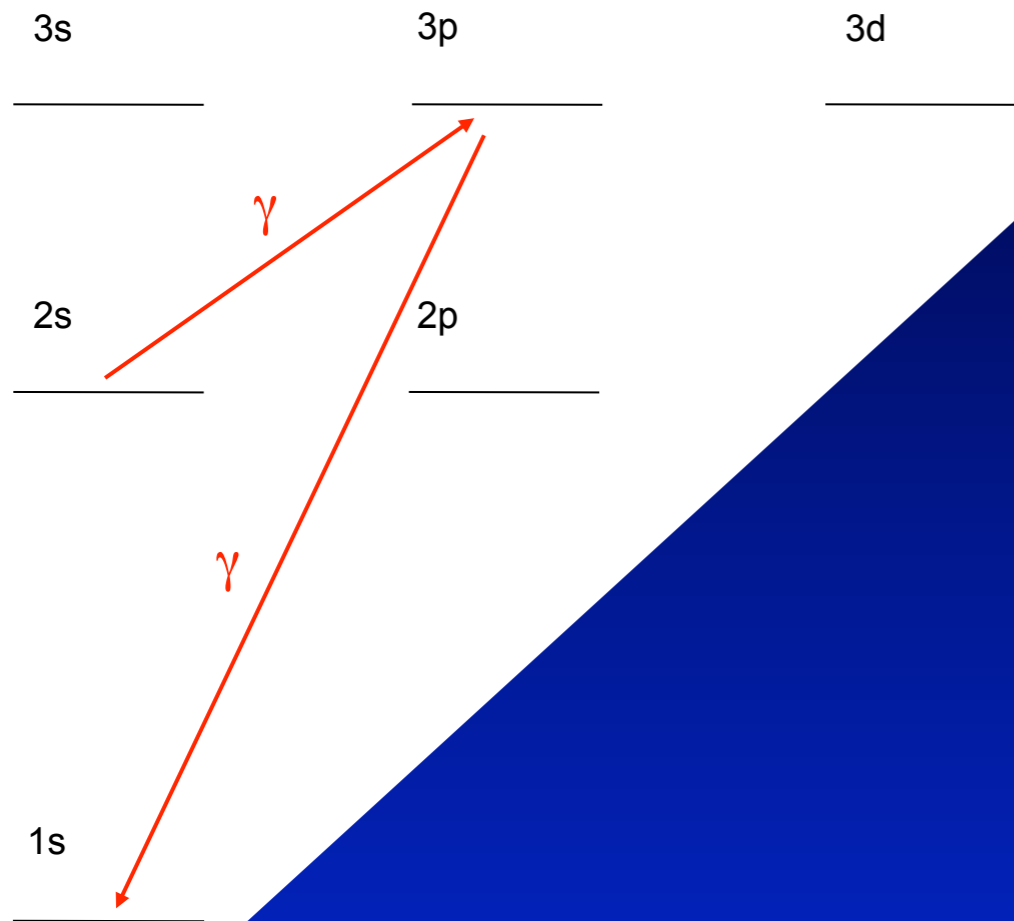


Direct Escape in optically thin regions:

→ HI -recombination is a bit *slower* due to 2γ -transitions from s-states

→ HI -recombination is a bit *faster* due to 2γ -transitions from d-states

2s-1s Raman scattering



- Enhances blues side of Ly- α line
- associated feedback delays recombination around $z \sim 900$

- Computation similar to two-photon decay profiles
- collisions weak \implies process needs to be modeled as single quantum act

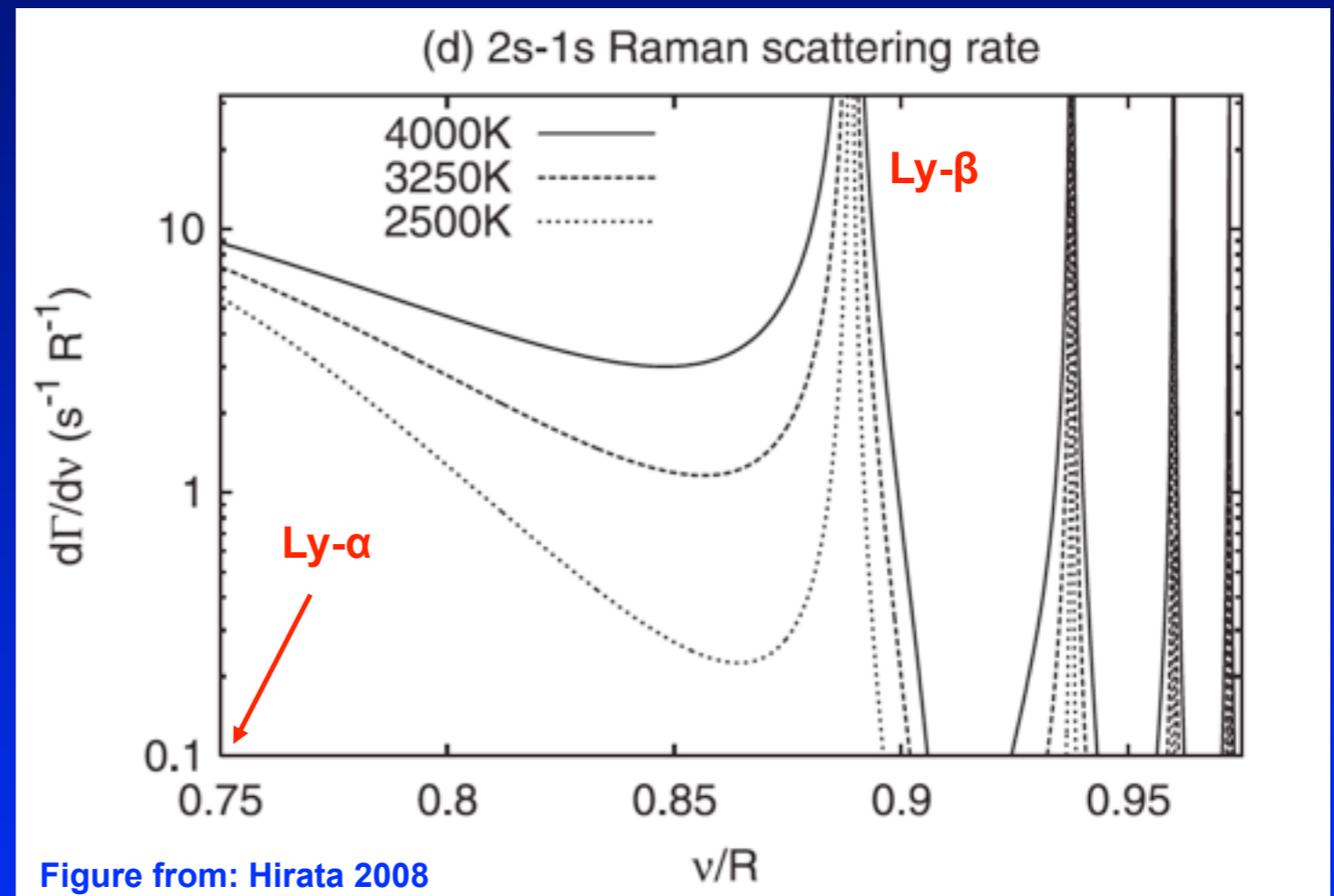
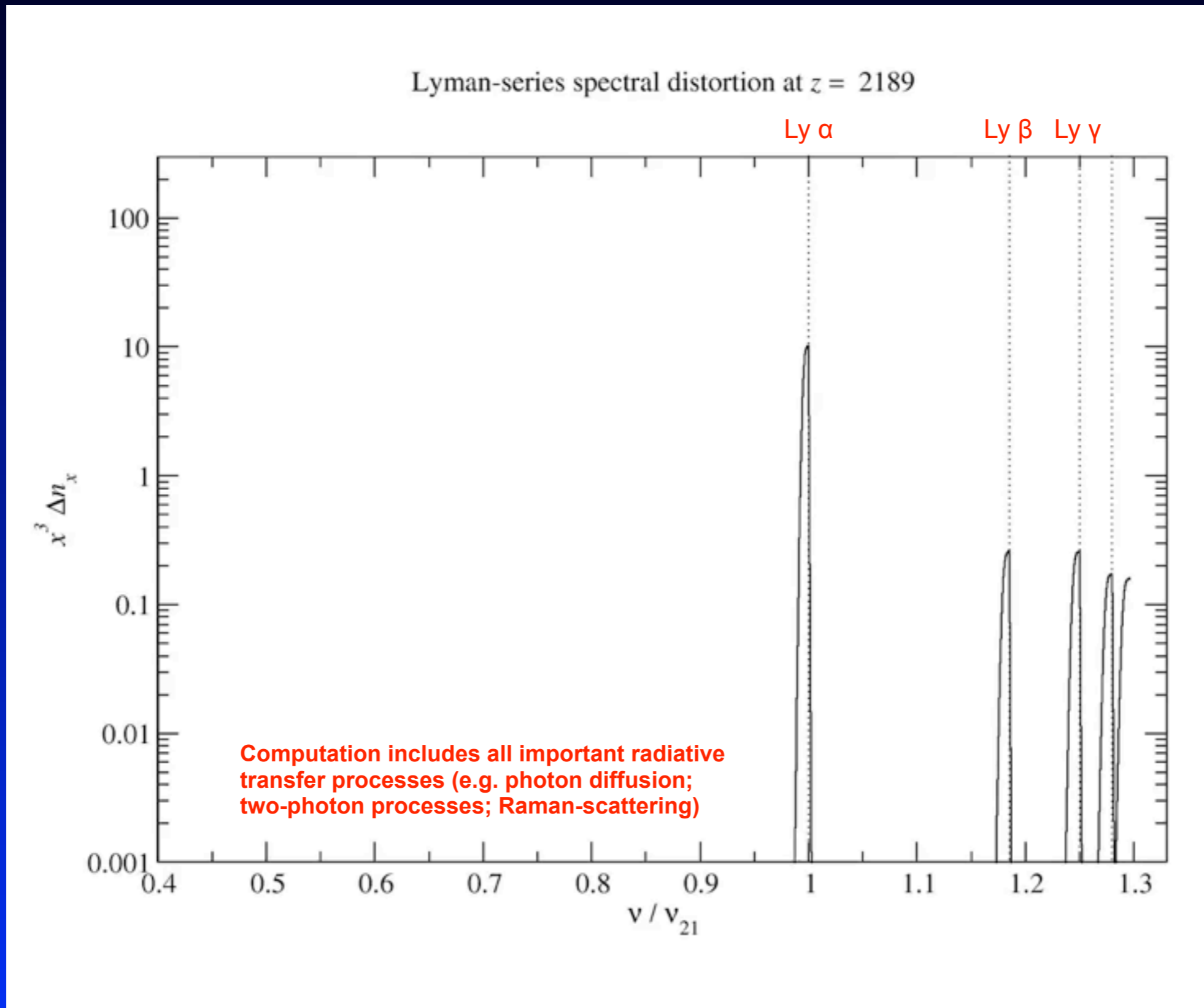
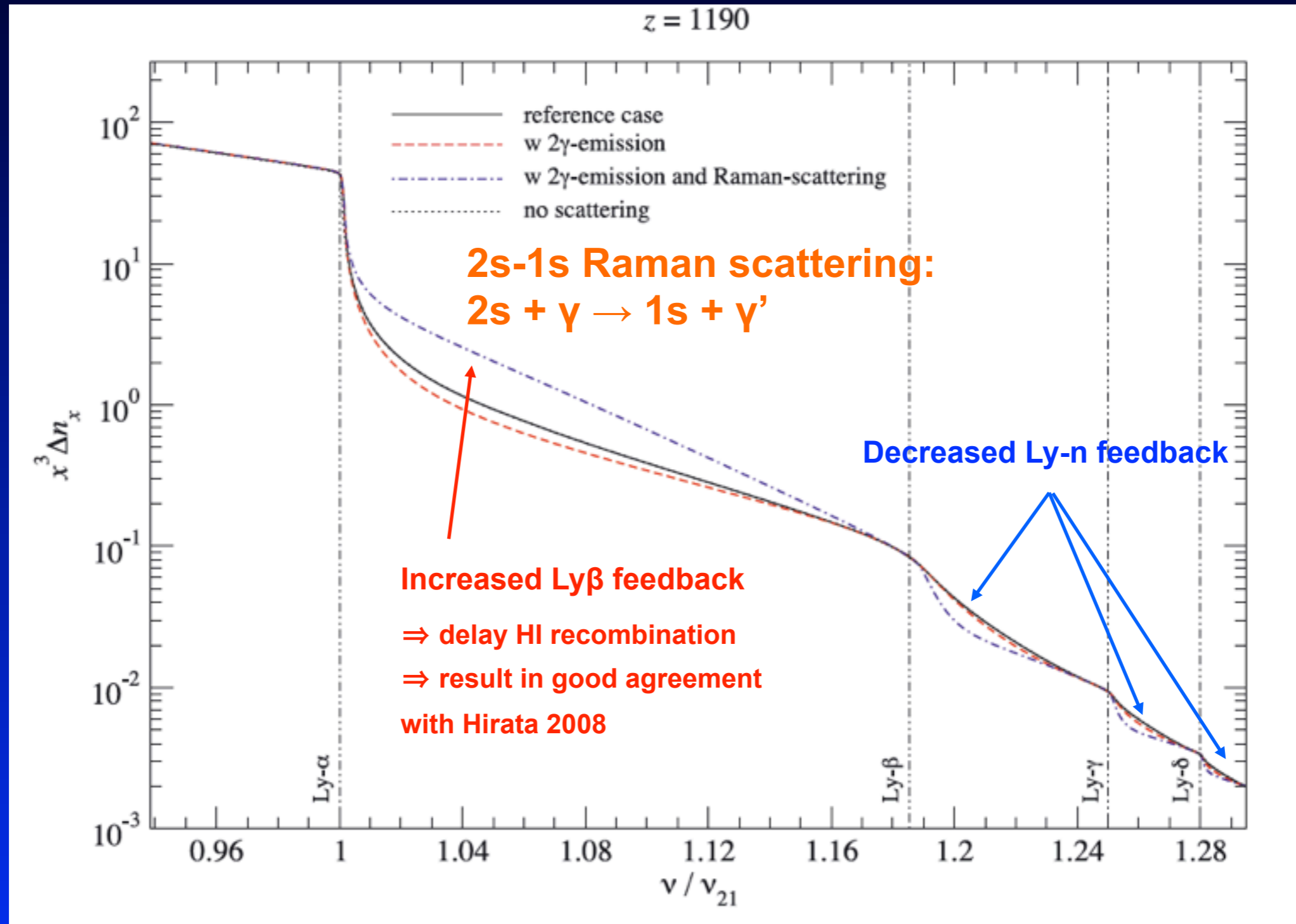


Figure from: Hirata 2008

Evolution of the HI Lyman-series distortion



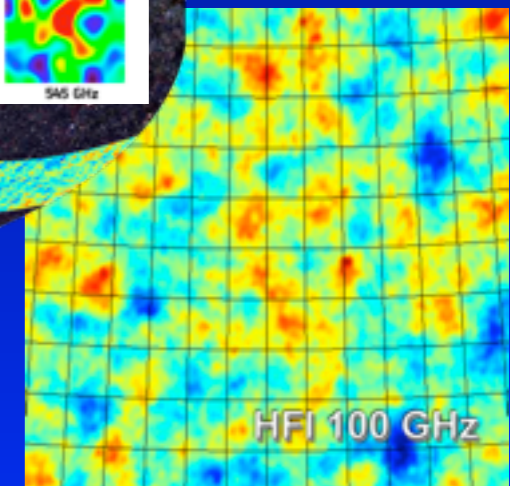
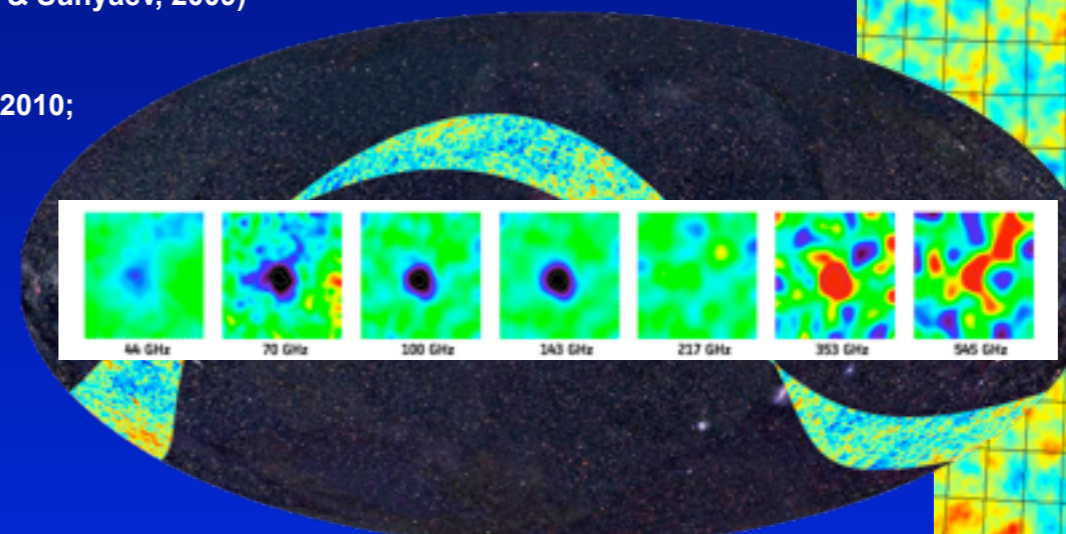
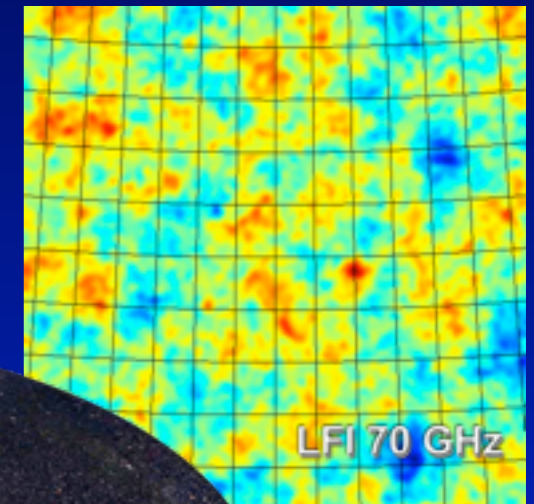
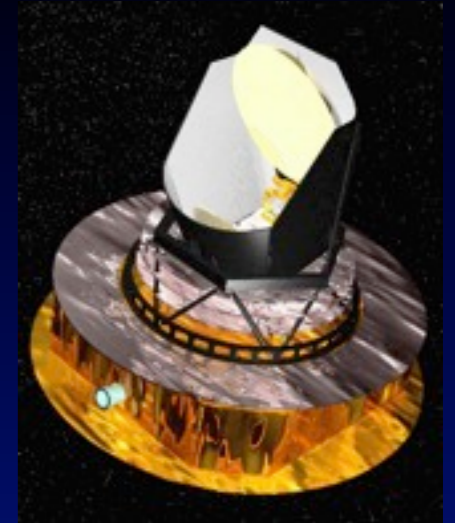
Effect of Raman scattering and 2γ decays



Getting Ready for Planck

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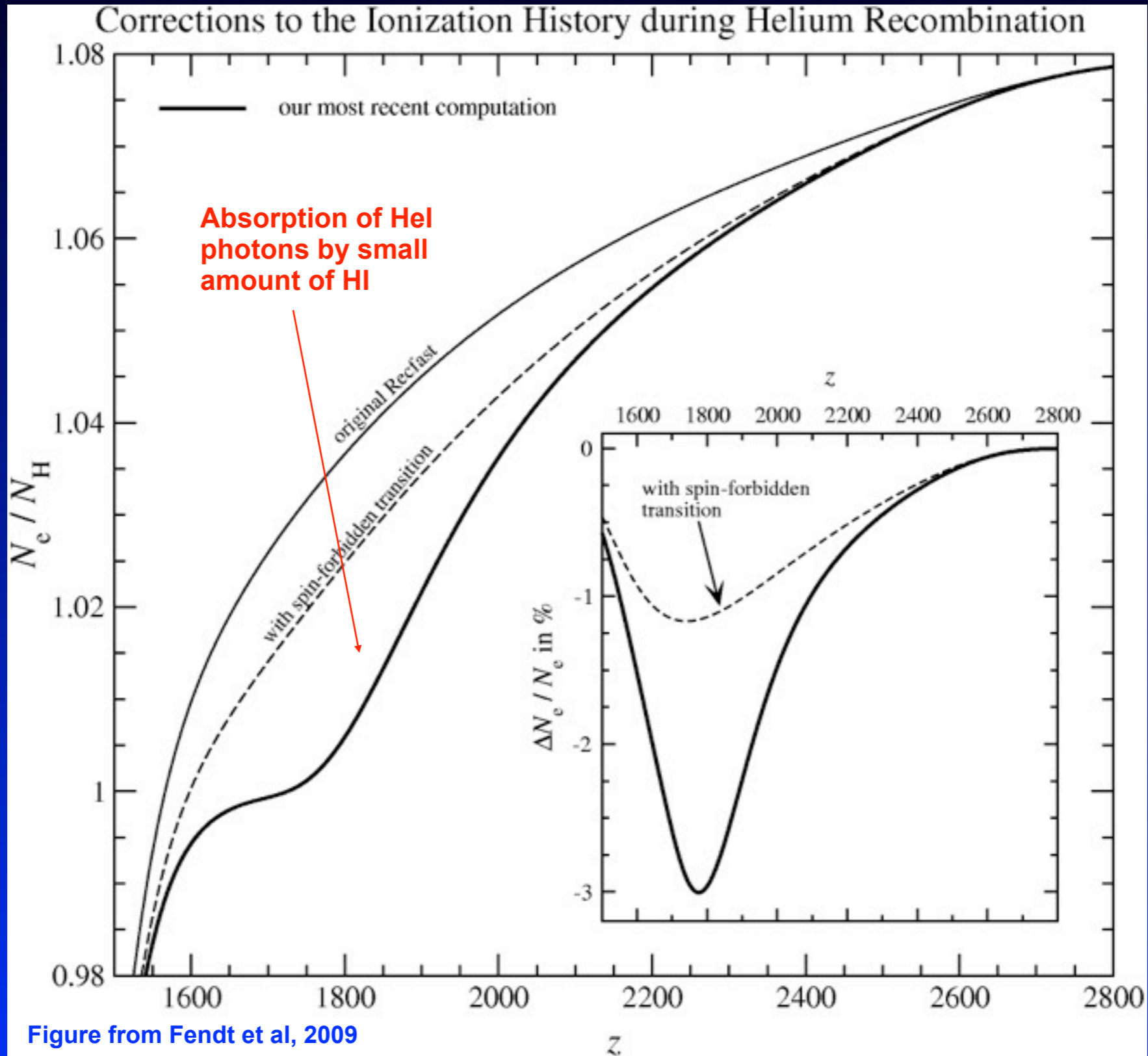


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$$\Delta N_e / N_e \sim 0.1 \%$$

Main corrections during HeI Recombination

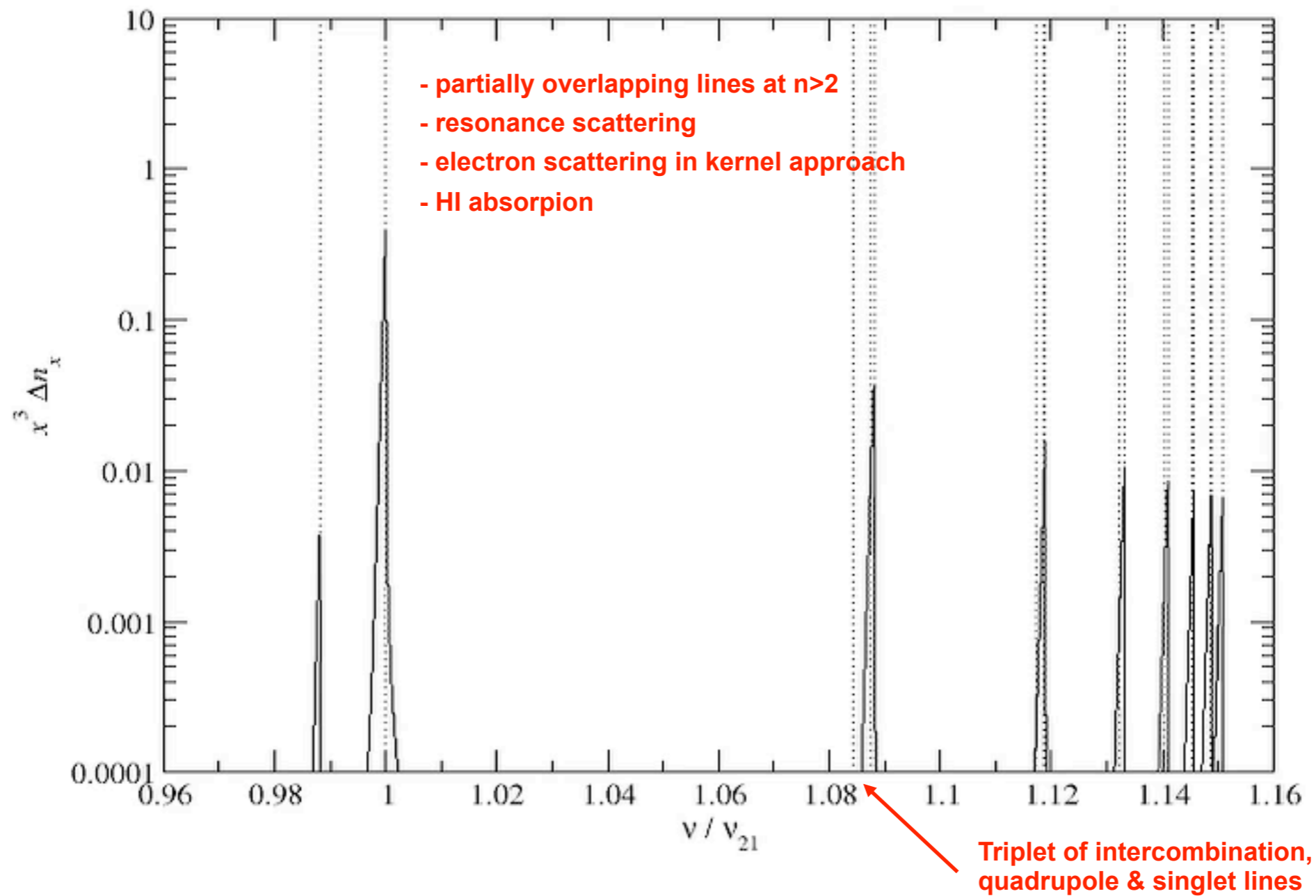


Kholupenko et al, 2007
Switzer & Hirata, 2007

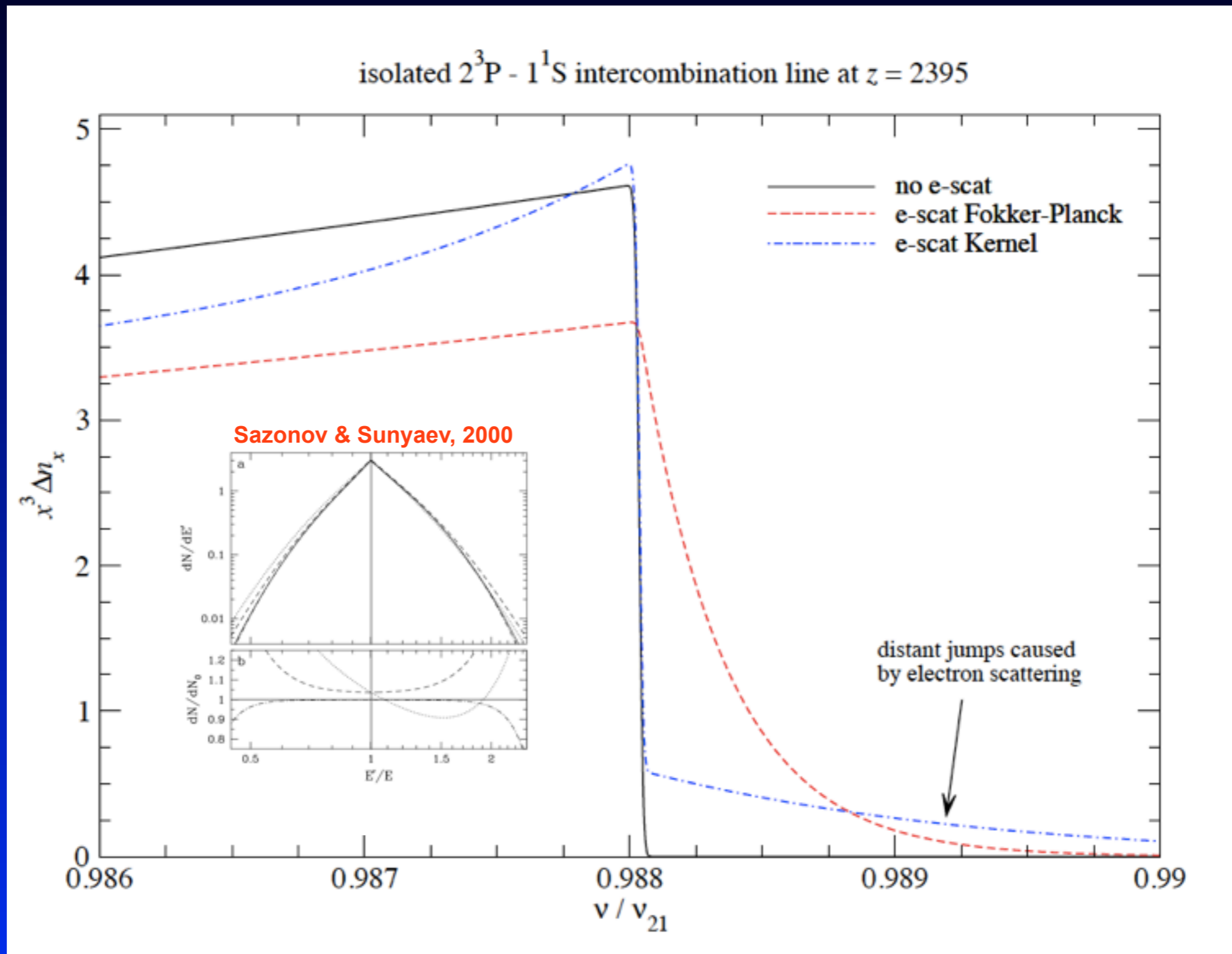
Evolution of the HeI high frequency distortion

CosmoRec v2.0 only!

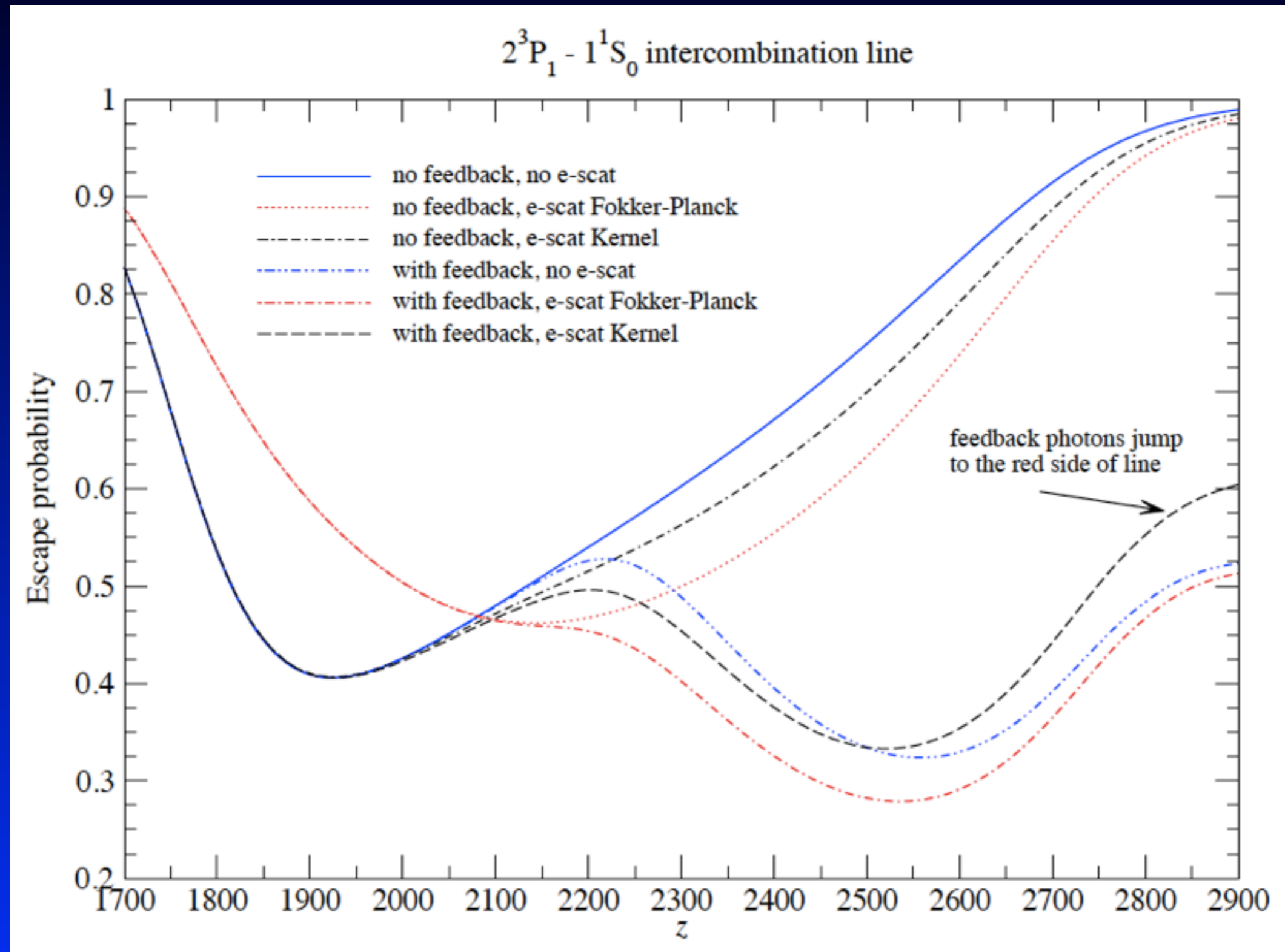
HeI Lyman-series spectral distortion at $z = 2996$



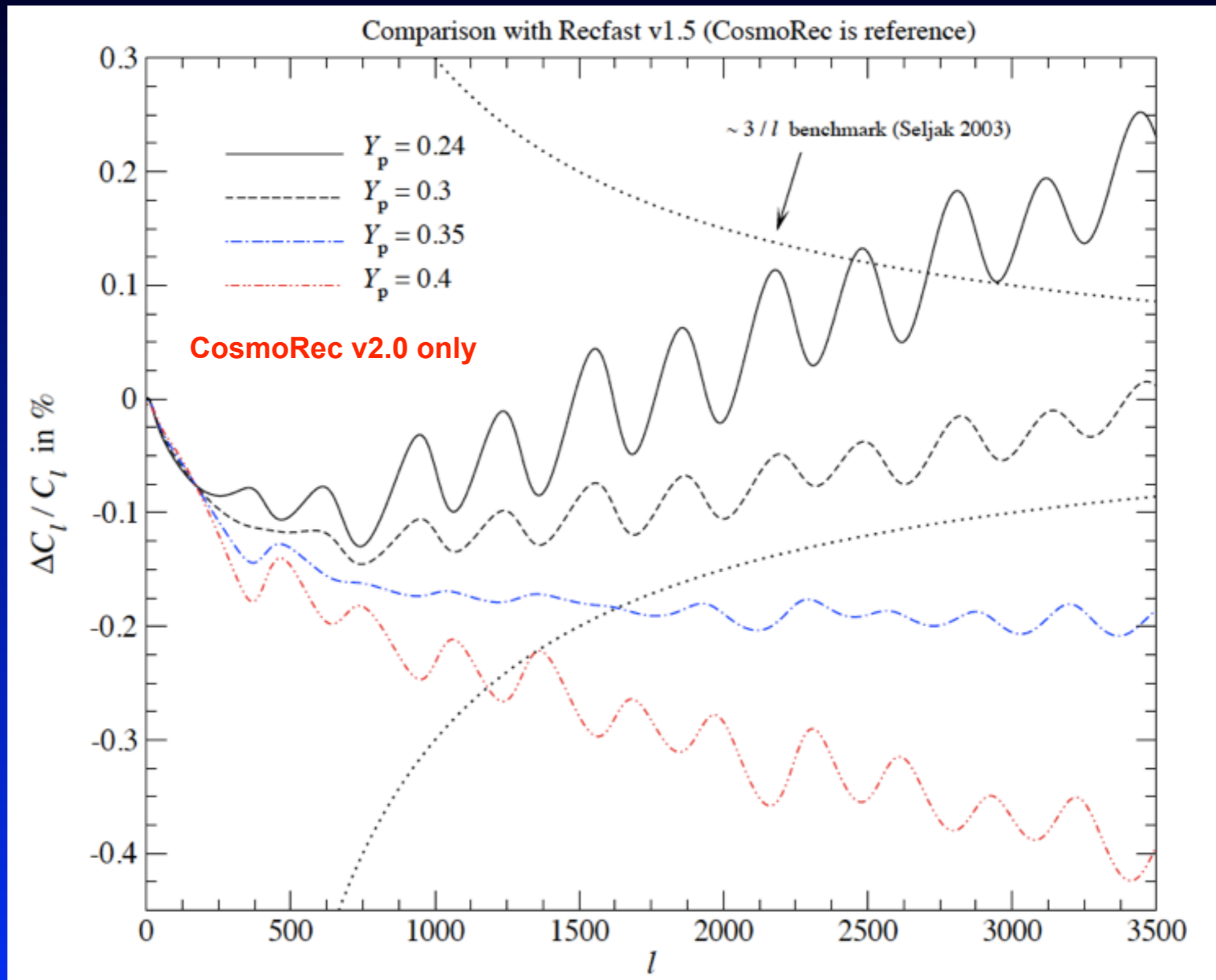
Effect of electron scattering during HeI recombination



Effect of electron scattering during HeI recombination



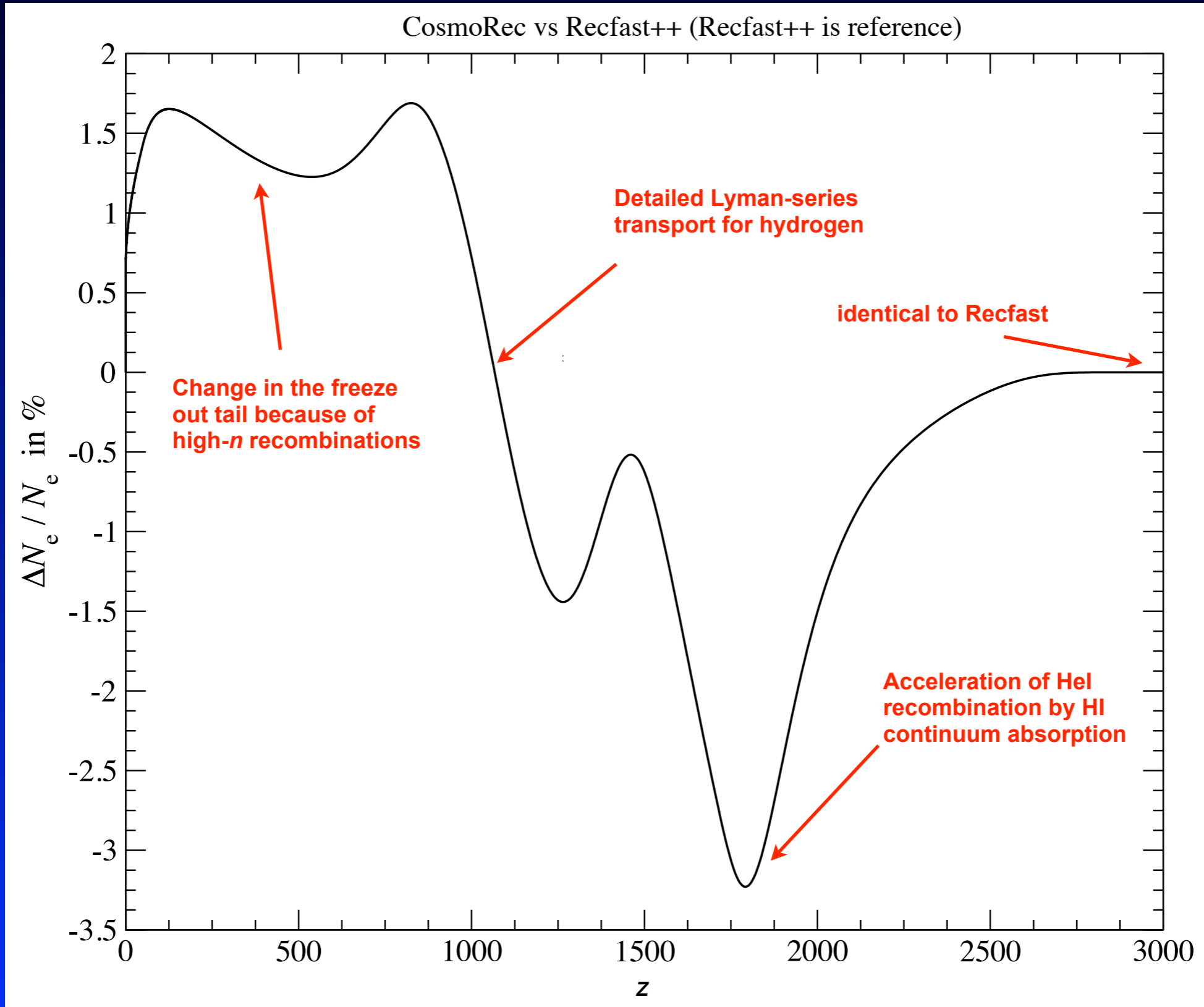
Overall effect of detailed HeI radiative transfer



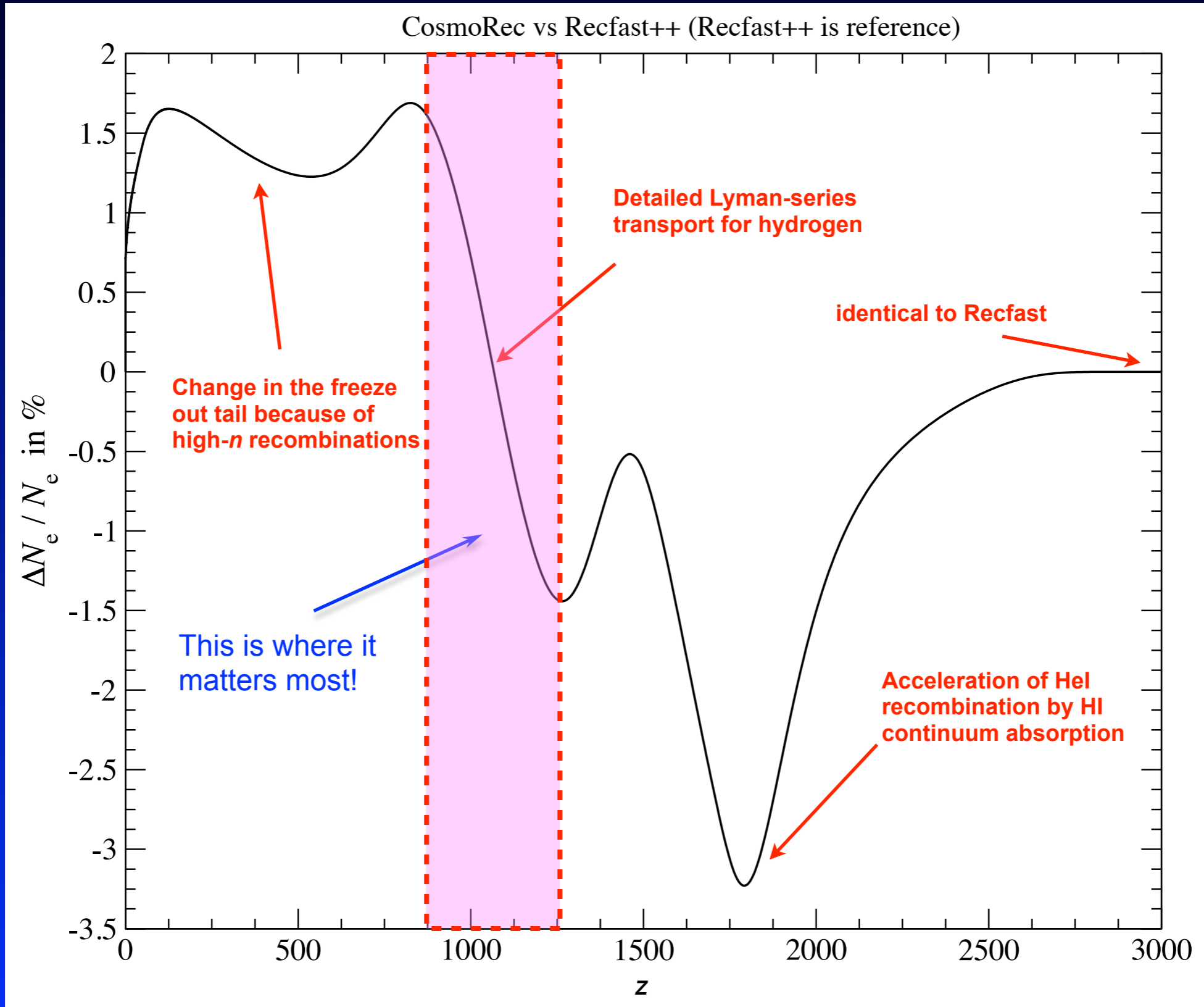
Cosmological Recombination Code: *CosmoRec*

- uses an effective multi-level approach (*Haimoud & Hirata, 2010*)
- very *accurate* and *fast* (for 'default' setting ~1.3 sec per model!)
- solves the detailed radiative transfer problem for Ly-*n*
- no *fudging* (*Recfast*) OR *multi-dimensional interpolation* (*RICO*)
- different *runmodes/accuracies* implemented
- easily *extendable* (effect of dark matter annihilation already included)
- was already tested in a wide range of cosmologies
- now runs smoothly with CAMB/CosmoMC (*Shaw & JC, MNRAS, 2011*)
- *CosmoRec* is available at: www.Chluba.de/CosmoRec

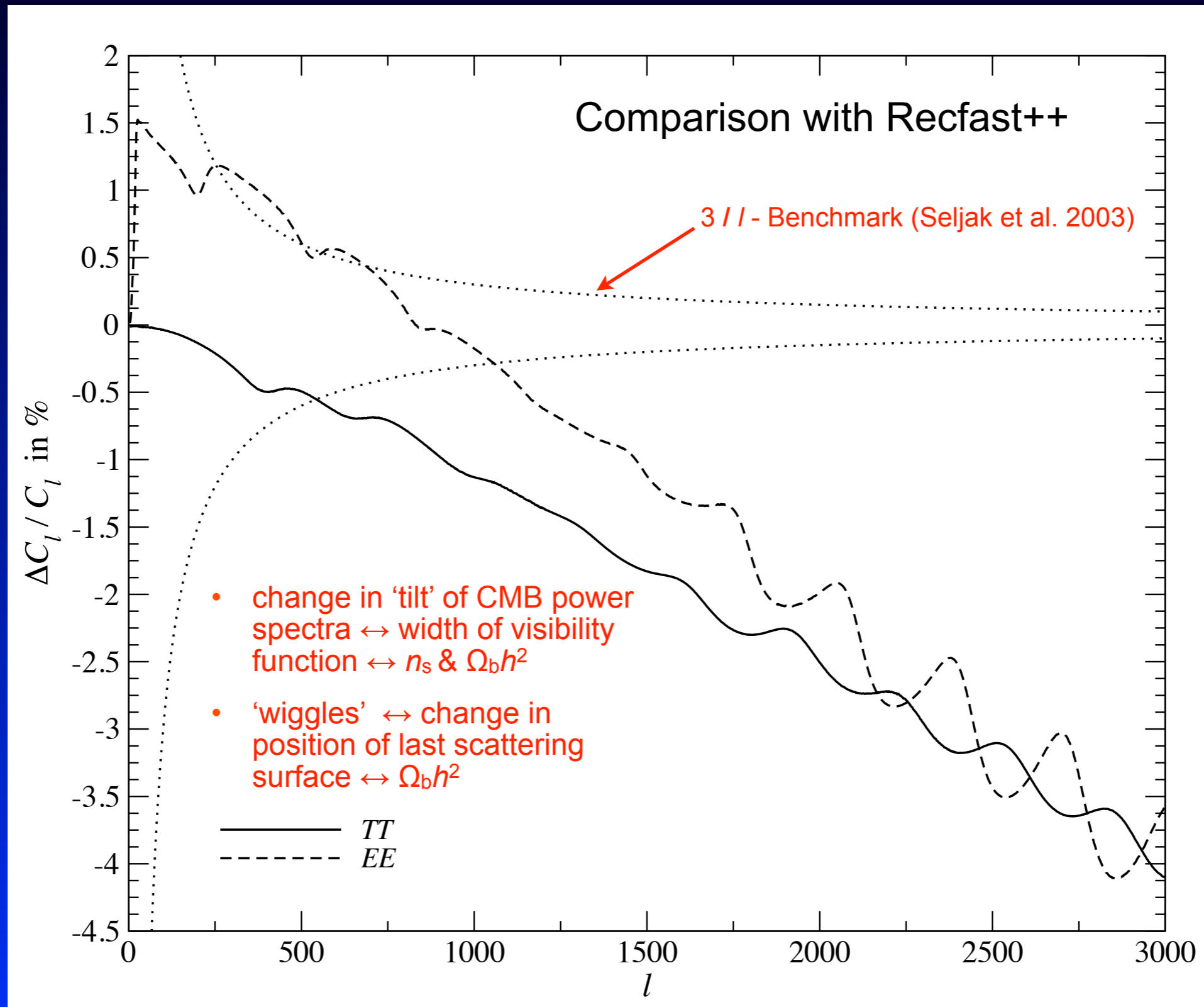
Cumulative Changes to the Ionization History



Cumulative Changes to the Ionization History

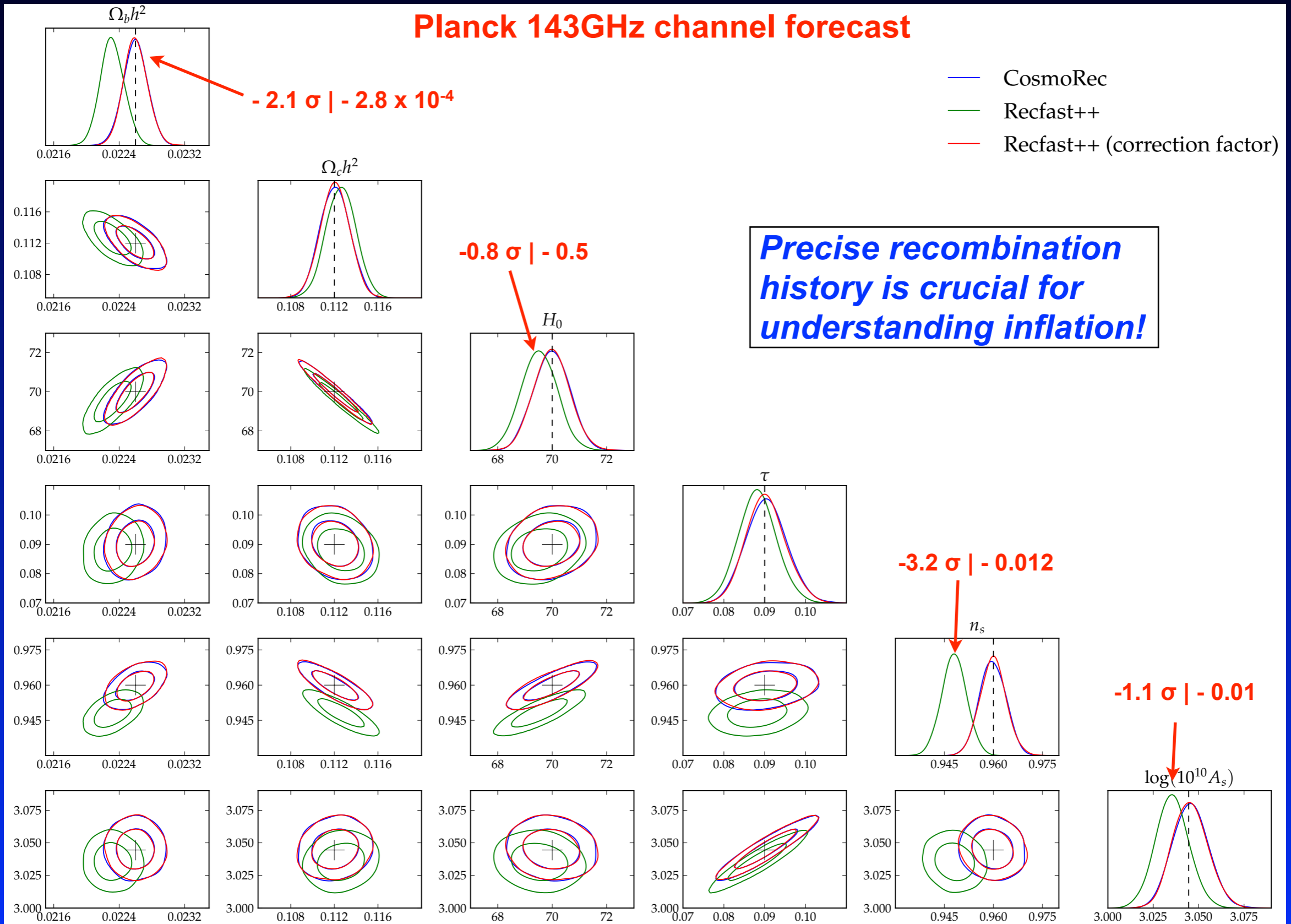


Cumulative Change in the CMB Power Spectra

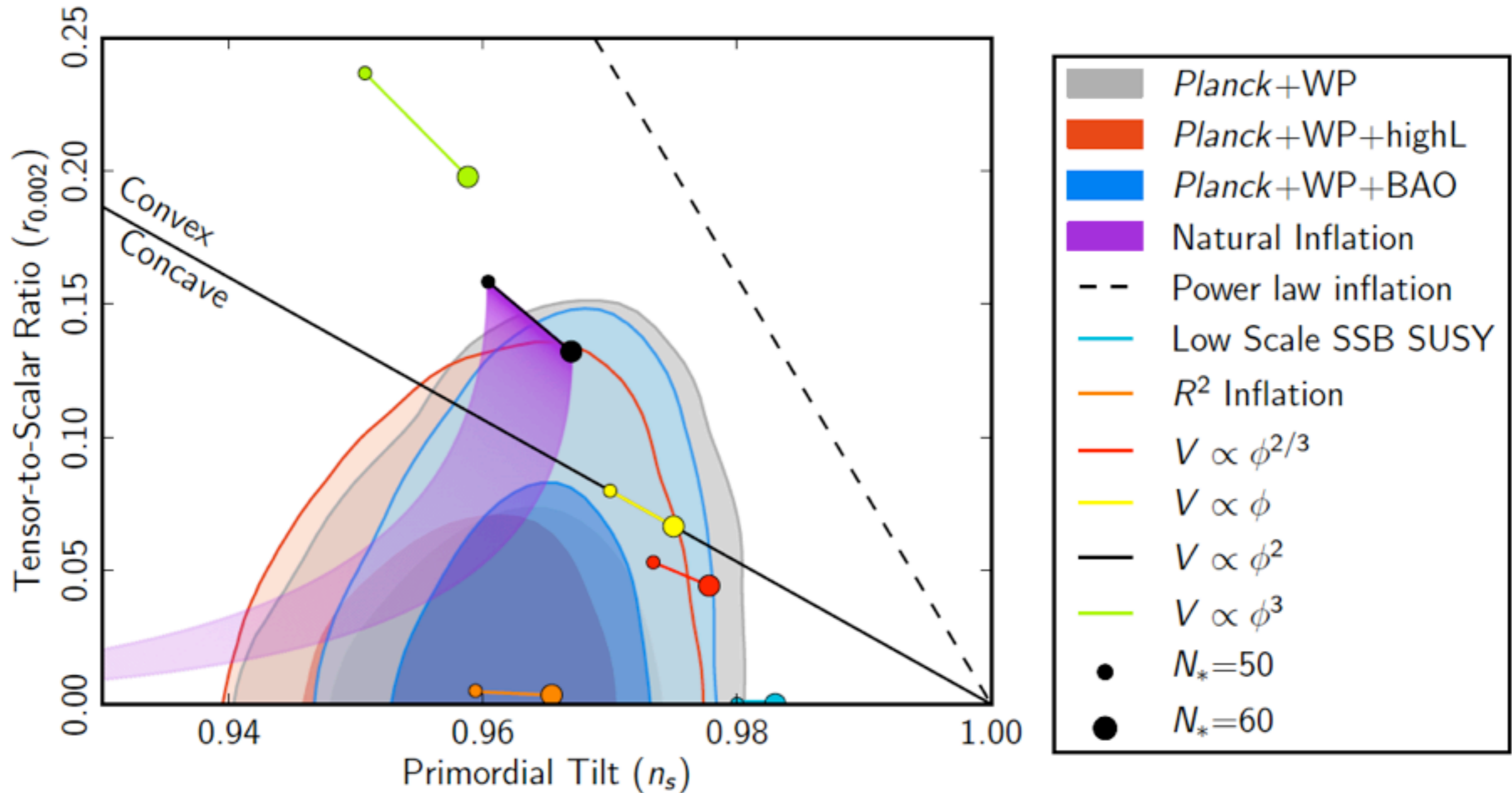


Importance of recombination for inflation

Planck 143GHz channel forecast



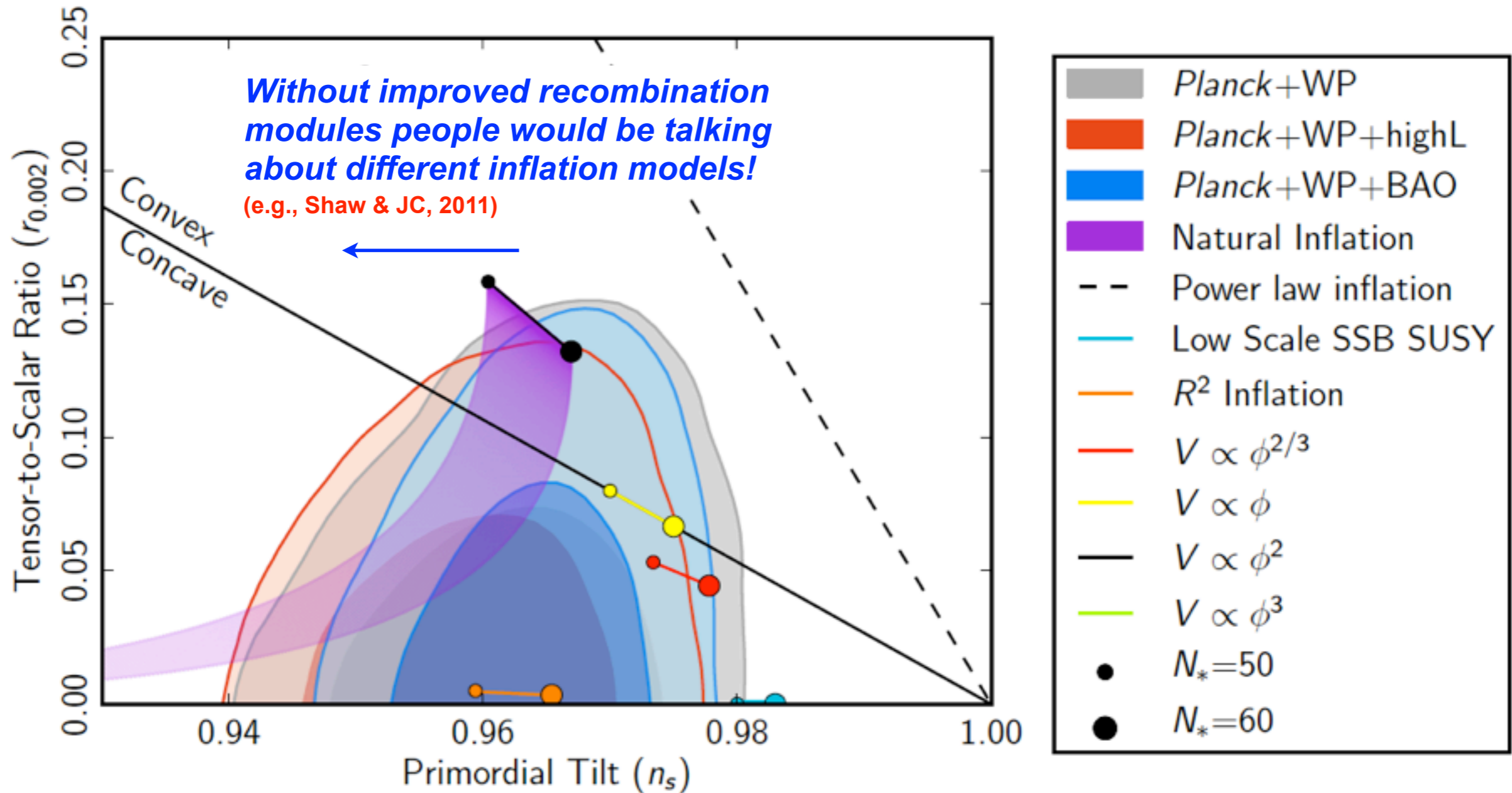
Importance of recombination for inflation constraints



Planck Collaboration, 2013, paper XXII

- Analysis uses refined recombination model (CosmoRec/HyRec)

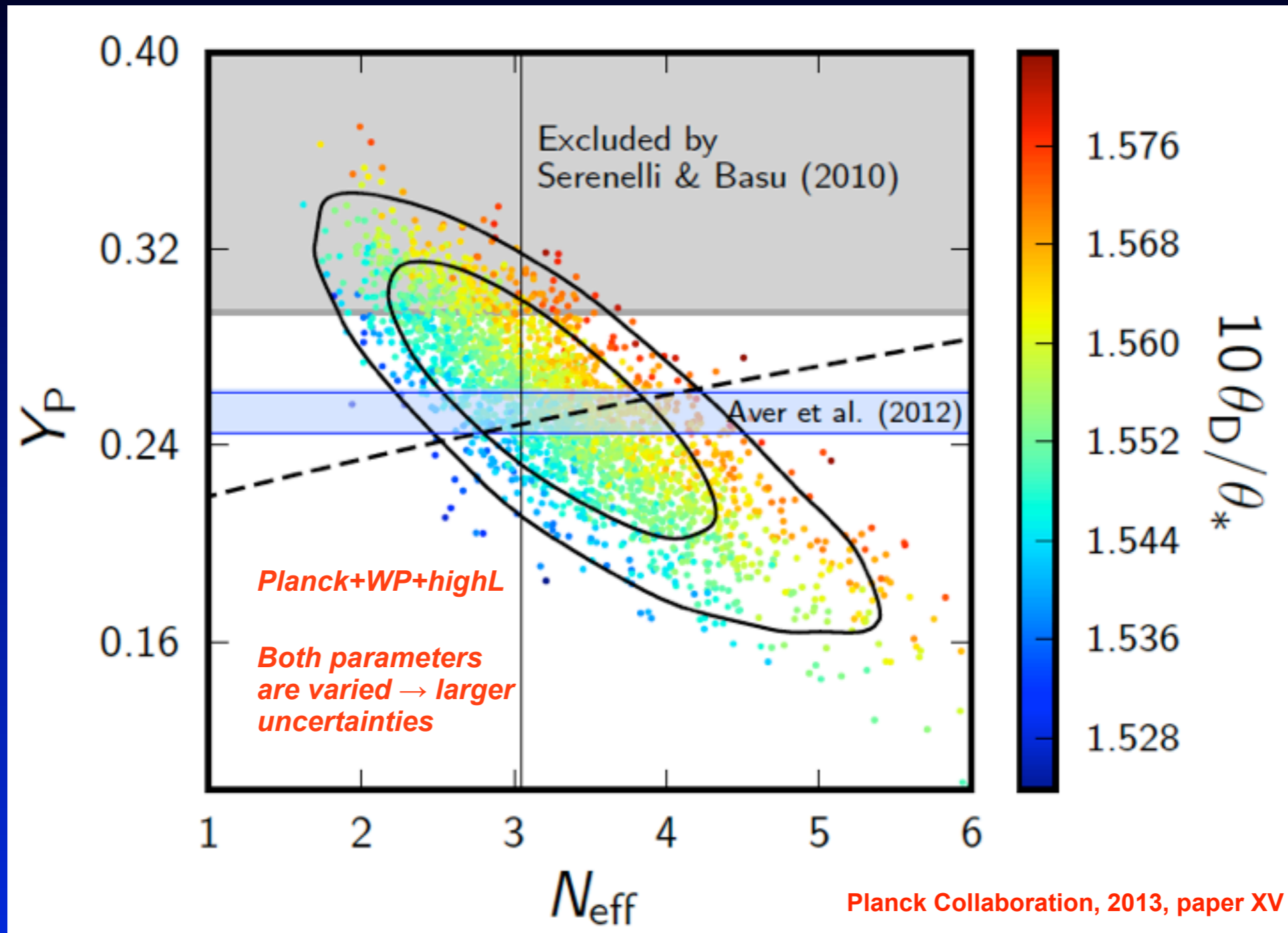
Importance of recombination for inflation constraints



Planck Collaboration, 2013, paper XXII

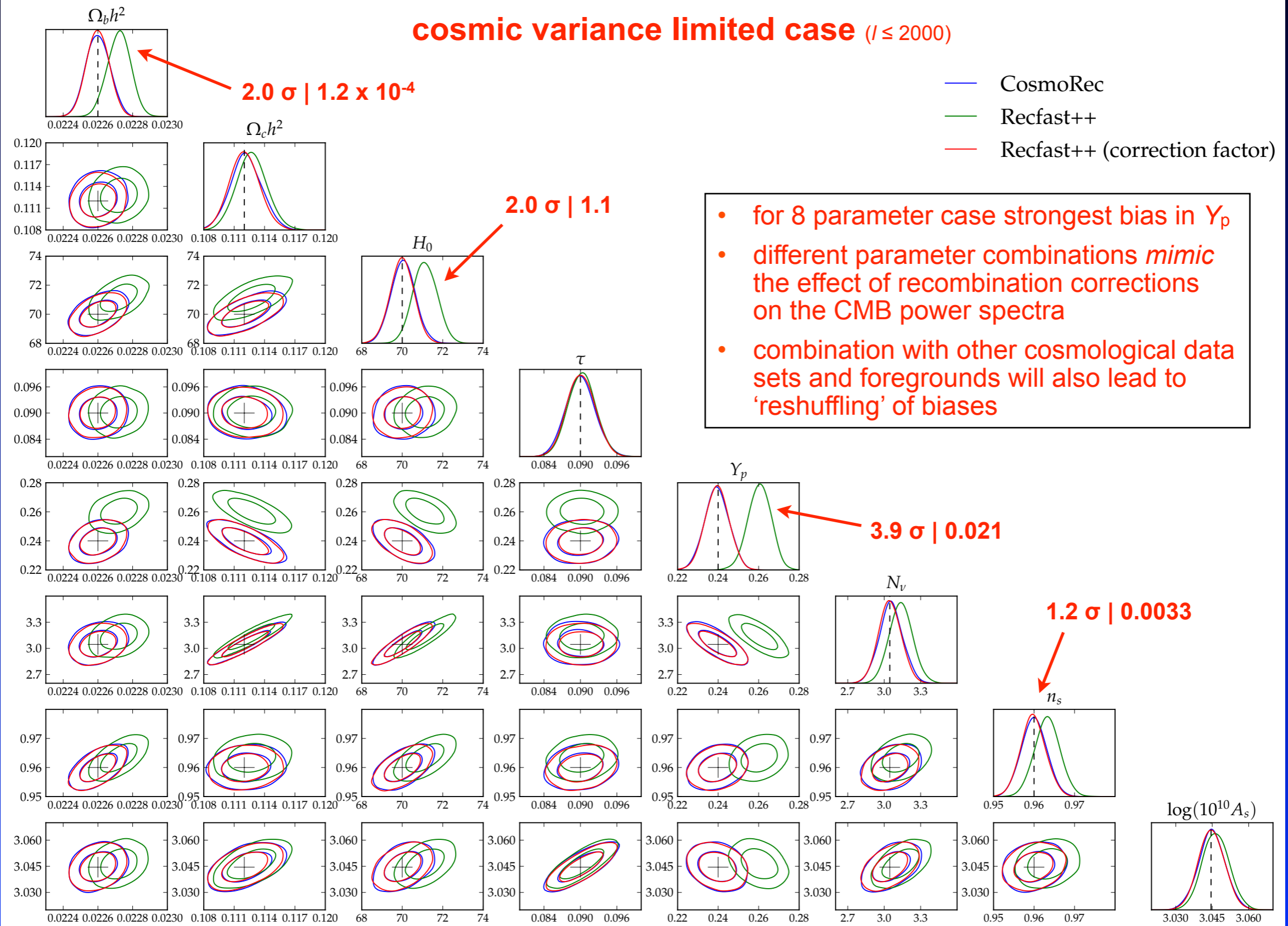
- Analysis uses refined recombination model (CosmoRec/HyRec)

CMB constraints on N_{eff} and Y_p



- Consistent with SBBN and standard value for N_{eff}
- Future CMB constraints (SPTPol & ACTPol) on Y_p will reach 1% level

Importance of recombination for measuring helium



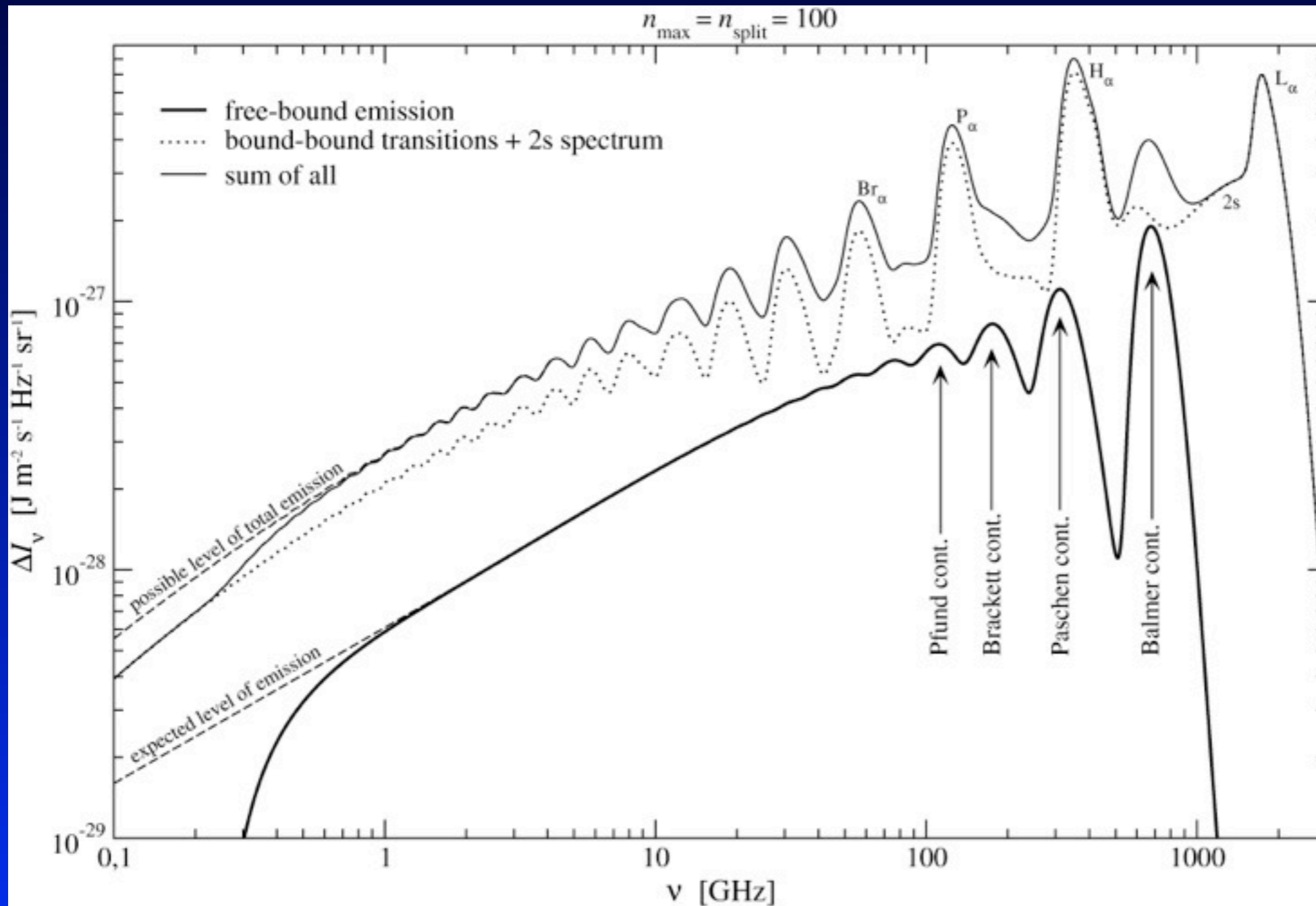
How does the cosmological recombination radiation look and how can it help us?

Simple estimates for hydrogen recombination

Hydrogen recombination:

- per recombined hydrogen atom an energy of ~ 13.6 eV in form of photons is released
 - at $z \sim 1100 \rightarrow \Delta\varepsilon/\varepsilon \sim 13.6 \text{ eV } N_b / (N_\gamma 2.7kT_r) \sim 10^{-9} - 10^{-8}$
- recombination occurs at redshifts $z < 10^4$
- At that time the *thermalization* process doesn't work anymore!
- There should be some *small* spectral distortion due to additional Ly- α and 2s-1s photons!
- (Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278; Peebles, 1968, ApJ, 153, 1)
- In 1975 **Viktor Dubrovich** emphasized the possibility to observe the recombinational lines from $n > 3$ and $\Delta n \ll n$!

100-shell hydrogen atom and continuum CMB spectral distortions



bound-bound & 2s:

- at $\nu > 1\text{GHz}$: distinct features
- slope ~ 0.46

free-bound:

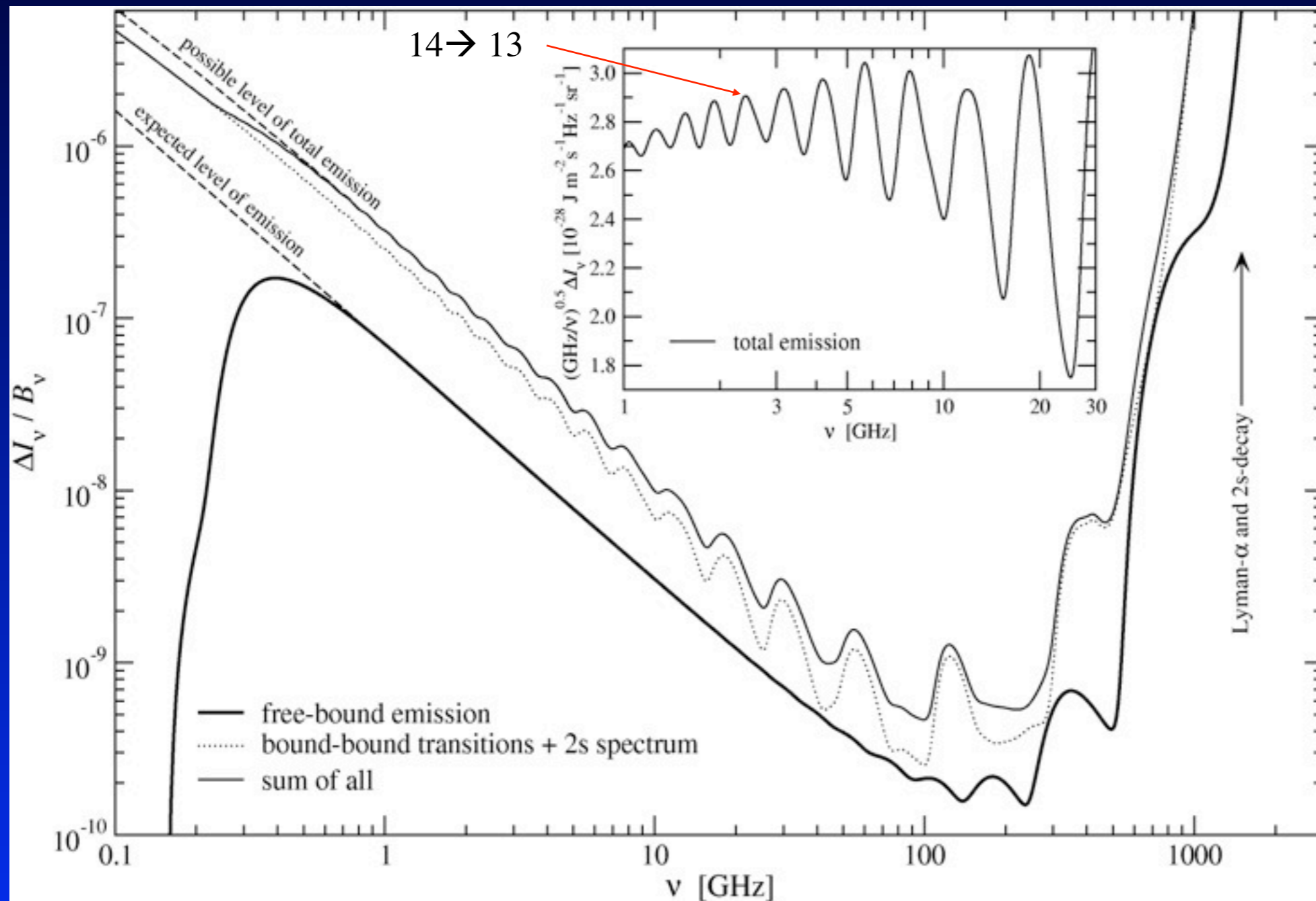
- only a few features distinguishable
- slope ~ 0.6

Total:

- f-b contributes $\sim 30\%$ and more
- Balmer cont. $\sim 90\%$
- Balmer: 1γ per HI
- in total 5γ per HI

100-shell hydrogen atom and continuum

Relative distortions



Wien-region:

- L_α and 2s distortions are very strong
- but CIB more dominant

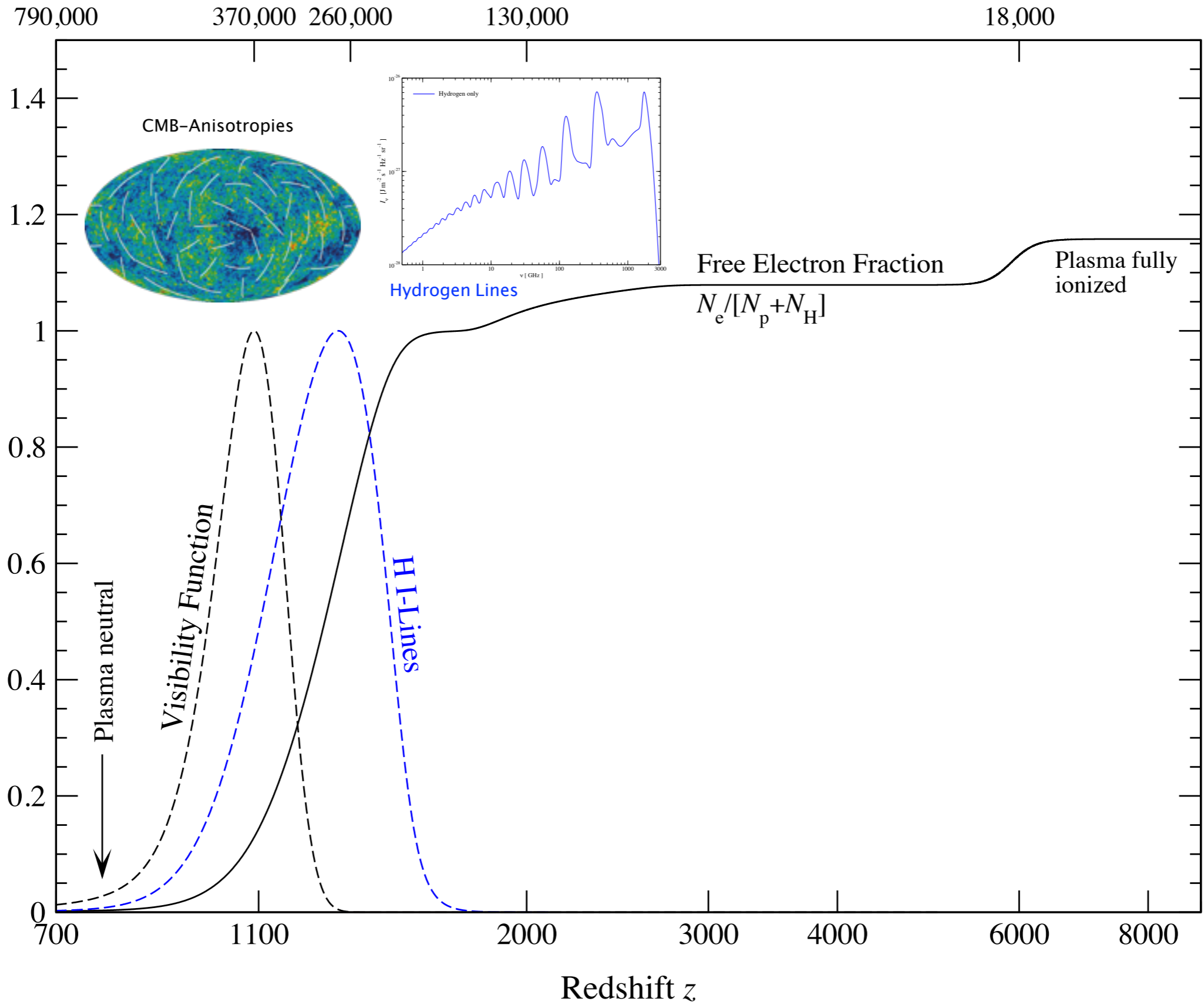
@ CMB maximum:

- relative distortions extremely small
- strong ν -dependence

RJ-region:

- relative distortion exceeds level of $\sim 10^{-7}$ below $\nu \sim 1$ -2 GHz
- oscillatory frequency dependence with ~ 1 -10 percent-level amplitude:
- *hard to mimic by known foregrounds or systematics*

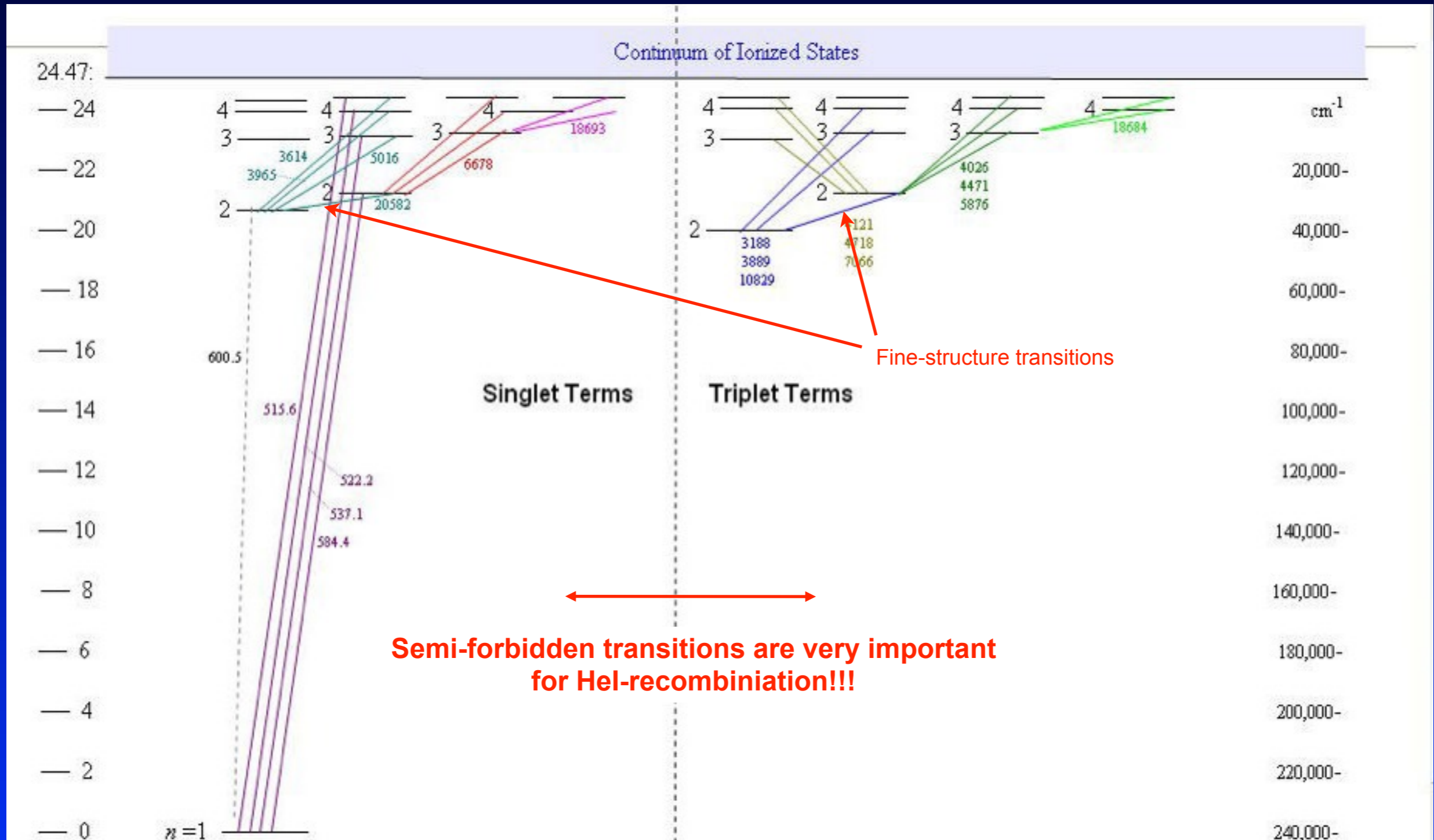
Cosmological Time in Years



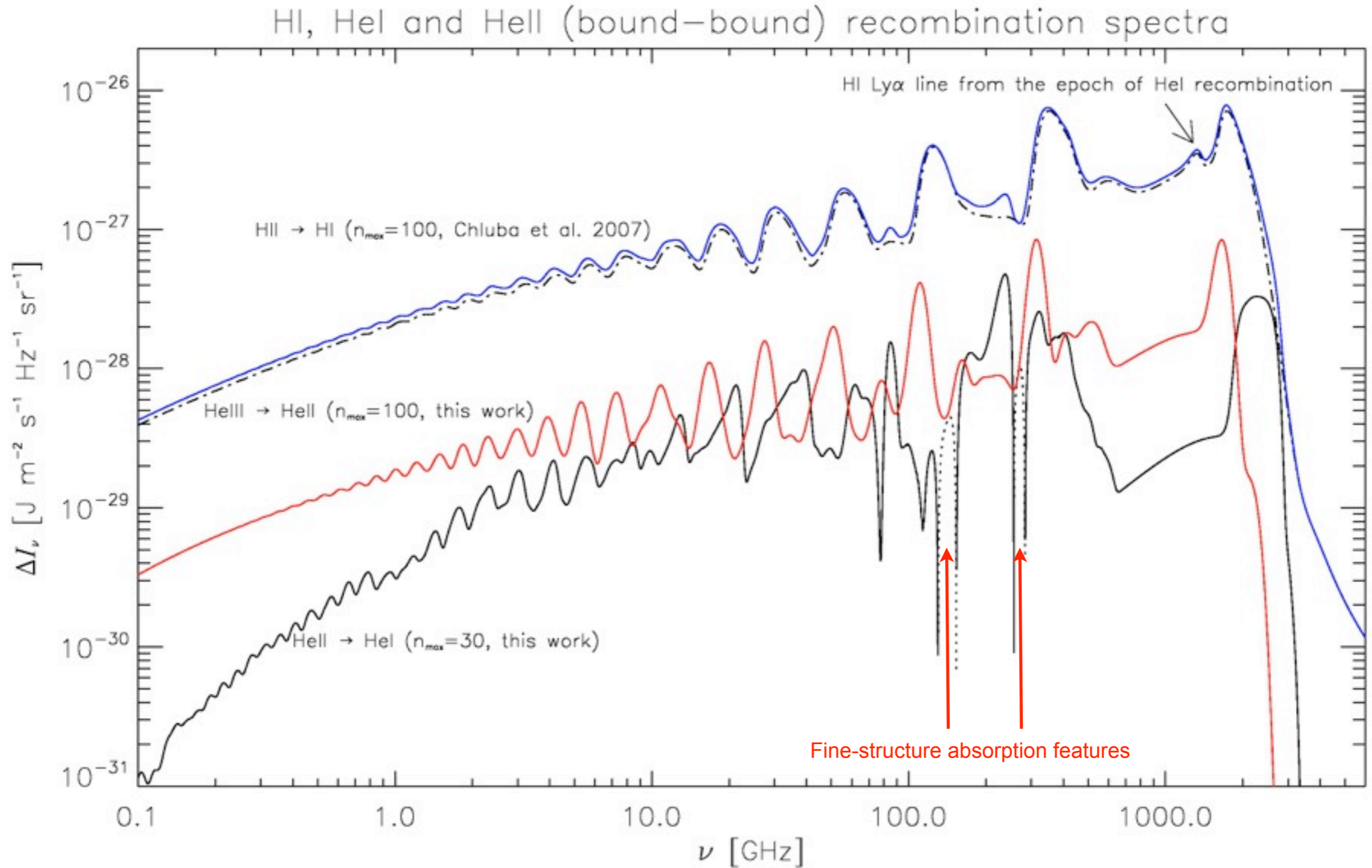
What about the contributions from helium recombination?

- Nuclear reactions: $Y_p \sim 0.24 \leftrightarrow N_{\text{HeI}} / N_{\text{H}} \sim 8 \%$
 - expected photon number rather small
- **BUT:**
 - (i) two epochs of He recombination
HeII → HeI at $z \sim 6000$ and HeII → HeI at $z \sim 2500$
 - (ii) Helium recombinations faster
 - more *narrow* features with *larger* amplitude
 - (iii) non-trivial superposition
 - local amplification possible
 - (iv) **reprocessing** of HeII & HeI photons by HeI and HI
 - increases the number of helium-related photons
 - May opens a way to **directly** measure the primordial (pre-stellar!!!) helium abundance!

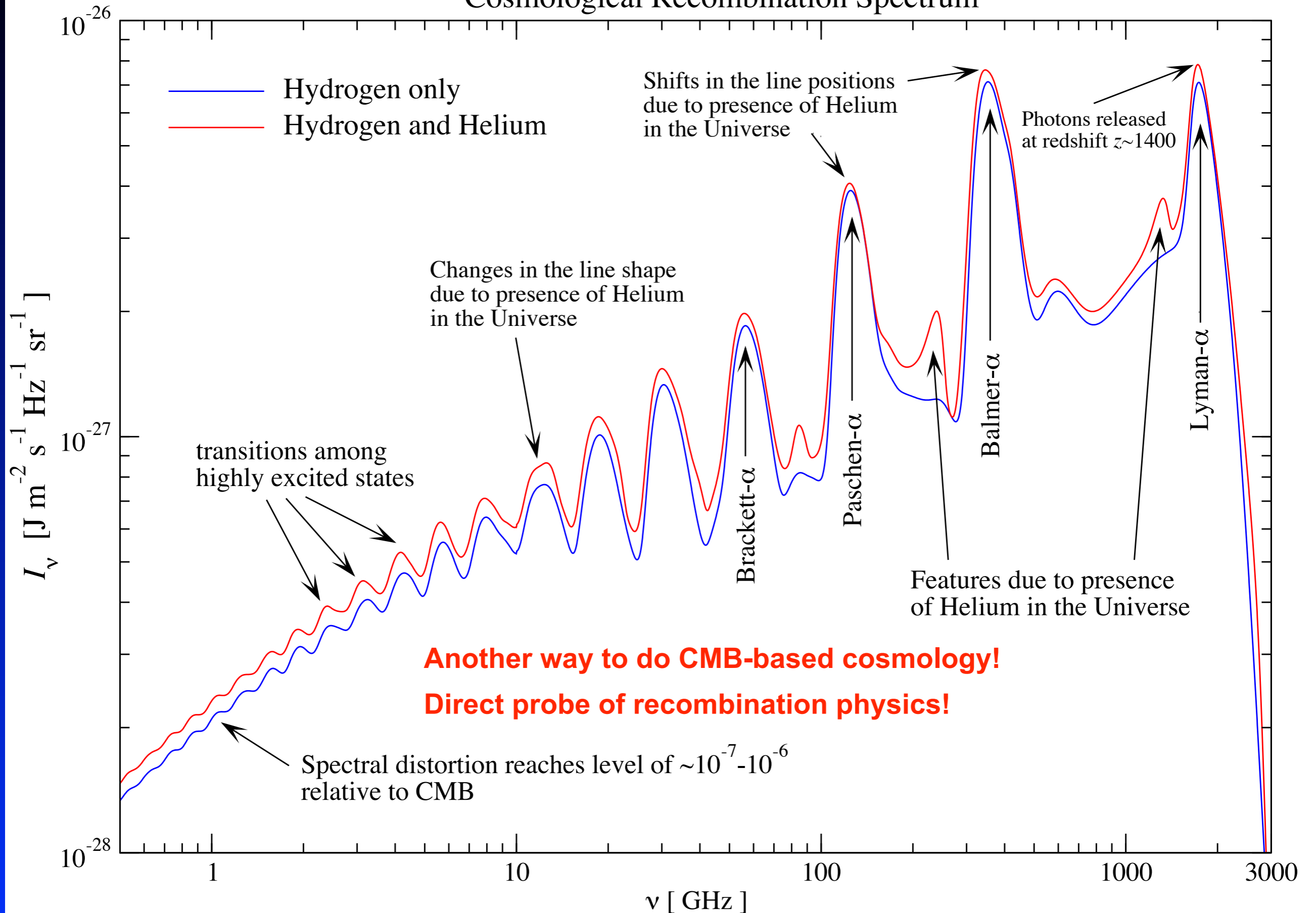
Grotrian diagram for neutral helium



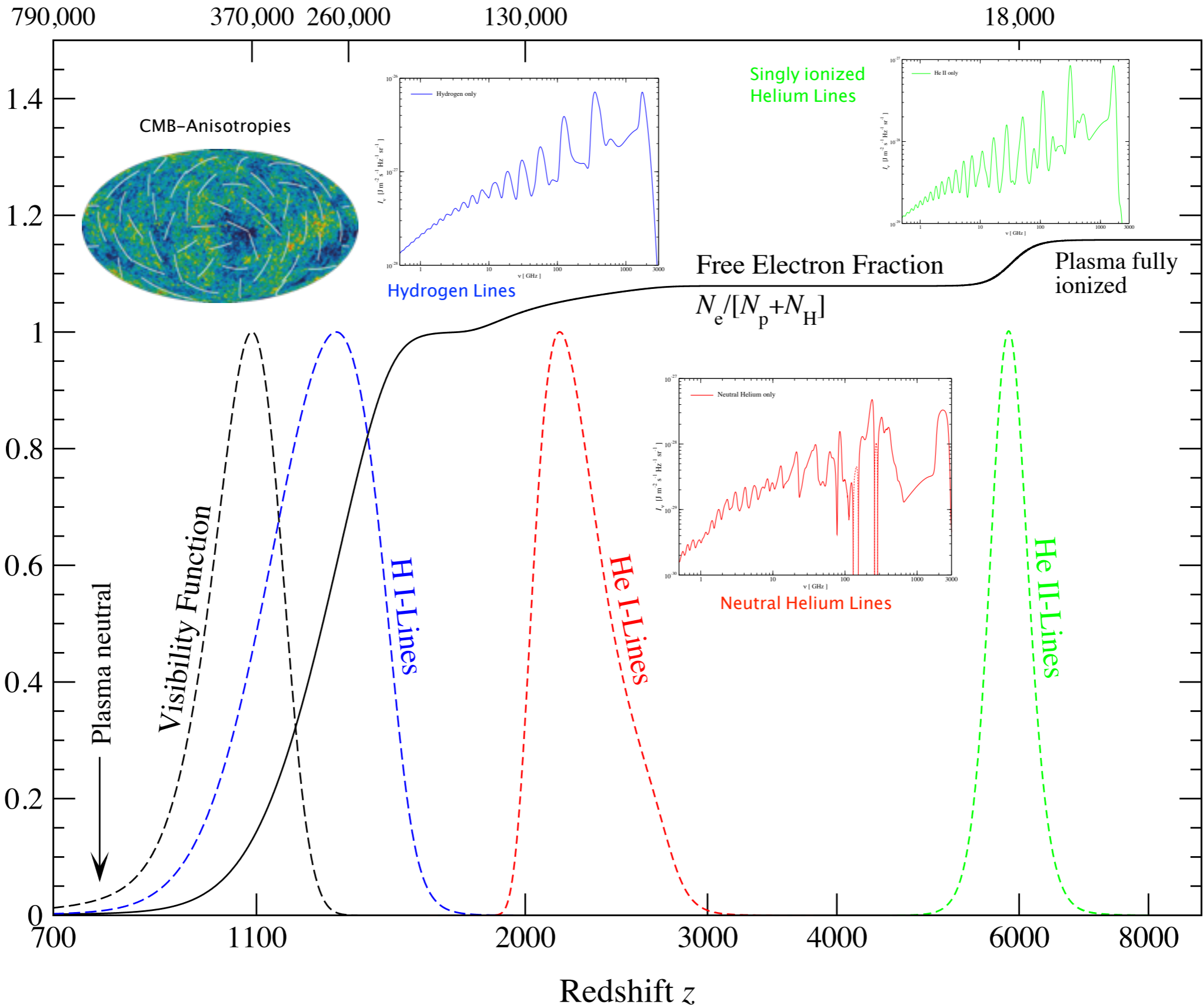
Helium contributions to the cosmological recombination spectrum



Cosmological Recombination Spectrum



Cosmological Time in Years



What would we actually learn by doing such hard job?

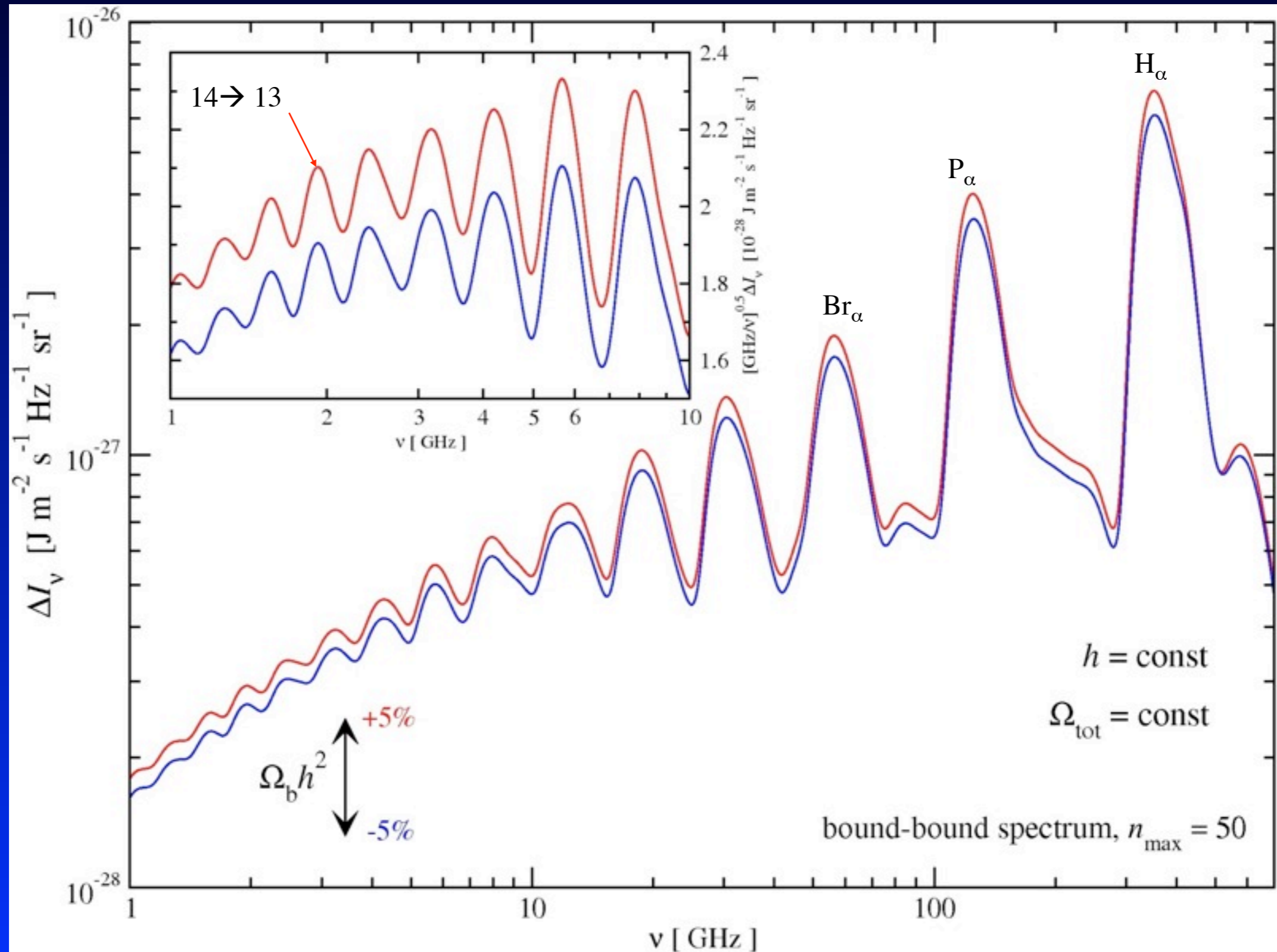
Cosmological Recombination Spectrum opens a way to measure:

→ the specific *entropy* of our universe (related to $\Omega_b h^2$)

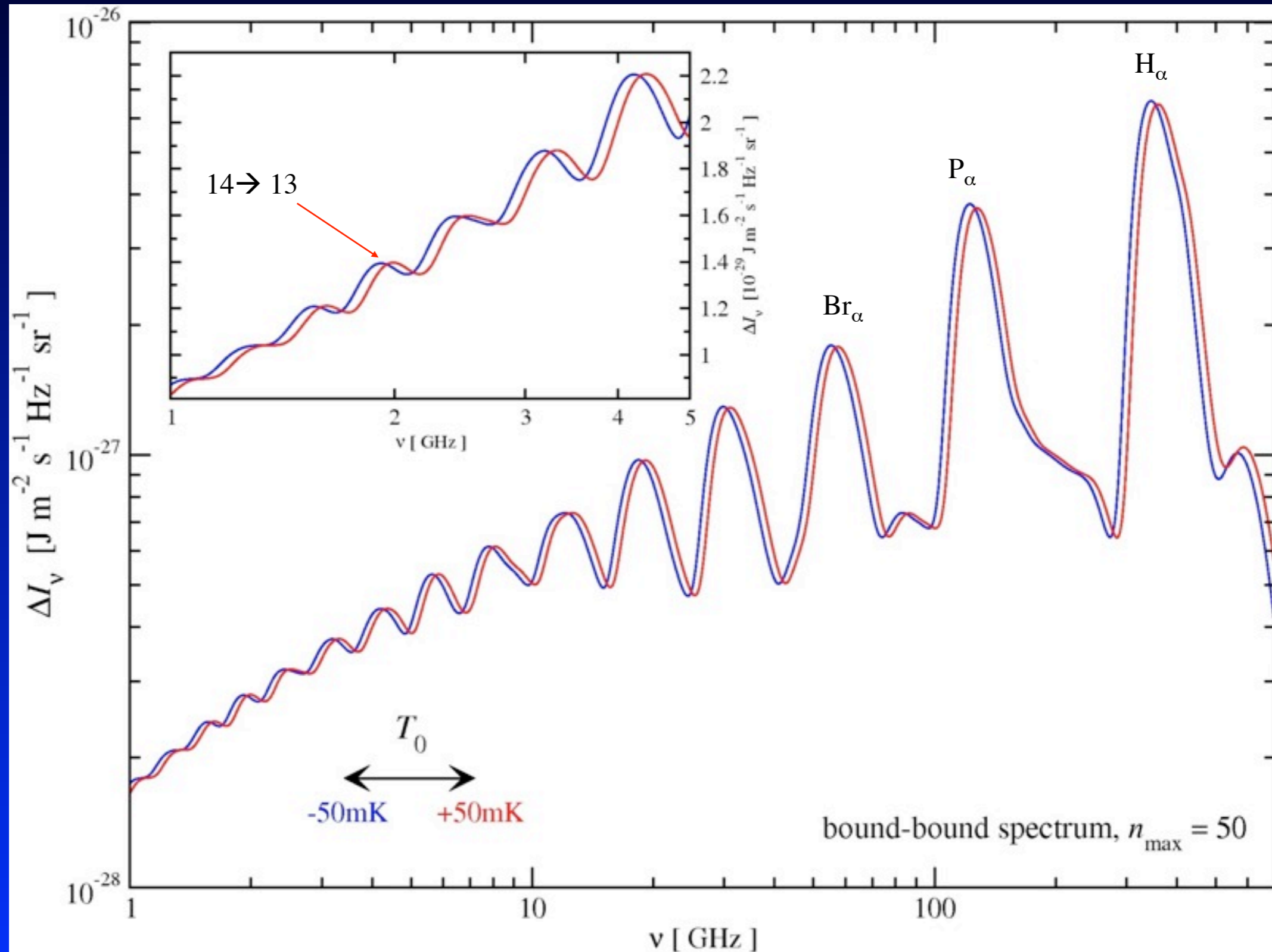
→ the CMB *monopole* temperature T_0

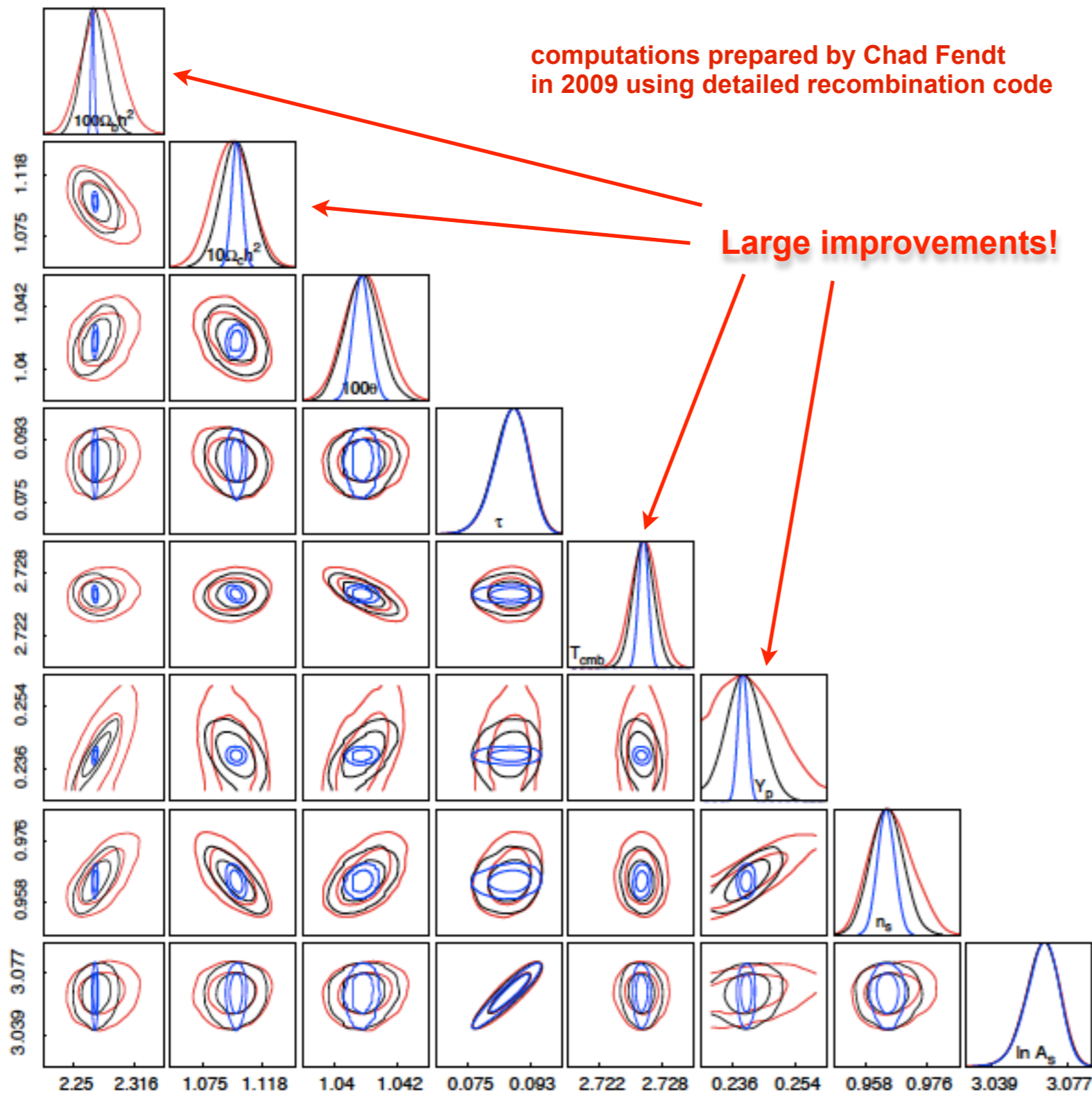
→ *the pre-stellar abundance of helium* Y_p

Hydrogen recombination spectrum: *dependence on $\Omega_b h^2$*



Hydrogen recombination spectrum: *dependence on T_0*





- CMB based cosmology alone
- Spectrum helps to break some of the parameter degeneracies
- Planning to provide a module that computes the recombination spectrum in a fast way
- detailed forecasts: which lines to measure; how important is the absolute amplitude; how accurately one should measure; best frequency resolution;

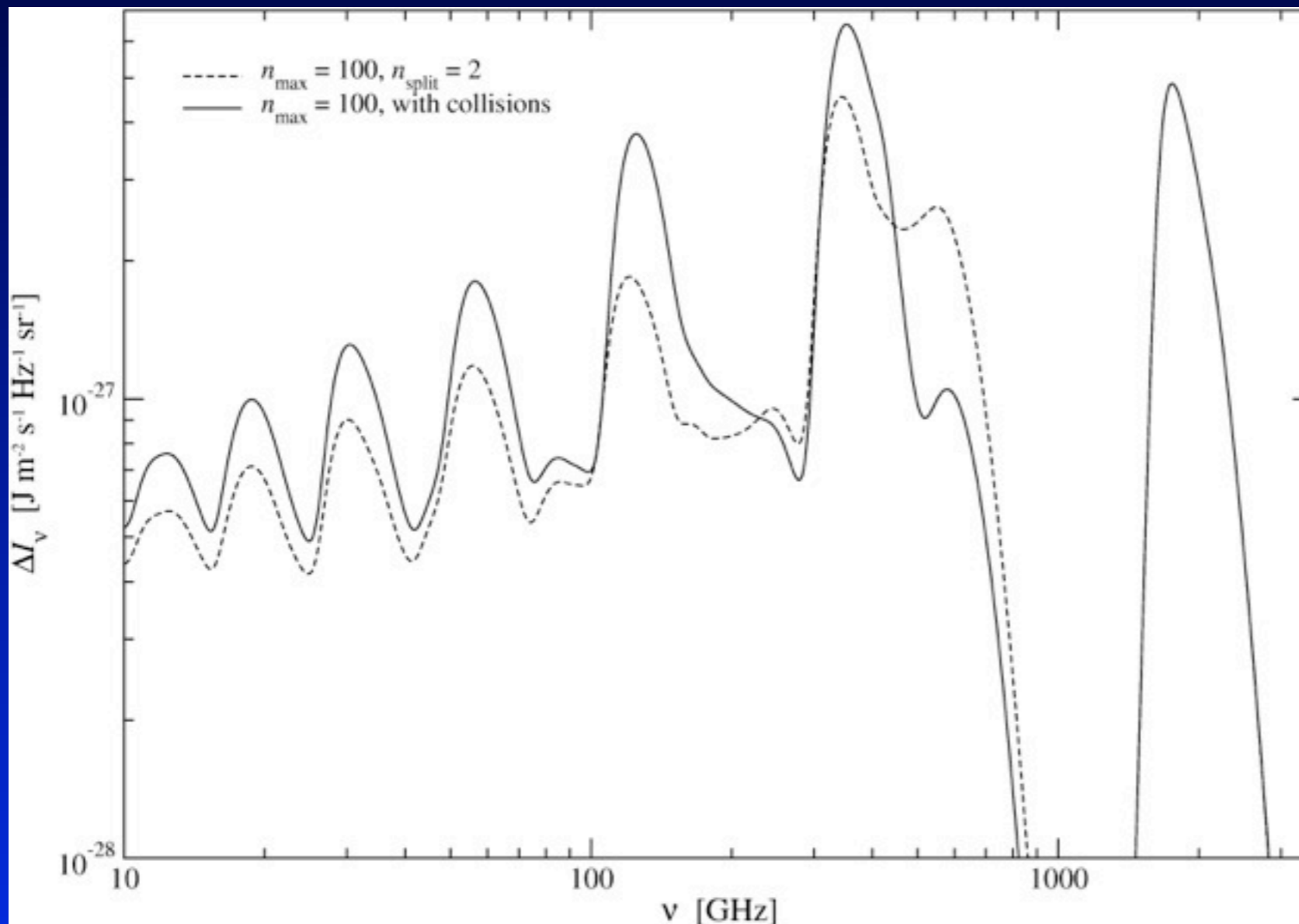
Figure 7.3: The 1 and 2 dimensional marginalized parameter posterior using the CMB spectral distortions. All three cases constrain the CMB power spectrum using a Gaussian likelihood based on Planck noise levels. The black line adds constraints due to a 10% measurement of the spectral distortions, while the blue line assumes a 1% measurement. The red line does not include the data from the spectral distortions.

What would we actually learn by doing such hard job?

Cosmological Recombination Spectrum opens a way to measure:

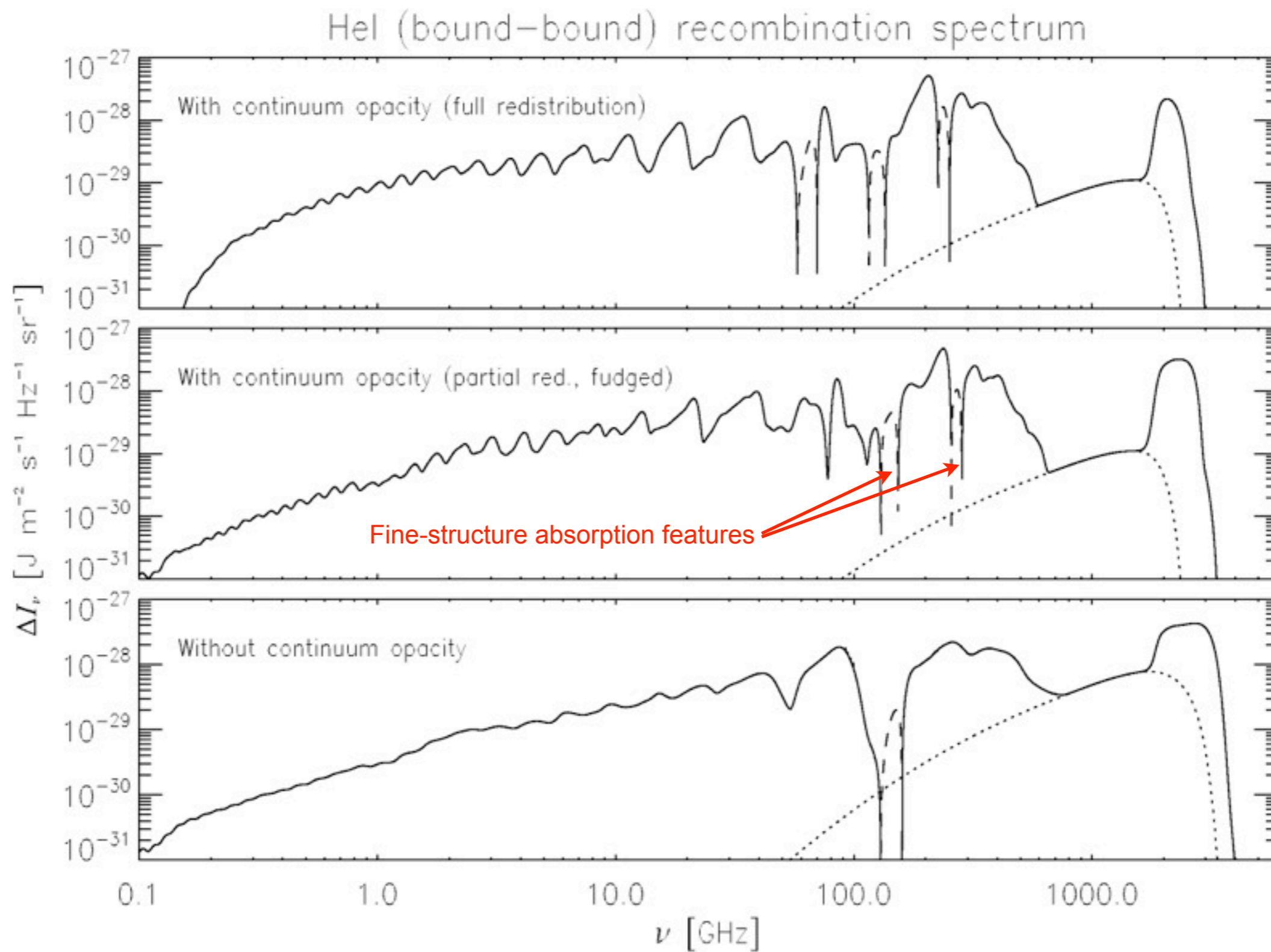
- the specific *entropy* of our universe (related to $\Omega_b h^2$)
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- *the pre-stellar abundance of helium* Y_p
- *If recombination occurs as we think it does, then the lines can be predicted with very high accuracy!*
- *In principle allows us to directly check our understanding of the standard recombination physics*

Difference in the hydrogen spectrum if collisions were more efficient

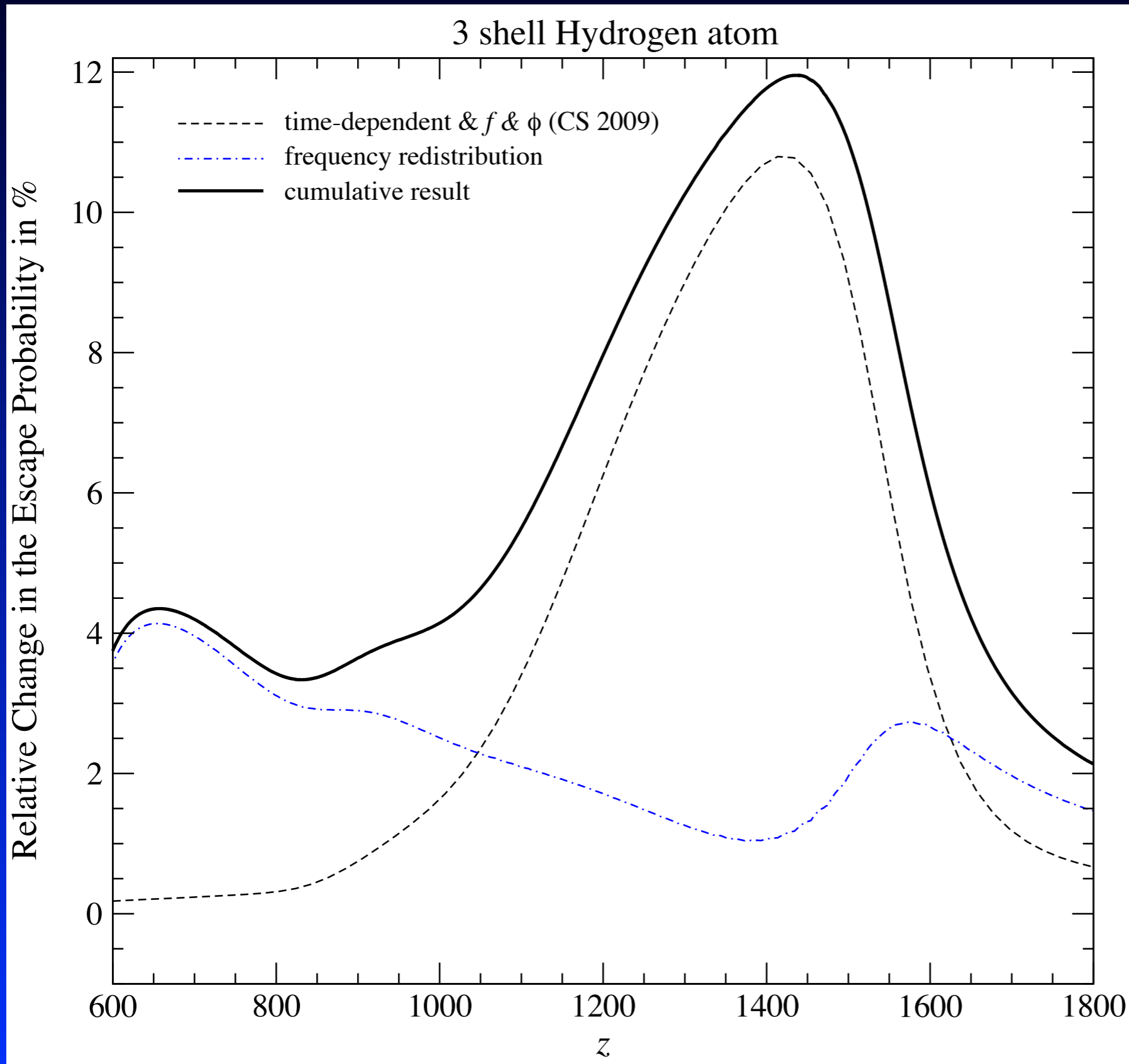


- Lyman- α unchanged
- Balmer-series:
 - B_α lower for $n_{\text{split}}=2$
 - for $n_{\text{split}}=2$ second peak more than 2 times higher
 - ratio first to second peak decreases from 6 \rightarrow 2
- higher series:
 - $n_{\text{split}}=2 \rightarrow$ emission lower

The importance of HI continuum absorption



Changes in the Lyman α escape probability



- Changes in Ly α escape probability *directly* translate into changes of the CMB Ly α distortion

- $\Delta P/P=10\% \Rightarrow \Delta I_\nu/I_\nu=10\%$

- Since Ly α line controls dynamics of recombination also all other lines will be affected by this process

What would we actually learn by doing such hard job?

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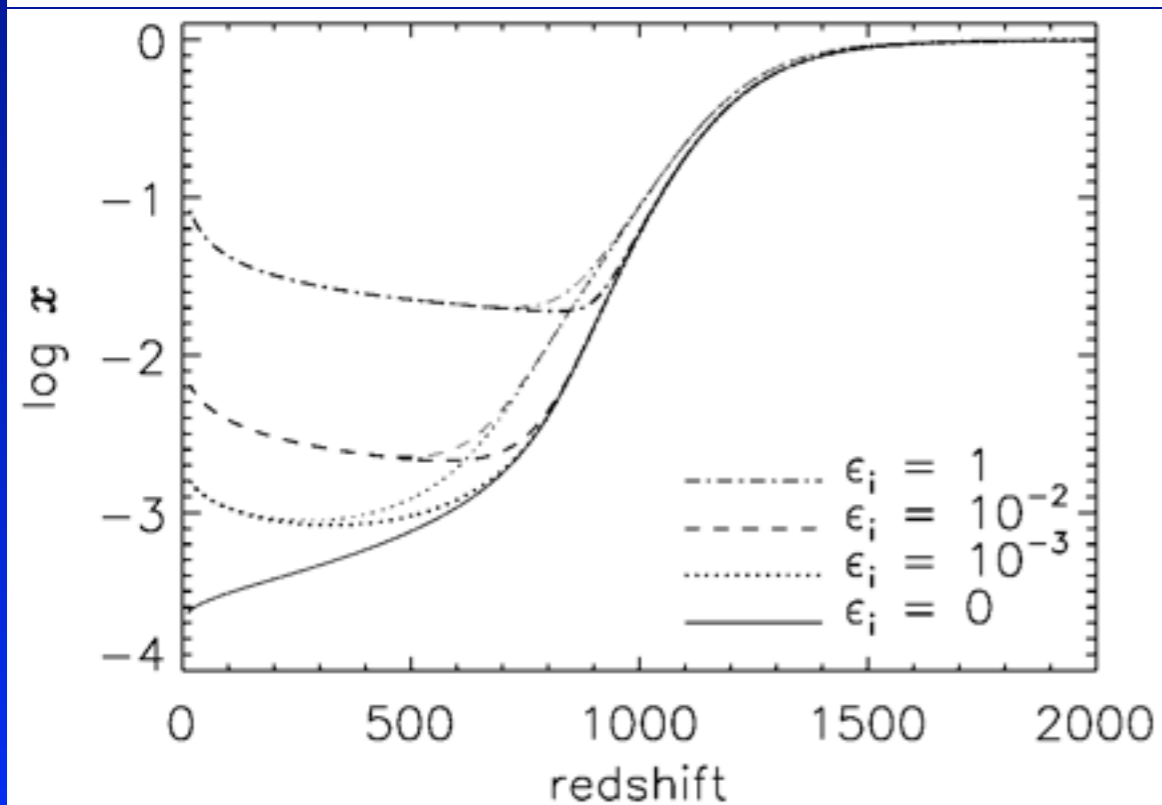
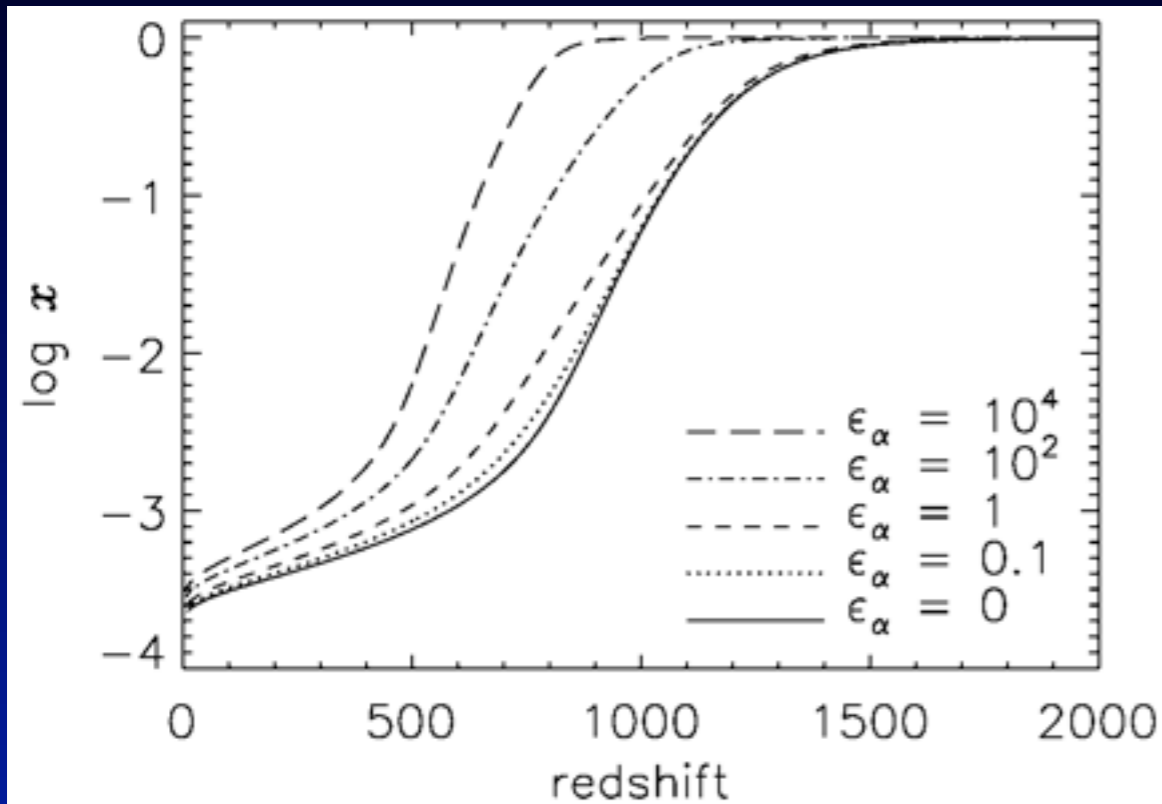
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If something unexpected or non-standard happened:

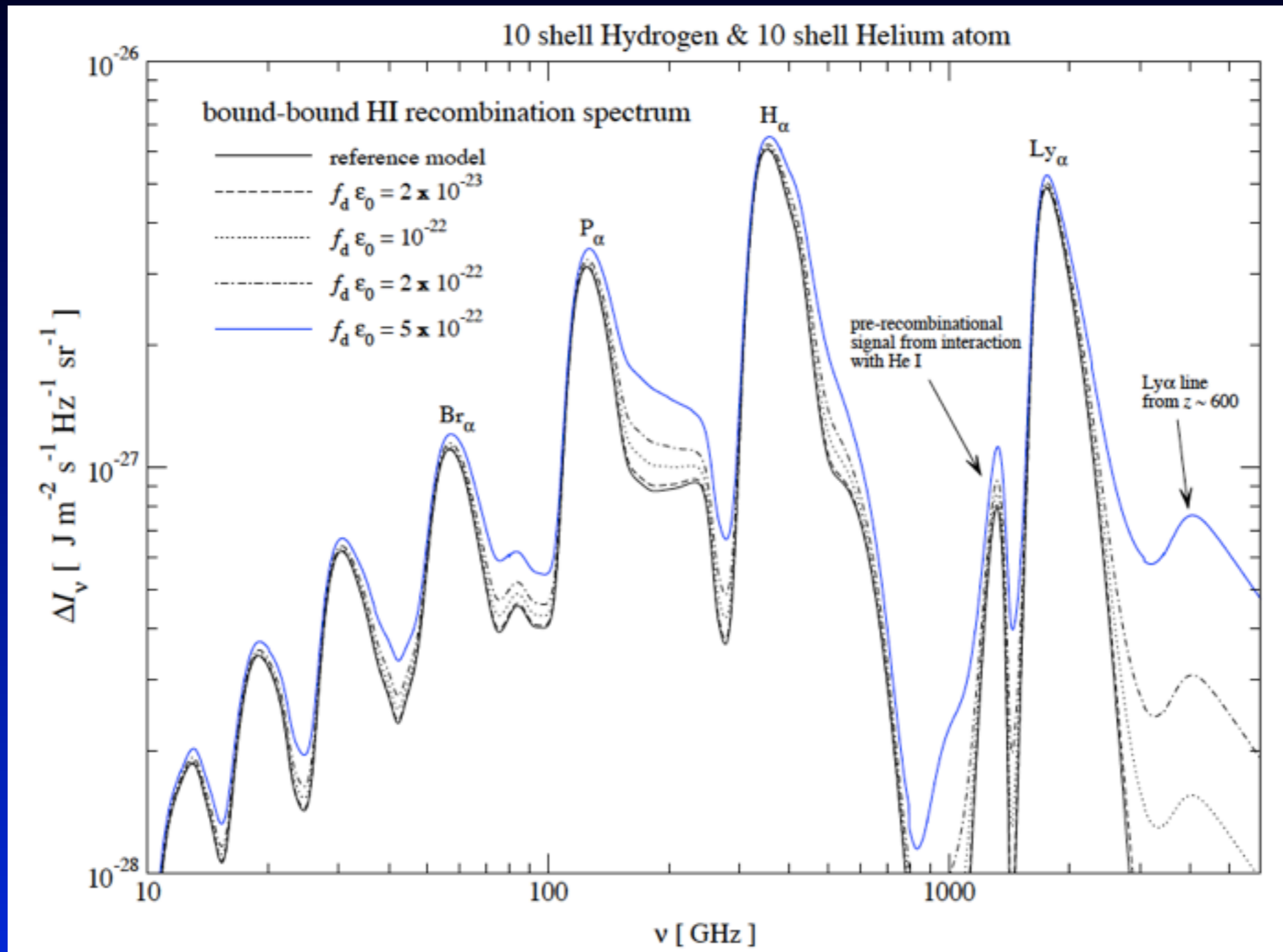
Extra Sources of Ionizations or Excitations



- ,Hypothetical' source of extra photons parametrized by ϵ_α & ϵ_i
- Extra **excitations** \Rightarrow delay of Recombination
- Extra **ionizations** \Rightarrow affect 'freeze out' tail
- This affects the Thomson visibility function
- From WMAP $\Rightarrow \epsilon_\alpha < 0.39$ & $\epsilon_i < 0.058$ at 95% confidence level (Galli et al. 2008)

- Extra **ionizations & excitations** should also lead to **additional photons** in the recombination radiation!!!
- This in principle should allow us to check for such sources at $z \sim 1000$

Dark matter annihilations / decays



JC, 2009, arXiv:0910.3663

- Additional photons at all frequencies
- Broadening of spectral features
- Shifts in the positions

Energy injection \Rightarrow CMB Spectral Distortions

How easy is it actually to learn something interesting about the thermal history?

- CMB distortion can be predicted for different energy injection histories and mechanisms (e.g. Hu & Silk, 1993a&b; Burigana & Salvaterra, 2003)
 - \rightarrow Spectral distortions are *broad* and *featureless*
 - \rightarrow Absolute (COBE-type) measurements are required
- Different injection histories yield very similar spectral distortion!
 - Simplest example: *pre-* and *post-recombinational y-type distortions*
 - energy release at redshifts $1000 < z < 50000$
 - SZ-effect e.g. due to unresolved clusters, supernova remnants, shockwaves, etc.

\Rightarrow y-distortion

Energy injection \Rightarrow CMB Spectral Distortions

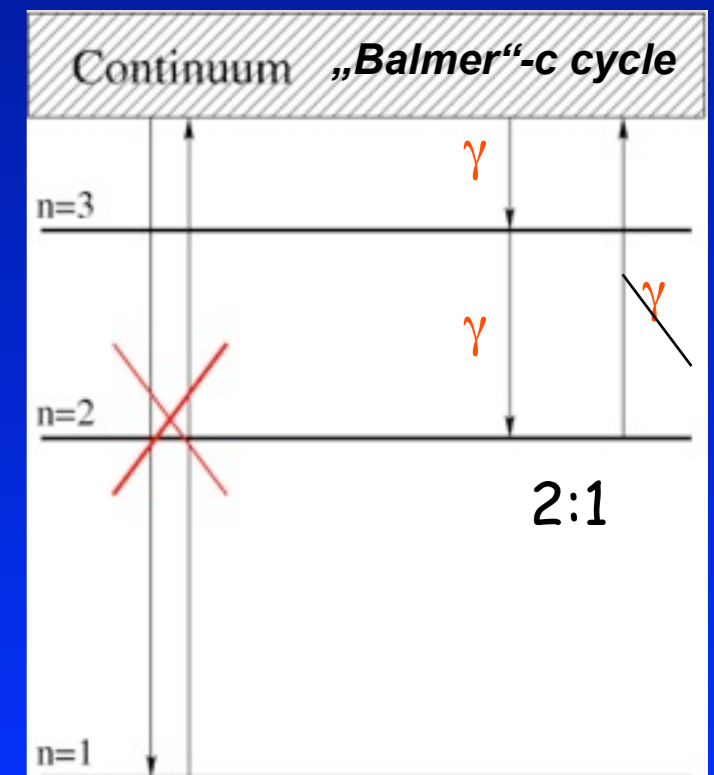
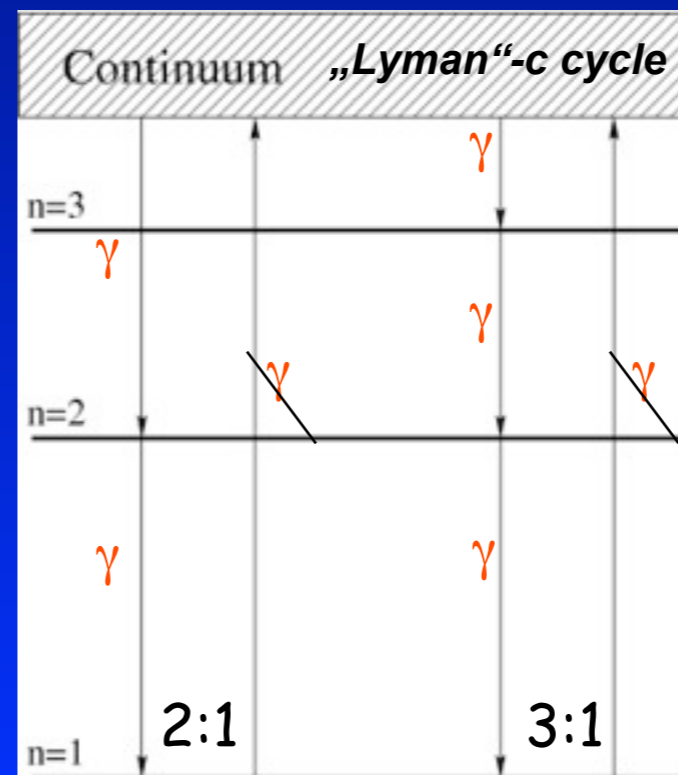
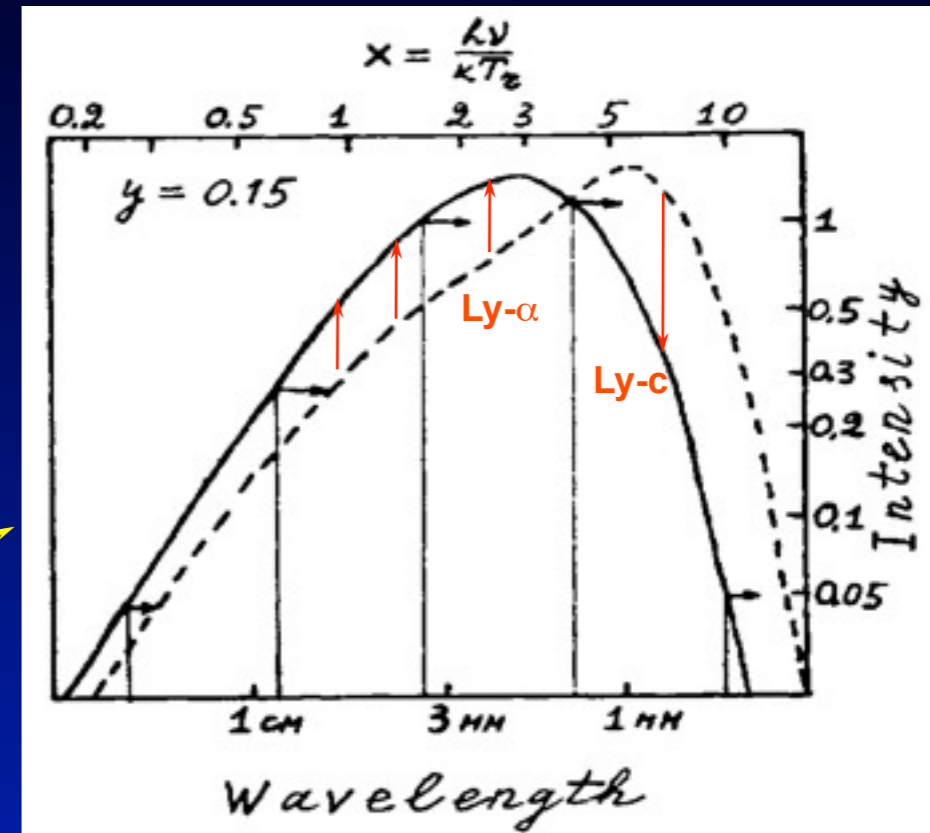
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Absence of *narrow spectral features* makes it very hard to understand real details!!!

Pre-recombinational atomic transitions after possible early energy release

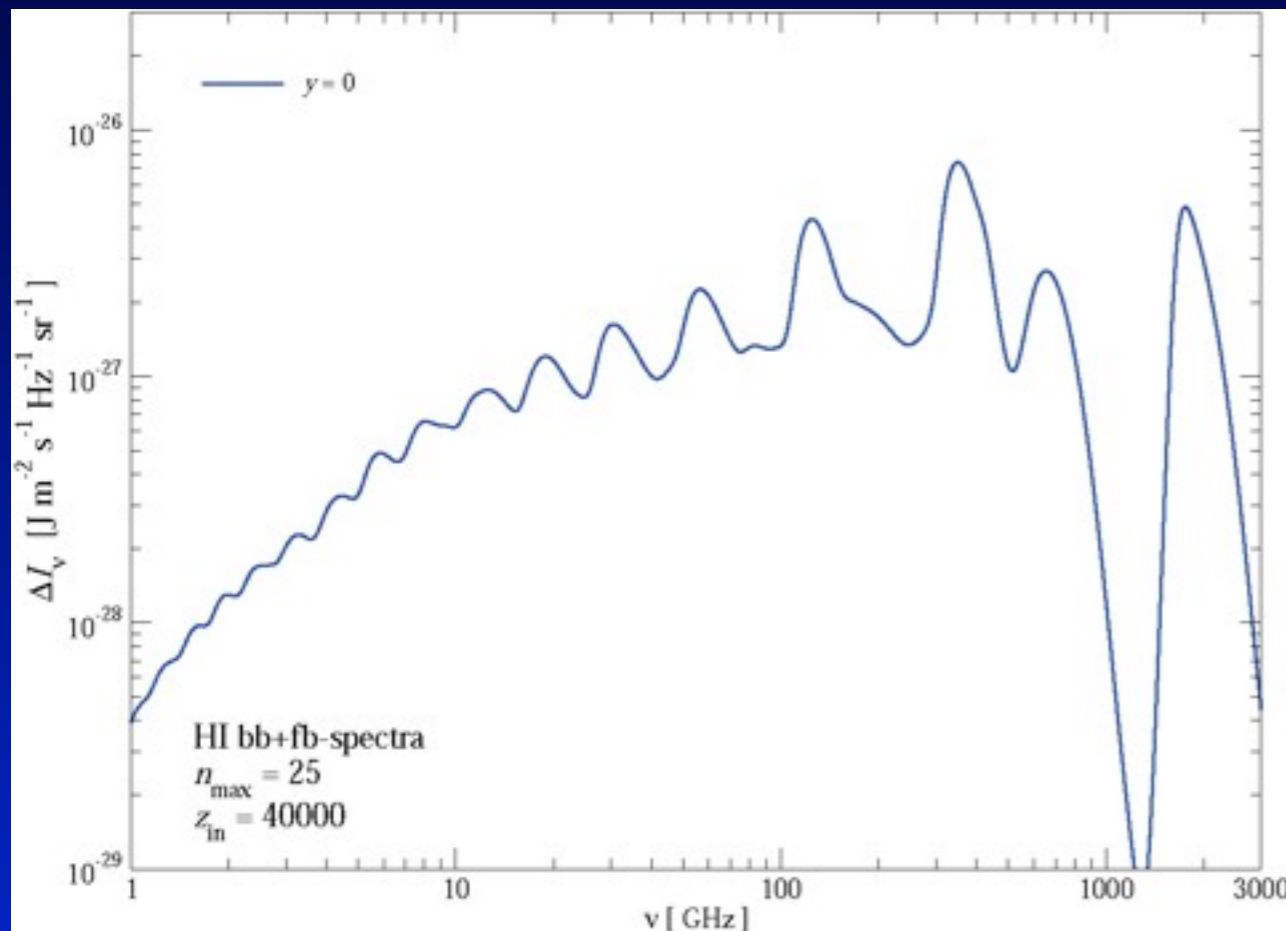
- pure blackbody CMB
 - *no net emission or absorption of photons before recombination epoch!*
- non-blackbody CMB (Lyubarsky & Sunyaev, 1983)
 - atoms “try” to restore full equilibrium
 - *atomic loops* develop (cont. → bound → cont.)
 - “splitting” of photons
 - cycles mainly end in Lyman-continuum
 - Balmer-cont. cycles work just before recombination



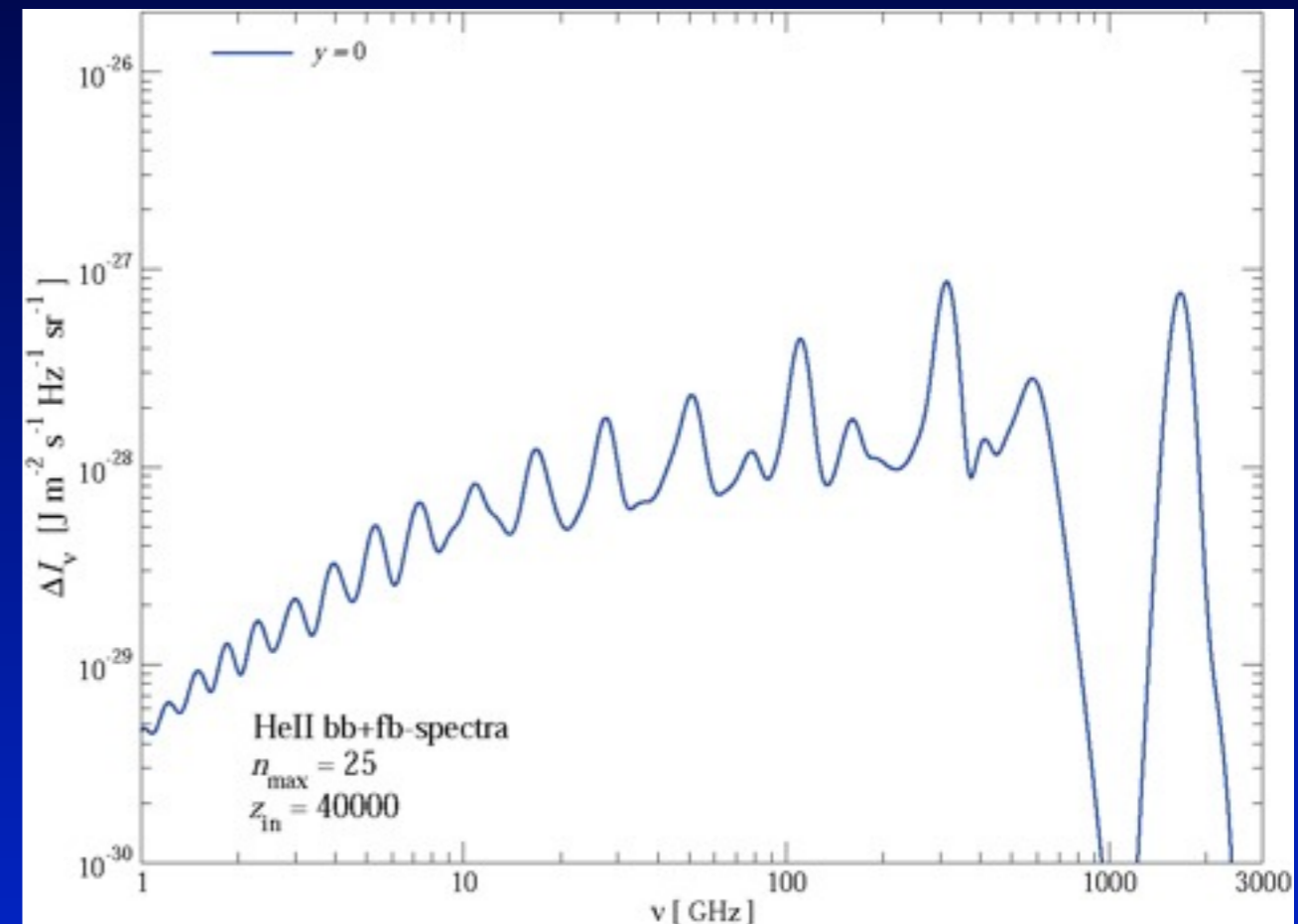
CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on y*

Hydrogen



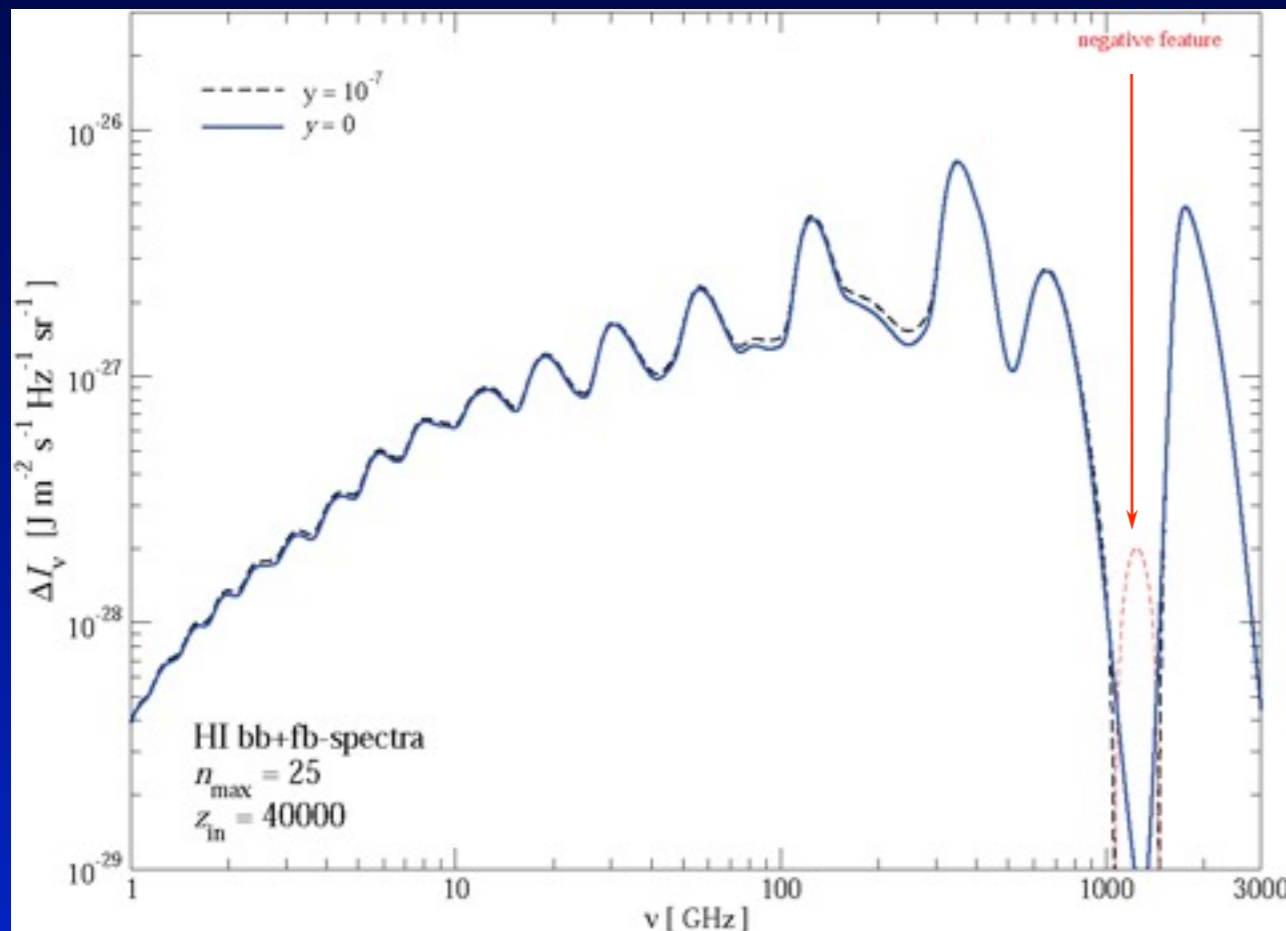
Helium +



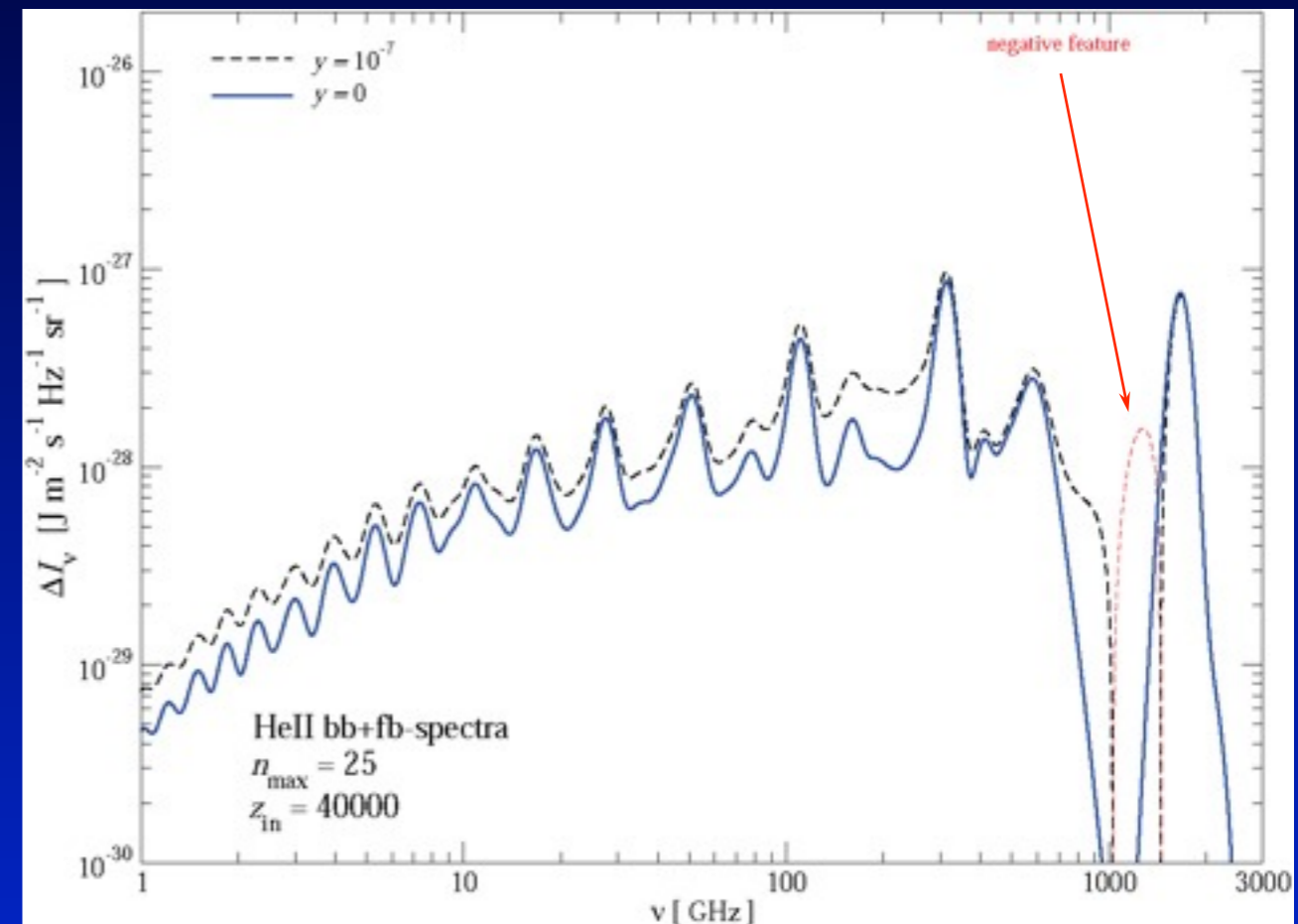
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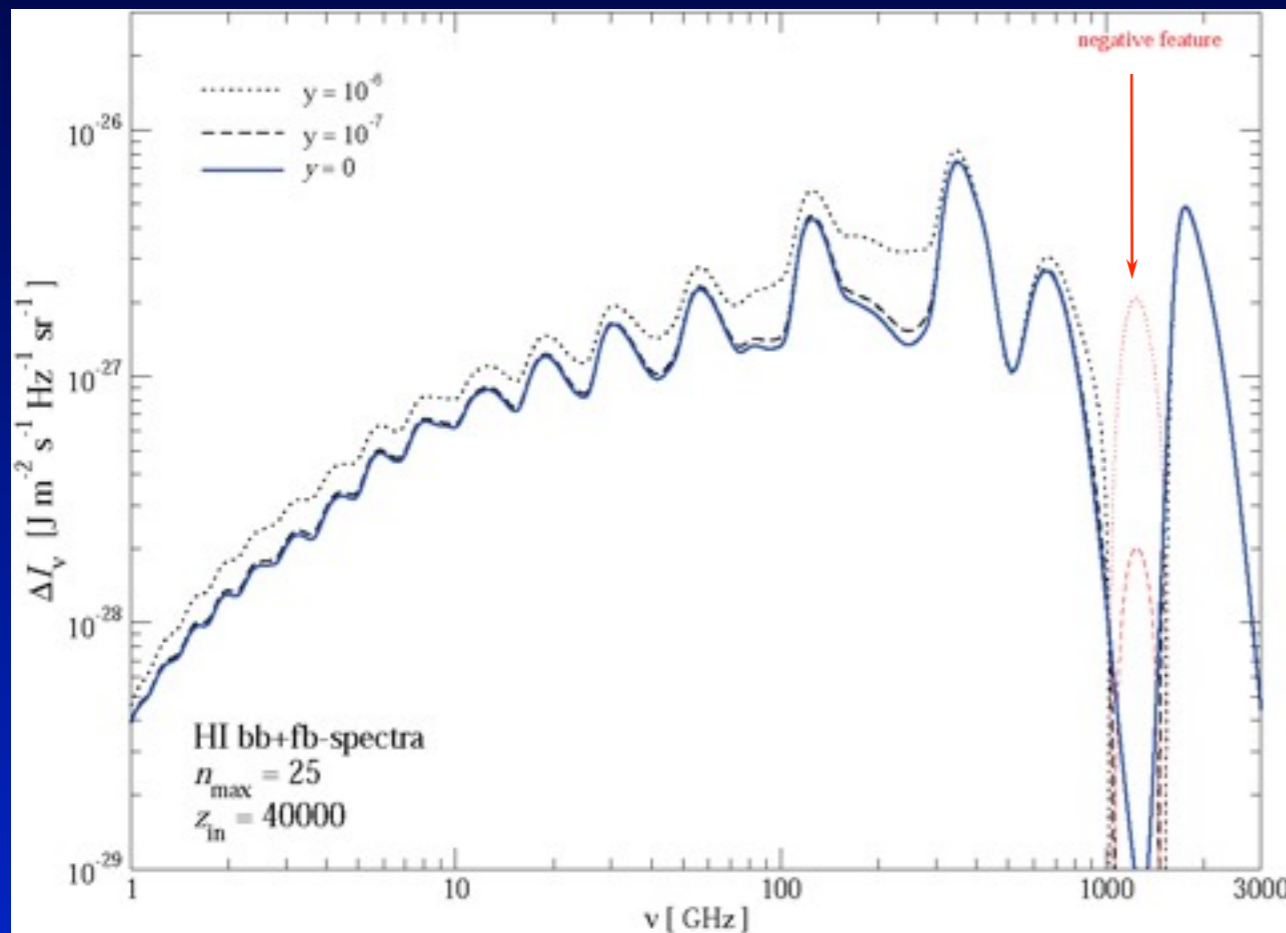
Helium +



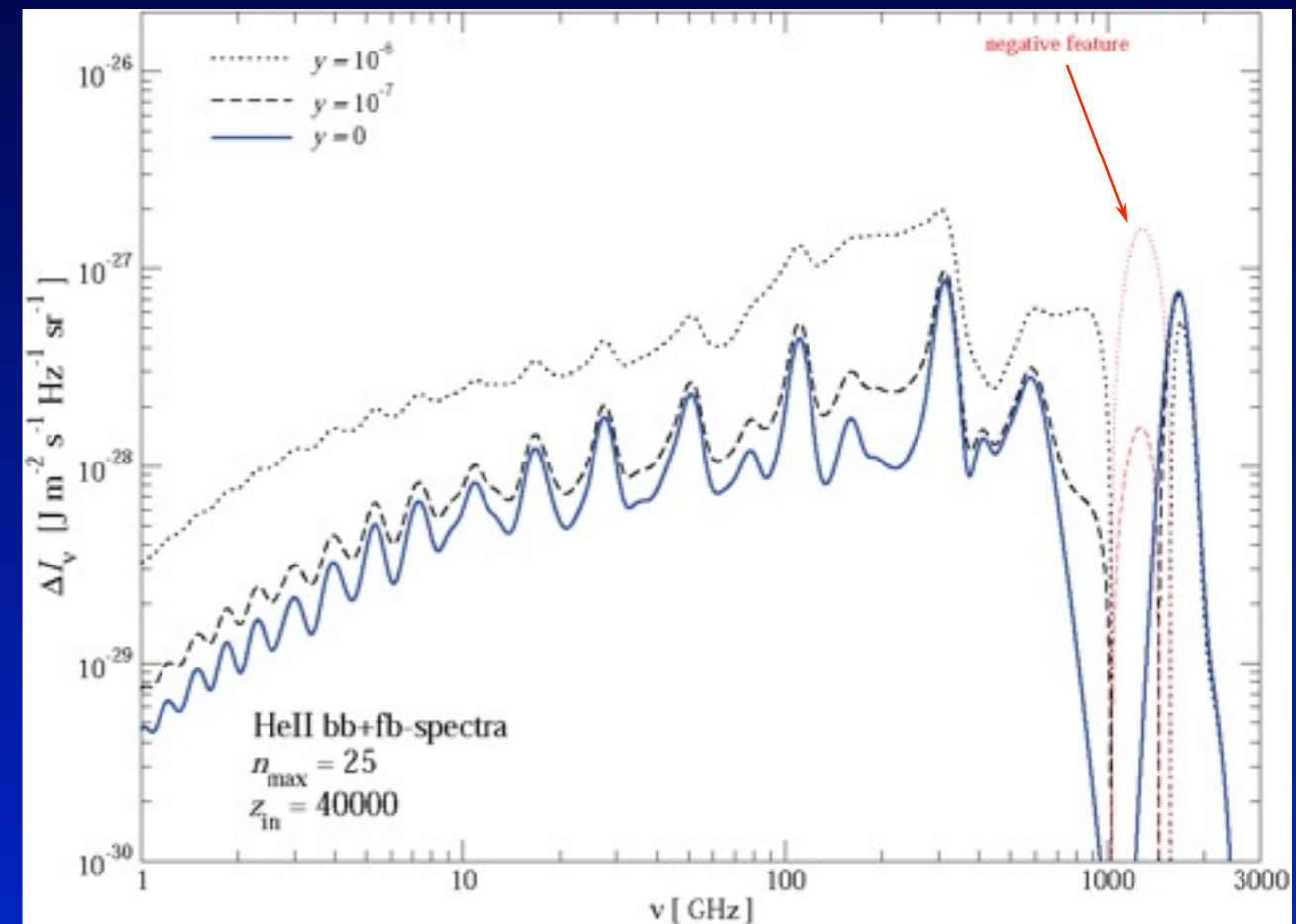
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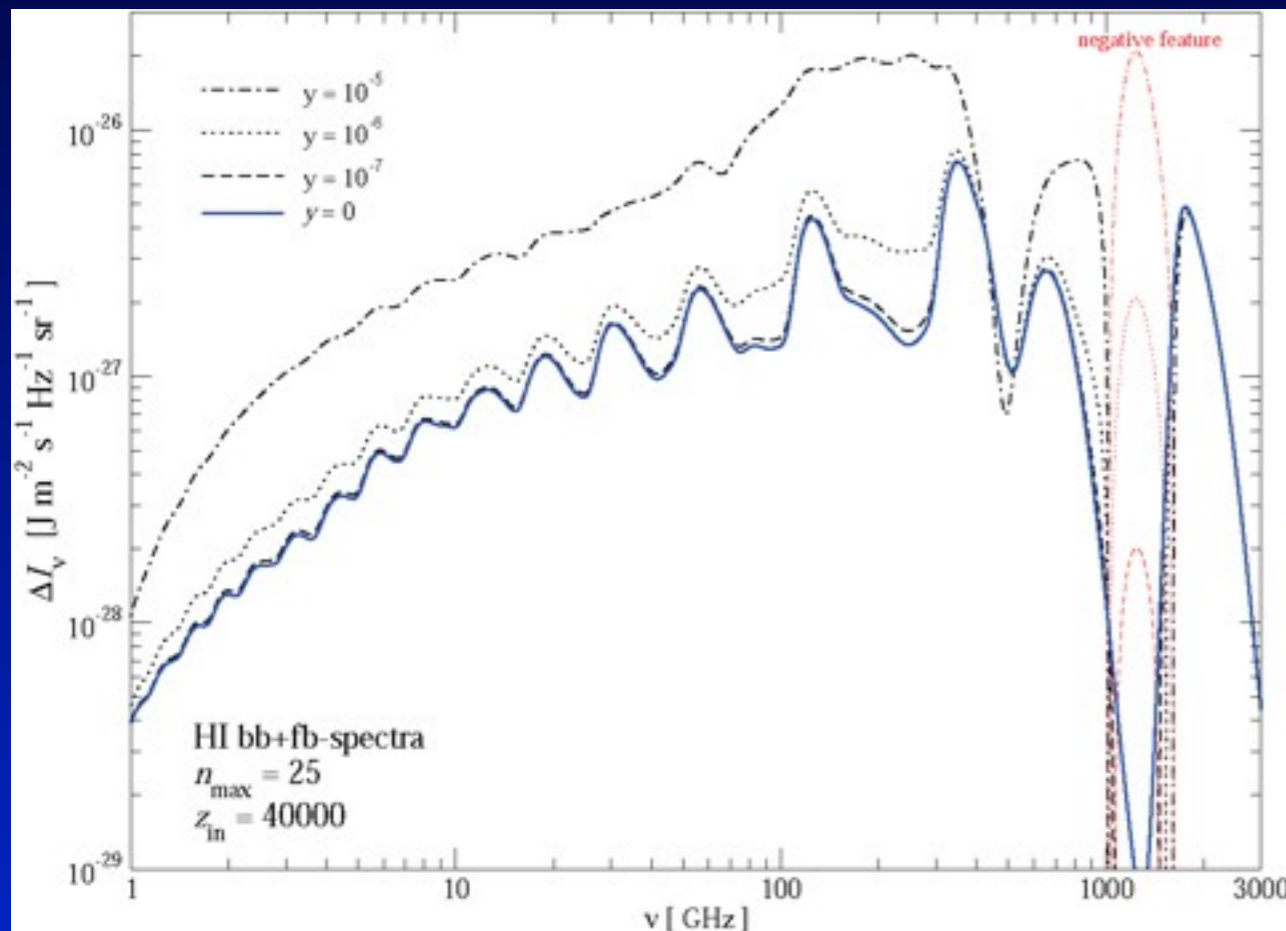
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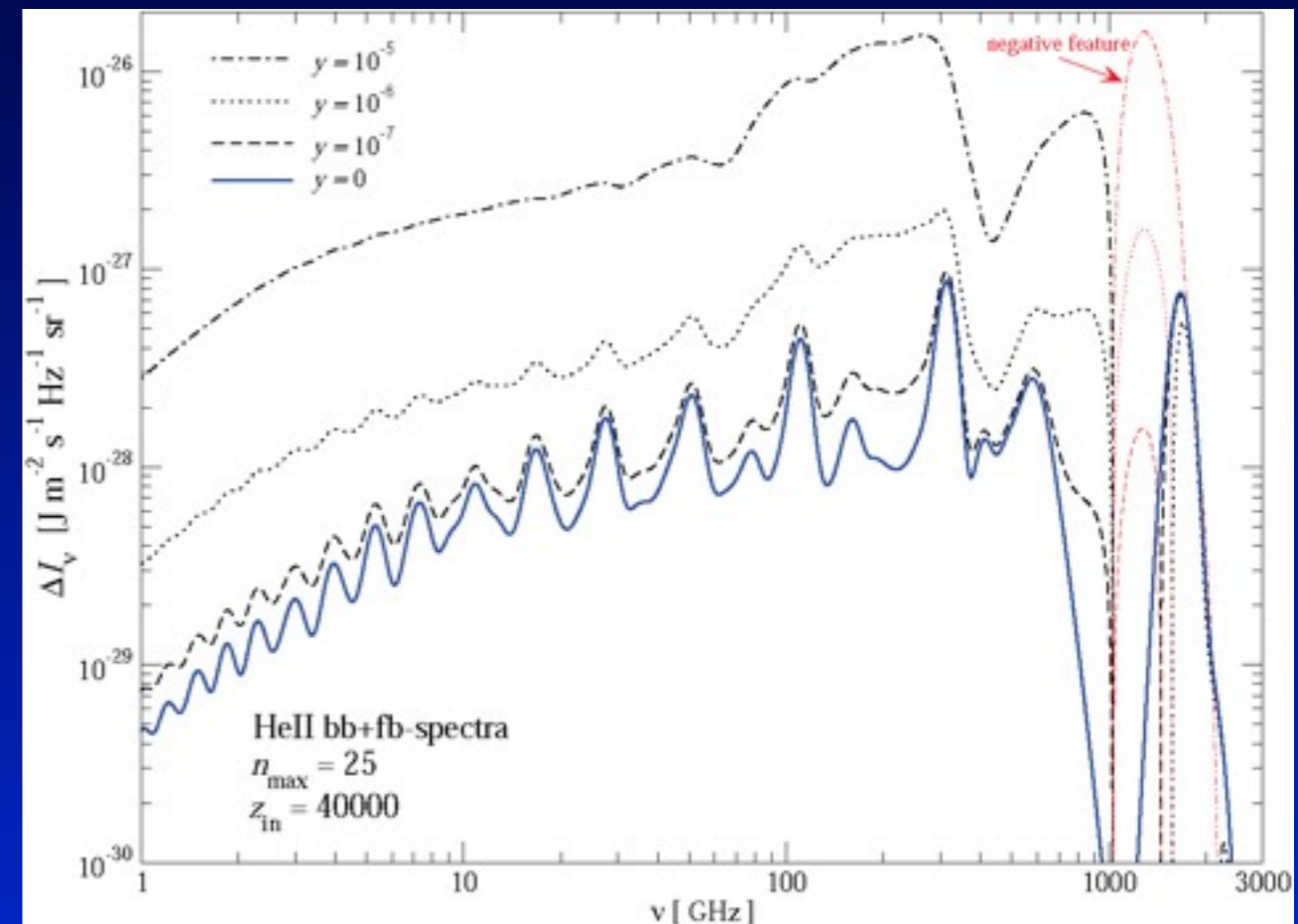
CMB spectral distortions after single energy release

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Helium +



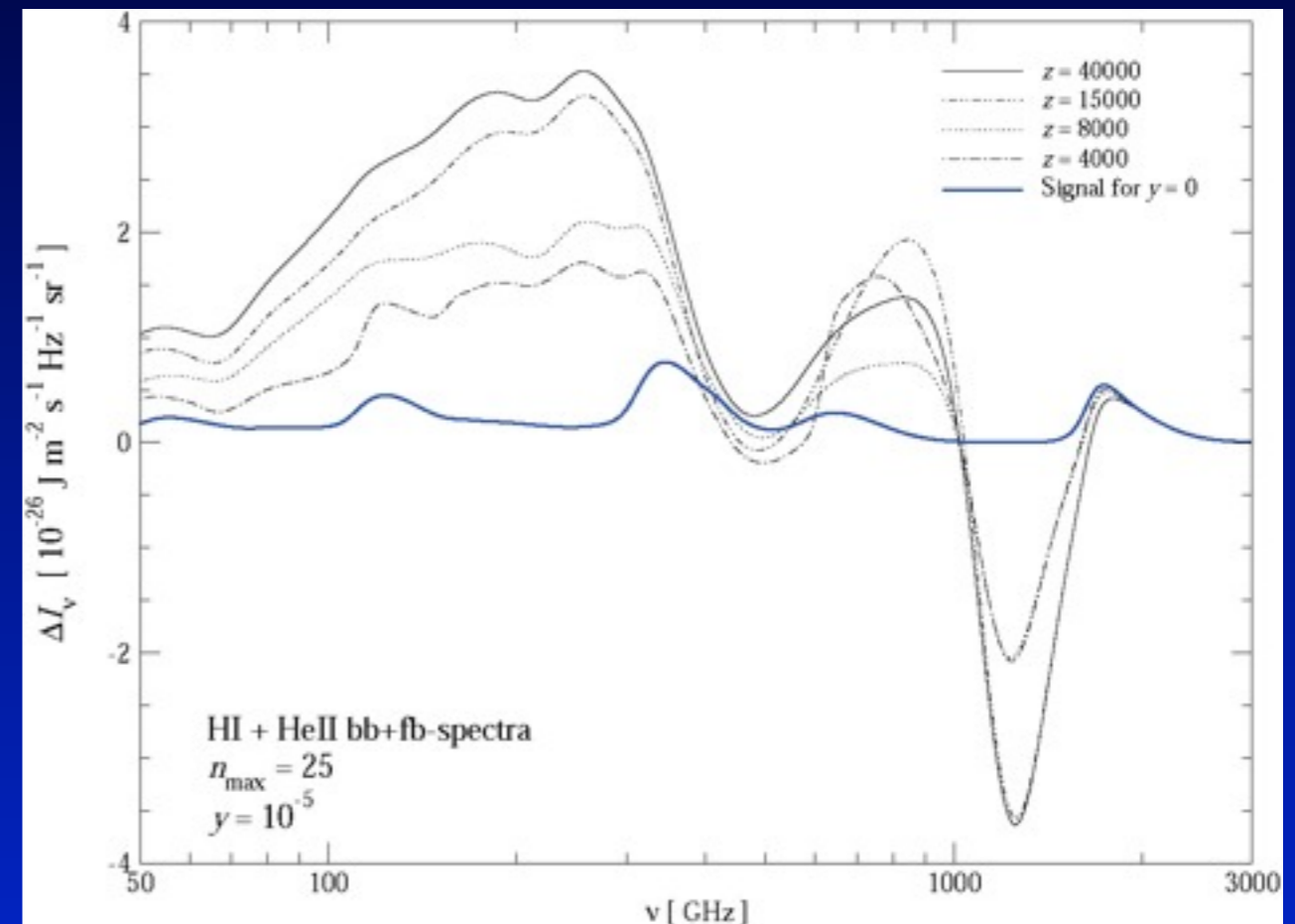
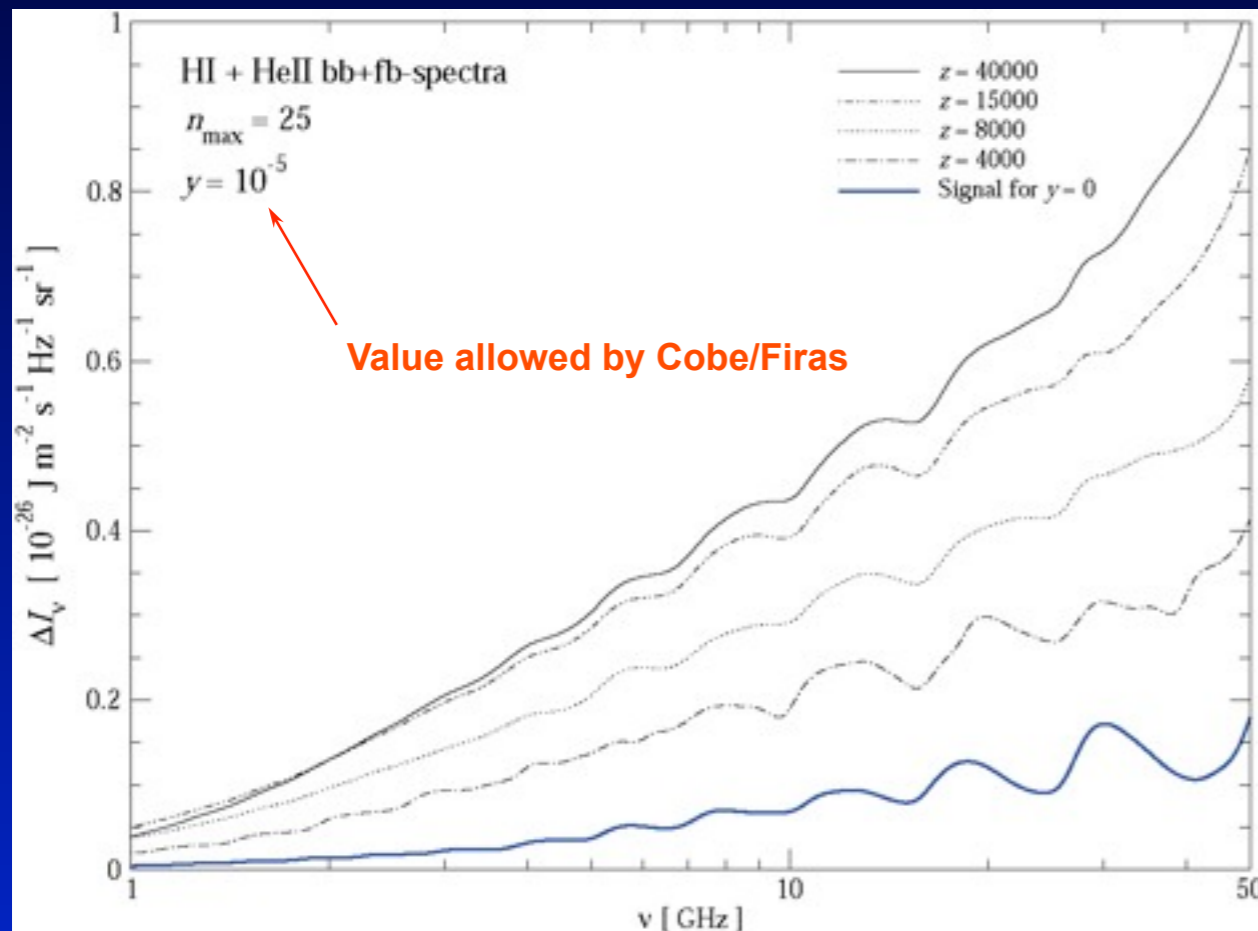
JC & Sunyaev, 2008, astro-ph/0803.3584

- ◆ Large increase in the total amplitude of the distortions with value of y !
- ◆ Strong emission-absorption feature in the Wien-part of CMB (absent for $y=0$!!!)
- ◆ HeII contribution to the pre-recombinational emission as strong as the one from Hydrogen alone !

CMB spectral distortions after single energy release

25 shell HI and HeII bb&fb spectra: *dependence on z*

Hydrogen and Helium +



JC & Sunyaev, 2008, astro-ph/0803.3584

- ◆ Large increase in the total amplitude of the distortions with injection redshift!
- ◆ Number of spectral features depends on injection redshift!
- ◆ Emission-Absorption feature increases ~ 2 for energy injection $z \Rightarrow 11000$

What would we actually learn by doing such hard job?

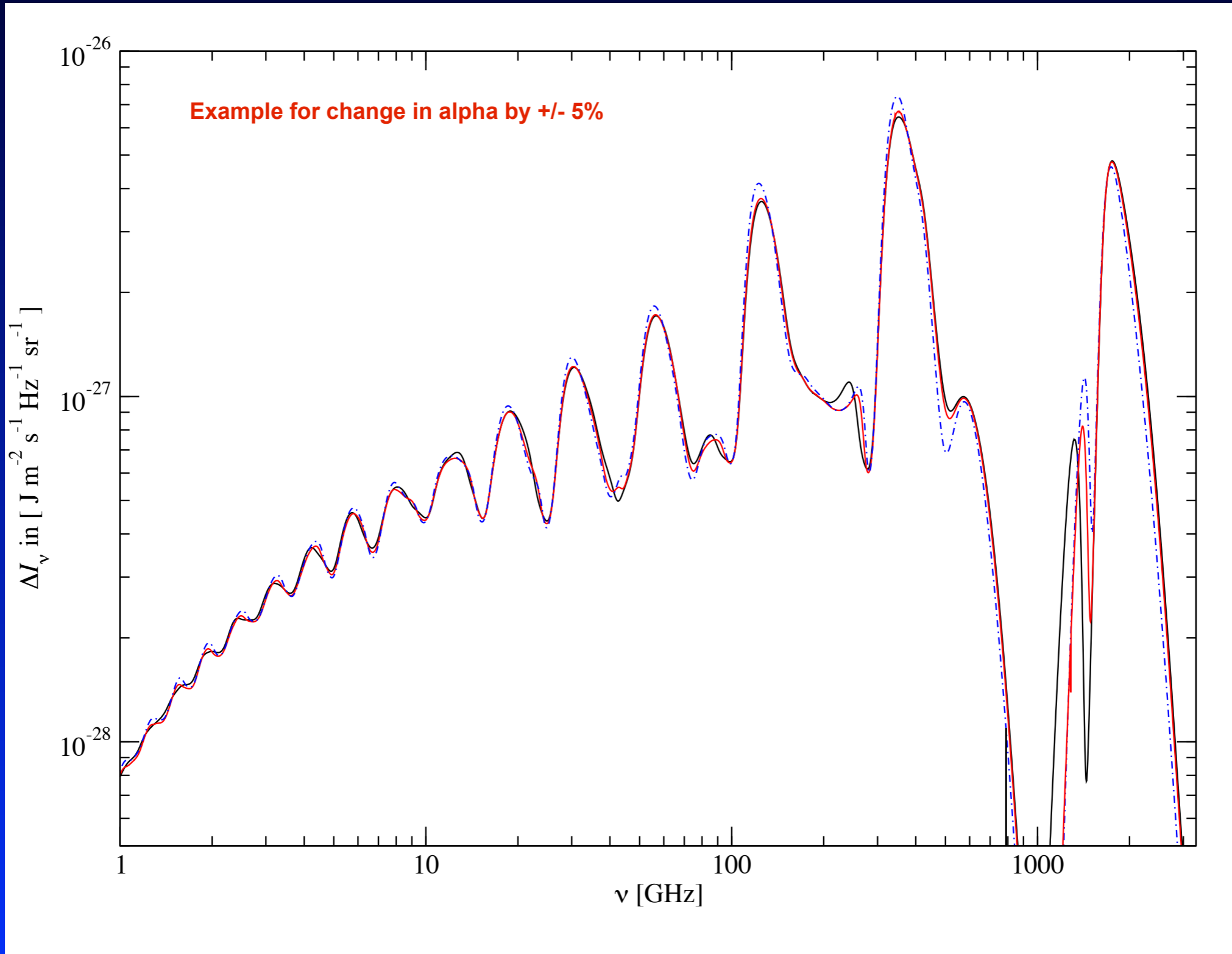
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If something unexpected or non-standard happened:

- *non-standard thermal histories should leave some measurable traces*
- *possibility to distinguish pre- and post-recombinational y-type distortions*
- *sensitive to energy release during recombination epochs*

Change of HI distortion because of difference in α



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- *variation of fundamental constants*

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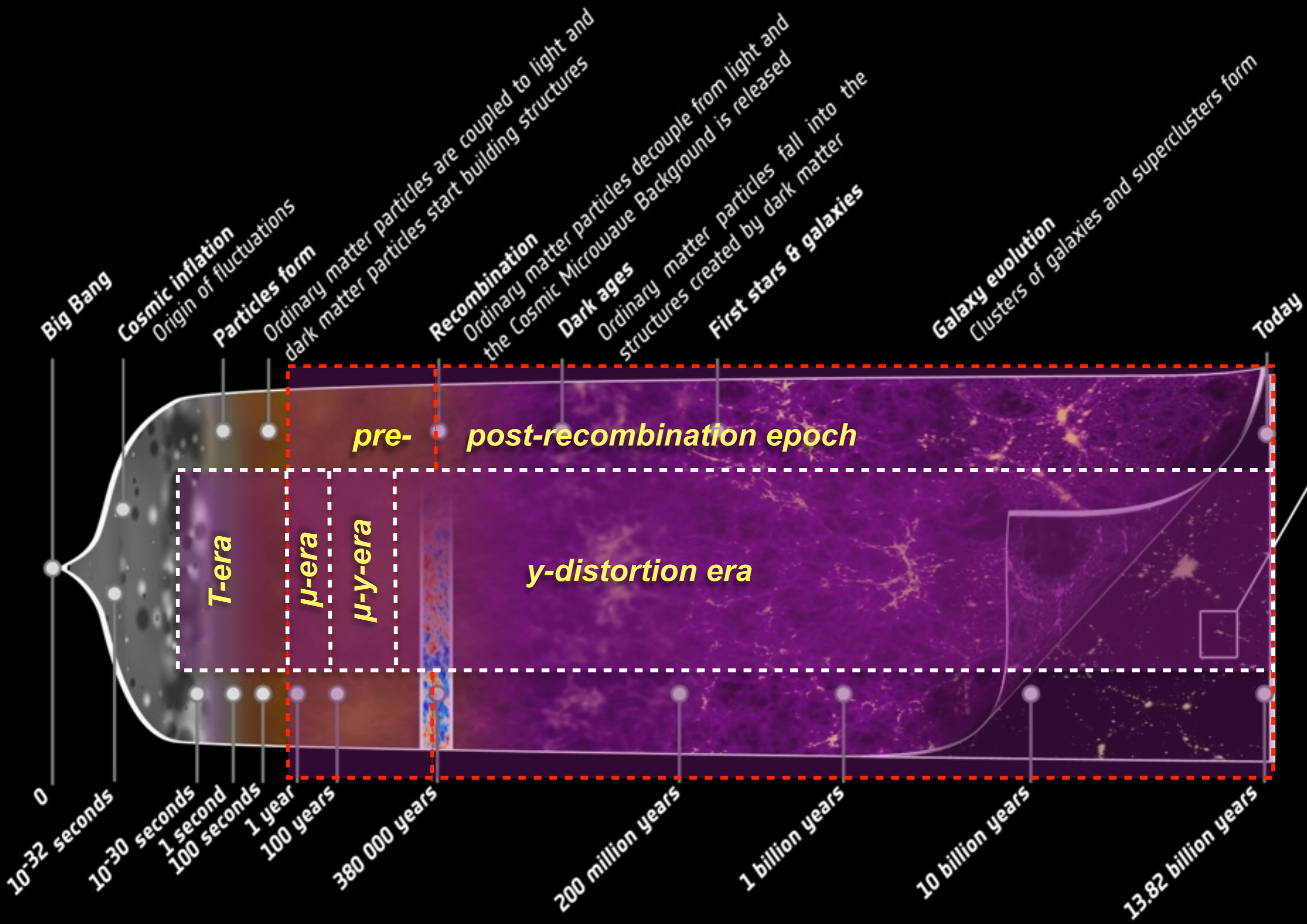
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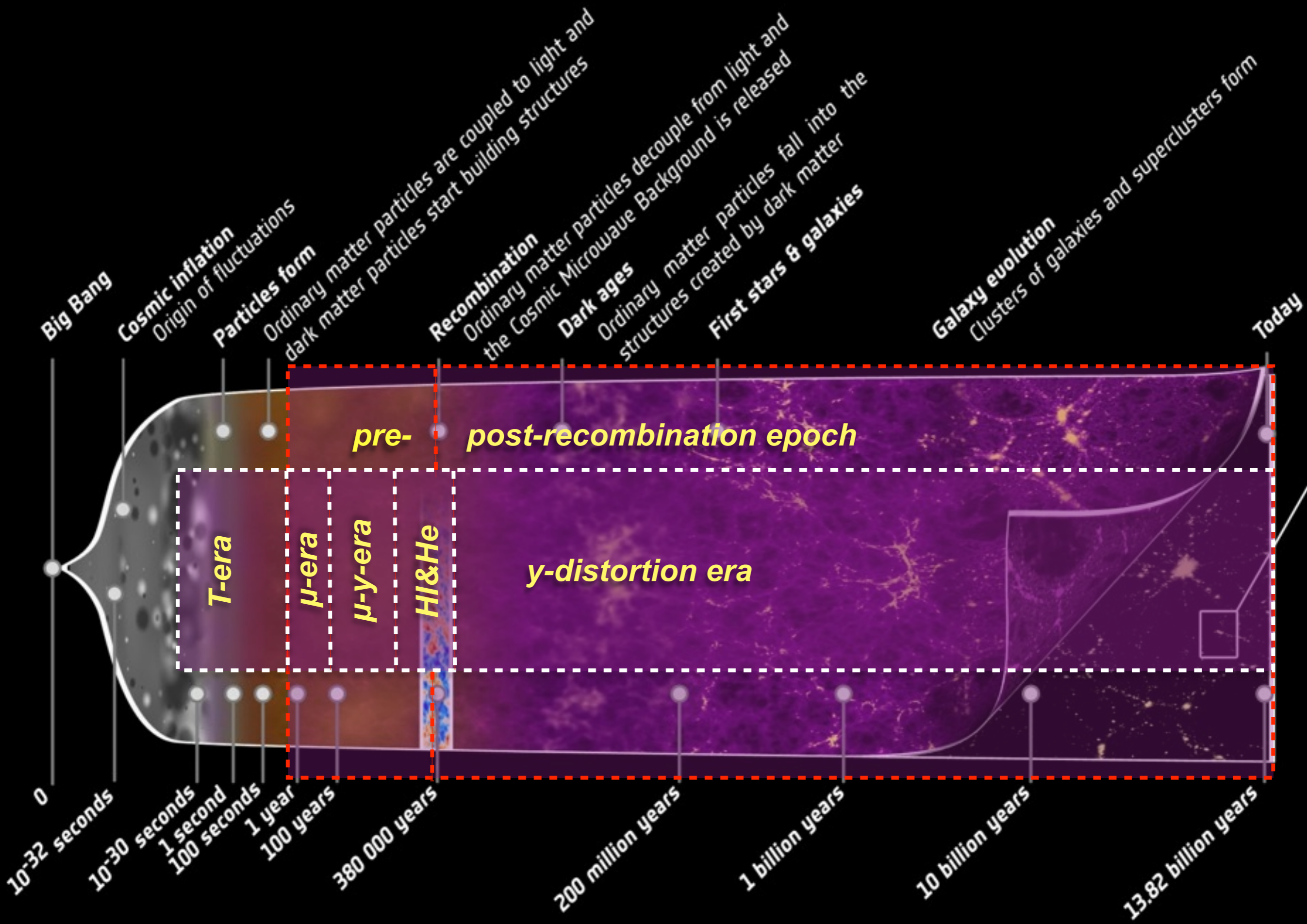
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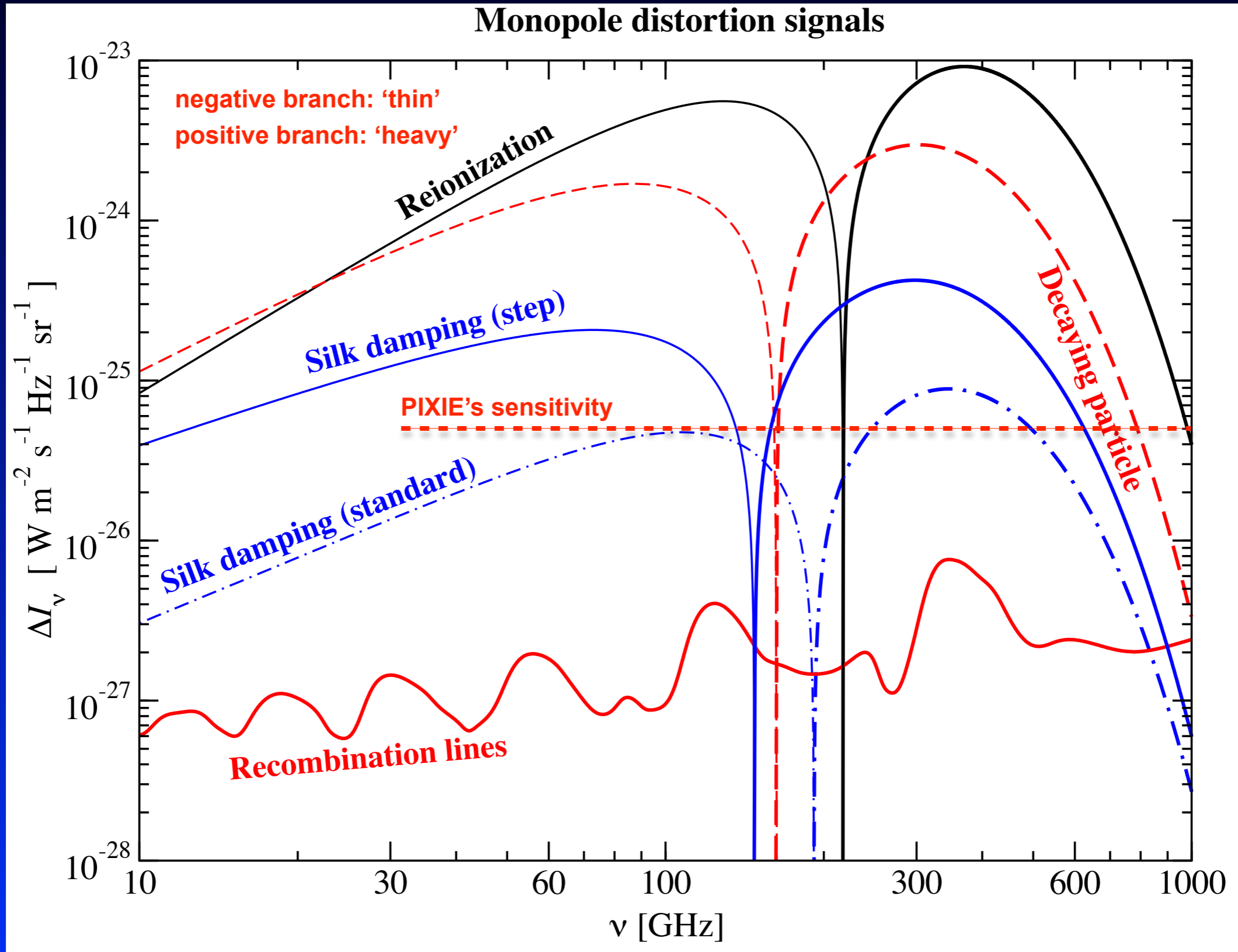
This would open a new way to constrain cosmological models





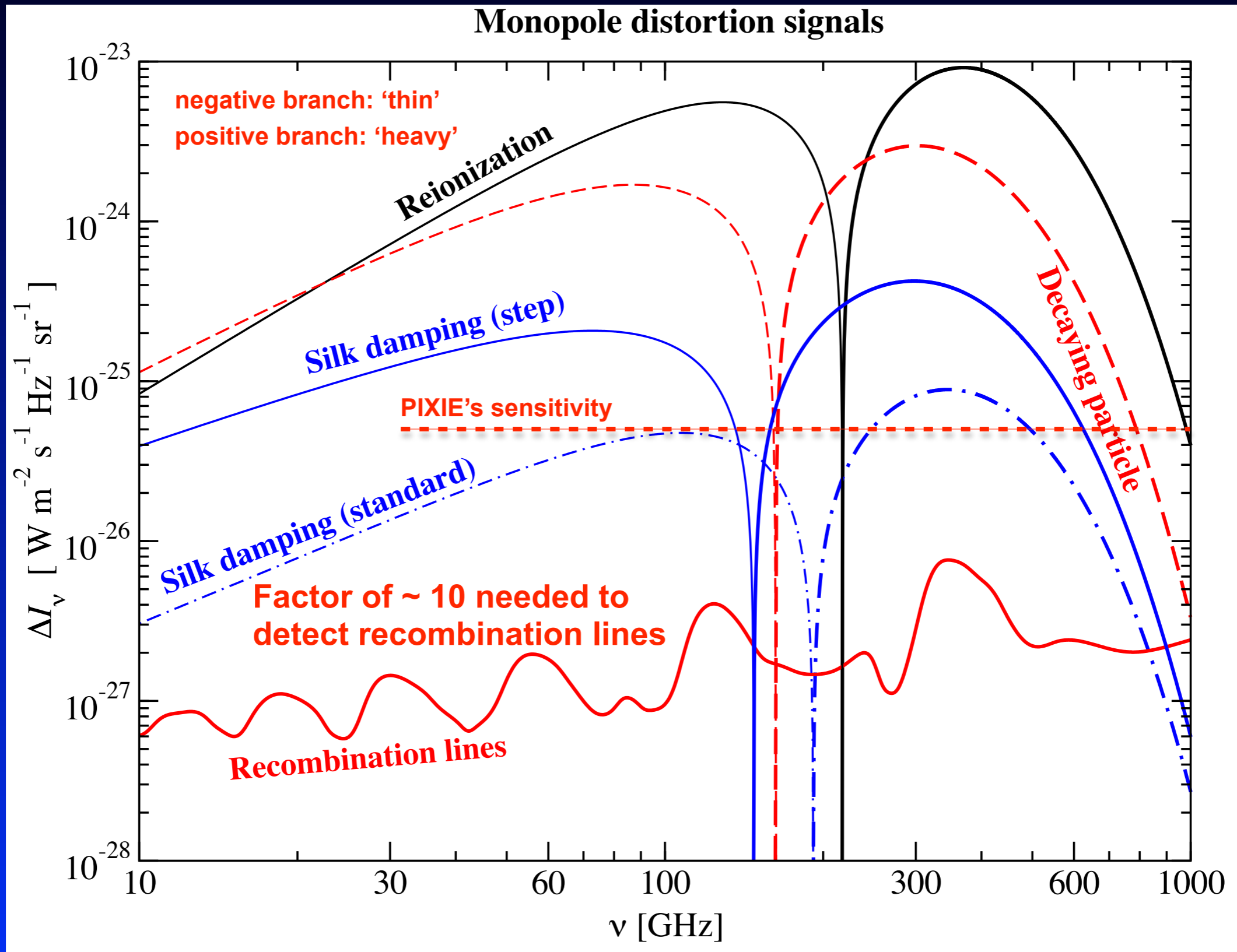
Average CMB spectral distortions

Absolute value of Intensity signal



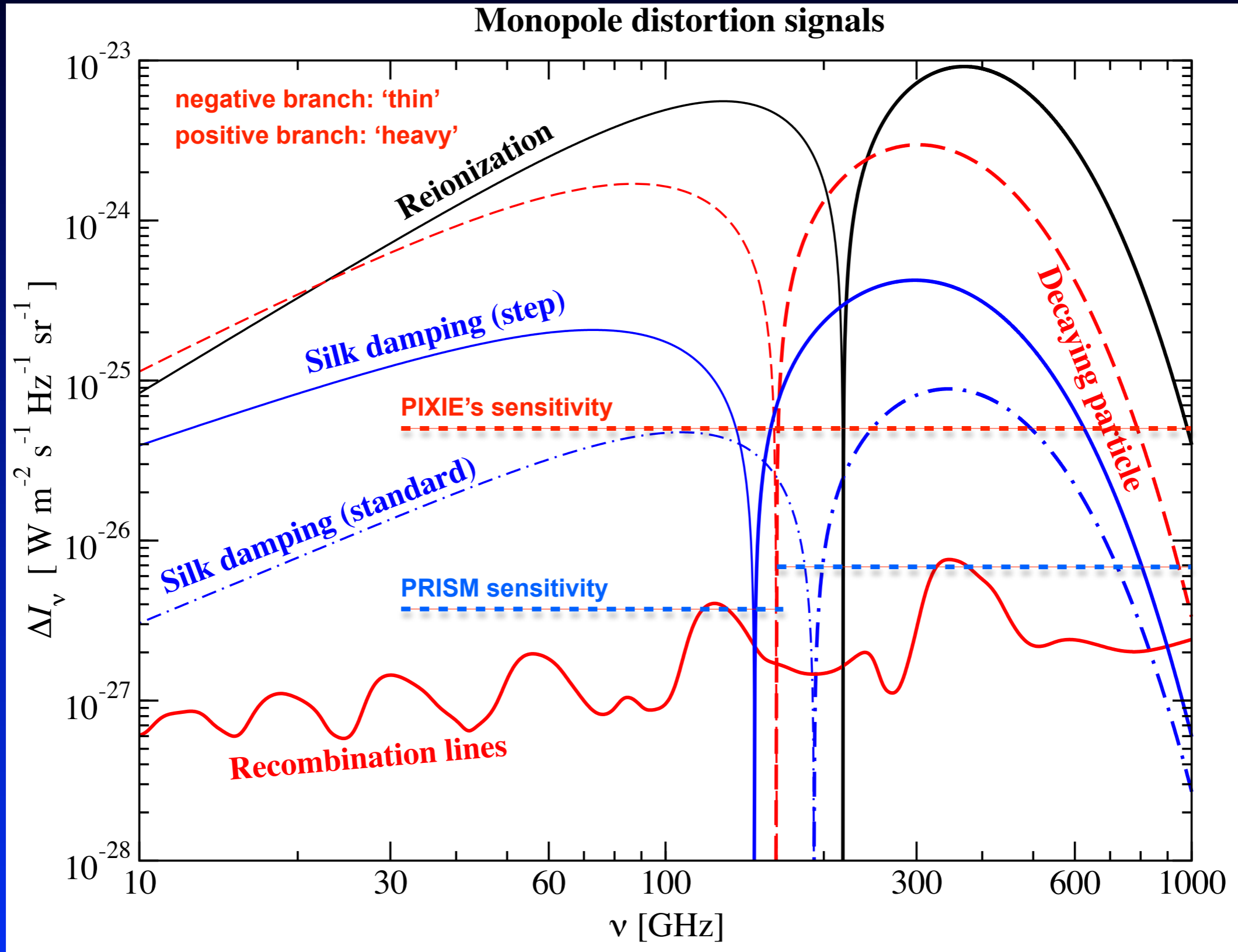
Average CMB spectral distortions

Absolute value of Intensity signal



Average CMB spectral distortions

Absolute value of Intensity signal



Other extremely interesting new signals

- **Scattering signals from the dark ages**

(e.g., Basu et al., 2004; Hernandez-Monteagudo et al., 2007; Schleicher et al., 2009)

- constrain abundances of chemical elements at high redshift
- learn about star formation history

- **Rayleigh / HI scattering signals**

(e.g., Yu et al., 2001; Rubino-Martin et al., 2005; Lewis 2013)

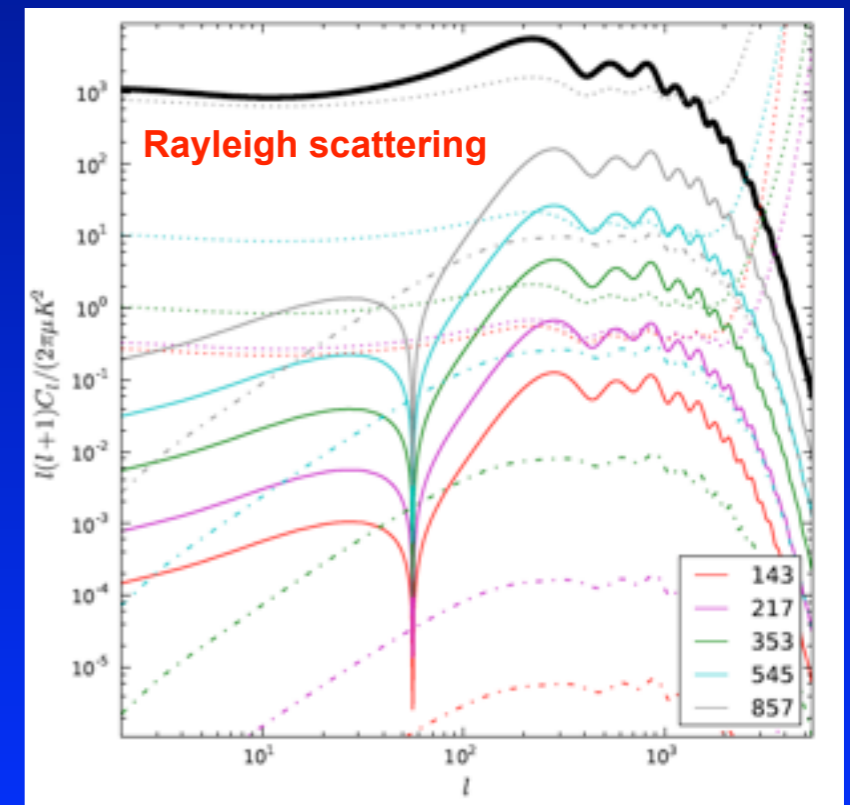
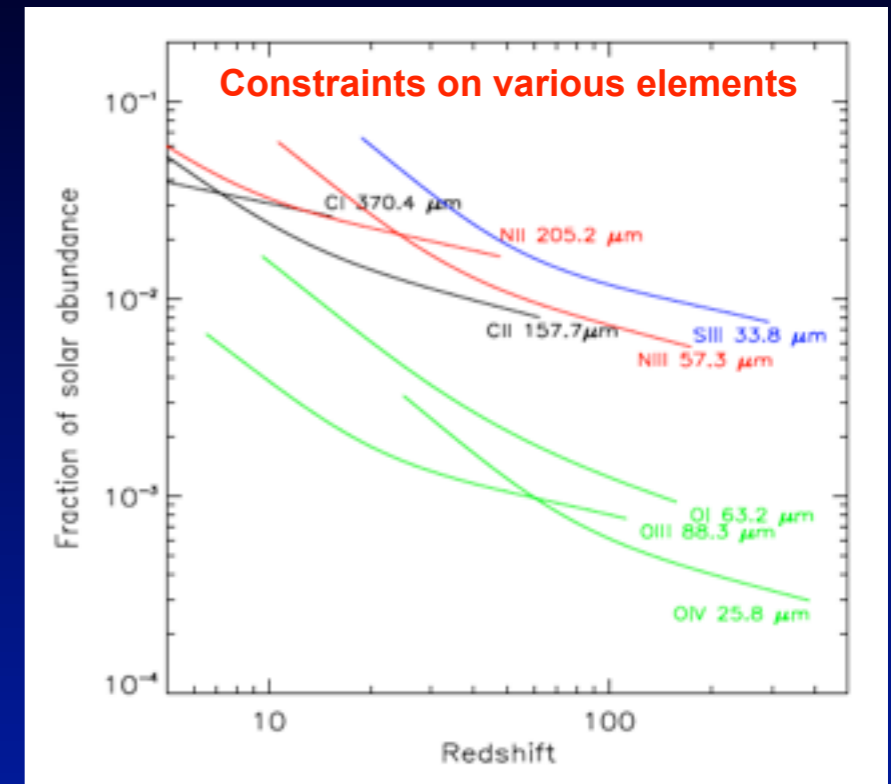
- provides way to constrain recombination history
- important when asking questions about N_{eff} and Y_p

- **Free-free signals from reionization**

(e.g., Burigana et al. 1995; Trombetti & Burigana, 2013)

- constrains reionization history
- depends on clumpiness of the medium

All these effects give spectral-spatial signals, and an absolute spectrometer will help with channel cross calibration!



Physical mechanisms that lead to spectral distortions

- *Cooling by adiabatically expanding ordinary matter*

(JC, 2005; JC & Sunyaev 2011; Khatri, Sunyaev & JC, 2011)

Standard sources
of distortions

- Heating by *decaying* or *annihilating* relic particles

(Kawasaki et al., 1987; Hu & Silk, 1993; McDonald et al., 2001; JC, 2005; JC & Sunyaev, 2011; JC, 2013; JC & Jeong, 2013)

- *Evaporation of primordial black holes & superconducting strings*

(Carr et al. 2010; Ostriker & Thompson, 1987; Tashiro et al. 2012; Pani & Loeb, 2013)

- *Dissipation of primordial acoustic modes & magnetic fields*

(Sunyaev & Zeldovich, 1970; Daly 1991; Hu et al. 1994; JC & Sunyaev, 2011; JC et al. 2012 - Jedamzik et al. 2000; Kunze & Komatsu, 2013)

- *Cosmological recombination radiation*

(Zeldovich et al., 1968; Peebles, 1968; Dubrovich, 1977; Rubino-Martin et al., 2006; JC & Sunyaev, 2006; Sunyaev & JC, 2009)

„high“ redshifts

„low“ redshifts

- *Signatures due to first supernovae and their remnants*

(Oh, Cooray & Kamionkowski, 2003)

- *Shock waves arising due to large-scale structure formation*

(Sunyaev & Zeldovich, 1972; Cen & Ostriker, 1999)

- *SZ-effect from clusters; effects of reionization*

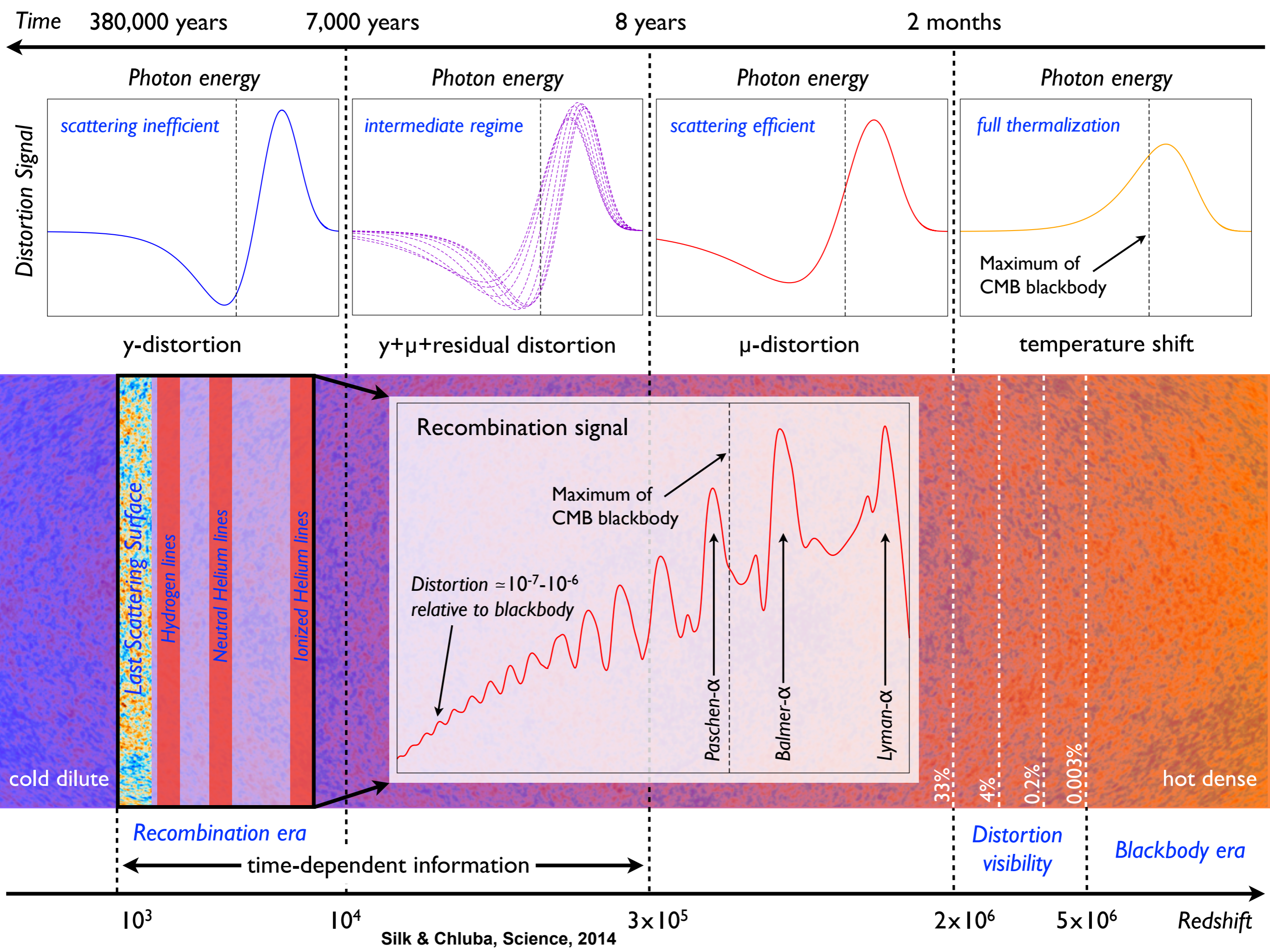
(Refregier et al., 2003; Zhang et al. 2004; Trac et al. 2008)

- *more exotic processes*

(Lochan et al. 2012; Bull & Kamionkowski, 2013; Brax et al., 2013; Tashiro et al. 2013)

pre-recombination epoch

post-recombination



Conclusions

- CMB spectral distortions *will* open a *new window* to the early Universe
- new probe of the *inflation epoch* and *particle physics*
- *complementary* and *independent* source of information *not* just confirmation
- in *standard cosmology* several processes lead to *early energy release* at a level that will be detectable in the future
- extremely interesting *future* for CMB-based science!

We should make use of all this information!

